



# Simulation and Modeling of Turbulence Subjected to Plane Strain

**Blair Perot**  
**Chris Zusi**

**Theoretical and Computational Fluid Dynamics Laboratory**

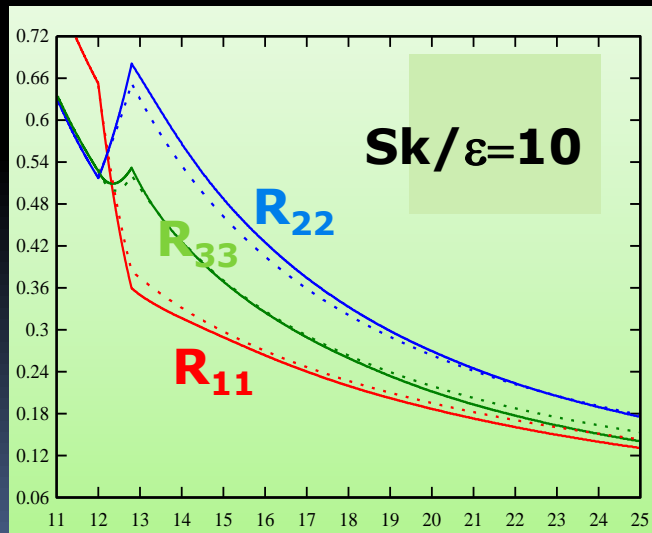
**Parviz 60<sup>th</sup> Birthday Workshop, Oct 13, 2012**

# Motivation

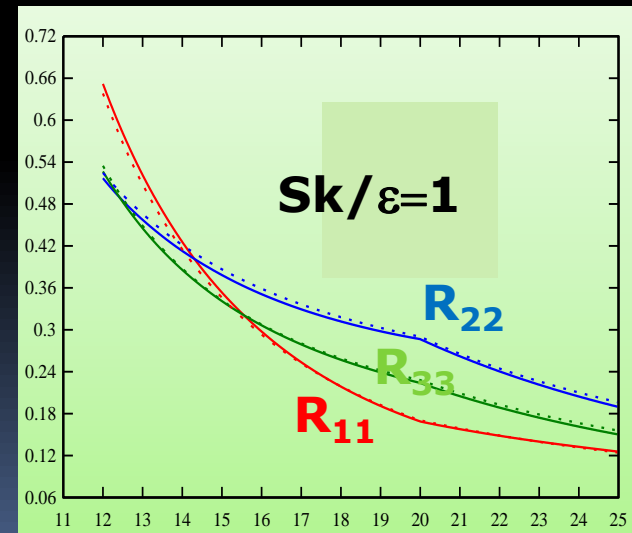
Explore the energy cascade for non-isotropic turbulence

Revisit the Return-to-isotropy modeling problem

Reynolds  
Stresses



time



time

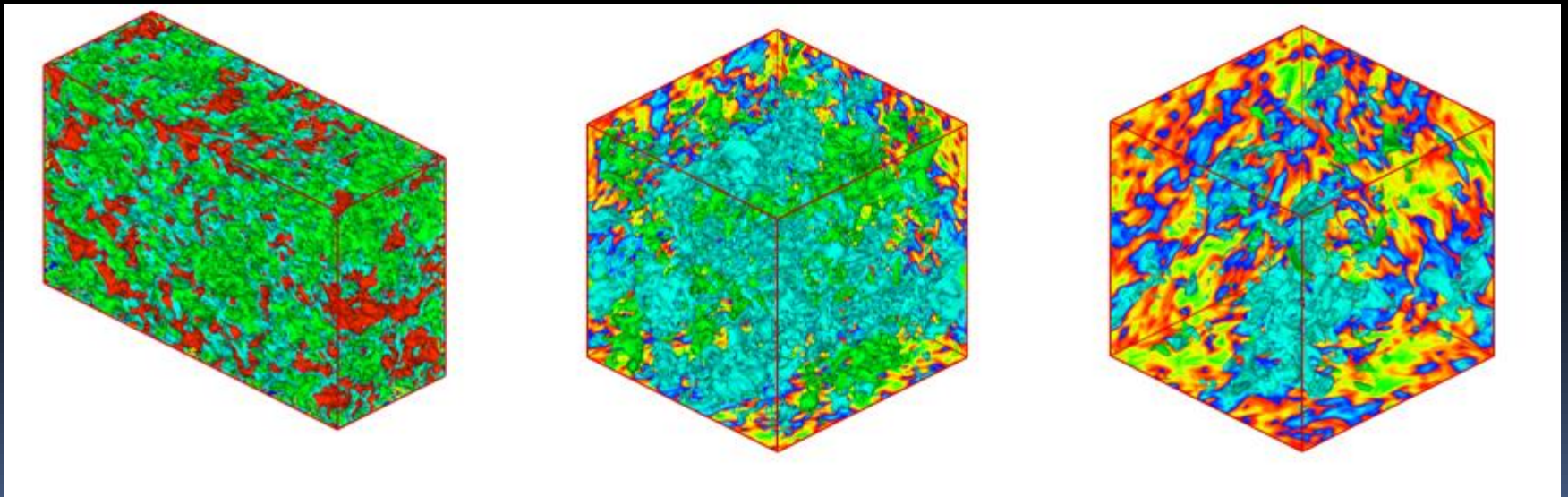


# Approach

**Generate real turbulence (with  $512^3$  DNS).**

**Strain it. (Many strain rates,  $Re$ , etc)**

**Observe the resulting anisotropic decay.**



# Simulation Details

- **2<sup>nd</sup>-order Staggered Mesh**
- **Exact Fractional Step**
- **Low storage, 3-step Runge-Kutta**
- **Moving mesh**
- **64 GPUs**

**$\sim 5 \times 10^{-7}$  s**  
**/grid point**  
**/ timestep.**

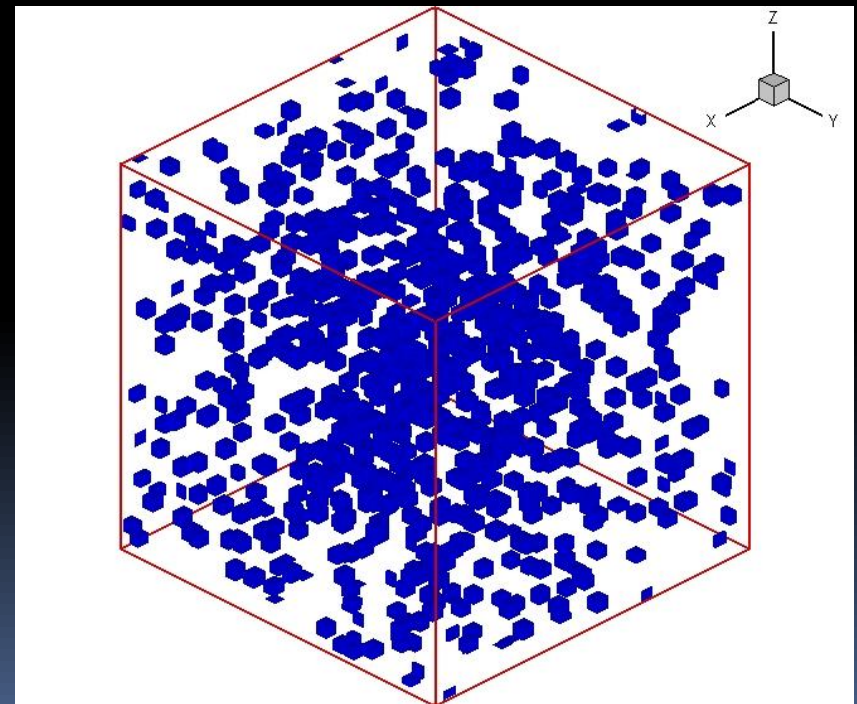


# Initial Conditions

**Initially zero velocity and pressure**  
**No large scale forcing**  
**No initial spectra**

**Acceleration of  
fluid past 768  
small solid boxes.  
(1/35 of domain size)**

J. B. Perot, *Determination of the Decay Exponent in Mechanically Stirred Isotropic Turbulence*, *Advances in Physics*, **1**, 2011.

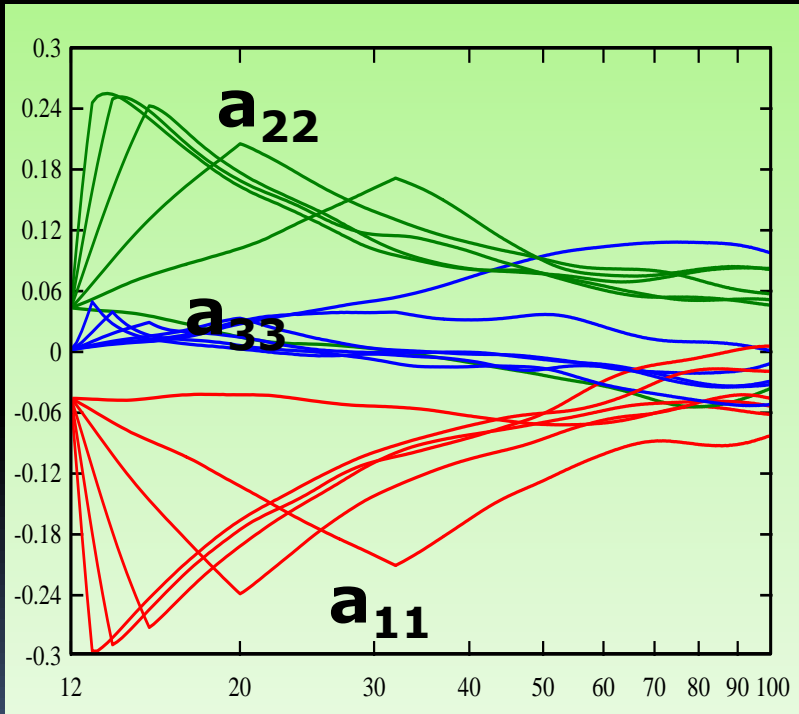


# Shear Rate

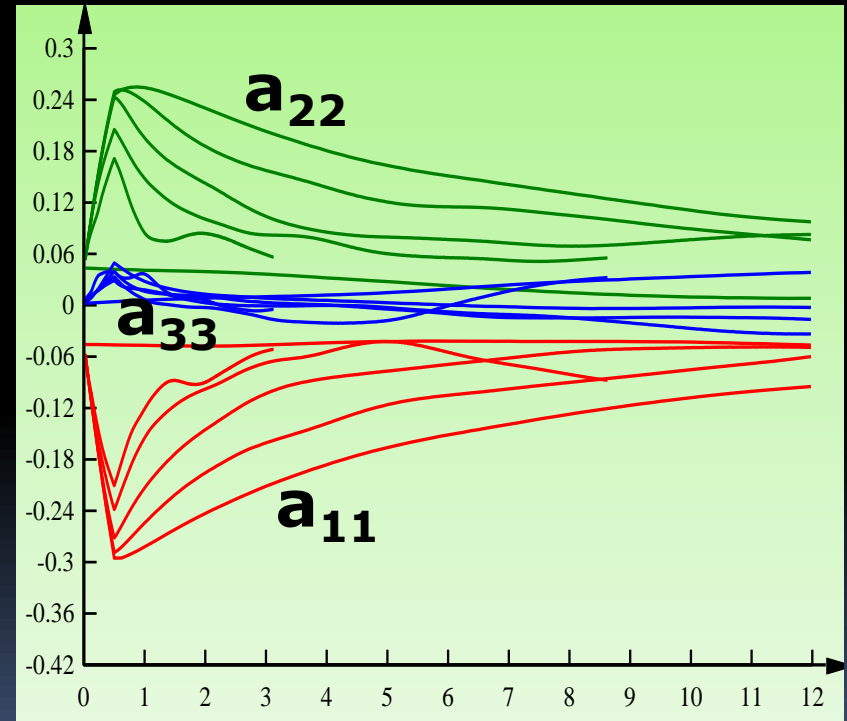
**ST = 0.5**

**Sk/ε = 10, 5, 2.5, 1, 0.4**

$$a_{ij} = \frac{R_{ij}}{k} - \frac{2}{3} \delta_{ij}$$



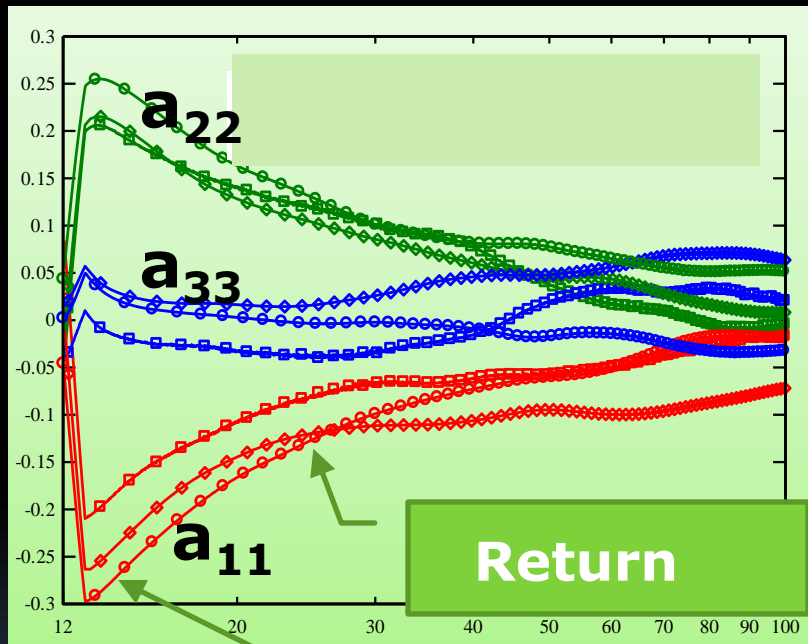
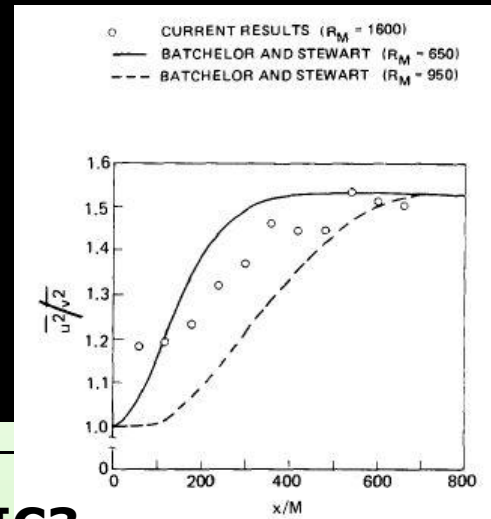
time



$S \cdot \text{time}$

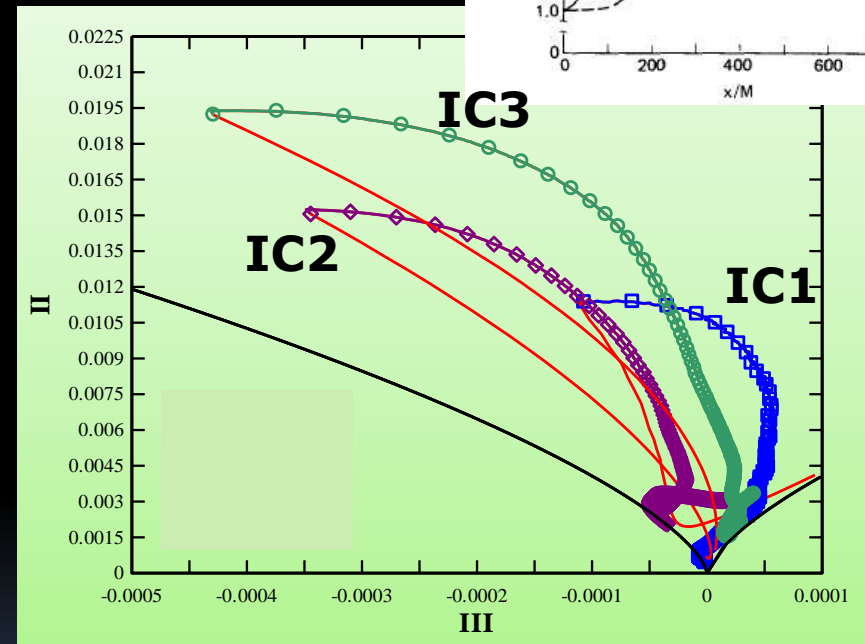


# Statistical Variation



time

Recovery



$$II = a_{ij} a_{ji}$$

$$III = a_{ij} a_{jk} a_{ki}$$

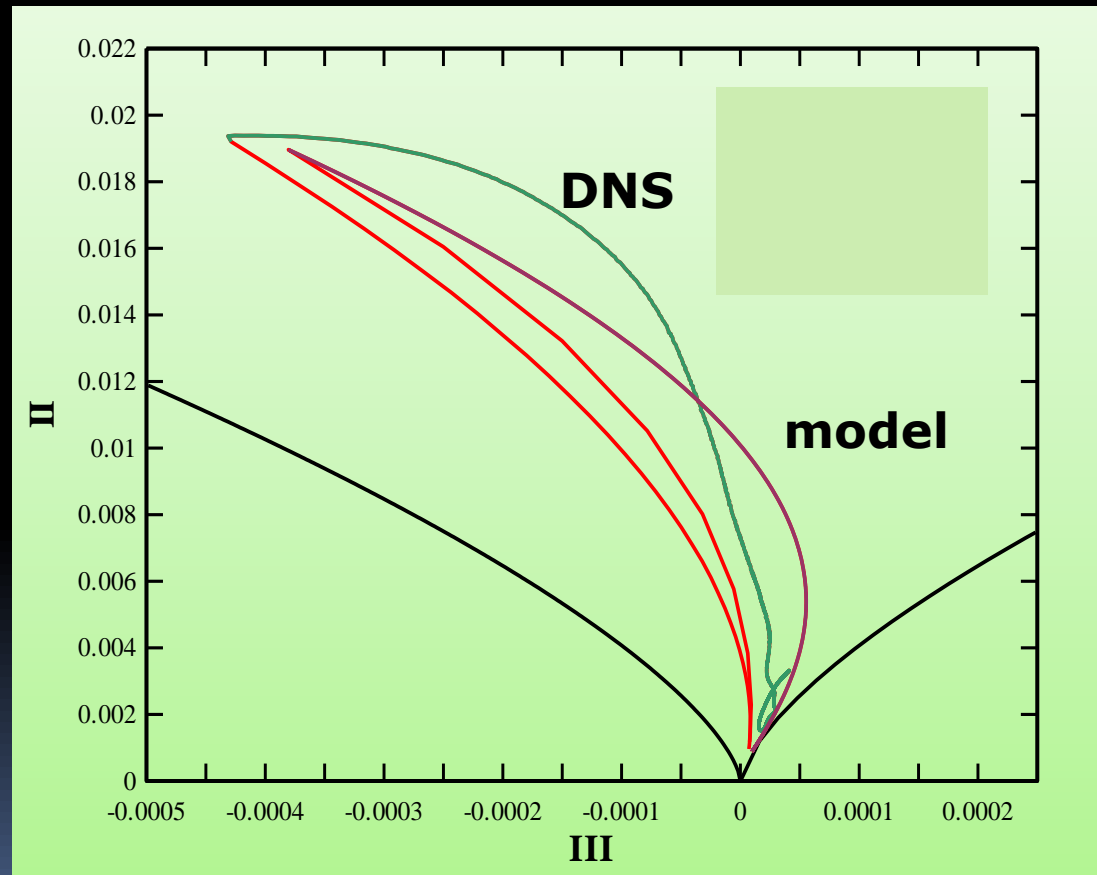


# Modeling

## Oriented Eddy Collision (OEC) model

A method to model 2-point velocity correlation evolution

Eddy structure also returns to isotropy





# Conclusions

- **Long time – no return (Corrsin)**
- **RST models are fundamentally unable to predict anisotropic turbulent decay.**
- **It is possible to model recovery and return with a very simple model (for the 2-point correlations).**

**[www.ecs.umass.edu/mie/tcfd](http://www.ecs.umass.edu/mie/tcfd)**