



**The carbon dioxide marginal abatement cost
calculation of Chinese provinces
-based on stochastic frontier analysis**

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Background

- Commitment : 40%-45% reduction in carbon emissions per GDP by 2020 compared with 2005.
- Lack of central government's differential CO₂ reduction allocation, most provinces just follow the national commitment.
- Flaw: provinces have different attributes
- CO₂ Marginal Abatement Cost (MAC) varied



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Literature Review

- **Distance Function** was widely used in CO₂ marginal abatement cost calculation.
- **Parametric Distance Function:** needs to pre-establish a function form.
easy to manipulate algebraically
- **Nonparametric Distance Function**

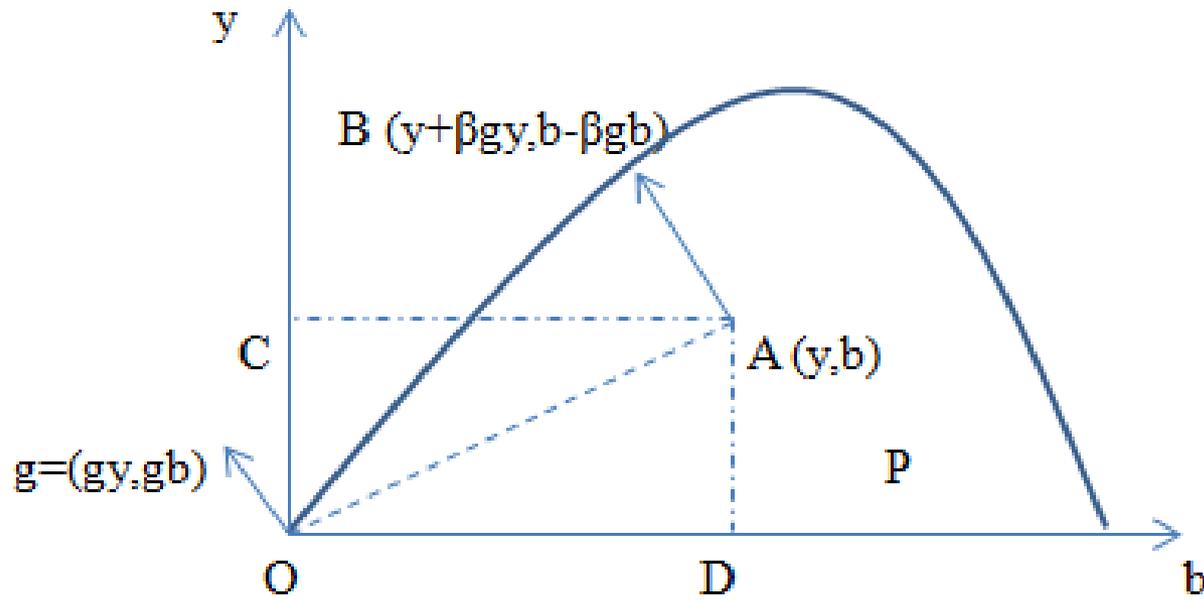
Studies	Method	Sample	MAC
Wang et al.	DDF/DEA	28 provinces, 2007	¥475/ton
Huang & Wei	DDF/LP	29 provinces, 1995-2007	¥1128/ton
Zhang et al.	DDF/LP	29 provinces, 2006-2010	¥80.19/ton
He	DF/LP	29 provinces, 2000-2009	¥104/ton
Liu et al.	DF/DEA	30 provinces, 2005-2007	¥1739/ton

- **Directional Distance Function(DDF):** increase desirable output while decrease undesirable output.
- **Distance Function(DF):** desirable & undesirable outputs are changed in same ratio.
- **Data Envelopment Analysis(DEA):** function needs to be differentiable everywhere.
- **Linear Programming(LP):** cannot deal with isolated point



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- P: production technology set

$$P = \{(y, b) : X \text{ can produce } (y, b)\}$$
- A: region in P with desirable output y and undesirable output b
- B: Efficient point
- g : directional vector $g = (g_y, g_b)$
- DDF is measured by $\beta = AB/Og$.

- Directional Distance Function

$$\bar{D}(X, y, b; g) = \sup \{ \beta : (y + \beta g_y, b - \beta g_b) \in P \}$$

- Parametric Directional Distance Function

X: inputs (capital X_k , labor X_l , energy X_E)

y: desirable output (GDP)

b: undesirable output (CO₂ emission)

Quadratic form of production function:

$$\bar{D}(x, y, b; g_y, -g_b) =$$

$$\alpha_0 + \sum_{i \in K, L, E} \alpha_i x_i + \alpha_y y + \alpha_b b + \frac{1}{2} \sum_{i \in K, L, E} \sum_{j \in K, L, E} \alpha_{ij} x_i x_j + \frac{1}{2} \alpha_{yy} y^2 + \frac{1}{2} \alpha_{bb} b^2 + \sum_{i \in K, L, E} \alpha_{iy} x_i y + \sum_{i \in K, L, E} \alpha_{ib} x_i b + \alpha_{yb} y b$$

- Stochastic Frontier Analysis(SFA) method which can manage random error was applied.

$$\bar{D}_0(x^n, y^n, b^n; g_y, -g_b) + v^n - u^n = 0$$

- v: noise, satisfies normal distribution $v^n \sim N(0, \sigma_v^2)$
- u: random error, satisfies half-normal distribution $u^n \sim N^+(0, \sigma_u^2)$

$$R = p[y + (1 - \bar{D}_0)g_y] - p_b[b - (1 - \bar{D}_0)g_b]$$

- R: revenue of a certain region
- p: price of GDP, p=1
- P_b: price of CO₂ (Marginal abatement cost)

$$p_b = -\frac{y}{b} \left(\frac{\partial \ln D_0}{\partial \ln b} / \frac{\partial \ln D_0}{\partial \ln y} \right)$$

$$= -\frac{y}{b} (\gamma_b + \gamma_{bb} \ln b + \eta_k \ln x_k + \eta_l \ln x_l + \eta_e \ln x_e)$$

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Data

- Data resource

2013 China Statistic Yearbook:

capital stock, labor, GDP

2013 China Energy Statistic Yearbook:

energy consumption

- Energy sources:

coal, coke, kerosene, gasoline, fuel oil, diesel and natural gas

- CO₂ EMISSION:

$$C = E_{ij} \times \delta_j$$

$$= E_{ij} \times M_j \times \beta_j \times \varepsilon_j \times \omega$$

- E_{ij} : consumption of energy j in province i
- δ_j : coefficient of CO₂ emissions of energy j
- M_j : net calorific value of energy j
- β_j : carbon content of the unit heat value of energy j
- ε_j : carbohydrate oxidation of energy j
- ω : gasification coefficient of CO₂, has constant value of 44/12

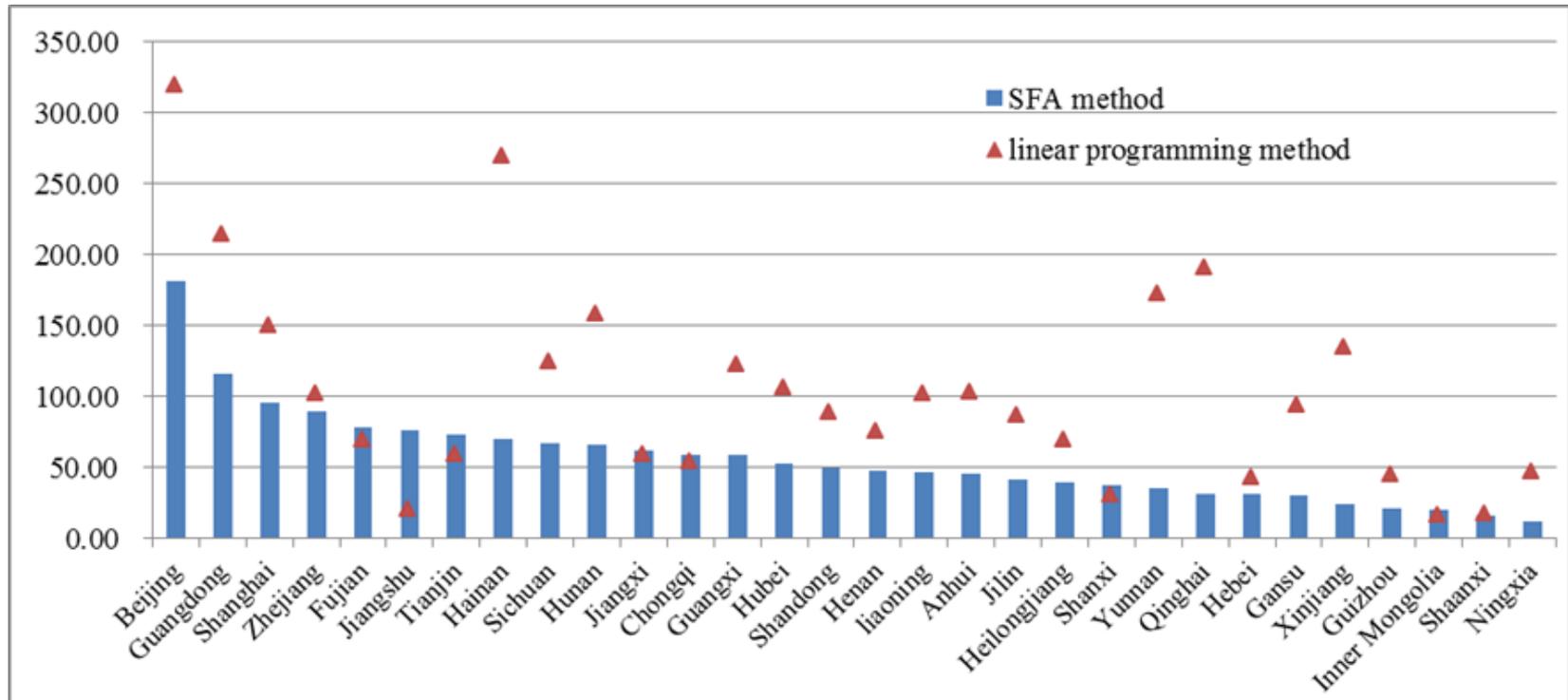


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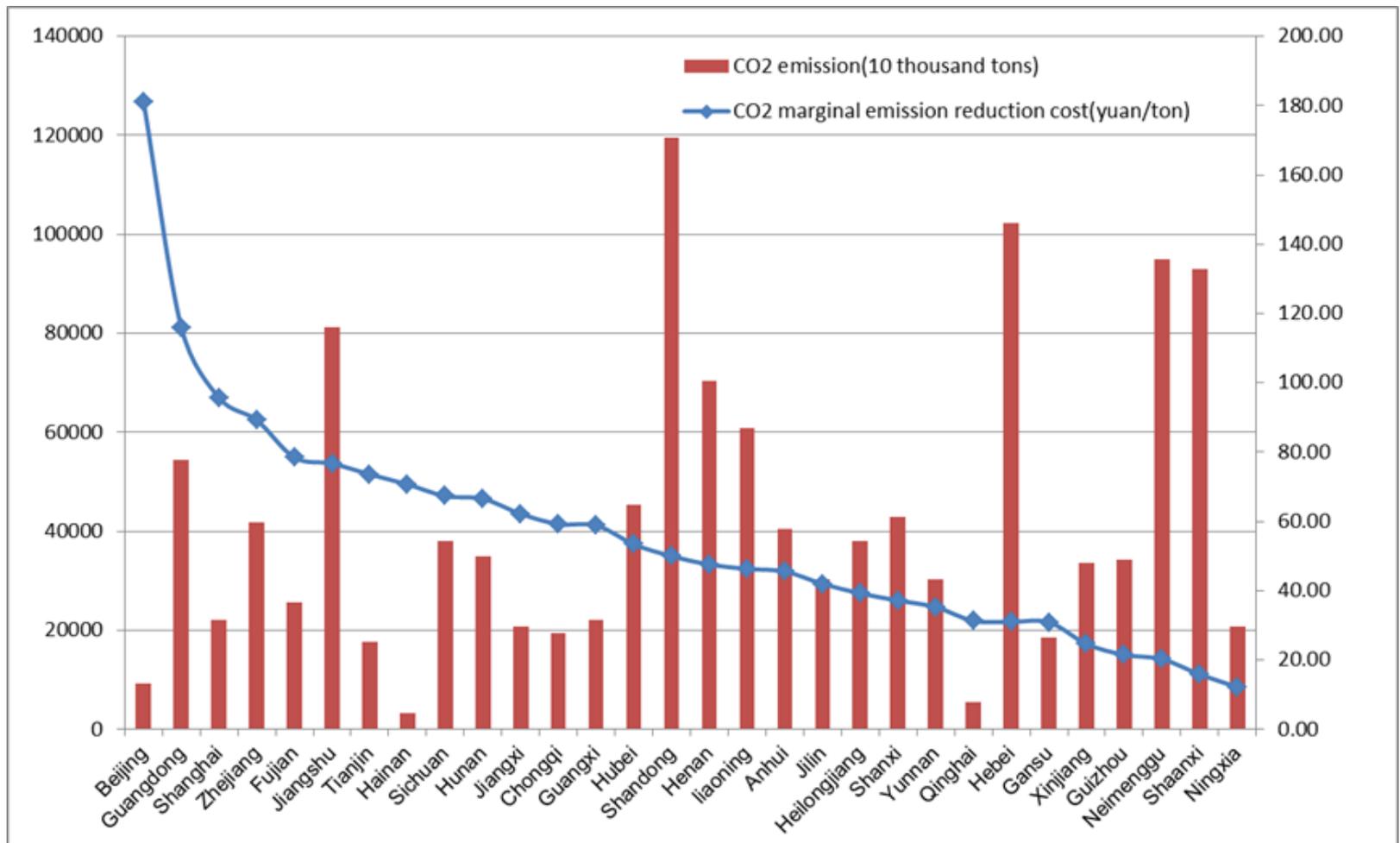
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Results

MAC of Chinese provinces



- MAC: ¥12.21/ton-¥181.1/ton
- The average result of MAC calculated by SFA method is 46% lower than LP method.



- There are no distinct correlation between CO2 emission and MAC.

Discussion

- Reliability Test of the MAC Results

(1) Is SFA necessary?

$$r^2 = \sigma_u^2 / \sigma^2 = 0.8.$$

80% of error was caused by random error.

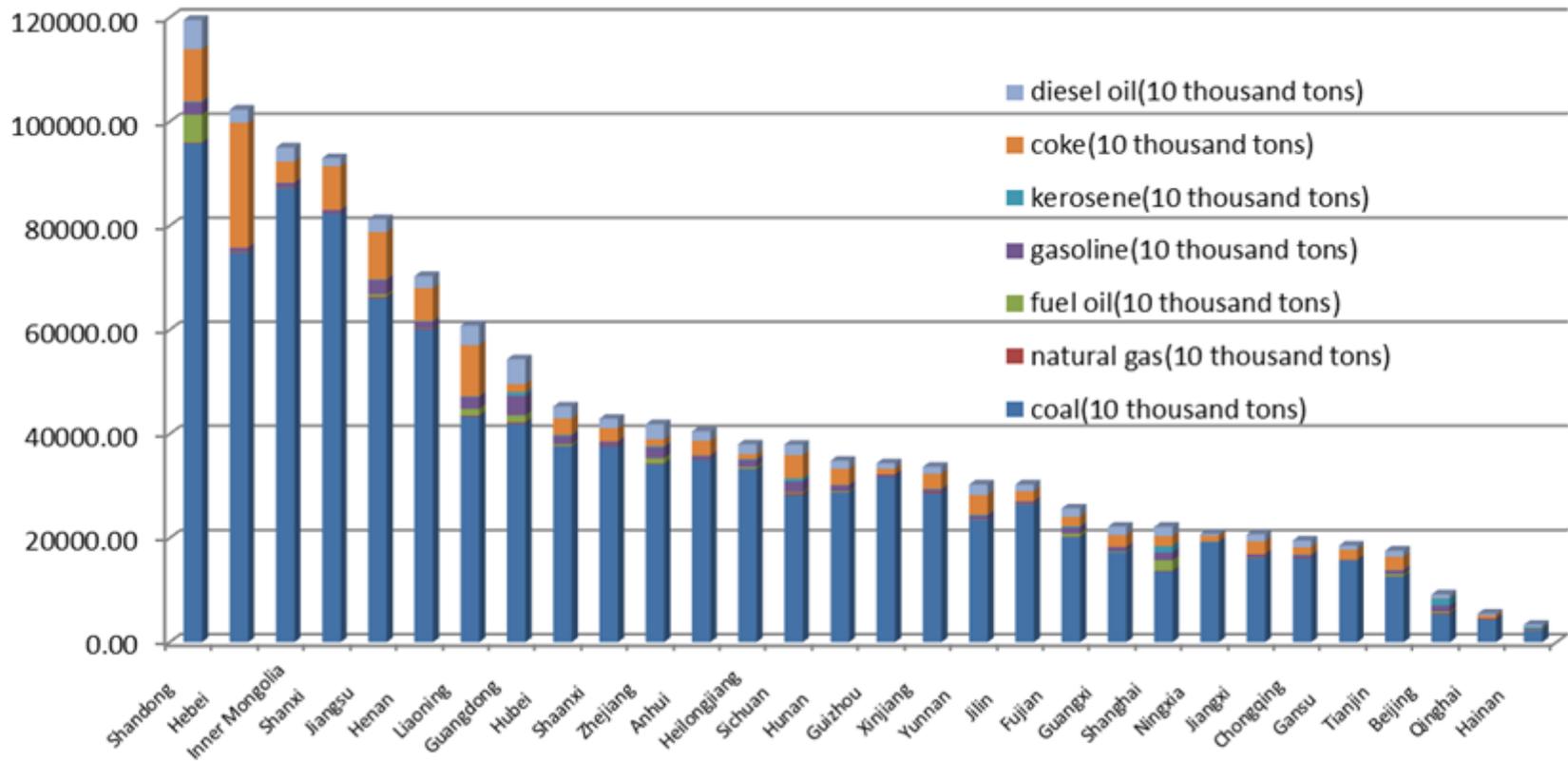
(2) Is DDF's coefficient reliable?

|t ratio| >
critical value

coefficient ⁺	coefficient value ⁺	T ratio ⁺
Γ_b ⁺	-0.038 ⁺	-1.825 ⁺
Γ_{bb} ⁺	0.068 ⁺	3.376 ⁺
η_k ⁺	-0.031 ⁺	-2.319 ⁺
η_l ⁺	-0.019 ⁺	-1.923 ⁺
η_s ⁺	0.008 ⁺	-7.082 ⁺

• Influence factor analysis of MAC

CO2 emission of Chinese provinces

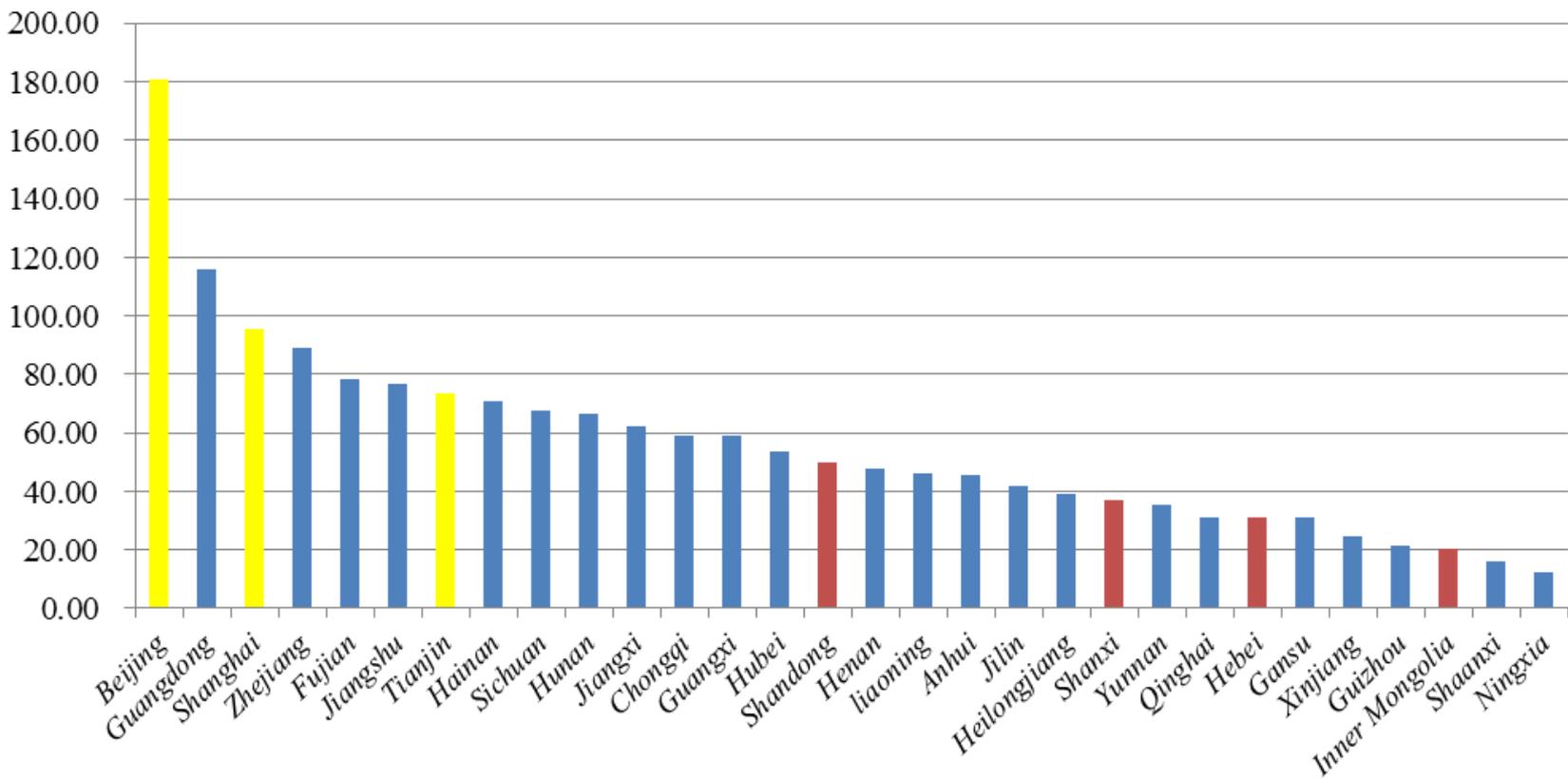


Energy Consumption Structures:

Coal: main emitter **used for:** power generation, production of building materials and domestic-use

Coke: Hebei, Shandong, Liaoning provinces **used for:** metal smelting

Fuel oil: Shandong, Shanghai, Zhejiang provinces **used for:** ship fuel



MAC of each Chinese provinces

Industrial Structures:

Beijing, Shanghai and Tianjin: The ratios of low-carbon industry in those provinces are more than half of total ratio of tertiary industry.

Shandong, Hebei, Shanxi and Inner Mongolia: the ratios of secondary industry of large emitters are more than 50%

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Conclusion

- (1) Applying SFA method, MAC results are precise but are 46% less than LP method in this paper as random errors were taken into concerned.
- (2) There are no distinct correlation between CO₂ emission and MAC.
- (3) Because of different industrial structures, and energy consumption structures among Chinese provinces, the CO₂ emission and MAC of each province varied.

Policy suggestions

- **Change energy consumption structures**

Coal is the main consumption energy . 68.4%

Natural Gas: 5% of total energy consumption

Clean Energy: 8% of total energy consumption

Hydro-power: Hubei, Sichuan and Yunnan

Wind power: Inner Mongolia, Hebei and Liaoning

Solar power: start-up Ningxia, Gansu, Xinjiang
and Tibet

- **Synergetic development in industry structure and economy among provinces**

(1) Economic development of low MACs provinces will be destructed if simply reduce CO₂ emission of those provinces.

(2) During the development, pollutions are transfer into the low MACs provinces while secondary industry is the leading industry in those provinces.



- Thank You!