

Detecting Mobility Patterns using Spatial Query Answering over Streams

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Introduction

Scenarios, Features, and Requirements

Overview Methods and Technology

Qualitative Evaluation

Conclusion and Future Work

Motivation - Cooperative-ITS

■ Cooperative-ITS Vision (C-ITS)

- Health & Safety by monitoring
- Efficient urban mobility by optimizations
- **Help autonomous cars**



V2X Overview [ETSI2010]

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■ Vehicle-to-X communication (V2X)

- Traffic participants exchange information as **V2X messages**
- Real time, simultaneously, and location based



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- Goal: Find “traffic patterns” by monitoring V2X messages in a complex and fast changing environment



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- **Goal:** Find **“traffic patterns”** by **monitoring V2X messages** in a complex and fast changing environment

- Use of a **spatial-stream database** for V2X messages, where a **C-ITS domain ontology** is build on top [Netten2013]



V2X Overview [ETSI2010]

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Three Scenarios - What are Patterns?

■ S1 - Traffic statistics:

1. Object level
2. Road/Lane level
3. **Intersection level**
4. Network level

■ S2 - Vehicle maneuvers:

1. Slow down or speed up
2. **Drive straight on, turn left, turn right**
3. Stop, unload, park
4. Lane change
5. Overtake, u-turn

■ S3 - Event detection:

1. Red-light violation
2. Obstructed view
3. **Accident**
4. Traffic rule violation
5. Traffic congestion



Vissim Traffic Simulation Luxembourg City

Feature	Details
F1: Time model	Point-based or interval-based model
F2: Process model	Push-based, pull-based, or combined queries
F3: Spatial relations	Point-set model, more detailed dim. ext. 9-Intersection model, or qualitative spatial reasoning (e.g. RCC8)
F4: Temporal relations	Linear temporal logic (LTL), Allen's time interval algebra, or Metric temporal logic (MTL)
F5: Numerical aggregations	Aggregations (e.g., sum) on a set or multiset (bag) of data items
F6: Spatial aggregations	Build geometric objects (e.g., paths) from more granular objects (e.g., points)
F7: Numerical predictions	Prediction of new data items (using e.g., linear regression)
F8: Trajectory predictions	Predict (possible) movements of vehicle (e.g., linear path)
F9: Geo matching	Match to geometric object
F10: Advanced	Graph connectivity, negation as failure, and repairs

Requirements Matrix

Case	F1	F2	F3	F4	F5	F6	F7	F8	F9	F10
S1.1	Po	Pull	N	N	Y	P	P	P	N	
S1.2	Po	Pull	Y	N	Y	Y	P	P	N	
S1.3	Po	Pull	Y	N	Y	Y	P	P	P	
S1.4	Int	Pull	Y	Y	Y	Y	Y	Y	P	CN
S2.1	Po	Pull	N	N	Y	P	P	N	N	
S2.2	Po	Pull	Y	N	Y	Y	P	Y	Y	
S2.3	Po	Pull	Y	P	Y	Y	Y	N	N	
S2.4	Po	Push	Y	N	Y	Y	P	P	P	
S2.5	Bo	Push	Y	N	Y	Y	Y	Y	P	
S3.1	Bo	Comb	Y	P	Y	Y	Y	Y	Y	
S3.2	Bo	Comb	Y	P	Y	Y	Y	Y	Y	
S3.3	Int	Comb	Y	Y	Y	Y	P	P	Y	NA
S3.4	Int	Comb	Y	Y	Y	Y	Y	Y	Y	NA, CN
S3.5	Int	Comb	Y	Y	Y	Y	Y	Y	Y	NA, CN

Legend:

- Y: required, N: not required, P: possibly required
- Po: point-based; Int: interval-based; Bo: Both possible
- Push: push-based; Pull: pull-based; Comb: combined
- NA: Negation as Failure; CN: graph connectivity

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- **Data model**: point-based (vs. interval-based) and valid time (vs. transaction time)
- A **data stream** is a triple $F = (\mathbb{T}, \nu, P)$:
 - **Timeline** \mathbb{T} , which is a *closed* interval of (\mathbb{N}, \leq)
 - Function $\nu : \mathbb{T} \rightarrow \mathcal{F}$ that assigns to each element of \mathbb{T} , data items (one ABox assertions) of a stream database $\mathcal{S}_{\mathcal{F}}$
 - **Pulse** P is the general interval of consecutive data items [Özçep2015]

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- **Example 1**: Timeline $\mathbb{T} = [0, 10]$ with two streams:

Stream of vehicles $F_1 = (\mathbb{T}, \nu, 1)$:

$\nu(0) = \{\text{speed}(c_1, 30), \text{pos}(c_1, (5, 5)), \text{speed}(b_1, 10), \text{pos}(b_1, (1, 1))\}$,

$\nu(1) = \{\text{speed}(c_1, 29), \text{pos}(c_1, (6, 5)), \text{speed}(b_1, 5), \text{pos}(b_1, (2, 1))\}$

$\nu(2) = \{\text{speed}(c_1, 34), \text{pos}(c_1, (7, 5))\}$

Stream of signal phases $F_2 = (\mathbb{T}, \nu, 3)$:

$\nu(0) = \{\text{hasState}(t_1, \text{Green})\}$, $\nu(3) = \{\text{hasState}(t_1, \text{Red})\}$, $\nu(6) =$

$\{\text{hasState}(t_1, \text{Green})\}$

- Extend CQ with **spatial** and **stream** atoms over a DL-Lite_A KB

- CQ have answer \mathbf{x} resp. existentially quantified \mathbf{y} variables

$$q(x, y) : \text{LaneIn}(x) \wedge \text{hasLocation}(x, u) \wedge \text{intersects}(u, v) \wedge \text{pos}_{(\text{line}, 4s)}(y, v) \\ \wedge \text{Vehicle}(y) \wedge \text{speed}_{(\text{avg}, 4s)}(y, r) \wedge (r > 30) \wedge \text{isManaged}(x, z) \\ \wedge \text{SignalGroup}(z) \wedge \text{hasState}_{(\text{first}, -4s)}(z, \text{Stop})$$

- We have our three types of atoms:

- $Q_{O_i}(\mathbf{x}, \mathbf{y})$: Q_{O_i} is a concept/role atom, unfold regarding \mathcal{T} of KB
- $Q_{S_j}(\mathbf{x}, \mathbf{y})$: Q_{S_j} is a spatial relation or a localization
- $Q_{F_k}(\mathbf{x}, \mathbf{y})$: Q_{F_k} is a stream atom

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- A **closer look** at stream atoms Q_{F_k} :

- $Q_{F_k}(\text{agr}, L)$: aggregate of last/next L time units (relative to query time)

- $Q_{F_k}(\text{agr}, O)$: aggregate of all previous L time units

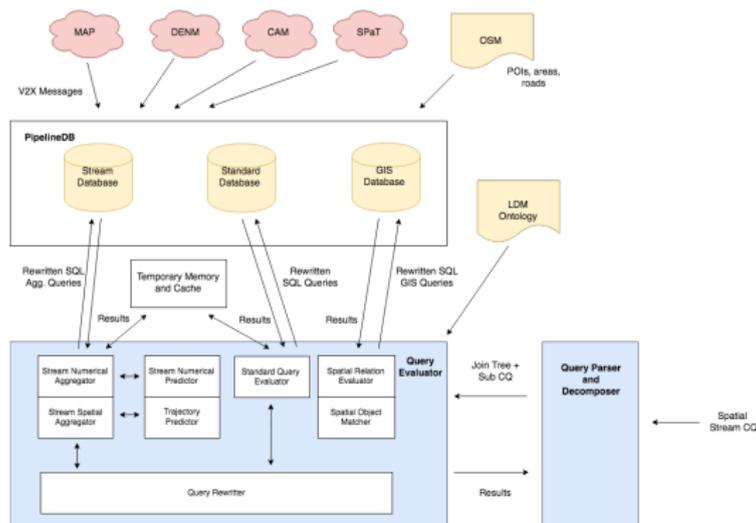
- $Q_{F_k}(\text{agr}, L, T)$: tuples that are between L and T (**historic data**)

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 - $Q_{F_k}(\text{agr}, L, T)$: tuples that are between L and T (**historic data**)
- **Aggregate function agr** can be:
 - **Numerical**: *count, min, max, sum, mean, sd*
 - **Prediction**: *linreg, loglinreg, polyreg* (simple models)
 - **Position**: *first, last*
 - **Spatial**: *point, line, angle, tree, area, **traject***

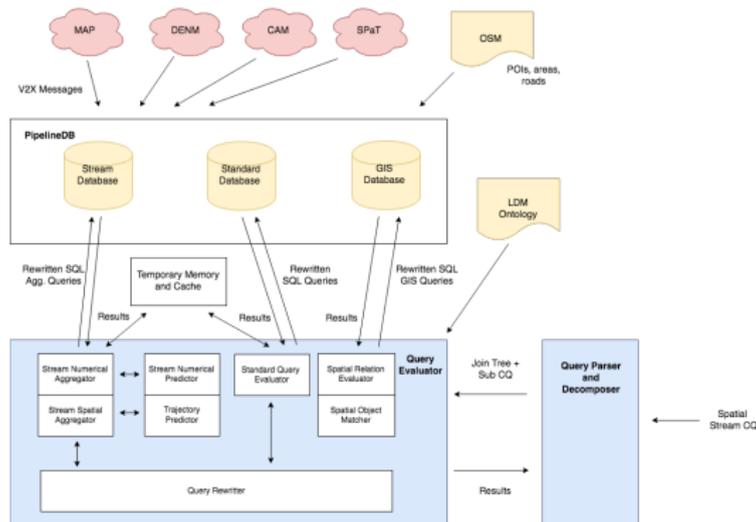
- Goal: Pull-based spatial-stream CQ in ontology-mediated QA
- Challenges:
 - How to **untangle different types** of query atoms?
 - **Clear semantics** for QA?
 - Evaluation on an RDBMS (detect red-light violations below 1s):
 - **LOGSPACE** data complexity
 - **Problems with aggregates** in DL-Lite_A:
 - Certain answers semantics → Intersection of answers over all possible models of the KB → **Empty models**

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- Solution:
 - Staging (in-memory): (1) **Stream detemporalization**, (2) **Standard rewriting**, (3) **Spatial evaluation**
 - **Hypertree decomposition** [Maier1983]
 - Stream Aggregation by *detemporalizing* stream atoms
 - **Epistemic Aggregate Queries (EAQ)** [Calvanese2008]

■ System architecture:



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■ Components:

- **Spatial-stream RDBMS:** PIPELINEDB
- **Query parser and decomposer:** hypertree decomposition (preprocessing)
- **Ontology evaluator:** OWLGRES 0.1 [Stocker2008] rewriting
- **Stream evaluator:** stream detemporalization by grouping and aggregation
- **Spatial evaluator:** evaluated using JTS TOPOLOGY SUITE

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- **Finished:**
 - **F3 - Spatial relations:** Point-set model done, RCC8 nice extension
 - **F5 - Numerical aggregations:** Fully done
 - **F6 - Spatial aggregations:** Implemented, specific aggregates (e.g., convex hull) missing

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- **F2 - Process model:** Pull-based queries done, push-based desired, but tricky with PIPELINEDB
- **F7 - Numerical predictions:** Linear regression done, other methods challenging, i.e., model building on top of streams
- **F8 - Trajectories:** Linear path extension done, but map matching (to a road graph) missing

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■ Open:

- **F4 - Temporal relations:** Not included yet (important for Scenario 3), LTL [Thost2015], MTL [Brandt2017], Allen's Time Interval Algebra extension for DL-Lite_A
- **F9/10 - Advanced:** Features (e.g., transitivity) go beyond DL-Lite_A and FO-rewritability, different language needed

- **Syntax:** Detect red-light violations by **vehicles** that **might speed above 30km/h**

$$q_1(x, y) : \text{LaneIn}(x) \wedge \text{hasLocation}(x, u) \wedge \text{intersects}(u, v) \wedge \text{pos}(y, v)[\text{traject}, -10] \\ \wedge \text{Vehicle}(y) \wedge \text{speed}(y, r)[\text{linreg}, \text{avg}, -10] \wedge (r > 30) \wedge \text{isManaged}(x, z) \\ \wedge \text{SignalGroup}(z) \wedge \text{hasState}(z, \text{Stop})[\text{first}, -5]$$

- **Sub queries:** **Count vehicles** that start at l_1 and **pass through** either l_2 or l_3

$$q_a(y, u) : \text{Vehicle}(y) \wedge \text{pos}(y, z, u)[\text{line}, 240] \wedge \text{intersects}(y, u) \wedge \text{hasGeo}(x, u) \\ \wedge \text{Intersection}(x) \wedge (x = l_1)$$

$$q_b(y) : \text{Vehicle}(y) \wedge \text{pos}(y, z, v)[\text{line}, 60] \wedge \text{intersects}(z, u) \wedge \text{hasGeo}(x, u) \\ \wedge \text{Intersection}(x) \wedge (x = l_2) \wedge \text{before}(u, v) \wedge q_a(w, u) \wedge (y = w)$$

$$q_c(y) : \text{Vehicle}(y) \wedge \text{pos}(y, z, v)[\text{line}, 60] \wedge \text{intersects}(y, u) \wedge \text{hasGeo}(x, u) \\ \wedge \text{Intersection}(x) \wedge (x = l_3) \wedge \text{before}(u, v) \wedge q_a(w, u) \wedge (y = w)$$

$$q_2(x, y) : q_b(x)[\text{count}, 60] \wedge q_c(y)[\text{count}, 60]$$

- **Matching:** **Count vehicles** that **might turn left/right** or **head-straight on**

$$q_a(x, y) : \text{Vehicle}(y) \wedge \text{pos}(y, z)[\text{traject}, -10] \wedge \text{match}(z, \text{Left}) \wedge \text{intersects}(z, u) \\ \wedge \text{hasGeo}(x, u) \wedge \text{Intersection}(x)$$

$$q_b(x, y) : \text{Vehicle}(y) \wedge \text{pos}(y, z)[\text{traject}, -10] \wedge \text{match}(z, \text{Straight}) \wedge \text{intersects}(z, u) \\ \wedge \text{hasGeo}(x, u) \wedge \text{Intersection}(x)$$

$$q_c(x, y) : \text{Vehicle}(y) \wedge \text{pos}(y, z)[\text{traject}, -10] \wedge \text{match}(z, \text{Right}) \wedge \text{intersects}(z, u) \\ \wedge \text{hasGeo}(x, u) \wedge \text{Intersection}(x)$$

$$q_3(z, u, v, w) : q_a(z, u)[\text{avg}, 60] \wedge q_b(z, v)[\text{avg}, 60] \wedge q_c(z, w)[\text{avg}, 60]$$

- **Order, long-term memory:** Detect **cars** that **perform an u-turn**

$$q_a(x, z) : \text{Car}(y) \wedge \text{pos}(x, y, z)[\text{line}, 30, 15] \wedge \text{match}(z, \text{Straight})$$

$$q_b(x, z) : \text{Car}(y) \wedge \text{pos}(x, y, z)[\text{line}, 15, 10] \wedge \text{match}(z, \text{Left})$$

$$q_c(x, z) : \text{Car}(y) \wedge \text{pos}(x, y, z)[\text{line}, 10, 5] \wedge \text{match}(z, \text{Left})$$

$$q_d(x, z) : \text{Car}(y) \wedge \text{pos}(x, y, z)[\text{line}, 5] \wedge \text{match}(z, \text{Straight})$$

$$q_4(x) : q_a(x, u) \wedge \text{before}(u, v) \wedge q_b(x, v) \wedge \text{before}(v, w) \wedge q_c(x, w) \wedge \text{before}(w, t) \wedge q_d(x, t)$$

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- Aim to extend spatial QA over streams to **detect mobility patterns**
- **Future work (short-term):**
 - **Push-based** queries → Allow a combination with **pull-based** queries
 - **Long-term memory** for patterns extracted from streams
 - Spatial matching that includes map matching for trajectories
 - **Optimizations** → Improved caching and “better” query rewriting
 - Bag semantics → **inconsistencies** in larger windows → Repairs
- **Future work (long-term):**
 - **Interval-based** data model → Temporal relations (Allen Time Interval Algebra)
 - Allow (spatial topological relations (RCC8) → Datalog-rewriting [Koubarakis2017])
 - **Statistical model** building on streams for predictions
 - Lift to **SPARQL**

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- 2 Calvanese, D., Giacomo, G.D., Lembo, D., Lenzerini, M., Rosati, R.: Tractable reasoning and efficient query answering in description logics: The *dl-lite* family. *J. Autom. Reasoning* 39(3), 385–429 (2007)
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- Has four **layers** of information:
 - **Highly dynamic** (e.g., sensing)
 - **Temporary regional** (e.g., weather, signal phases)
 - **Transient static** (e.g., topology)
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- Represented by a **spatial-stream database** for V2X messages, where a **C-ITS domain ontology** is build on top [Netten2013]

- Semantics for **spatial extension**: given in [Eiter2013]
- Semantics for **streaming**: Interpret the stream over the full \mathbb{T} , **point-based model**
- We define as a sequence $\mathcal{I}_F = (\mathcal{I}_i)_{\mathbb{T}_{\min} \leq i \leq \mathbb{T}_{\max}}$ of interpretations $\mathcal{I}_i = \langle \Delta^{\mathcal{I}}, \cdot^{\mathcal{I}_i} \rangle$
- Then \mathcal{I}_F is a model of $\mathcal{K}_{\mathcal{S}\mathcal{F}}$, such that $\mathcal{I}_F \models \mathcal{K}_{\mathcal{S}\mathcal{F}}$ iff $\mathcal{I}_i \models \mathcal{S}_{\mathcal{F}i}$ and $\mathcal{I}_i \models \mathcal{A}$, and $\mathcal{I}_i \models \mathcal{T}$, for all $i \in \mathbb{T}$.
- The **stream axioms** ($stream_F C$) and ($stream_F R$) are interpreted along the same line:

$$(stream_F C)^{\mathcal{I}} = \bigcap_{i \in \mathbb{T}} (\{e \in \Delta^{\mathcal{I}} \mid e \in C^{\mathcal{I}_i}\})$$

$$(stream_F R)^{\mathcal{I}} = \bigcap_{i \in \mathbb{T}} (\{(a_1, a_2) \mid (a_1, a_2) \in R^{\mathcal{I}_i}\})$$

- Only for **satisfiability** of the KB, no QA yet!

■ Example 2: EAQ with query time \mathbb{T}_3

$speed_{(avg, 4s)}(y, r)$ $pos_{(line, 4s)}(y, v)$ $hasState_{(first, -4s)}(z, m)$

(1) Windowed ABoxes:

$$\mathcal{A}_{\boxplus[0,3]} = \mathcal{A} \cup_{0 \leq i \leq 3} \mathcal{A}_i \text{ and } \mathcal{A}_{\boxplus[3,7]} = \mathcal{A} \cup_{3 \leq i \leq 7} \mathcal{A}_i$$

(2) Grouping:

q_{speed} : $G_{c_1} = \{|29, 30, 34|\}$ and $G_{b_1} = \{|10, 5|\}$ (or $G_{b_1} = \{|10, 5, 5|\}$?)

q_{pos} : $G_{c_1} = \{|(5, 5), (6, 5), (7, 5)|\}$ and $G_{b_1} = \{|(1, 1), (2, 1)|\}$

$q_{hasState}$: $G_{t_1} = \{|Red, Green|\}$

(3) Aggregation:

$avg(q_{speed}) = \{(c_1, 31), (b_1, 7.5), (t_1, 0)\}$

$line(q_{pos}) = \{(c_1, ((5, 5), (6, 5), (7, 5))), (b_1, ((1, 1), (2, 1)))\}$

$first(q_{hasState}) = \{(t_1, Red)\}$

■ Two semantics for data items validity!

■ Detemporalize stream atoms:

(1) Create windowed ABoxes:

$$\mathcal{A}_{\boxplus_k} = \mathcal{A} \cup \bigcup \{ \mathcal{A}_i \mid w_s \leq i \leq w_e \}, \text{ } w_s \text{ resp. } w_e \text{ is from } L \text{ and } \mathbb{T}_i$$

(2) Drop temporal order in $\mathcal{A}_{\boxplus_k} \rightarrow$ Bags (multisets) of data items \rightarrow Grouping of bags

(3) Eval aggregate functions on bags