

Lecture slides for
Automated Planning: Theory and Practice

Chapter 10

Control Rules in Planning

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Motivation

- Often, planning can be done much more efficiently if we have domain-specific information
- Example:
 - ◆ classical planning is EXPSPACE-complete
 - ◆ block-stacking can be done in time $O(n^3)$
- But we don't want to have to write a new domain-specific planning system for each problem!
- *Domain-configurable* planning algorithm
 - ◆ Domain-independent search engine (usually a forward state-space search)
 - ◆ Input includes domain-specific information that allows us to avoid a brute-force search
 - » Prevent the planner from visiting unpromising states

Motivation (Continued)

- If we're at some state s in a state space, sometimes a domain-specific test can tell us that
 - ◆ s doesn't lead to a solution, or
 - ◆ for any solution below s , there's a better solution along some other path
- In such cases we can to prune s immediately
- Rather than writing the domain-dependent test as low-level computer code, we'd prefer to talk directly about the planning domain
- One approach:
 - ◆ Write logical formulas giving conditions that states must satisfy; prune states that don't satisfy the formulas
- Presentation similar to the chapter, but not identical
 - ◆ Based partly on TLPlan [Bacchus & Kabanza 2000]

```
Abstract-search( $u$ )
  if Terminal( $u$ ) then return( $u$ )
   $u \leftarrow$  Refine( $u$ )           ;; refinement step
   $B \leftarrow$  Branch( $u$ )        ;; branching step
   $B' \leftarrow$  Prune( $B$ )        ;; pruning step
  if  $B' = \emptyset$  then return(failure)
  nondeterministically choose  $v \in B'$ 
  return(Abstract-search( $v$ ))
end
```

Quick Review of First Order Logic

- First Order Logic (FOL):
 - ◆ constant symbols, function symbols, predicate symbols
 - ◆ logical connectives ($\vee, \wedge, \neg, \Rightarrow, \Leftrightarrow$), quantifiers (\forall, \exists), punctuation
 - ◆ Syntax for formulas and sentences
 - $on(A,B) \wedge on(B,C)$
 - $\exists x on(x,A)$
 - $\forall x (ontable(x) \Rightarrow clear(x))$
- First Order Theory T :
 - ◆ “Logical” axioms and inference rules – encode logical reasoning in general
 - ◆ Additional “nonlogical” axioms – talk about a particular domain
 - ◆ Theorems: produced by applying the axioms and rules of inference
- Model: set of objects, functions, relations that the symbols refer to
 - ◆ For our purposes, a model is some state of the world s
 - ◆ In order for s to be a model, all theorems of T must be true in s
 - ◆ $s \models on(A,B)$ read “ s satisfies $on(A,B)$ ” or “ s models $on(A,B)$ ”
 - » means that $on(A,B)$ is true in the state s

Linear Temporal Logic

- Modal logic: FOL plus *modal operators*
to express concepts that would be difficult to express within FOL
- Linear Temporal Logic (LTL):
 - ◆ Purpose: to express a limited notion of time
 - » An infinite sequence $\langle 0, 1, 2, \dots \rangle$ of time instants
 - » An infinite sequence $M = \langle s_0, s_1, \dots \rangle$ of states of the world
 - ◆ Modal operators to refer to the states in which formulas are true:
 - $\bigcirc f$ - *next f* - f holds in the next state, e.g., $\bigcirc on(A,B)$
 - $\diamond f$ - *eventually f* - f either holds now or in some future state
 - $\square f$ - *always f* - f holds now and in all future states
 - $f_1 \cup f_2$ - *f_1 until f_2* - f_2 either holds now or in some future state, and f_1 holds until then
 - ◆ Propositional constant symbols TRUE and FALSE

Linear Temporal Logic (continued)

- Quantifiers cause problems with computability
 - ◆ Suppose $f(x)$ is true for infinitely many values of x
 - ◆ Problem evaluating truth of $\forall x f(x)$ and $\exists x f(x)$
- Bounded quantifiers
 - ◆ Let $g(x)$ be such that $\{x : g(x)\}$ is finite and easily computed
 - $\forall[x:g(x)] f(x)$
 - means $\forall x (g(x) \Rightarrow f(x))$
 - expands into $f(x_1) \wedge f(x_2) \wedge \dots \wedge f(x_n)$
 - $\exists[x:g(x)] f(x)$
 - means $\exists x (g(x) \wedge f(x))$
 - expands into $f(x_1) \vee f(x_2) \vee \dots \vee f(x_n)$

Models for LTL

- A model is a triple (M, s_i, v)
 - ◆ $M = \langle s_0, s_1, \dots \rangle$ is a sequence of states
 - ◆ s_i is the i 'th state in M ,
 - ◆ v is a *variable assignment* function
 - » a substitution that maps all variables into constants
- Write $(M, s_i, v) \models f$
to mean that $v(f)$ is true in s_i
- Always require that
$$(M, s_i, v) \models \text{TRUE}$$
$$(M, s_i, v) \models \neg \text{FALSE}$$

Examples

- Suppose $M = \langle s_0, s_1, \dots \rangle$

$(M, s_0, v) \models \bigcirc\bigcirc \text{on}(A, B)$ means A is on B in s_2

- Abbreviations:

$(M, s_0) \models \bigcirc\bigcirc \text{on}(A, B)$ no free variables, so v is irrelevant:
 $M \models \bigcirc\bigcirc \text{on}(A, B)$ if we omit the state, it defaults to s_0

- Equivalently,

$(M, s_2, v) \models \text{on}(A, B)$ same meaning with no modal operators
 $s_2 \models \text{on}(A, B)$ same thing in ordinary FOL

- $M \models \square \neg \text{holding}(C)$

◆ in every state in M , we aren't holding C

- $M \models \square(\text{on}(B, C) \Rightarrow (\text{on}(B, C) \cup \text{on}(A, B)))$

◆ whenever we enter a state in which B is on C , B remains on C until A is on B .

Where We're Going

- Basic idea:
 - ◆ TLPLAN does a forward search, using LTL to do pruning tests
 - ◆ Input includes a current state s , and a **control formula** f written in LTL
 - » If f isn't satisfied, then s is unacceptable \Rightarrow backtrack
 - » Else keep going
- We'll need to augment LTL to include a way to refer to goal states
 - ◆ Include a GOAL operator such that $\text{GOAL}(f)$ means f is true in every goal state
 - ◆ $((M, s_i, V), g) \models \text{GOAL}(f)$ iff $(M, s_i, V) \models f$ for every $s_i \in g$
- Next, some examples of control formulas

Example: Blocks World

unstack(x,y)

Precond: $on(x,y)$, $clear(x)$, $handempty$

Effects: $\neg on(x,y)$, $\neg clear(x)$, $\neg handempty$,
 $holding(x)$, $clear(y)$

stack(x,y)

Precond: $holding(x)$, $clear(y)$

Effects: $\neg holding(x)$, $\neg clear(y)$,
 $on(x,y)$, $clear(x)$, $handempty$

pickup(x)

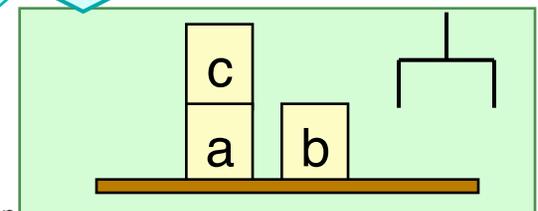
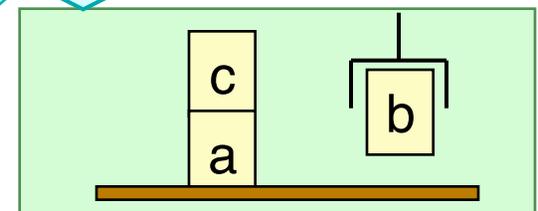
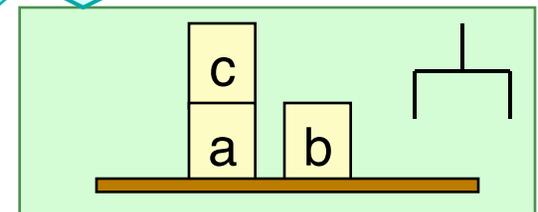
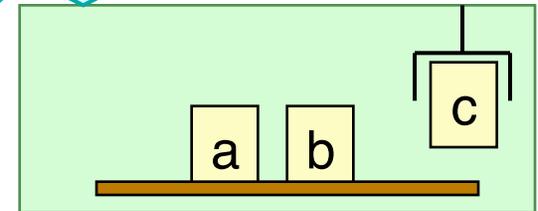
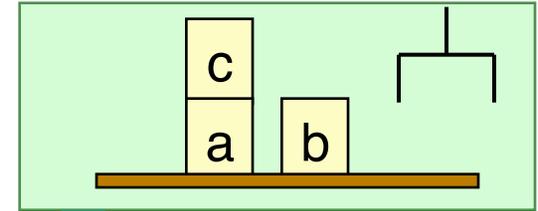
Precond: $ontable(x)$, $clear(x)$, $handempty$

Effects: $\neg ontable(x)$, $\neg clear(x)$,
 $\neg handempty$, $holding(x)$

putdown(x)

Precond: $holding(x)$

Effects: $\neg holding(x)$, $ontable(x)$,
 $clear(x)$, $handempty$



Supporting Axioms

- Want to define conditions under which a stack of blocks will never need to be moved
- If x is the top of a stack of blocks, then we want $goodtower(x)$ to hold if
 - ◆ x doesn't need to be anywhere else
 - ◆ None of the blocks below x need to be anywhere else
- Definitions to support this:
 - ◆ $goodtower(x) \Leftrightarrow clear(x) \wedge \neg GOAL(holding(x)) \wedge goodtowerbelow(x)$
 - ◆ $goodtowerbelow(x) \Leftrightarrow$

$$[ontable(x) \wedge \neg \exists[y:GOAL(on(x,y))]]$$

$$\vee \exists[y:on(x,y)] \{ \neg GOAL(ontable(x)) \wedge \neg GOAL(holding(y))$$

$$\wedge \neg GOAL(clear(y)) \wedge \forall[z:GOAL(on(x,z))] (z = y)$$

$$\wedge \forall[z:GOAL(on(z,y))] (z = x) \wedge goodtowerbelow(y) \}$$
 - ◆ $badtower(x) \Leftrightarrow clear(x) \wedge \neg goodtower(x)$

Blocks World Example (continued)

Three different control formulas:

(1) Every goodtower must always remain a goodtower:

$$\square \left(\forall [x:clear(x)] goodtower(x) \Rightarrow \bigcirc (clear(x) \vee \exists [y:on(y, x)] goodtower(y)) \right)$$

(2) Like (1), but also says never to put anything onto a badtower:

$$\square \left(\forall [x:clear(x)] goodtower(x) \Rightarrow \bigcirc (clear(x) \vee \exists [y:on(y, x)] goodtower(y)) \right. \\ \left. \wedge badtower(x) \Rightarrow \bigcirc (\neg \exists [y:on(y, x)]) \right)$$

(3) Like (2), but also says never to pick up a block from the table unless you can put it onto a goodtower:

$$\square \left(\forall [x:clear(x)] goodtower(x) \Rightarrow \bigcirc (clear(x) \vee \exists [y:on(y, x)] goodtower(y)) \right. \\ \wedge badtower(x) \Rightarrow \bigcirc (\neg \exists [y:on(y, x)]) \\ \left. \wedge (ontable(x) \wedge \exists [y:GOAL(on(x, y))] \neg goodtower(y)) \right. \\ \left. \Rightarrow \bigcirc (\neg holding(x)) \right)$$

Outline of How TLPlan Works

- Recall that TLPlan's input includes a current state s , and a control formula f written in LTL
 - ◆ How can TLPlan determine whether there exists a sequence of states M beginning with s , such that $M \models f$?
- We can compute a formula f^+ such that for every sequence $M = \langle s, s^+, s^{++}, \dots \rangle$,
 - ◆ $M \models f^+$ iff $M^+ = \langle s^+, s^{++}, \dots \rangle$ satisfies f^+
 - ◆ f^+ is called the **progression** of f through s
- If $f^+ = \text{FALSE}$ then no M^+ can satisfy f^+
 - ◆ Thus no M can satisfy f , so TLPlan can backtrack
- Otherwise, need to determine whether there is an M^+ that satisfies f^+
 - ◆ For every child s^+ of s , call TLPlan recursively on s^+ and f^+
- How to compute the progression of f through s ?

Procedure Progress(f, s)

Case

1. f contains no temporal operators:

$$f^+ := \text{TRUE if } s \models f, \text{ FALSE otherwise.}$$

2. $f = f_1 \wedge f_2$: $f^+ := \text{Progress}(f_1, s) \wedge \text{Progress}(f_2, s)$

3. $f = \neg f_1$: $f^+ := \neg \text{Progress}(f_1, s)$

4. $f = \bigcirc f_1$: $f^+ := f_1$

5. $f = f_1 \cup f_2$: $f^+ := \text{Progress}(f_2, s) \vee (\text{Progress}(f_1, s) \wedge f)$

6. $f = \diamond f_1$: $f^+ := \text{Progress}(f_1, s) \vee f$

7. $f = \square f_1$: $f^+ := \text{Progress}(f_1, s) \wedge f$

8. $f = \forall[x:\gamma(x)] f_1$: $f^+ := \bigwedge_{i=1,\dots,n} \text{Progress}(f_i, s)$

9. $f = \exists[x:\gamma(x)] f_1$: $f^+ := \bigvee_{i=1,\dots,n} \text{Progress}(f_i, s)$

where $\{c_1, \dots, c_n\} = \{x : s \models \gamma(x)\}$, and $f_i = f$ with x replaced by c_i

Boolean simplification rules:

1. $[\text{FALSE} \wedge \phi \mid \phi \wedge \text{FALSE}] \mapsto \text{FALSE}$,

3. $\neg \text{TRUE} \mapsto \text{FALSE}$,

2. $[\text{TRUE} \wedge \phi \mid \phi \wedge \text{TRUE}] \mapsto \phi$,

4. $\neg \text{FALSE} \mapsto \text{TRUE}$.

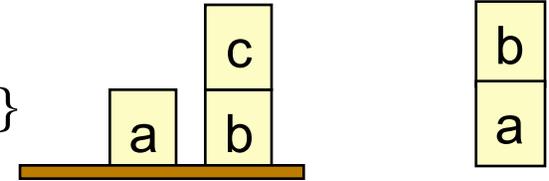
Examples

- Suppose $f = \square \text{on}(a,b)$
 - ◆ $f^+ = \text{Progress}(\text{on}(a,b), s) \wedge \square \text{on}(a,b)$
 - ◆ If $\text{on}(a,b)$ is true in s then
 - » $f^+ = \text{TRUE} \wedge \square \text{on}(a,b)$
 - » simplifies to $\square \text{on}(a,b)$
 - ◆ If $\text{on}(a,b)$ is false in s then
 - » $f^+ = \text{FALSE} \wedge \square \text{on}(a,b)$
 - » simplifies to FALSE
- Summary:
 - ◆ \square generates a test on the current state
 - ◆ If the test succeeds, \square propagates it to the next state

Examples (continued)

- Suppose $f = \Box(on(a,b) \Rightarrow Oclear(a))$
 - ◆ $f^+ = \text{Progress}[\Box(on(a,b) \Rightarrow Oclear(a)), s]$
 - ◆ $= \text{Progress}[on(a,b) \Rightarrow Oclear(a), s] \wedge \Box(on(a,b) \Rightarrow Oclear(a))$
 - ◆ If $on(a,b)$ is true in s , then
 - » $f^+ = clear(a) \wedge \Box(on(a,b) \Rightarrow Oclear(a))$
 - Since $on(a,b)$ is true in s , s^+ must satisfy $clear(a)$
 - The “always” constraint is propagated to s^+
 - ◆ If $on(a,b)$ is false in s , then
 - » $f^+ = \Box(on(a,b) \Rightarrow Oclear(a))$
 - The “always” constraint is propagated to s^+

Example

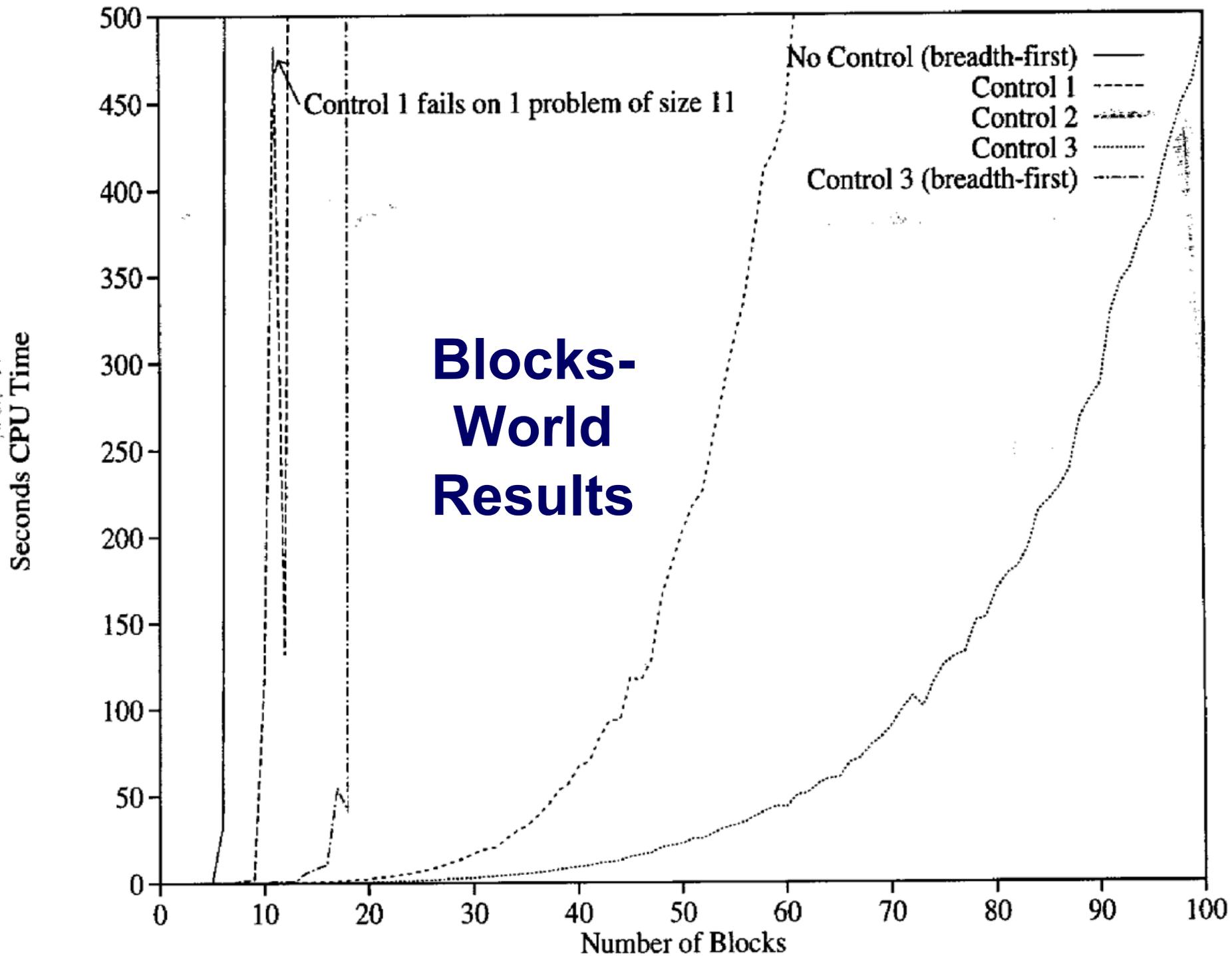


- $s = \{ontable(a), ontable(b), clear(a), clear(c), on(c,b)\}$
- $g = \{on(b, a)\}$
- $f = \Box \forall [x:clear(x)] \{(ontable(x) \wedge \neg \exists [y:GOAL(on(x,y))]) \Rightarrow O \neg holding(x)\}$
 - ◆ never pick up a block x if x is not required to be on another block y
- $f^+ = Progress(f,s) \wedge f$
- $Progress(f,s)$
 - = $Progress(\forall [x:clear(x)] \{(ontable(x) \wedge \neg \exists [y:GOAL(on(x,y))]) \Rightarrow O \neg holding(x)\},s)$
 - = $Progress((ontable(a) \wedge \neg \exists [y:GOAL(on(a,y))]) \Rightarrow O \neg holding(a)),s)$
 - $\wedge Progress((ontable(b) \wedge \neg \exists [y:GOAL(on(b,y))]) \Rightarrow O \neg holding(b)),s)$
 - = $\neg holding(a) \wedge TRUE$
- $f^+ = \neg holding(a) \wedge TRUE \wedge f$
 - = $\neg holding(a) \wedge$
 - $\Box \forall [x:clear(x)] \{(ontable(x) \wedge \neg \exists [y:GOAL(on(x,y))]) \Rightarrow O \neg holding(x)\}$

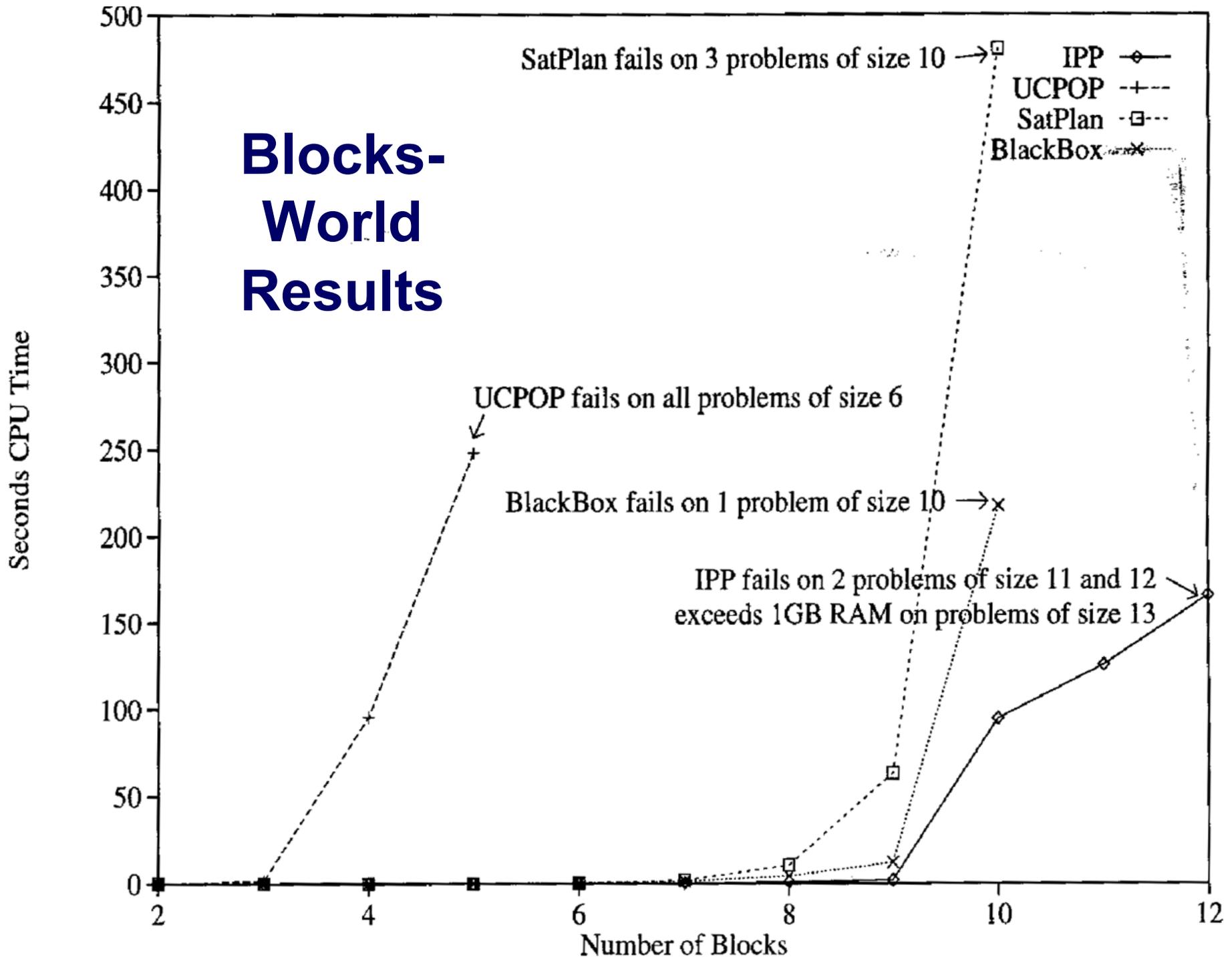
Pseudocode for TLPlan

- Nondeterministic forward search
 - ◆ Input includes a control formula f for the current state s
 - ◆ When we expand a state s , we progress its formula f through s
 - ◆ If the progressed formula is false, s is a dead-end
 - ◆ Otherwise the progressed formula is the control formula for s 's children

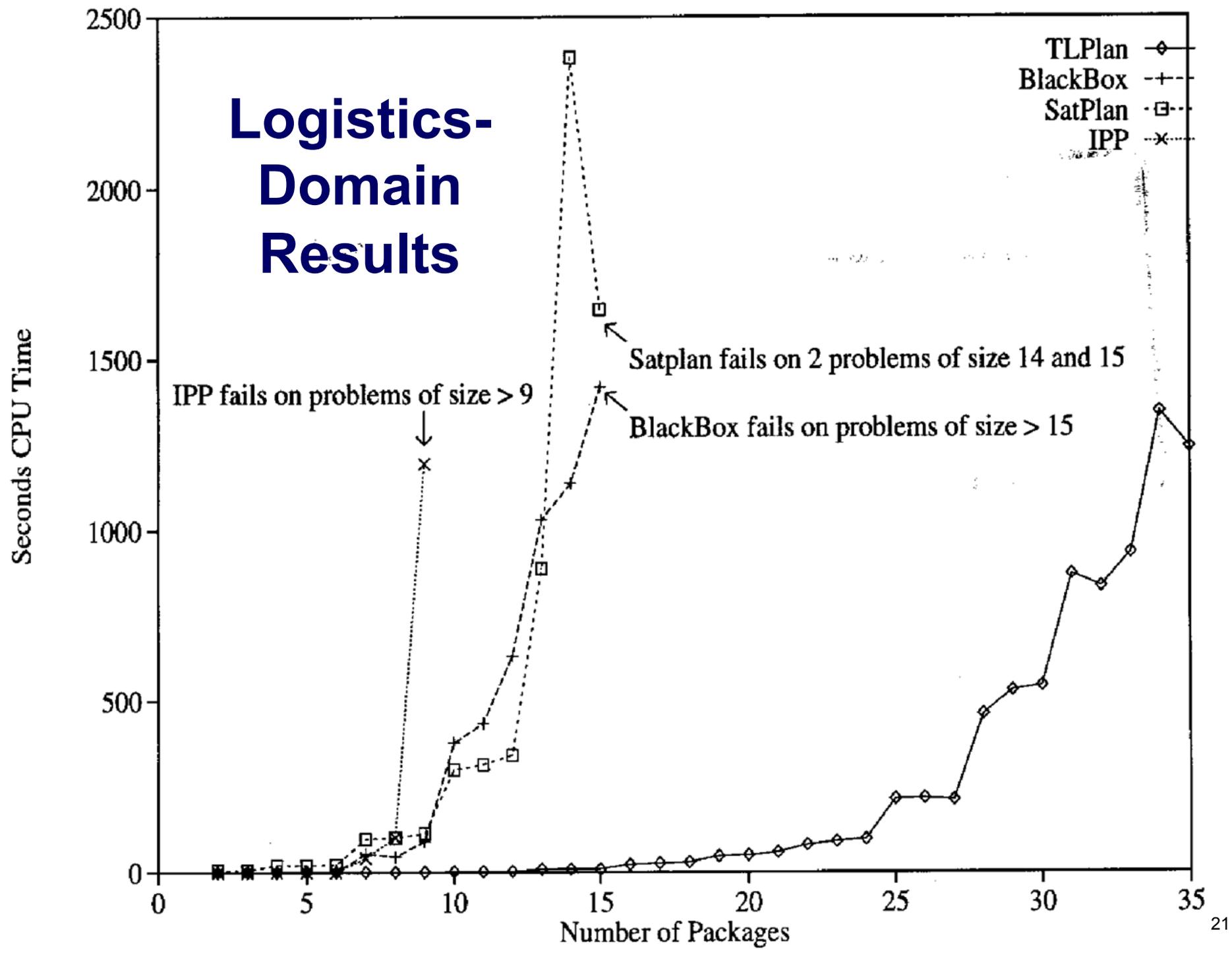
```
Procedure TLPlan ( $s, f, g, \pi$ )  
   $f^+ \leftarrow \text{Progress}(f, s)$   
  if  $f^+ = \text{FALSE}$  then return failure  
  if  $s$  satisfies  $g$  then return  $\pi$   
   $A \leftarrow \{\text{actions applicable to } s\}$   
  if  $A = \text{empty}$  then return failure  
  nondeterministically choose  $a \in A$   
   $s^+ \leftarrow \gamma(s, a)$   
  return TLPlan ( $s^+, f^+, g, \pi.a$ )
```



Blocks-World Results



Logistics-Domain Results



Discussion

- 2000 International Planning Competition
 - ◆ TALplanner: same kind of algorithm, different temporal logic
 - » received the top award for a “hand-tailored” (i.e., domain-configurable) planner
- TLPlan won the same award in the 2002 International Planning Competition
- Both of them:
 - ◆ Ran several orders of magnitude faster than the “fully automated” (i.e., domain-independent) planners
 - » especially on large problems
 - ◆ Solved problems on which the domain-independent planners ran out of time/memory