

# g-BDI: a graded intentional agent model for practical reasoning

–an application of the fuzzy modal approach to uncertainty reasoning–

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# Outline

- Introduction: BDI agent architectures and multi-context systems
- Background on the fuzzy logic approach to reasoning about uncertainty
- The g-BDI agent model
- A case study
- Concluding remarks

## (Software) Agent theories and architectures

- **Theory:** a specification of an agent behaviour (properties it should satisfy)
  - **The intentional stance** (Dennet, 87)

*The behaviour can be predicted by ascribing certain mental attitudes e.g. beliefs, desires and rational acumen*

- **Architecture:** software engineering model, middle point between specification and implementation (Wooldridge, 2001):
  - Logic-based: deliberative agents
  - Reactive: reactive agents
  - Layered: hybrid agents
  - **Practical reasoning: BDI agents**

*an explicitly representation of the agent's beliefs (B), desires (D) and intentions (I).*

## BDI agent models

The BDI agent model is based on M. Bratman's theory of *human practical reasoning* (reasoning to decide what and how to do), also referred to as Belief-Desire-Intention, or BDI:

- Intention and desire are both pro-attitudes (mental attitudes concerned with action), but intention is distinguished as a conduct-controlling pro-attitude: Intention = Desire + Commitment.

Several logical models to define and reason about BDI agents, e.g.

- Rao and Georgeff's BDI-CTL logic (1991) combines a multi-modal logic (with modalities representing beliefs, desires and intentions) with the temporal logic CTL\*.
- Wooldridge (2000) has extended BDI-CTL to define LORA (the Logic Of Rational Agents), by incorporating an action logic, also allowing to reason about interaction in a multi-agent system.

## g-BDI: a graded BDI agent model

Based on (Parsons et al., 98), we have proposed the **g-BDI model** that allows to specify agent architectures able to deal with the **environment uncertainty** and with **graded mental (informational and proactive) attitudes**.

- **Belief degrees** represent to what extent the agent believes a formula is true.
- **Degrees of positive or negative desires** allow the agent to set different ideal levels of preference or rejection respectively.
- **Intention degrees** also refer to preference but take into account the cost/benefit trade-off of reaching an agent's goal.

### Working assumption

- Agents having different kinds of behavior can be modeled on the basis of the representation and interaction of these three attitudes.

# Multi-Context Systems (Giunchiglia et al.)

MCSs exploits the idea of locality in reasoning and contain two basic components: **contexts** and **bridge rules**

A MCS is defined as  $\langle \{C_i\}_{i \in I}, \Delta_{br} \rangle$ ,

where

- Each context  $C_i$  is specified by
  - a logic  $\langle L_i, A_i, \Delta_i \rangle$  where,  $L_i$ : language,  $A_i$ : axioms and  $\Delta_i$ : inference rules
  - a theory  $T_i \subseteq L_i$ , encoding the available knowledge to  $C_i$
- $\Delta_{br}$  is a set of bridge rules, i.e. rules of inference with premises and conclusions in different contexts

$$\frac{C_1 : \psi, C_2 : \varphi}{C_3 : \theta}$$

The deduction mechanism of a MCS is then based on the interplay between inter-context  $\Delta_i$  and intra-context  $\Delta_{br}$  deductions

## g-BDI: a multi-context system based specification

A g-BDI agent is defined as a Multi-context System (MCS):

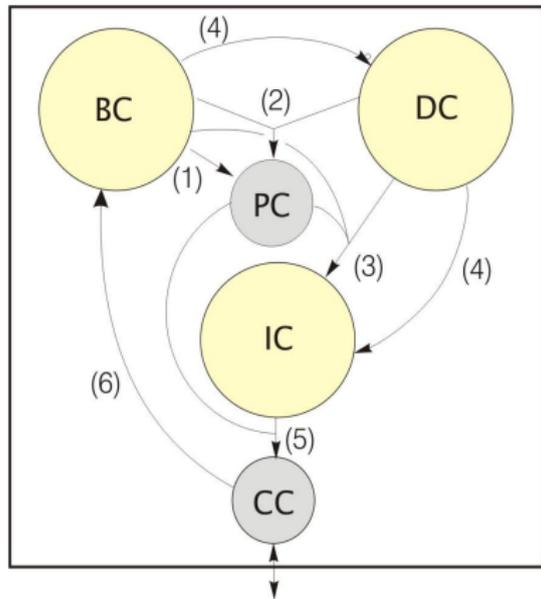
$$A_g = (\{BC, DC, IC, PC, CC\}, \Delta_{br})$$

where:

- The **mental contexts** represent: beliefs (BC), desires (DC) and intentions (IC).
- Two **functional contexts** are used for: Planning (PC) and Communication (CC).
- A suitable set of **bridge rules** ( $\Delta_{br}$ ) encode a particular pattern of interaction between Bs, Ds and Is

*Such a MCS specification has advantages both from a logical and a software engineering perspectives (use of different logics, clear separation, modularity and efficiency, etc.)*

# g-BDI: a multi-context system based specification



Bridge Rule (5)

$$\frac{IC : (I_{\alpha_b}\varphi, i_{max}), PC : bestplan(\varphi, \alpha_b, P, A, c)}{CC : C(does(\alpha_b))}$$

## g-BDI: graded logical framework

To represent and reason about the different graded mental attitudes in the g-BDI agent model, we use a **fuzzy modal approach** (Hájek et al.).

- *the belief / desire / intention degree of a Boolean proposition is considered as the truth-degree of a fuzzy (modal) proposition.*
- the algebraic semantics of different fuzzy logics can be used to characterize different models of measures.

This approach provides a uniform, quite powerful and flexible logical framework.

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- Introduction: BDI agent architectures and multi-context systems
- Background on the fuzzy logic approach to reasoning about uncertainty
  - Fuzzy logic treatment of uncertainty
  - Probability logics
  - Possibilistic logics
- The g-BDI agent model
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# Graded representation of uncertainty

When belief is a matter of degree ...

**B**: set of events (**Boolean algebra**)

logical setting:  $\mathbf{B} = \mathcal{L} / \equiv$

events as propositions (mod. logical equivalence)

$\top$  always true event,

$\perp$  always false event

Uncertainty, belief measures  $\mu : \mathcal{L} \rightarrow [0, 1]$

$\mu(\varphi)$ : quantifies an agent's confidence/belief on  $\varphi$  being true

$$(1) \mu(\top) = 1, \mu(\perp) = 0$$

$$(2) \mu(\varphi) \leq \mu(\psi), \text{ if } \models \varphi \rightarrow \psi$$

$$(3) \mu(\varphi) = \mu(\psi), \text{ if } \models \varphi \equiv \psi$$

Fuzzy measures (Sugeno) or Plausibility measures (Halpern)

# Uncertainty measures: some classes of interest

## (Finitely additive) Probability measures

**Finite additivity:**  $P(\varphi \vee \psi) = P(\varphi) + P(\psi)$ , whenever  $\vdash \neg(\varphi \wedge \psi)$

- $P(\neg\varphi) = 1 - P(\varphi)$  (auto-dual)

## Extension to conditional probabilities:

$P : \mathcal{L} \times \mathcal{L}^0 \rightarrow$  is a (coherent) conditional probability (De Finetti, Coletti and Scozzafava, ...):

- $P(\varphi | \varphi) = 1$ , for all  $\varphi \in \mathcal{L}^0$
- $P(\cdot | \varphi)$  is a (finitely additive) probability for any  $\varphi \in \mathcal{L}^0$
- $P(\chi \wedge \psi | \varphi) = P(\chi | \varphi) \cdot P(\psi | \chi \wedge \varphi)$ , for all  $\psi \in \mathcal{L}$  and  $\varphi, \chi \wedge \varphi \in \mathcal{L}^0$ .

# Uncertainty measures: some classes of interest

## Possibility and Necessity measures

**Possibility:**  $\Pi(\varphi \vee \psi) = \max(\Pi(\varphi), \Pi(\psi))$

**Necessity:**  $N(\varphi \wedge \psi) = \min(N(\varphi), N(\psi))$

Dual pairs of measures  $(N, \Pi)$ : when  $\Pi(\varphi) = 1 - N(\neg\varphi)$

Representation in terms of **possibility distributions**

$$\pi : \Omega \rightarrow [0, 1]$$

$\pi(w) = 1$ :  $w$  is totally plausible / preferred

$\pi(w) < \pi(w')$ :  $w$  is less plausible / preferred than  $w'$

$\pi(w) = 0$ :  $w$  is impossible / rejected

$$N(\varphi) = \inf_{\omega \not\models \varphi} 1 - \pi(\omega) \quad \Pi(\varphi) = \sup_{\omega \models \varphi} \pi(\omega)$$

**Guaranteed possibility:**  $\Delta(\varphi) = \inf_{\omega \models \varphi} \pi(\omega)$       min. level of satisfaction

# Framing uncertainty reasoning in fuzzy modal theories

After P. Hájek (truth-degrees  $\neq$  belief degrees!):

- for each crisp proposition  $\varphi$ , introduce a modality **P**

**$P\varphi$**  reads e.g. “ $\varphi$  is probable”

- $P\varphi$  is a **gradual, fuzzy proposition**: the higher is the probability of  $\varphi$ , the truer is  $P\varphi$
- for  $\varphi$  a two-valued, crisp proposition one can define e.g.

$$\text{truth-value}(P\varphi) = \text{probability}(\varphi)$$

(which is different from  $\text{truth-value}(\varphi) = \text{probability}(\varphi)$ !!! )

# Framing uncertainty reasoning in fuzzy modal theories

**Crucial observation:** laws and computations with probability (and many other measures) can be expressed by well-known fuzzy logic truth-functions on  $[0, 1]$ .

$$\begin{aligned} \text{Prob}(\varphi \vee \psi) &= \text{Prob}(\varphi) + \text{Prob}(\psi) - \text{Prob}(\varphi \wedge \psi) \\ &= \text{Prob}(\varphi) \oplus (\text{Prob}(\psi) \ominus \text{Prob}(\varphi \wedge \psi)) \end{aligned}$$

$$\text{Prob}(\varphi \wedge \psi) = \text{Prob}(\varphi) \cdot \text{Prob}(\psi \mid \varphi)$$

$$\text{Nec}(\varphi \wedge \psi) = \min(\text{Nec}(\varphi), \text{Nec}(\psi))$$

$$\text{Pos}(\varphi \vee \psi) = \max(\text{Pos}(\varphi), \text{Pos}(\psi))$$

**Idea:** axioms of different uncertainty measures on  $\varphi$ 's to be encoded as *axioms of suitable fuzzy logic theories* over the  $P\varphi$ 's

# Main systems of fuzzy logic

Extensions of Hájek's BL, whose standard semantics are given by the three outstanding t-norms:

**Lukasiewicz logic:**  $\mathbf{L} = \text{BL} + \neg\neg\varphi \equiv \varphi$

- $e(\varphi \&_{\mathbf{L}} \psi) = \max(0, e(\varphi) + e(\psi) - 1)$   
 $e(\varphi \rightarrow_{\mathbf{L}} \psi) = \min(1, 1 - e(\varphi) + e(\psi))$

**Gödel logic:**  $\mathbf{G} = \text{BL} + \varphi \& \psi \equiv \varphi$

- $e(\varphi \&_{\mathbf{G}} \psi) = \min(e(\varphi), e(\psi))$   
 $e(\varphi \rightarrow_{\mathbf{G}} \psi) = 1$  if  $e(\varphi) \leq e(\psi)$ ,  $e(\varphi \rightarrow_{\mathbf{G}} \psi) = e(\psi)$  otherwise

**Product logic:**  $\mathbf{\Pi} = \text{BL} + (\Pi 1), (\Pi 2)$

- $e(\varphi \&_{\mathbf{\Pi}} \psi) = e(\varphi) \cdot e(\psi)$   
 $e(\varphi \rightarrow_{\mathbf{\Pi}} \psi) = \min(1, e(\psi)/e(\varphi))$

**Lukasiewicz-Product logic:**  $\mathbf{L\Pi}_{\frac{1}{2}} = \mathbf{L} + \mathbf{\Pi} + \text{few additional axioms}$

# Definable connectives and truth functions

## Connective

## Definition

## Truth function

$\neg_{\mathcal{L}}\varphi$	$\varphi \rightarrow_{\mathcal{L}} \bar{0}$	$1 - x$
$\varphi \oplus \psi$	$\neg_{\mathcal{L}}\varphi \rightarrow_{\mathcal{L}} \psi$	$\min(1, x + y)$
$\varphi \ominus \psi$	$\varphi \& \neg_{\mathcal{L}}\psi$	$\max(0, x - y)$
$\varphi \equiv_{\mathcal{L}} \psi$	$(\varphi \rightarrow_{\mathcal{L}} \psi) \& (\psi \rightarrow_{\mathcal{L}} \varphi)$	$1 -  x - y $
$\varphi \wedge \psi$	$\varphi \& (\varphi \rightarrow_{\mathcal{L}} \psi)$	$\min(x, y)$
$\varphi \vee \psi$	$(\varphi \rightarrow_{\mathcal{L}} \psi) \rightarrow_{\mathcal{L}} \psi$	$\max(x, y)$
$\Delta\varphi$	$\neg_{\mathcal{N}}\neg_{\mathcal{L}}\varphi$	$\begin{cases} 1, & \text{if } x = 1 \\ 0, & \text{otherwise} \end{cases}$
$\neg_{\mathcal{N}}\varphi$	$\varphi \rightarrow_{\mathcal{N}} \bar{0}$	$\begin{cases} 1, & \text{if } x = 0 \\ 0, & \text{otherwise} \end{cases}$

## A simple probability logic (HEG, 95), (Hájek, 98)

A two-level language:

- (i) **Non-modal formulas:**  $\varphi, \psi$ , etc. , built from a set  $V$  of propositional variables  $\{p_1, p_2, \dots, p_n, \dots\}$  using the classical binary connectives  $\wedge$  and  $\neg$ . The set of non-modal formulas will be denoted by  $\mathcal{L}$ .
  
- (ii) **Modal formulas:**  $\Phi, \Psi$ , etc. are built:
  - from elementary modal formulas  $P\varphi$ , with  $\varphi \in \mathcal{L}$
  - using Lukasiewicz logic  $\mathbb{L}$  connectives: ( $\&_{\mathbb{L}}, \rightarrow_{\mathbb{L}}$ ) and rational truth constants  $\bar{r}$

Examples of FP- formulas:  $\overline{0.8} \rightarrow_{\mathbb{L}} P(\varphi \wedge \chi)$ ,  $P(\neg\varphi) \rightarrow_{\mathbb{L}} P(\chi)$ ,

Examples of non FP-formulas:  $\varphi \rightarrow_{\mathbb{L}} P\psi$ ,  $\overline{0.5} \rightarrow_{\mathbb{L}} P(P\varphi \wedge \chi)$

# The logic $FP(CPC, RPL)$ : axiomatization

- The set  $Taut(\mathcal{L})$  of CPC tautologies
- Axioms of **Rational Pavelka logic** (Łukasiewicz logic + rational truth-constants) for modal formulas
- **Probabilistic axioms:**
  - (FP1)  $P(\varphi \rightarrow \psi) \rightarrow_{\perp} (P\varphi \rightarrow_{\perp} P\psi)$
  - (FP2)  $P(\varphi \vee \psi) \equiv (P\varphi \rightarrow_{\perp} P(\varphi \wedge \psi)) \rightarrow_{\perp} P\psi$   
or equiv.  $P(\varphi \vee \psi) \equiv P\varphi \oplus (P\psi \ominus P(\varphi \wedge \psi))$
  - (FP3)  $P(\neg\varphi) \equiv \neg_{\perp} P(\varphi)$
- Deduction rules of  $FP(CPC, RPL)$  are *modus ponens* for  $\rightarrow_{\perp}$  and (-) *necessitation* for  $P$ : from  $\varphi$  derive  $P\varphi$

## The logic $FP(CPC, RPL)$ : Semantics

**Semantics:** (weak) Probabilistic Kripke models  $M = (W, e, \mu)$

- $e : W \times Var \rightarrow \{0, 1\}$
- $\mu : \mathcal{U} \subseteq 2^W \rightarrow [0, 1]$  probability s.t. the sets  
 $[\varphi] = \{w \in W \mid \|\varphi\|_{M,w} = 1\}$  are  $\mu$ -measurable
- atomic modal formulas:  $\|P\varphi\|_M = \mu([\varphi])$
- compound modal formulas:  $\|\Phi\|_{M,w}$  is computed from atomic using Łukasiewicz connectives

$M = (W, e, \mu)$  is a model of  $\Phi$  if for any  $w \in W$ ,  $\|\Phi\|_{M,w} = 1$   
(if  $\Phi$  modal, it does not depend on  $w$ , only on  $\mu$ )

**Completeness of  $FP(CPC, RPL)$ :** If  $T$  finite,  $T \vdash_{FP} \Phi$  iff  $T \models_{FP} \Phi$

**Pavelka-style:**  $\sup\{r \mid T \vdash_{FP} \bar{r} \rightarrow_L \Phi\} = \inf\{\|\Phi\|_M \mid M \text{ model of } T\}$

## $FP(CPC, RPL)$ : a two-level framework

$$P\varphi \equiv_{\mathcal{L}} \overline{0.3}, \quad P(\varphi \wedge \psi) \rightarrow_{\mathcal{L}} P\chi, \quad \overline{0.6} \rightarrow_{\mathcal{L}} P(\psi \vee \varphi), \dots$$

uncertainty

Łukasiewicz

---

events

CPC

$$\neg(\psi \wedge \chi), \quad \varphi \wedge \psi \rightarrow \chi, \quad \varphi \vee (\psi \rightarrow \chi), \dots$$

## Generalization to other two-level logics

### Fuzzy modal-like logics $FM(L_1, L_2)$

- $L_1$ : logic of events, e.g. CPC, S5, Dynamic logic, Deontic logic, ...
- $L_2$ : suitable fuzzy logic able to capture the corresponding intensional modality (probability, preference, belief, etc.)

Properties of  $FM(L_1, L_2)$  obviously depend on those of  $L_1$  and  $L_2$

### Some examples:

- conditional probability logic:  $FP(CPC, \perp\Pi_{\frac{1}{2}})$ ,
- belief function logic:  $FP(S5, \perp\Pi_{\frac{1}{2}})$
- possibilistic logics:  $FN(CPC, G)$ ,
- graded deontic logics:  $FP(SDL, RPL)$ ,  $FN(SDL, G)$
- ...

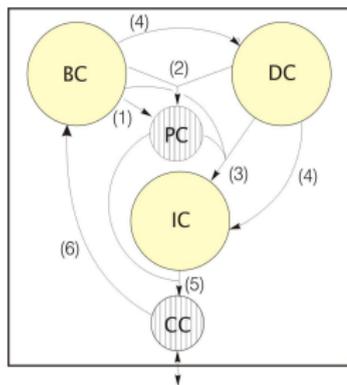
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- Introduction: BDI agent architectures and multi-context systems
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- Belief context
- Desire Context
- Intention Context
- Bridge rules
- Operational elements



- A case study
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# The Belief Context

The purpose of this context is to model the **agent's beliefs about the environment**.

To represent knowledge related to action execution, we use Propositional Dynamic logic, PDL, (Fischer and Ladner, 79), as the base propositional logic

To account for the uncertainty on action execution, a probability-based approach and a necessity-based approach have been considered:

- $BC_{nec} = FN(PDL, G_{\Delta}(C))$  (strong standard completeness)
- $BC_{prob} = FP(PDL, RPL)$  (Pavelka-style completeness)

Typically, a theory will contain:

- **quantitative formulas:**  $(B[\alpha]\varphi, 0.6)$  a shorthand for  $\overline{0.6} \rightarrow_{\perp} B[\alpha]\varphi$   
–the agent believes that the probability of  $\varphi$  being true after performing action  $\alpha$  is at least 0.6–
- **qualitative formulas:**  $B[\alpha]\varphi \rightarrow_{\perp} B[\beta]\varphi$

## The Belief Context: $BC_{prob}$

### Language:

- start from a PDL propositional language  $\mathcal{L}_{PDL}$  built from a set of actions  $\Pi$ .
- introduce a belief operator  $B$ : if  $\Phi \in \mathcal{L}_{PDL}$  then  $B\Phi$  is a B-formula  
 $P[\alpha]\varphi := \text{“}\varphi \text{ is believed to be true after performing } \alpha\text{”}$
- combine B-formulas with RPL connectives

**Semantics:** given by probabilistic Kripke structures:

$$\mathcal{M} = \langle W, \{R_\alpha : \alpha \in \Pi\}, e, \mu \rangle$$

where  $\langle W, \{R_\alpha : \alpha \in \Pi\}, e \rangle$  is a regular Kripke model of PDL, and  $\mu : F \rightarrow [0, 1]$  is a probability on a Boolean algebra  $F \subseteq 2^W$

- $\|B\varphi\|_{\mathcal{M}} = \mu(\{w \in W \mid e(\varphi, w) = 1\})$

**Axiomatics:** PDL axioms + RPL axioms + (FP1), (FP2), (FP3)

**Pavelka-style completeness**

# The Desire Context

The DC represents the agent's desires.

- Desires represent the *ideal agent's preferences*, regardless of the agent's current world and regardless of the cost involved in actually achieving them.
- Using the possibilistic approach to **bipolar representation of preferences** (Benferhat et al.) one can provide a formal account of :
  - **(graded) positive desires**: what the agent would like to be the case.
  - **(graded) negative desires**: restrictions or rejections over the possible worlds it can reach.
  - **indifference**

# The Desire Context

## The Language $\mathcal{L}_{DC}$

- We start from a basic propositional language  $\mathcal{L}$ .
- To represent positive and negative desires over formulae of  $\mathcal{L}$ , we introduce two modal operators  $D^+$  and  $D^-$ .

$D^+\varphi :=$  “ $\varphi$  is positively desired”

$D^-\varphi :=$  “ $\varphi$  is negatively desired ” (or “ $\varphi$  is rejected”).

- We use RPL to reason about modal formulas:
  - If  $\varphi \in \mathcal{L}$  then  $D^+\varphi, D^-\varphi \in \mathcal{L}_{DC}$
  - If  $r \in \mathbb{Q} \cap [0, 1]$  then  $\bar{r} \in \mathcal{L}_{DC}$
  - If  $\Phi, \Psi \in \mathcal{L}_{DC}$  then  $\Phi \rightarrow_{\mathbb{L}} \Psi \in \mathcal{L}_{DC}$  and  $\neg_{\mathbb{L}}\Phi \in \mathcal{L}_{DC}$

Notation:  $(D^+\psi, r)$  will stand for  $\bar{r} \rightarrow_{\mathbb{L}} D^+\psi$

# The Desire Context

## Semantics - Intuition

- degrees of desire: a conservative approach

minimum satisfaction / rejection levels

- the degree of (positive / negative) desire for a disjunction of goals  $\varphi \vee \psi$  is taken to be the minimum of the degrees for  $\varphi$  and  $\psi$ .

This is basically the characterizing property of the **guaranteed possibility measures** (Dubois-Prade et al.)

- the satisfaction degree of reaching both  $\varphi$  and  $\phi$  can be strictly greater than reaching one of them separately. *The same for negative desires.*

# The Desire Context

**Semantics:** intended models for  $\mathcal{L}_{DC}$  are Kripke-like structures  $\mathcal{M} = \langle W, e, \pi^+, \pi^- \rangle$ , *Bipolar Desire models*, where:

- $\pi^+ : W \rightarrow [0, 1]$  and  $\pi^- : W \rightarrow [0, 1]$  are positive and negative preference distributions over worlds.

$\pi^+(w) = 1$	full satisfaction	$\pi^-(w) = 1$	full rejection
$0 < \pi^+(w) < 1$	partial satisfaction	$0 < \pi^-(w) < 1$	partial rejection
$\pi^+(w) = 0$	indifference (nothing in favour)	$\pi^-(w) = 0$	indifference (nothing against)

- $\|D^+\varphi\|_{\mathcal{M}} = \inf\{\pi^+(w') \mid e(\varphi, w') = 1\}$   
 $\|D^-\varphi\|_{\mathcal{M}} = \inf\{\pi^-(w') \mid e(\varphi, w') = 1\}$
- $e$  is extended to compound modal formulae by means of the usual truth-functions for Łukasiewicz connectives.

$\mathcal{M} \models \Phi$  and  $T \models_{\mathcal{M}} \Phi$  as usual.

# The Desire Context

We define the *Basic logic for DC* (DC logic) as follows:

## Axioms and rules:

(CPC) Axioms and rules of classical logic for non-modal formulas

(RPL) Axioms and rules of Rational Pavelka logic for modal formulas

$$(DC^+) \quad D^+(\varphi \vee \psi) \equiv_{\mathbf{L}} D^+\varphi \wedge_{\mathbf{L}} D^+\psi$$

$$(DC^-) \quad D^-(\varphi \vee \psi) \equiv_{\mathbf{L}} D^-\varphi \wedge_{\mathbf{L}} D^-\psi$$

Introduction of  $D^+$  and  $D^-$  for implications:

$$(ID^+) \text{ from } \varphi \rightarrow \psi \text{ derive } D^+\psi \rightarrow_{\mathbf{L}} D^+\varphi$$

$$(ID^-) \text{ from } \varphi \rightarrow \psi \text{ derive } D^-\psi \rightarrow_{\mathbf{L}} D^-\varphi.$$

## Soundness and Completeness

The above axiomatization is correct with respect to the defined semantics and is complete as well for finite theories of modal formulas.

# The Desire Context

Encoding different types of desires in a DC theory: some examples

Suppose María looks for possible touristic destinations matching her preferences:

- She likes beach and mountain destinations, beach is a bit more preferred  
 $(D^+ beach, 0.8)$ ,  $(D^+ mountain, 0.7)$   
 $D^+ mountain \rightarrow_{\perp} D^+ beach$
- She is totally indifferent to destinations with or without a zoo  
 $\neg_{\perp} D^+ zoo$ ,  $\neg_{\perp} D^+ \neg zoo$   
 $\neg_{\perp} D^- zoo$ ,  $\neg_{\perp} D^- \neg zoo$
- She does not want to travel with bus.  
 $(D^- bus, 0.9)$
- She likes the train but she is a bit afraid of possible delays. Anyway, she does not discard the train, but the plane would be preferable.  
 $(D^+ train, 0.5)$ ,  $(D^+ \neg train, 0.2)$ ,  $\neg_{\perp} D^- train$   
 $D^+ train \rightarrow_{\perp} D^+ plane$

# The Desire Context

## Too much freedom?

For some classes of problems we may want to restrict the allowed assessments of degrees of positive and negative desires.

- Different axiomatic extensions can be proposed to show how different consistency constraints can be added to the basic DC logic, both at the semantical and syntactical levels, while preserving completeness.
- One think of such extensions as modelling different types of agents.

## DC<sub>1</sub> Schema

It may be natural in some domain applications to forbid to simultaneously positively (negatively) desire  $\varphi$  and  $\neg\varphi$

These constraints amount to require in the intended models:

- $\min(\|D^+\varphi\|_M, \|D^+\neg\varphi\|_M) = 0$ , and
- $\min(\|D^-\varphi\|_M, \|D^-\neg\varphi\|_M) = 0$

At the level of Kripke structures, this corresponds to:

- $\inf_{w \in W} \pi^+(w) = 0$ , and
- $\inf_{w \in W} \pi^-(w) = 0$

At the syntactic level, this is captured by :

$$(DC1^+) \quad \neg_{\perp}(D^+\varphi \wedge_{\perp} D^+(\neg\varphi))$$

$$(DC1^-) \quad \neg_{\perp}(D^-\varphi \wedge_{\perp} D^-(\neg\varphi))$$

## DC<sub>2</sub> Schema

The logical schema DC<sub>1</sub> does not put any restriction on positive and negative desires for a same goal.

Benferhat et al.'s coherence condition: An agent cannot desire to be in a world more than the level at which it is tolerated, i.e. not rejected.

Translated to our framework, it amounts to require:

- $\forall w \in W, \pi^+(w) \leq 1 - \pi^-(w)$

This captured at the syntactical level by:

$$(DC_2) \quad \neg_{\perp}(D^+\varphi \otimes D^-\varphi)$$

where  $\otimes$  is Łukasiewicz strong conjunction.

## DC<sub>3</sub> Schema

An stronger consistency condition between positive and negative preferences may be considered:

If an agent rejects (desires) to be in a world to some extent, it cannot be positively desired (rejected) at all

At the semantical level, this amounts to require:

$$\min(\pi^+(w), \pi^-(w)) = 0$$

At the syntactic level:

$$(DC3) \quad (D^+\varphi \wedge_L D^-\varphi) \rightarrow_L \bar{0}$$

# The Intention Context

## From Desires to Intentions

In the g-BDI agent model, positive and negative desires are used as pro-active and restrictive elements respectively in order to set up intentions.

- intentions cannot depend just on the satisfaction of reaching a goal  $\varphi$  (represented by  $D^+\varphi$ ) but also on the state of the world and the cost of transforming it into a world where the formula  $\varphi$  is true.
- a graded representation allows us to define the **strength of an intention as a measure of the cost/benefit relationship of the feasible actions** the agent can take toward the intended goal.

# Intention context

## Language $\mathcal{L}_{IC}$ :

- Elementary modal formulae  $I_\alpha\varphi$ , where  $\alpha \in \Pi^0 \subset \Pi$  (finite)  
*The truth-degree of  $I_\alpha\varphi$  will represent the strength the agent intends  $\varphi$  by means of the execution of the particular action  $\alpha$ .*  
- intended semantics: trade-off between preference and cost –
- $\mathcal{L}_{IC}$  formulas are built from  $Var_{cost} = \{c_\alpha\}_{\alpha \in \Pi^0}$  and elementary modal formulae  $I_\alpha\varphi$ , using **Rational Łukasiewicz logic** (Gerla, 01) connectives .

## Intention context

**Semantics:** intended models will be enlarged Kripke structures

$M = \langle W, e, \pi^+, \pi^-, \{\pi_\alpha\}_{\alpha \in \Pi^0} \rangle$  where  $\pi_\alpha : W \times W \rightarrow [0, 1]$  is a *utility* distribution corresponding to  $\alpha$

$\pi_\alpha(w, w')$ : *utility degree of applying  $\alpha$  to transform world  $w$  into world  $w'$ .*

- $e(w, I_\alpha \varphi) = \inf \{ \pi_\alpha(w, w') \mid w' \in W, e(w', \varphi) = 1 \}$

### Additional axioms and rules

1. (DC) axiom for  $I_\alpha$  modalities:  $I_\alpha(\varphi \vee \psi) \equiv_{\mathcal{L}} I_\alpha \varphi \wedge_{\mathcal{L}} I_\alpha \psi$
2. introduction of  $I_\alpha$  for implications: from  $\varphi \rightarrow \psi$  derive  $I_\alpha \psi \rightarrow_{\mathcal{L}} I_\alpha \varphi$  for each  $\alpha \in \Pi^0$

### Theorem

Let  $T$  be a finite theory of modal formulas and  $\Phi$  a modal formula. Then  $T \vdash_{IC} \Phi$  iff  $T \models_{\mathcal{M}_{IC}} \Phi$ .

# Intention context

## A particular semantics

Intended semantics:  $e(w, I_\alpha\varphi)$  = trade-off between the degree of ideal preference (positive desire) of  $\varphi$  and  $1 -$  the cost of achieving  $\varphi$  by performing  $\alpha$  at  $w$ .

**Example:** assume we take Rational Łukasiewicz logic (Gerla) to reason about modal formulas ( $\text{Ł logic} + \delta_n$ 's). Then consider the additional axiom:

$$I_\alpha\varphi \equiv_{\text{Ł}} \delta_2 D^+\varphi \oplus \delta_2 c_\alpha$$

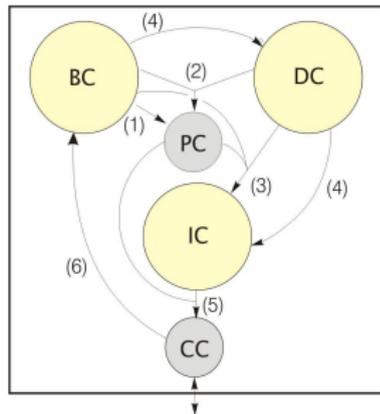
This axiom is valid in extended structures  $M = \langle W, e, \pi^+, \{\pi_\alpha\}_{\alpha \in \Pi^0} \rangle$  iff

$$\pi_\alpha(w, w') = \pi^+(w') + 1 - e(w, c_\alpha)$$

... but bridge rules offer a lot of flexibility ...

# Bridge Rules

Bridge rules allow to embed results from a theory into another, they are part of the deduction mechanism of the g-BDI agent.



Intention generation rule:

$$BR(3) \quad \frac{DC : (D^+ \varphi, d), \quad BC : (B[\alpha] \varphi, r), \quad PC : fplan(\varphi, \alpha, P, A, c)}{IC : (I_\alpha \varphi, f(d, r, c))}$$

$$f(d, r, c) = r \cdot (w_d d + w_c (1 - c))$$

## Bridge Rules

Other bridge rules that can be used:

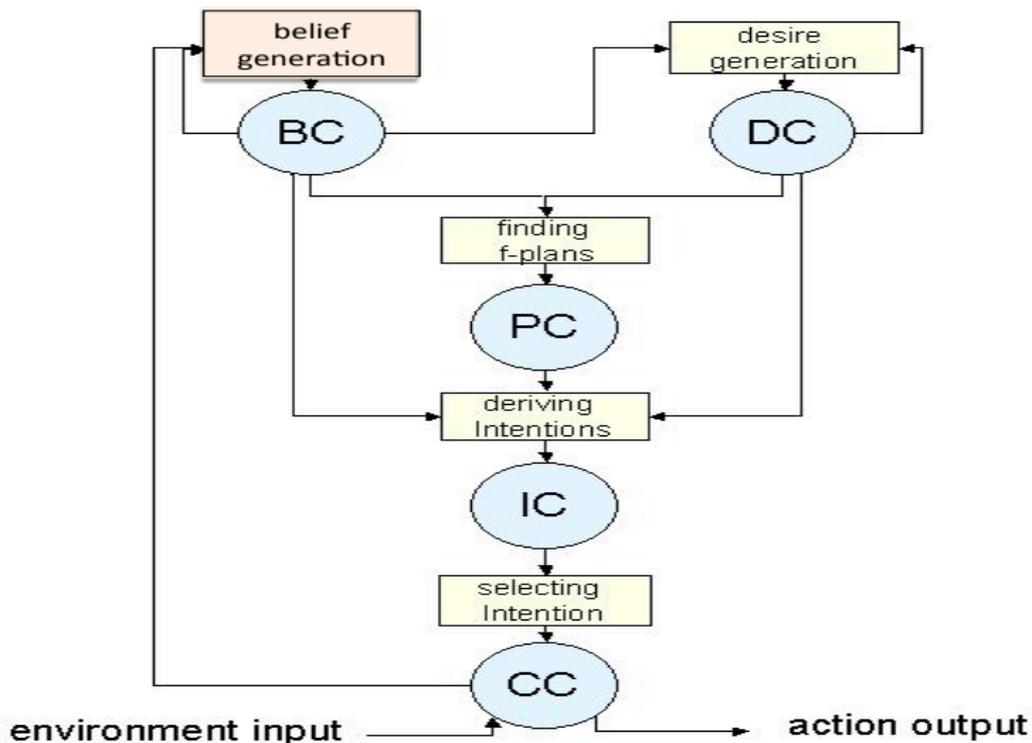
- Bridge rules to represent realism relations between mental attitudes (Cohen and Levesque), e.g.

$$\frac{BC : \neg B\varphi}{DC : \neg D^+\varphi} \quad \frac{DC : \neg D^+\varphi}{IC : \neg I\varphi}$$

- Bridge rules to generate desires in a dynamic way: Rahwan and Amgoud's *Desire-Generation Rules*

$$\frac{BC : (B\varphi_1 \wedge \dots \wedge B\varphi_n, b), \quad DC : (D^+\psi_1 \wedge \dots \wedge D^+\psi_m, c)}{DC : (D^+\psi, d)}$$

## How does the g-BDI model work?



# How does the g-BDI model work?

## Example

María, a tourist, activates a personal agent based on the g-BDI agent model, to get a tourist package that satisfies her preferences. She would be very happy going to a mountain place ( $m$ ), and rather happy practicing rafting ( $r$ ). On top of this, she wouldn't like to go farther than 1000km from Buenos Aires ( $f$ ) where she lives.

The recommender agent takes all desires expressed by María and follows the steps:

- **Desire generation:** the user interface that helps her express these desires ends up generating a desire theory for the DC as follows:

$$\mathcal{T}_{\mathcal{D}} = \{(D^+ m, 0.9), (D^+ r, 0.6), (D^+(m \wedge r), 0.96), (D^- f, 0.7)\}$$

## Example

- **Beliefs generation:** with the tourism plans offered, the tourism domain and its beliefs about how these packages can satisfy the user's preferences ( $\mathcal{T}_B$ ).
  - Plans: *Mendoza (Me)*, *SanRafael (Sr)*, *Cumbrecita (Cu)*, ...
  - Costs:  $c(Me) = 0.60$ ,  $c(Sr) = 0.70$ ,  $c(Cu) = 0.55$ , ...
  - Beliefs:  $(B[Me]m, 0.7)$ ,  $(B[Me]r, 0.6)$ ,  $(B[Me]m \wedge r, 0.6)$ ,  
 $(B[Sr]m, 0.5)$ ,  $(B[Sr]r, 0.6)$ ,  $(B[Sr]m \wedge r, 0.5)$ , ...
- **Looking for feasible packages:** from this set of positive and negative desires ( $\mathcal{T}_D$ ) and domain knowledge ( $\mathcal{T}_B$ ) the PC looks for *feasible plans*, that are believed to achieve positive desires ( $m$ ,  $r$ ,  $m \wedge r$ ) but avoiding the negative desire ( $f$ ) as a post-condition.
  - *Mendoza (Me)* and *SanRafael (Sr)* are feasible plans for the combined goal  $m \wedge r$ , while *Cumbrecita (Cu)* is feasible only for  $m$ .

## Example

- **Deriving the Intention formulae:** the intention degrees for satisfying each desire  $m$ ,  $r$  and  $m \wedge r$  by the different feasible plans are computed by the bridge rule that trades off the cost and benefit of satisfying a desire by following a plan. The IC context is filled up with the following formulas:

$$\mathcal{T}_{IC} = \{ \begin{array}{ll} (I_{Me}(m \wedge r), 0.675), & (I_{Sr}(m \wedge r), 0.625), \\ (I_{Me}(m), 0.60), & (I_{Me}(r), 0.50), \\ (I_{Sr}(m), 0.55), & (I_{Sr}(r), 0.45), \\ (I_{Cu}(m), 0.625) & \} \end{array}$$

- **Selecting Intention-plan:** the agent decides to **recommend the plan *Mendoza (Me)*** since it brings the best cost/benefit relation (represented by the intention degree 0.675) **to achieve  $m \wedge r$** , satisfying also the tourist's constraints.

# Outline

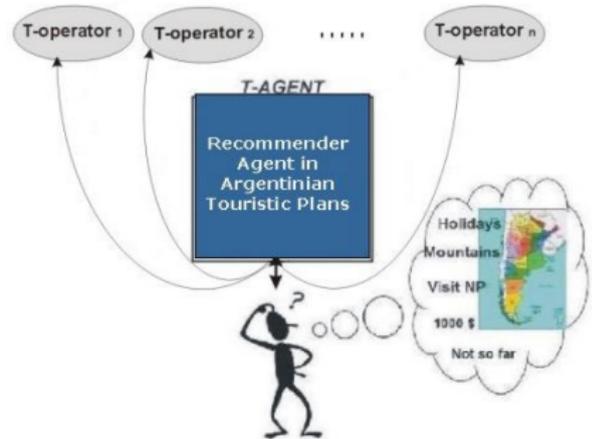
- Introduction: BDI agent architectures and multi-context systems
- Background on the fuzzy logic approach to reasoning about uncertainty
- The g-BDI agent model
- A case study
- Concluding remarks

# A Case Study

## A Tourism Recommender System

**Goal:** development (as a proof-of-concept) of a tourism recommender system to recommend the best tourist packages on Argentinian destinations according to different user's preferences and restrictions, provided by different tourist operators.

**Main task:** design of a Travel Assistant agent (*T-agent*), implementation, validation and experimentation



# T-Agent implementation

**Communication context:** is the *T-Agent* interface, interacting with

- **P-Agents (Tourist Operators)**, updating the information about current packages
- **the user (tourist customer)** that is looking for recommendation (Web service application).

**RECOMENDADOR DE TURISMO**

<b>USUARIO</b>	
NOMBRE	MARIA

<b>PREFERENCIAS</b>	
<input checked="" type="checkbox"/> ZONA	PATAGONIA 9
<input type="checkbox"/> RECURSOS NATURALES	MAR 5
<input type="checkbox"/> INFRAESTRUCTURA	MUSEO ARQUEOLOGIA 5
<input checked="" type="checkbox"/> TRANSPORTE	AVION 7
<input checked="" type="checkbox"/> ALOJAMIENTO	APART 6
<input type="checkbox"/> ACTIVIDADES	CABALGATA 5
FRECUENCIA DE LA ACTIVIDAD	BAJA

<b>RESTRICCIONES</b>	
<input checked="" type="checkbox"/> COSTO	2000
<input type="checkbox"/> DISTANCIA A RECORRER	0
<input type="checkbox"/> DIAS	0
TIPO DE RESTRICCIONES	FLEXIBLE

<b>PARAMETROS DE LA CONSULTA</b>	
PRIORIDAD	SATISFACCION DE RESTRICCIONES

## Experimentation and validation

Made over 52 queries, 35 different users (students)

**Some conclusions** (to be taken cautiously):

1. the g-BDI model has been proved useful to build concrete agents in real world applications.
2. the *T-Agent* recommended rankings (over 40 Tourism packages) are in most of the cases close to the user's own rankings.
3. g-BDI agent architecture allows us to engineer agents having different behaviours by suitably tuning some of its components.
4. the distinctive feature of recommender systems modelled using g-BDI agents, which is using graded mental attitudes, allows them to provide better results than those obtained with non-graded BDI models.

# Concluding remarks

## Future Work

- **Social aspects:**

An important topic for further work is to consider how to evaluate the **trust-reputation** in other agents, and how the agent updates this model along time.

- **Dynamic aspects:**

To model agents that interact in dynamic environments, the g-BDI agent should be extended to account for a **temporal dimension** in what regards her beliefs, desires and intentions.

- **Revision in g-BDI Agents:**

- g-BDI agents must be able to deal with **contextual inconsistencies** (revision mechanism, argumentation system?)
- need of a general process for multi-context system revision and then specialize it for the g-BDI agent model.

Thank you !