

XML and Databases

XPath evaluation using RDBMS

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Week 7

XPath

To handle XPath expressions correctly:

1) Rewrite your XPath expression in the *concrete syntax*, as per:

<http://www.w3.org/TR/xpath> :

.	↪	self::node()
//	↪	/descendant-or-self::node()/
.../foo	↪	.../child::foo

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.../foo \rightsquigarrow .../child::foo

2) Use a data-structure for XPath expressions

$$p ::= \text{bool} \times [(a_1, l_1, p_1); \dots; (a_n, l_n, p_n)]$$
$$a ::= \text{child} | \text{descendant} | \dots$$
$$l ::= * | \text{tagname} | \text{text}() | \text{node}()$$

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XPath (example)

The expression:

```
//a[./b]//following-sibling::a
```

becomes:

```
/descendant-or-self::node()/child::a[self::node()/child::b]/descendant-or-self::node()/following-sibling::a
```

And is represented by:

```
true, [  
  (descendant-or-self,node(), []);  
  (child,"a",(false, [ (self,node(), []); (child,"b", [])]));  
  (descendant-or-self,node(), []);  
  (following-sibling,"a", [])  
]
```

Compilation of XPath

The general algorithm now is:

1. rewrite the XPath expression;
2. transform it into a sequence of steps;
3. traverse the sequence step by step and build an SQL query

Represent each node of the document by an SQL table containing:

- ▶ pre-order, post-order, level of the node
- ▶ its tag in the tag field if the node is an element, NULL otherwise
- ▶ its text value if the node is a text node, NULL otherwise

Represent each attribute of the document by an SQL table containing:

- ▶ pre-order of the element containing the attribute
- ▶ the name of the attribute
- ▶ the text value of the attribute

you can use the same table/code as in Assignment 3

Logical encoding of axes

We think of the way to encode the XPath expression.

We use propositional formulae:

f	$::=$	$v \mid f \wedge f \mid f \vee f \mid \neg f \mid P(f, \dots, f)$	formulae
v	$::=$	$x \mid y \mid z \mid \dots$	node variables
P	$::=$	$pre \mid post \mid level \mid < \mid > \mid \dots$	predicates

The idea is to write *new predicates* which represent a particular axis.

For instance:

$$descendant(x,y) \equiv pre(x) < pre(y) \wedge post(x) > post(y)$$

We reads: “node y is a descendant of node x if the pre-order of x is less than the preorder of y and if the post-order of x is larger than the post-order of y ”

Logical encoding of axes

Most axes are straightforward. By using formulae, it is also easy to simplify some formulae by using logical rules:

$self(x, y)$	\equiv	$pre(x) = pre(y)$
$descendant(x, y)$	\equiv	$pre(x) < pre(y) \wedge post(x) > post(y)$
$descendant-or-self(x, y)$	\equiv	$pre(x) \leq pre(y) \wedge post(x) \geq post(y)$
$child(x, y)$	\equiv	$descendant(x, y) \wedge level(x) = level(y) - 1$
$ancestor(x, y)$	\equiv	$pre(x) > pre(y) \wedge post(x) < post(y)$
$parent(x, y)$	\equiv	$ancestor(x, y) \wedge level(x) = level(y) + 1$
$preceding(x, y)$	\equiv	$pre(x) > pre(y) \wedge post(x) > post(y)$
$following(x, y)$	\equiv	$pre(x) < pre(y) \wedge post(x) < post(y)$

It is also handy to have a predicate to say “x is the root of the document (the DOCUMENT_NODE)”:

$$root(x) \equiv pre(x) = 0$$

Logical encoding of tests

There are only a few tests. $T(x)$ is true if the test T is true for the node x :

$is_node(x) \equiv$ is always true

$is_text(x) \equiv$ is true if x is a text node

$is_star(x) \equiv$ is true if x is an element node

We also define the predicate $tag(x)$ which returns the tag of x and $text(x)$ which returns the text of x .

Example: If we are on a context node x and want to take the step `child::a` then, we want to select all nodes y such that:

$$child(x, y) \wedge tag(y) = "a"$$

which is equivalent to:

$$pre(x) < pre(y) \wedge post(x) > post(y) \wedge level(x) = level(y) + 1 \wedge tag(y) = "a"$$

Example of logical encoding

Consider the path `/*/b/text()`

1) Rewrite it into the expanded syntax:

`/child::* / descendant-or-self::node() / child::b / child::text()`

2) Compute the formula step by step:

$root(r_1)$	Starts at the document root
$\wedge child(r_1, r_2) \wedge is_star(r_2)$	
$\wedge descendant-or-self(r_2, r_3)$	The <code>node()</code> test is always true so we don't put anything
$\wedge child(r_3, r_4) \wedge tag(r_4) = "b"$	
$\wedge child(r_4, r_5) \wedge is_text(r_5)$	

From formulae to SQL

The SQL syntax is close to the one used for the formulae.

The previous query: `/*//b/text()`, which is:

```
/child::*//descendant-or-self::node()/child::b/child::text()
```

is written in SQL:

```
SELECT DISTINCT r5.pre
FROM table r1, table r2, table r3, table r4, table r5
WHERE r1.pre = 0                /* root(r1) */
AND   r1.pre < r2.pre AND r1.post > r2.post
      AND r1.level = r2.level + 1 /* child(r1,r2) */
      AND r2.tag != NULL          /* is_star(r2) */
AND   r2.pre <= r3.pre AND r2.post >= r3.post
AND   r3.pre < r4.pre AND r4.post > r4.post
      AND r3.level = r4.level + 1 /* child(r3,r4) */
      AND r4.tag = "a"
AND   r4.pre < r5.pre AND r4.post > r5.post
      AND r4.level = r5.level + 1 /* child(r4,r5) */
      AND r5.text != NULL        /* is_text(r5) */
ORDER BY r5.pre
```

SQL syntax

```
SELECT DISTINCT r5.pre
FROM table r1, table r2, table r3, table r4, table r5
WHERE r1.pre = 0
      :
ORDER BY r5.pre
```

- ▶ `SELECT DISTINCT x.pre`: returns the *set* (DISTINCT removes duplicates) of pre-order numbers for the nodes specified by `x`. `x` must correspond to the *last step* of the toplevel query (*i.e.* not in a filter).
- ▶ `FROM table r1, ...`: binds `n` variable to the element table.
- ▶ `ORDER BY x.pre` ensures that the results are in document order. `ORDER BY` and `SELECT DISTINCT` reference the same variable.

following-sibling axis

This axis is a bit trickier. First let's try to express (logically) the set of *siblings* y of a node x . The siblings of x are the nodes **with the same parent as x** . We would formally write:

$$\textit{sibling}(x, y) \equiv \exists z, \textit{parent}(x, z) \wedge \textit{parent}(y, z)$$

If we want following or preceding siblings, we just have to add a condition on the pre-order:

$$\begin{aligned} \textit{preceding-sibling}(x, y) &\equiv \exists z, \textit{parent}(x, z) \wedge \textit{parent}(y, z) \wedge \textit{pre}(x) > \textit{pre}(y) \\ \textit{following-sibling}(x, y) &\equiv \exists z, \textit{parent}(x, z) \wedge \textit{parent}(y, z) \wedge \textit{pre}(x) < \textit{pre}(y) \end{aligned}$$

Thus in SQL, for a step `following-sibling::t` we must introduce 2 variables and not one.

following-sibling axis

The query:

```
//a/following-sibling::b
```

is rewritten into:

```
/descendant-or-self::node()/child::a/following-sibling::b
```

which gives the SQL query:

```
SELECT DISTINCT r5.pre
FROM table r1, table r2, table r3, table r4, table r5
WHERE r1.pre = 0
  AND r1.pre <= r2.pre AND r1.post >= r2.post
  AND r2.pre < r3.pre AND r2.post > r3.post
  AND r2.level = r3.level - 1 AND r3.tag = "a"
  AND r3.pre > r4.pre AND r3.post < r4.post
  AND r3.level = r4.level + 1          /* parent(r3,r4) */
  r5.pre > r4.pre AND r5.post < r4.post
  AND r5.level = r4.level + 1        /* parent(r5,r4) */
  AND r3.pre < r5.pre
  AND r5.tag = "b"
ORDER BY r5.pre
```

Filters

Consider: //a[./preceding::b]

Rewrite as:

```
/descendant-or-self::node()/child::a[self::node()/preceding::b]
```

We have two paths:

```
/descendant-or-self::node()/child::a (1)
```

```
self::node()/preceding::b (2)
```

```
SELECT DISTINCT r3.pre
```

```
FROM table r1, table r2, table r3, table r4, table r5
```

```
WHERE r1.pre = 0
```

```
AND r1.pre <= r2.pre AND r1.post >= r2.post
```

```
AND r2.pre < r3.pre AND r2.post > r3.post
```

```
AND r2.level = r3.level-1
```

```
AND r3.tag = "a" /* This is exactly like before */
```

```
AND r3.pre = r4.pre /* self::node() */
```

```
AND r4.pre > r5.pre AND r4.post > r5.post /* preceding::b */
```

```
AND r5.tag = "b"
```

```
ORDER BY r3.pre
```

The filter is *relative* (does not start with /) so we link it to the previous step (here r3)

Filters

Consider: /a[//b]

Rewrite as:

```
/child::a[/descendant-or-self::node/child::b]
```

```
SELECT DISTINCT r2.pre
FROM table r1, table r2, table r3, table r4, table r5
WHERE r1.pre = 0
    AND r1.pre < r2.pre AND r1.post > r2.post
    AND r1.level = r2.level-1
    AND r2.tag = "a"
    AND r1.pre = r3.pre          /* Start at the root */
    AND r3.pre <= r4.pre AND r3.post >= r4.post
    AND r4.pre < r5.pre AND r4.post > r5.post
    AND r4.level = r5.level-1
    AND r5.tag = "b"
ORDER BY r2.pre
```

The filter is *absolute* (starts with /) so we link it to root (r1).

Multiple filters

//a[./b][./c]: a must have a child "b" and a child "c"

```
SELECT DISTINCT r3.pre
FROM table r1, table r2, table r3,
     table r4, table r5,
     table r6, table r7,
WHERE r1.pre = 0
     AND r1.pre <= r2.pre AND r1.post >= r2.post
     AND r2.pre < r3.pre AND r2.post > r3.post
     AND r2.level = r3.level-1
     AND r3.tag = "a"
AND r3.pre = r4.pre
     AND r4.pre < r5.pre AND r4.post > r5.post
     AND r4.level = r5.level-1
     AND r5.tag = "b"
AND r3.pre = r6.pre
     AND r6.pre < r7.pre AND r6.post > r7.post
     AND r6.level = r7.level-1
     AND r7.tag = "c"
ORDER BY r2.pre
```

Attributes

Attribute only appear in filters. We use the `.pre` of the previous step and the attribute name as a *key* in the attribute table:

```
//a[@x]/b[@y="foo"]
```

becomes:

```
/descendant-or-self::node()/child::a[attribute::x]/child::b[attribute::y="foo"]
```

```
SELECT DISTINCT r5.pre
FROM table r1, table r2, table r3, attr_table r4,
     table r5, attr_table r6
WHERE r1.pre = 0
     AND r1.pre <= r2.pre AND r1.post >= r2.post
     AND r2.pre < r3.pre AND r2.post > r3.post
     AND r2.level = r3.level - 1
     AND r3.tag = "a"
     AND r3.pre = r4.pre AND r4.name = "x"
     AND r3.pre < r5.pre AND r3.post > r5.post
     AND r3.level = r5.level - 1
     AND r5.tag = "b"
     AND r5.pre = r6.pre AND r6.name = "y"
     AND r6.text = "foo"
ORDER BY r5.pre
```

Summary

1. Rewrite the XPath query using the extended syntax. This way you don't have to wonder how to do `//preceding::a`, `//following-sibling::b` or `./@x`. Once the query is expanded, just use the formulae step by step!
2. Filters are not more difficult. Consider two cases: the filter starts with a `/` (absolute), you must link the path in the filter to the root node. If the filter is *relative* then just link it to the previous step.

Reminder for assignment 5, you only need to implement:

1. `/`, `//`, `following-sibling`, `preceding`, `*`, `tag`, `text()` and filters
2. for the bonus part, attributes in filters and test on attributes value.