

# Unsupervised Morphology Induction using Word Embeddings

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- vocabulary  $V$ , embedding function  $e: V \rightarrow \mathbf{R}^n$
- vector space encodes semantic similarity
  - $e(\text{car}) \simeq e(\text{automobile})$ ,  $e(\text{car}) \neq e(\text{seahorse})$
- vector space encodes compositionality
  - semantic:  $e(\text{king}) - e(\text{man}) + e(\text{woman}) \simeq e(\text{queen})$
  - syntactic:  $e(\text{cars}) - e(\text{car}) + e(\text{fireman}) \simeq e(\text{firemen})$
- vector space encodes syntactic/semantic transformations
  - $\text{anti+} \simeq e(\text{anticorruption}) - e(\text{corruption})$

*British scientists recreated Down 's syndrome in mice in order to study the disease and develop new treatments .*

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$$\arg \max_{v_w, v_c} \left( \sum_{(w,c) \in D_w} \log \sigma(v_w \cdot v_c) + \sum_{(w,c) \in \bar{D}_w} \log \sigma(-v_w \cdot v_c) \right)$$

$$\sigma(x) = \frac{1}{1 + e^x}$$

Train on large monolingual corpus



# SkipGram Embeddings: Introduction



size: 8,869 tuples  
king - man + woman = queen  
evaluation: accuracy (over entire vocabulary)

size: 10,675 tuples  
cars - car + fireman = firemer  
evaluation: accuracy closest point (over entire vocabulary)

size: 2003 pairs  
is a celebrated ...  
an English ?roc  
eval: Spearman (against 10-human)

size: 2034 pairs  
belligerence ≈ hostility 8.7  
amorphous ≈ inorganic 1.9  
eval: Spearman corr. (against 10-human score avg.)

Model	Compositionality (Acc%)		Similarity (Spearman ρ)	
	Semantic	Syntactic	Stanford-C	Stanford-RW
SkipGram (Wikipedia 1Bw)	76.7	68.3	66.3	35.8

$$\arg \max_{v_w, v_c} \left( \sum_{(w,c) \in D_w} \log \sigma(v_w \cdot v_c) + \sum_{(w,c) \in \overline{D_w}} \log \sigma(-v_w \cdot v_c) \right)$$

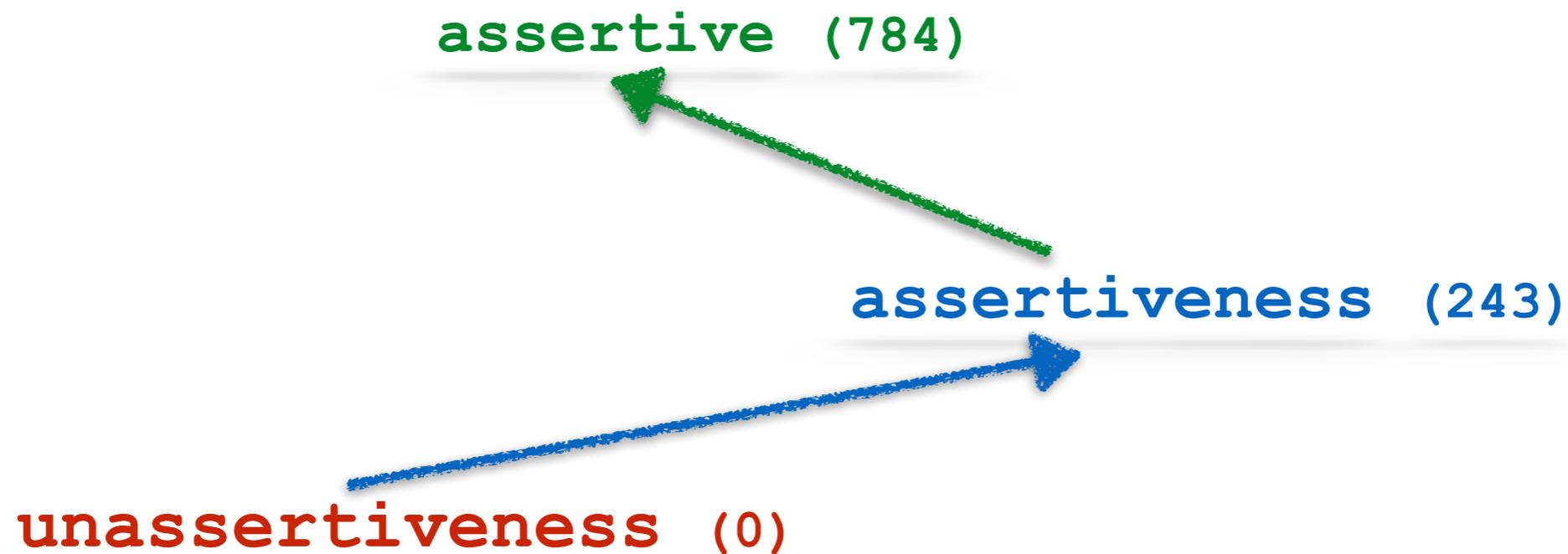
$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

# Unsupervised Morphology Induction

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Q: What do we want?

A: We want *high-quality* embeddings for all words (even ones outside  $V$ )

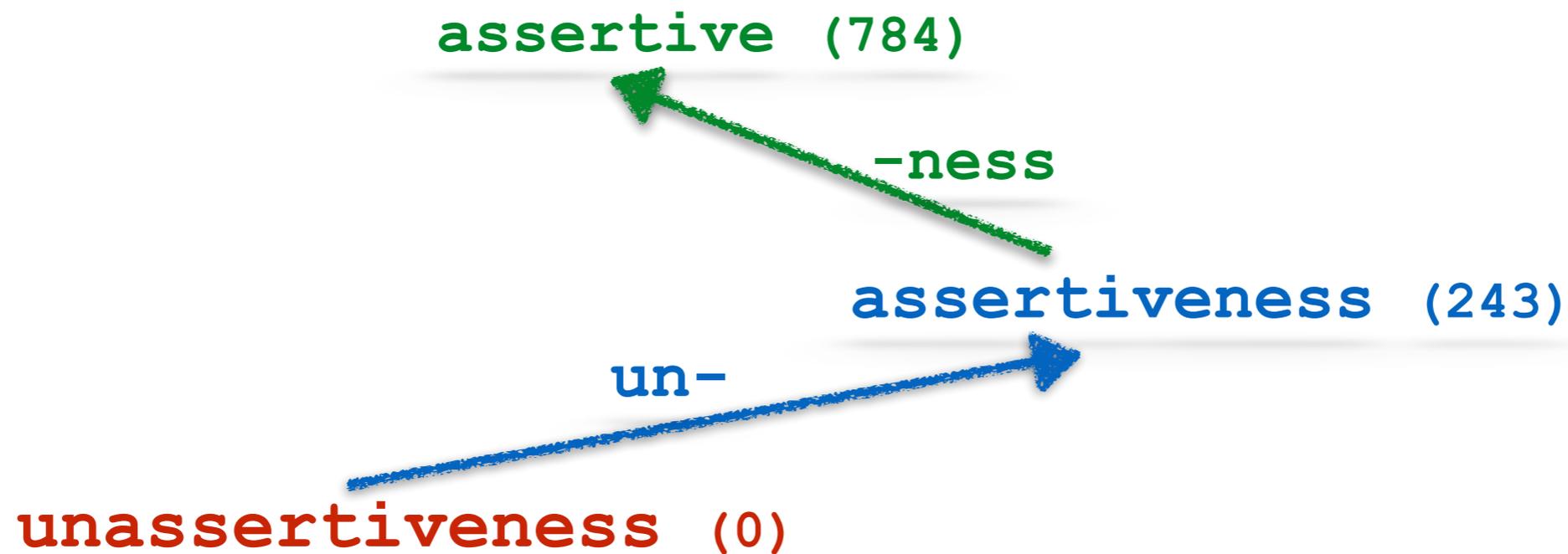


# Unsupervised Morphology Induction

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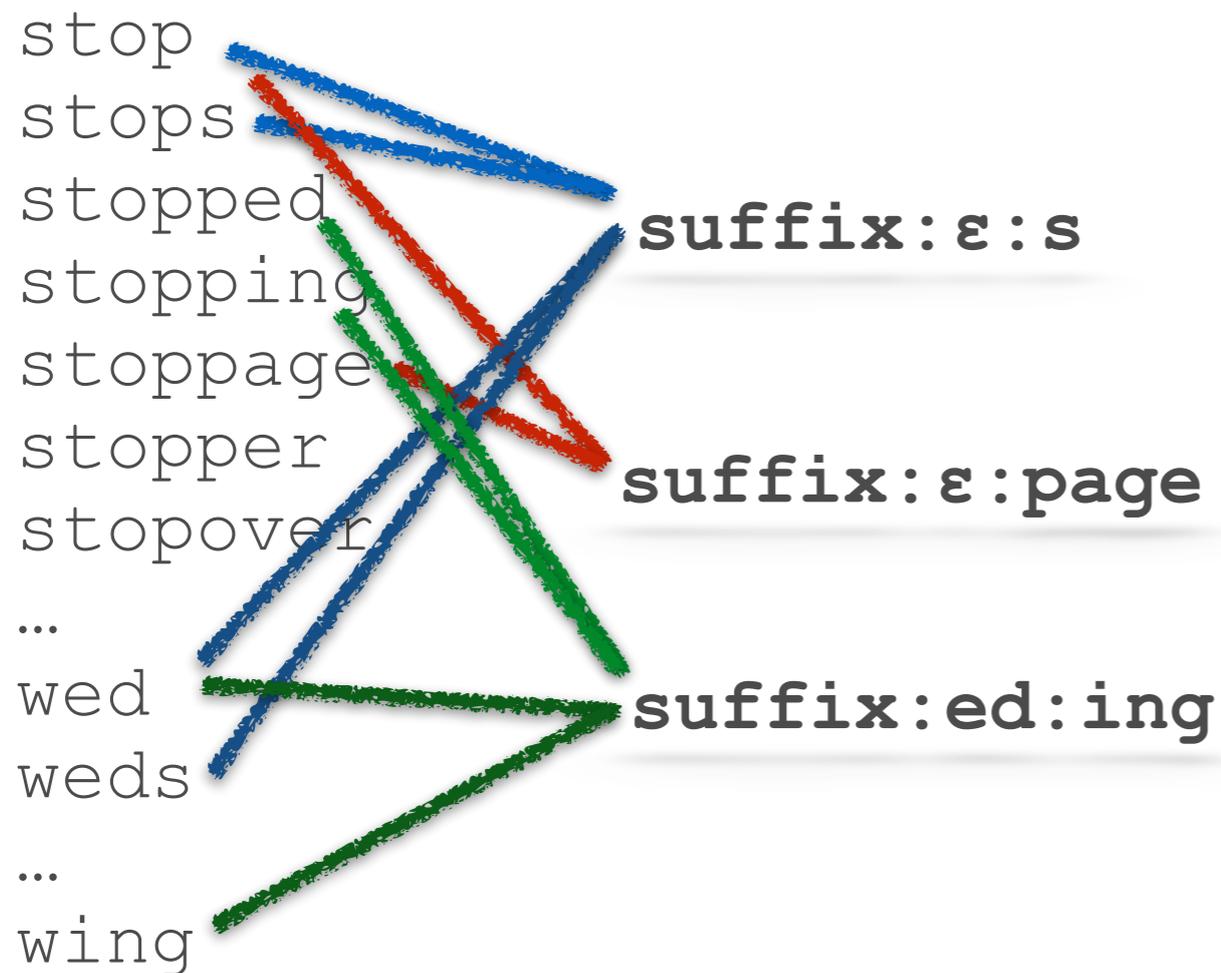
Q: What do we want?

A: We want *morphology-based transformations* that can accurately analyze words (even ones unseen at training time)



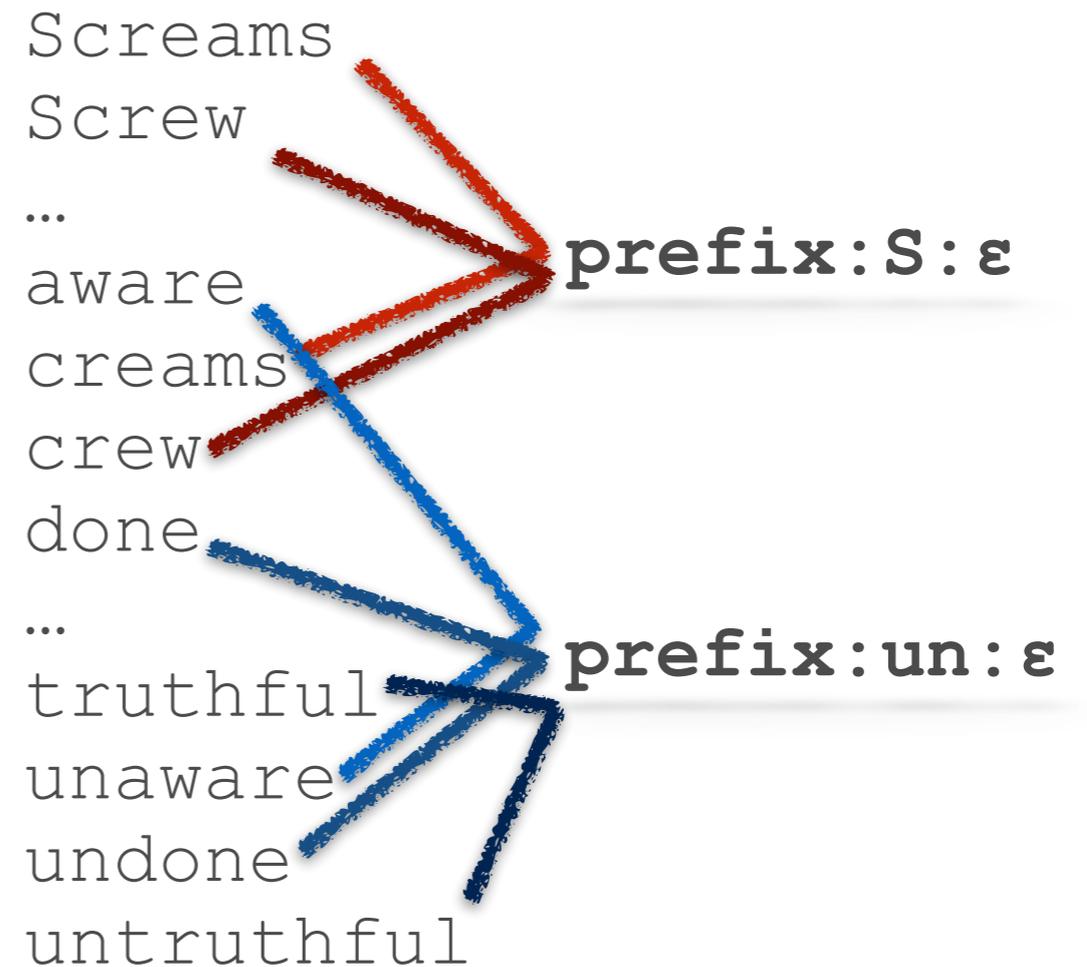
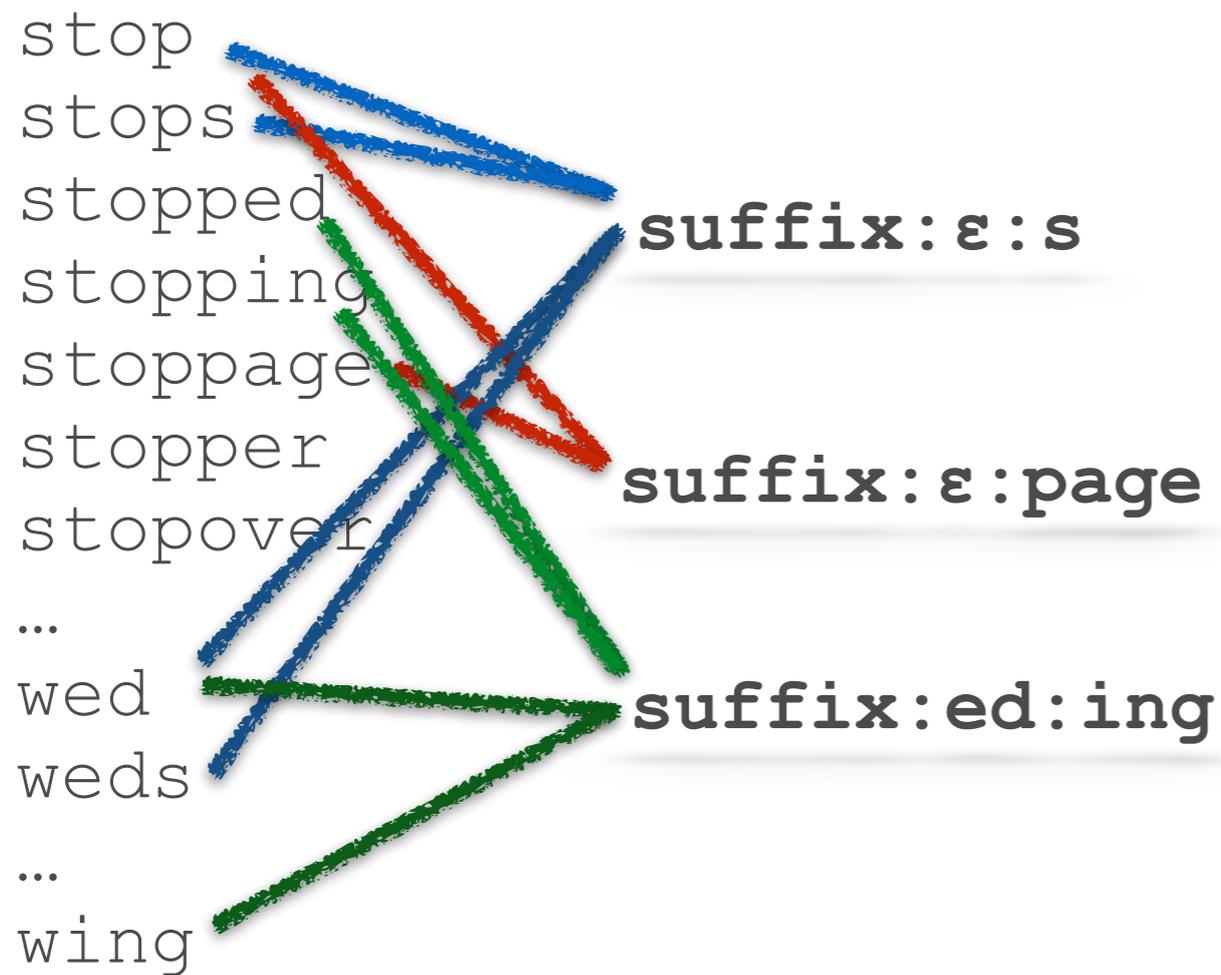
## Steps:

1. From  $V$ , extract candidates for morphological rules (prefix & suffix only)



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Steps:

2. Query against embedding space: *morphology does not shift meaning*

**suffix: ed: ing**

adored adorned affected ...  
blamed blitzed blogged ...  
stayed stepped stopped ...  
weaned wed wedged whirled

$rank(\text{blamed} \rightarrow \text{blaming}) = 1$   
 $rank(\text{stopped} \rightarrow \text{stopping}) = 2$   
 $rank(\text{wed} \rightarrow \text{wing}) = 28609$

**prefix: ε: S**

aura aux ave ...  
canned cans car care ...  
crape cream creams ...  
miles mitten mothers ...

$rank(\text{care} \rightarrow \text{Scare}) = 57778$   
 $rank(\text{cream} \rightarrow \text{Scream}) = 9434$   
 $rank(\text{miles} \rightarrow \text{Smiles}) = 18800$

Steps:

2. Query against embedding space: *morphology does not shift meaning*

**prefix: un: ε**

unabated unable unabridged...  
**unaware** unbalance unbeaten...  
undoing **undone** undoubted...  
untrusted untrustworthy...

$rank(\text{unaware} \rightarrow \text{aware}) = 1$

$rank(\text{undone} \rightarrow \text{done}) = 129$

Steps:

2. Query against embedding space: *morphology does not shift meaning*

*morphology shifts meaning consistently*

**prefix: un: ε**

unabated unable unabridged...  
**unaware** unbalance unbeaten...  
undoing **undone** undoubted...  
untrusted untrustworthy...

$rank(\text{unaware} \rightarrow \text{aware}) = 0$

$rank(\text{undone} \rightarrow \text{done}) = 129$

**↑ un-**

clear - unclear

delivered - undelivered

truthful - untruthful

$rank(\text{undone} + \text{↑ un-} \rightarrow \text{done}) = 4$

Steps:

3. Extract candidate rules using embedding-based stats

	Candidate Rule	Direction	#Correct	#Total	Acc10
<b>Bad</b>	<code>suffix:h:a</code>	↑Teh	1	449	0.4%
	<code>suffix:o:es</code>	↑Tono	7	688	1.0%
	<code>prefix:D:W</code>	↑Daring	9	675	1.3%
	...				
<b>Good</b>	<code>prefix:un:ε</code>	↑undelivered	166	994	23.3%
	<code>suffix:ed:ing</code>	↑procured	2138	4714	56.2%
	...				
	<code>suffix:ating:ate</code>	↑formulating	255	395	74.7%
	<code>suffix:sed:zed</code>	↑victimised	153	186	90.9%

# Unsupervised Morphology Induction: Algorithm



Steps:

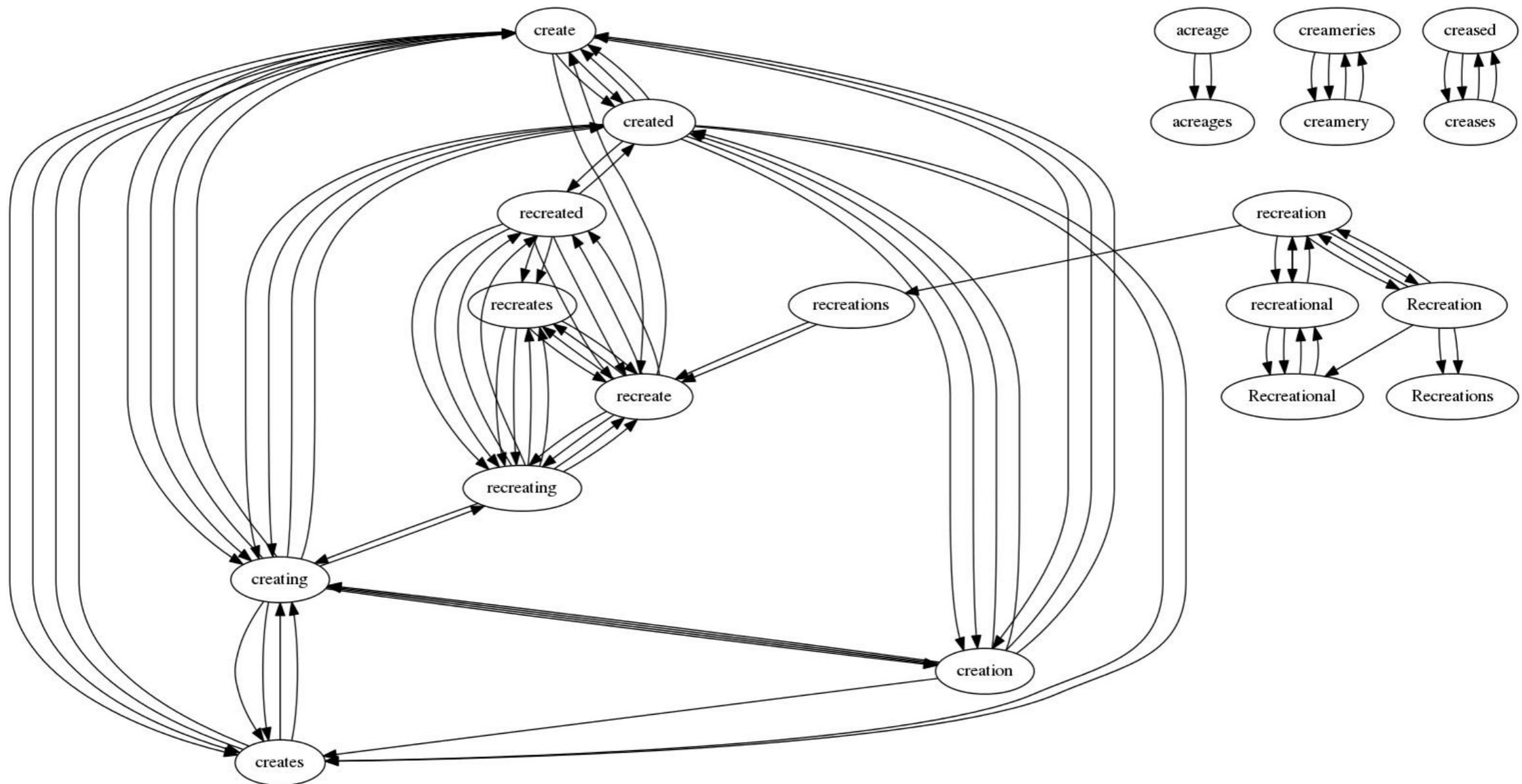
4. Use rules to extract lexicalized, weighted morphological transformations

Start	Rule + Direction = Transformation	End	Cosine	Rank
...				
recreations	suffix:ions:e + ↑ investigations	recreatee	0.69	1
recreations	suffix:tions:te + ↑ investigations	recreatee	0.70	1
recreations	suffix:ions:ed + ↑ delineations	recreateded	0.51	29
recreations	suffix:ions:ing + ↑ reconstruction	recreating	0.72	1
...				
unaware	prefix:un:ε + ↑ uncivilized	aware	0.77	1
unaware	prefix:un:ε + ↑ undelivered	aware	0.63	7

# Unsupervised Morphology Induction: Algorithm

Output (I): labeled, weighted, cyclic, directed multigraph  $G^V_{Morph}$

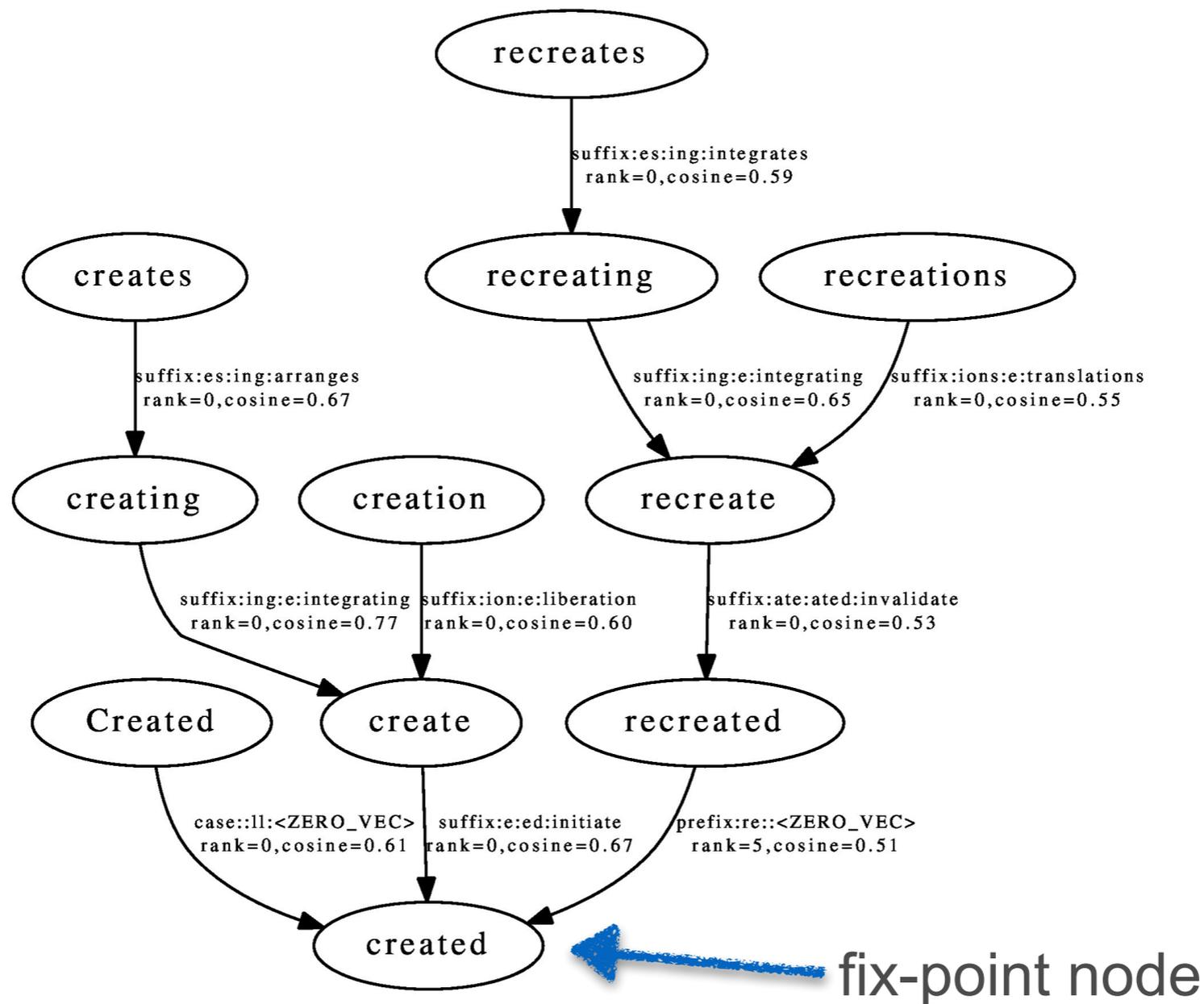
- words are nodes, morphological transformations are (weighted) edges



# Unsupervised Morphology Induction: Algorithm

Output (II): labeled, weighted, acyclic, directed graph  $D^V_{Morph}$

- words are nodes, morphological mappings are weighted edges

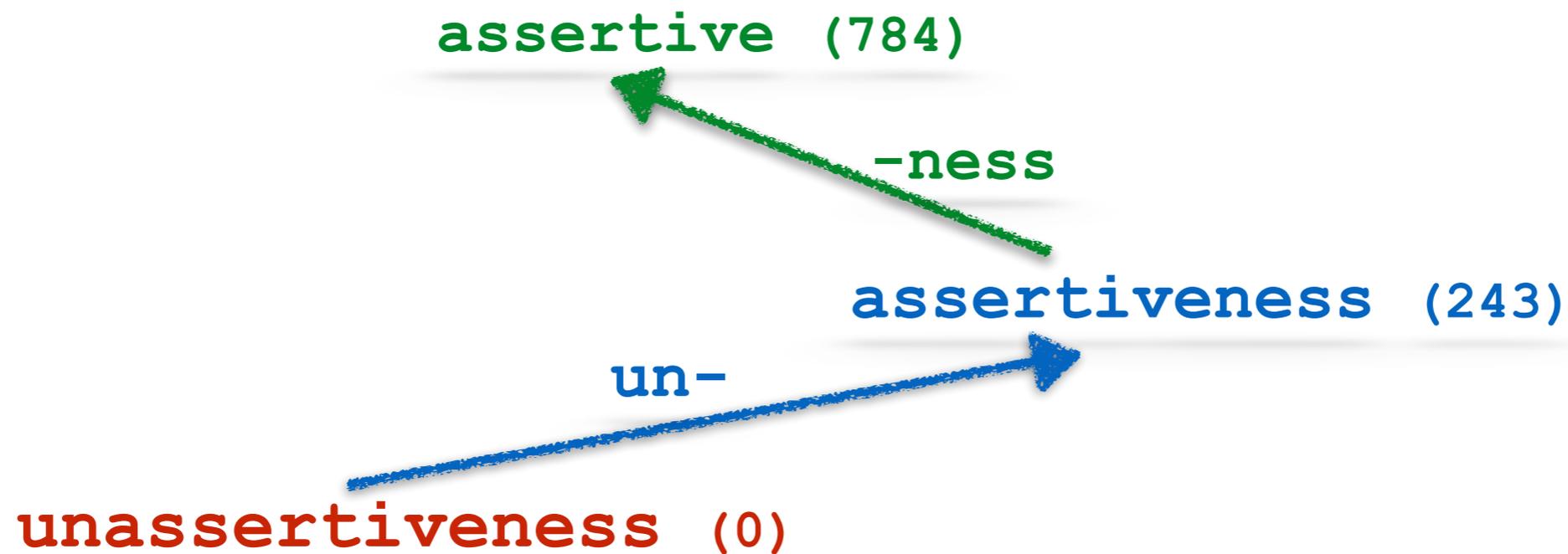


# Unsupervised Morphology Induction

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Q: What do we want?

A: We want *morphology-based transformations* that can accurately analyze words (even ones unseen at training time)



# Unsupervised Morphology Induction

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Basic algorithm: embedding words outside  $V$

Outside Wikipedia (1B tokens,  $|V| = 4.3\text{M}$ )

**animalize (0)**

**balminess (0)**

**caesarism (0)**

**containerful (0)**

**nonindulgent (0)**

**unassertiveness (0)**

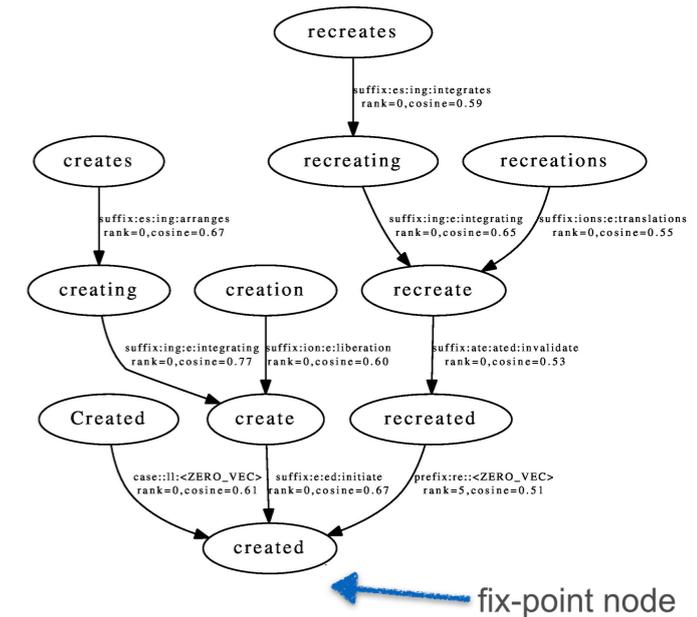
# Unsupervised Morphology Induction: Algorithm



Analyze words outside  $V$

1. Train time: extract and count all paths ending in a “fix-point” from the directed acyclic graph  $D^V_{Morph}$

- each path is called a “rule sequence”



rule sequence	count
<b>suffix:s:ε</b>	3119
<b>suffix:ed:ε</b>	687
<b>suffix:ing:ed</b>	412
<b>prefix:un:ε</b>	207
<b>suffix:ness:ε</b>	162
<b>suffix:ness:ly</b>	25
<b>suffix:y:ier, suffix:er:ness</b>	10
<b>prefix:un:ε, suffix:ed:ing</b>	5

# Unsupervised Morphology Induction: Algorithm

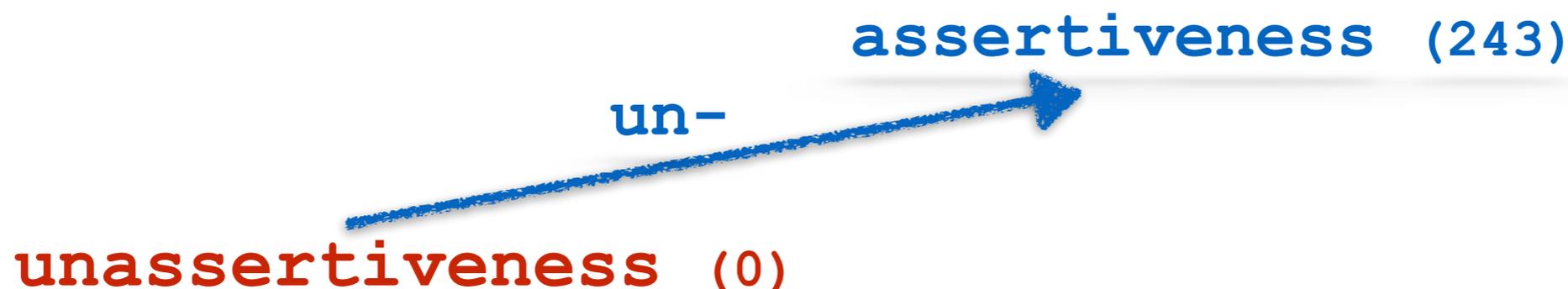
Analyze words outside  $V$

- Run time: apply each rule sequence in descending order of counts
  - if rule fires, check that result has count  $> 0$  and in-degree  $> 0$
  - stop at first winner

	rule sequence	count	
<b>unassertiveness (0)</b>	<b>suffix:s:ε</b>	3119	<b>unassertiveness (0)</b>
	suffix:ed:ε	687	
	suffix:ing:ed	412	
<b>unassertiveness (0)</b>	<b>prefix:un:ε</b>	207	<b>assertiveness (243)</b>
	suffix:ness:ε	162	
	suffix:ness:ly	25	
	suffix:y:ier, suffix:er:ness	10	
	prefix:un:ε, suffix:ed:ing	5	

$$\text{unassertiveness} = \text{assertiveness} + \uparrow \text{un+}$$

A: We want *morphology-based transformations* that can accurately analyze words unseen at training time

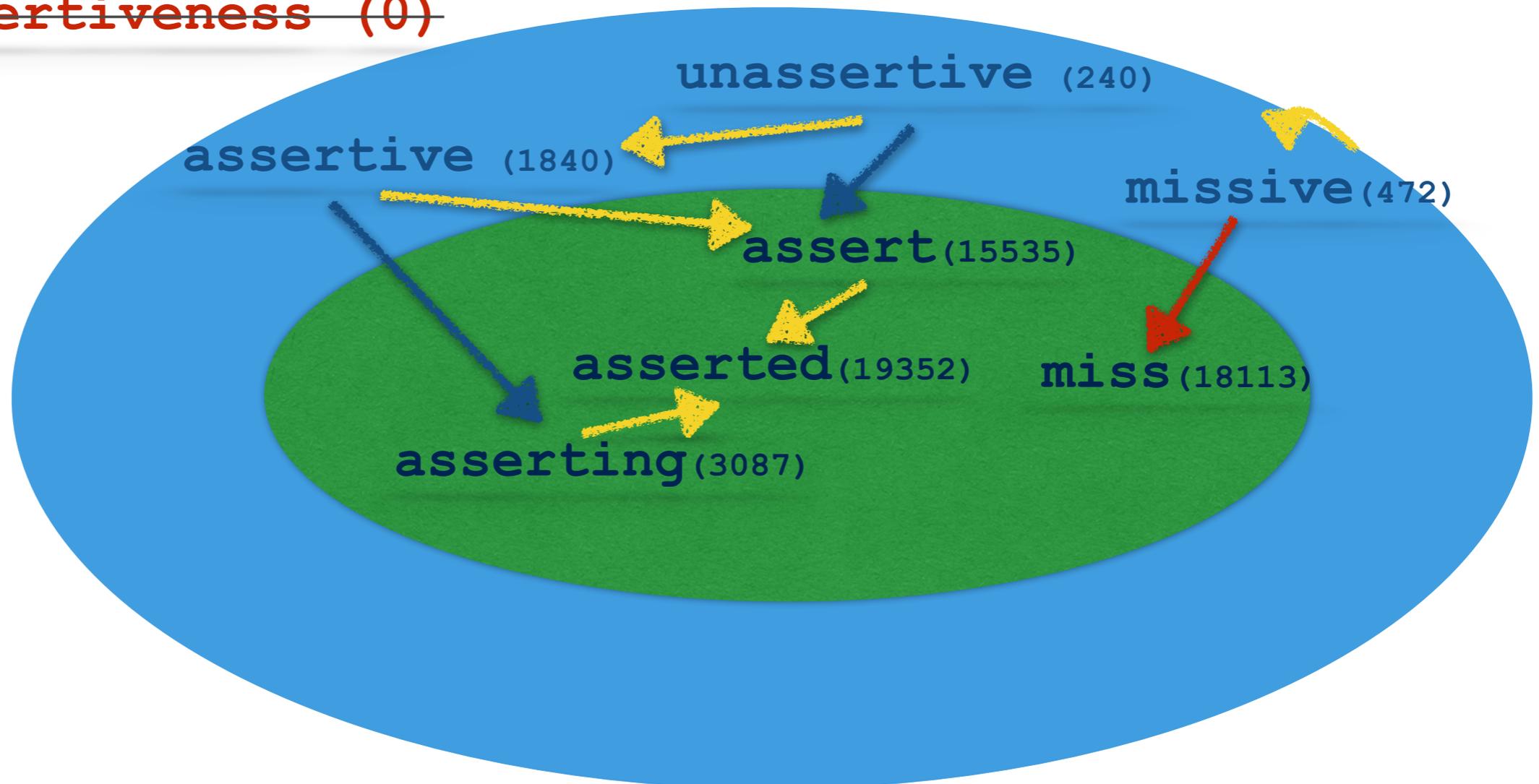


Language	Tokens	V	$ G^V_{Morph} $	$ D^V_{Morph} $
EN	1.1b	1.2m	780k	75,823
DE	1.2b	2.9m	3.7m	169,017
FR	1.5b	1.2m	1.8m	92,145
ES	566m	941k	2.2m	82,379
RO	1.7b	963k	3.8m	141,642
AR	453m	624k	2.4m	114,246
UZ	850m	2.0m	5.6m	194,717

# Unsupervised Morphology Induction: Evaluation

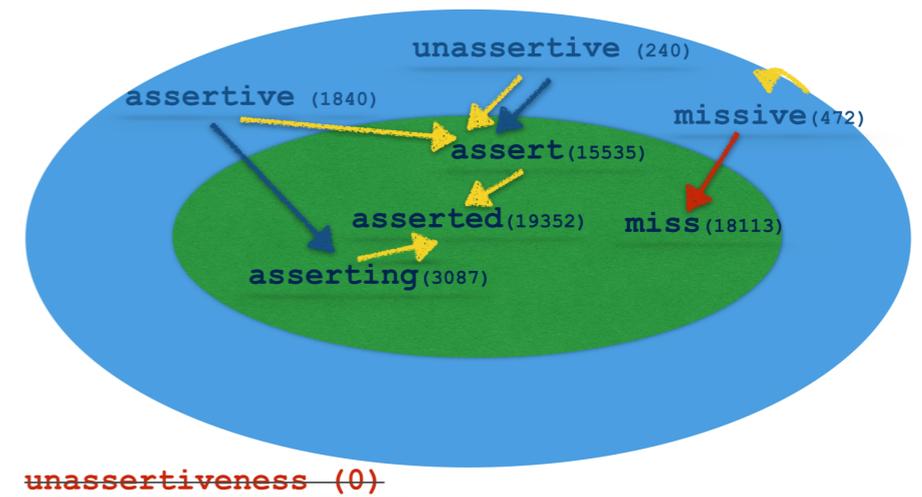
Evaluate OOV analysis using low-count words

~~unassertiveness (0)~~



# Unsupervised Morphology Induction: Evaluation

Evaluate OOV analysis using rare words



Language	$ V_{[1000,2000)} $		Accuracy	
	Have analysis	Don't have analysis	Have analysis	Don't have analysis
EN	3421	10617	89.7%	89.6%
DE	10778	21234	90.8%	93.1%
FR	6435	9807	90.3%	90.4%
ES	5724	7412	91.1%	90.3%
RO	11905	9254	86.5%	85.3%
AR	7913	5202	92.4%	69.0%
UZ	11772	9027	81.3%	84.1%

Q: What do we want?

A: We want *morphology-based transformations* that can accurately analyze words (even ones unseen at training time)

Key result

Improved word similarity judgment: unknown, low-count, high-count words

- evaluation on Stanford Rare Word similarity dataset (RW-EN)
- evaluation of similarity datasets on various languages (RG-DE)

# Unsupervised Morphology Induction: Evaluation



## Training Setup

	Language	Train Set	Tokens	V	$ G^V_{Morph} $	$ D^V_{Morph} $
Small	EN	Wiki-EN	1.1b	1.2m	780k	75,823
	DE	WMT-DE	1.2b	2.9m	3.7m	169,017
Large	EN	News-EN	120b	1.0m	2.9m	98,268
	DE	News-DE	20b	1.8m	6.7m	351,980

# Unsupervised Morphology Induction: Evaluation



Evaluation on similarity datasets (RG-DE, RW-EN)

size: 2034 pairs

impossibilities unattainableness 8.8  
 deregulating liberation 8.0  
 baseness unworthiness 4.0  
 transmigrating born 1.1

Language	Train Set	Tokens	V	$ G^V_{Morph} $	$ D^V_{Morph} $
EN	Wiki-EN	1.1b	1.2m	780k	75,823
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EN	News-EN	120b	1.0m	2.9m	98,268
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System	RW-EN Testset			
	Unembedded		Spearman $\rho$	
	Wiki-EN	News-EN	Wiki-EN	News-EN
SkipGram	78	177	35.8	44.7
SkipGram+Morph	1	0	41.8	52.0

Annotations: +9 (blue arrow from 35.8 to 44.7), +7 (green arrow from 44.7 to 52.0)

# Unsupervised Morphology Induction: Evaluation



Evaluation on similarity datasets (RG-DE, RW-EN)

size: 65 pairs

Edelstein	Juwel	3.8
Autogramm	Unterschrift	3.5
Irrenhaus	Friedhof	0.3
Kraftfahrzeug	Magier	0.0

Language	Train Set	Tokens	V	$ G^V_{Morph} $	$ D^V_{Morph} $
EN	Wiki-EN	1.1b	1.2m	780k	75,823
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RW-EN Testset				
	Unembedded		Spearman $\rho$	
System	Wiki-EN	News-EN	Wiki-EN	News-EN
SkipGram	80	177	35.8	44.7
SkipGram+Morph	1	0	41.8	52.0

*Note: Arrows indicate improvements: +9 for Wiki-EN Spearman  $\rho$  and +7 for News-EN Spearman  $\rho$ .*

RG-DE Testset				
	Unembedded		Spearman $\rho$	
System	WMT-DE	News-DE	WMT-DE	News-DE
SkipGram	0	20	62.4	62.1
SkipGram+Morph	0	0	64.1	69.1

*Note: Arrows indicate improvements: +0 for WMT-DE Spearman  $\rho$  and +7 for News-DE Spearman  $\rho$ .*

1. Method for inducing morphological transformations between words
  - from scratch, unsupervised, language agnostic
2. Provides morphology-based structure over embedding spaces
3. Provides high-quality embeddings for out-of-vocabulary and low-count morphological variants

- Going beyond suffix & prefix morphology
  - nothing in the approach prevents from extending it
- Use it for improved Machine Translation
  - quick and painless morphological analysis on source side
  - generate morphological variants on target side (even new ones!)
- Use it for improved Information Retrieval

Thank you

