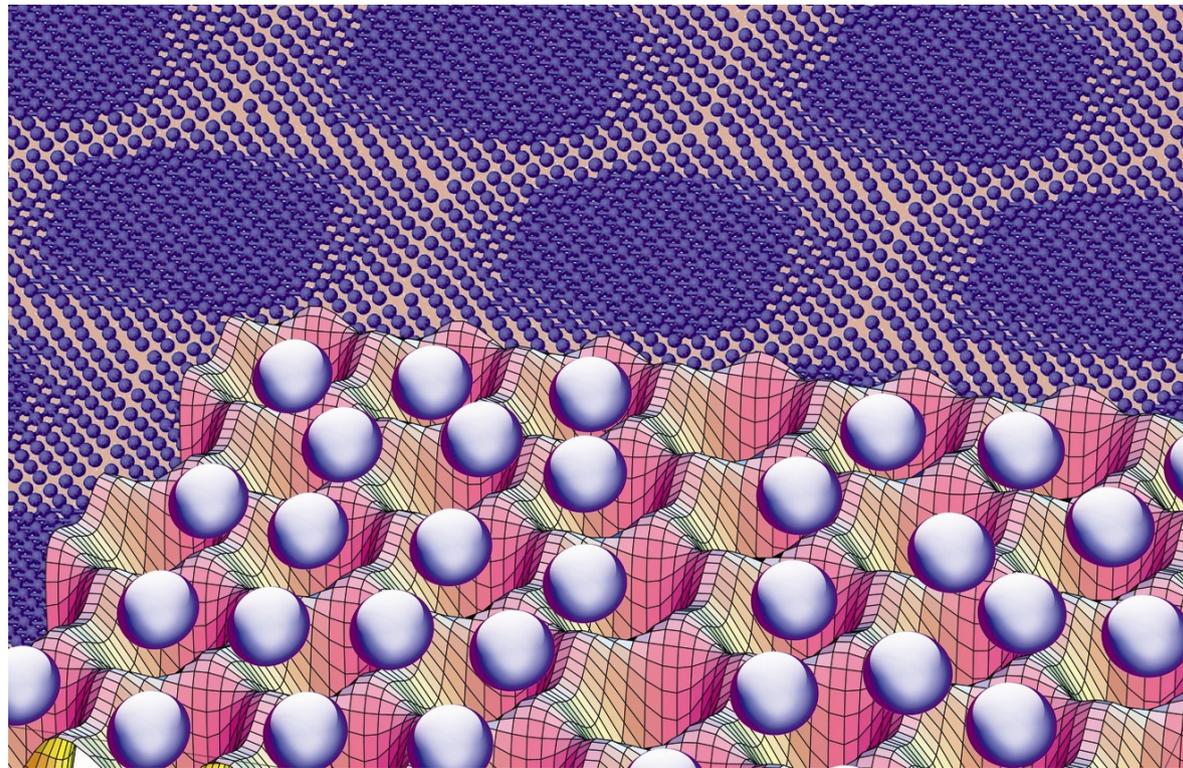


Static and dynamic friction in sliding colloidal monolayers

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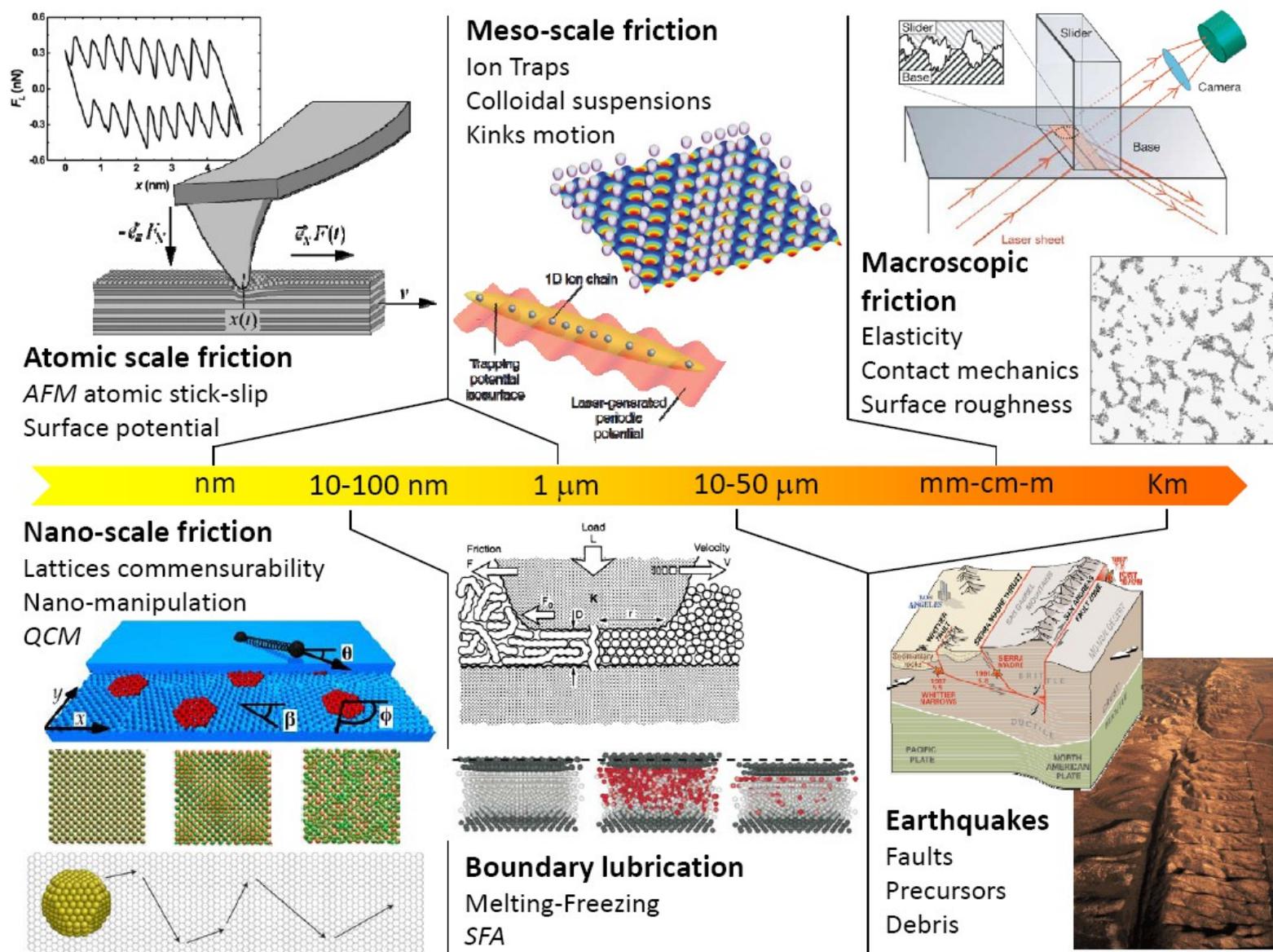


*in collaboration with: **A. Vanossi, E. Tosatti (Trieste)***

Outline

- *(Nano) friction at a glance*
- *Driven colloidal monolayers as a model system for nanotribology*
- *Experimental findings: role of topological solitons*
- *MD modeling of driven colloidal monolayers*
- *Static and dynamic friction*
- *Summary and Outlook*

(Nano-) friction at a glance



- Friction spans all length scales, **from micro up to macro**
- It involves **high-nonlinear out-of-equilibrium processes** usually **at a buried interface**

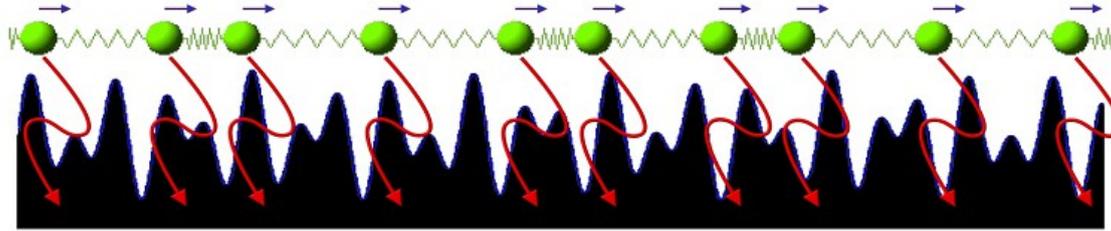
Why studying friction?

- **Fundamental understanding** of interface mechanisms
- **Bridging the gap** between micro and macro
- **(Nano)Technology, applications** and **energy/materials saving** (~ 6% GNP lost to friction)

Controlling friction is crucial

(Nano-) friction at a glance

Studying friction usually means describing the *dissipative dynamics of a slider* (e.g., a chain of interacting particles) *moving over a surface* (e.g., a rigid / deformable / periodic / disordered substrate potential) *due to the application of an external force*.

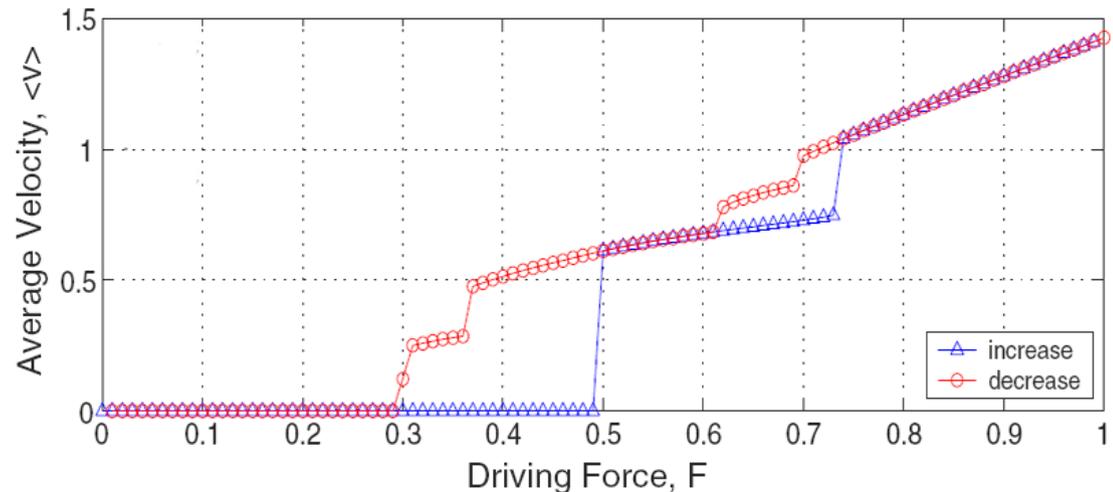


➤ How does the system respond to external driving ? ◀

• What are the features at the basis of:

- *pinning*
- *depinning transition*
- *sliding regimes*
- *stick-slip and smooth dynamics*
- *superlubricity*
- *energy dissipation*
- ... ?

• In general, *the mobility is a highly nonlinear function of the force*.



Urbakh et al., Nature 430, 525 (2004).

Muser et al., Adv. Chem. Phys. 126, 187 (2003).

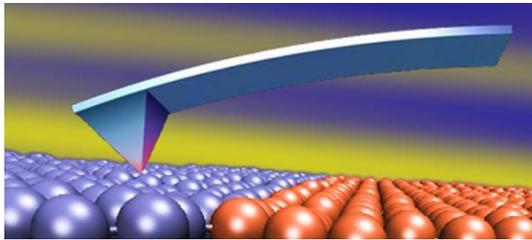
Vanossi and Braun, J. Phys.: Condens. Matter 19, 305017 (2007).

(Nano-) friction at a glance

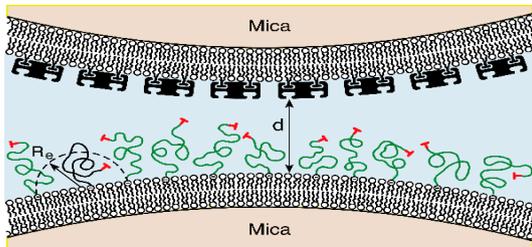
How to study all that?

Fundamental understanding begins at the smaller scales, where the basic processes are involved and *experiments at well-characterized interfaces* are now possible

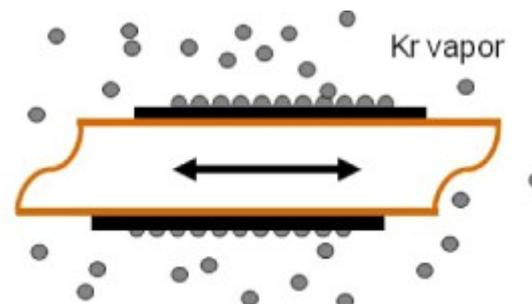
Experimentally



AFM/FFM

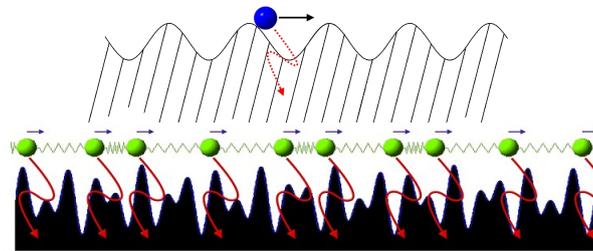


SFA

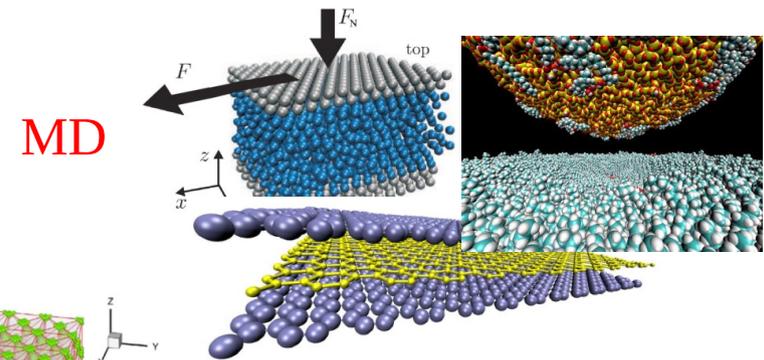


QCM

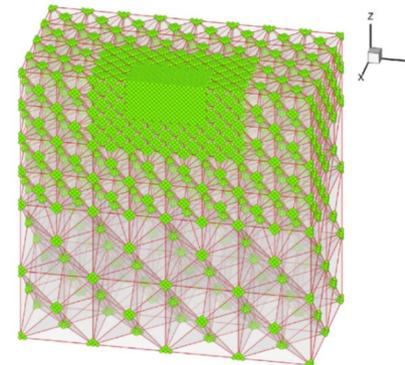
Theoretically



Minimalistic



MD



Multiscale

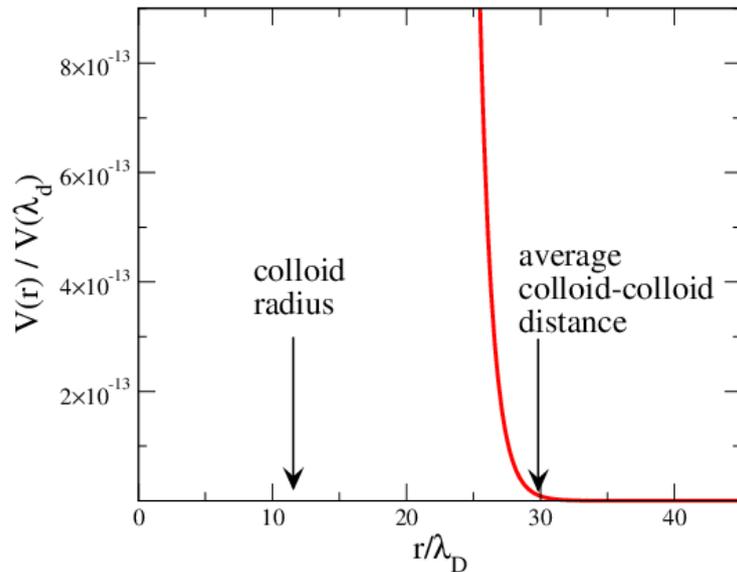
Robbins and Muser, in Modern Tribology Handbook (2001)

Vanossi, Manini, Urbakh, Zapperi, Tosatti, Rev. Mod. Phys, 2013

Friction in driven colloidal monolayers

- **Replace atoms with micron-sized colloidal particles**
- **Create substrate potentials with optical light fields**

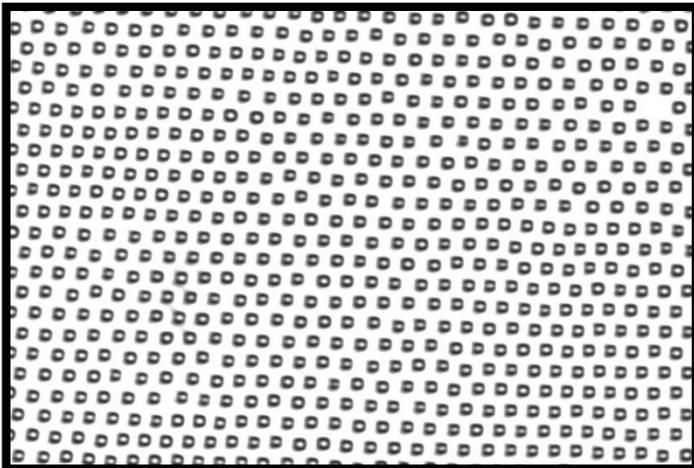
Specifically: highly charged polystyrene spheres ($R=1.95 \mu\text{m}$) suspended in water



Repulsive screened electrostatic-pair potential

$$V(r) = (Q/r) \exp(-r/\lambda_D)$$

with the Debye screening length $\lambda_D (= 0.16 \mu\text{m} \ll R)$
tuned by the ion concentration of the suspension



Formation of a **2D hexagonal crystal under confinement**

Driven colloidal monolayers

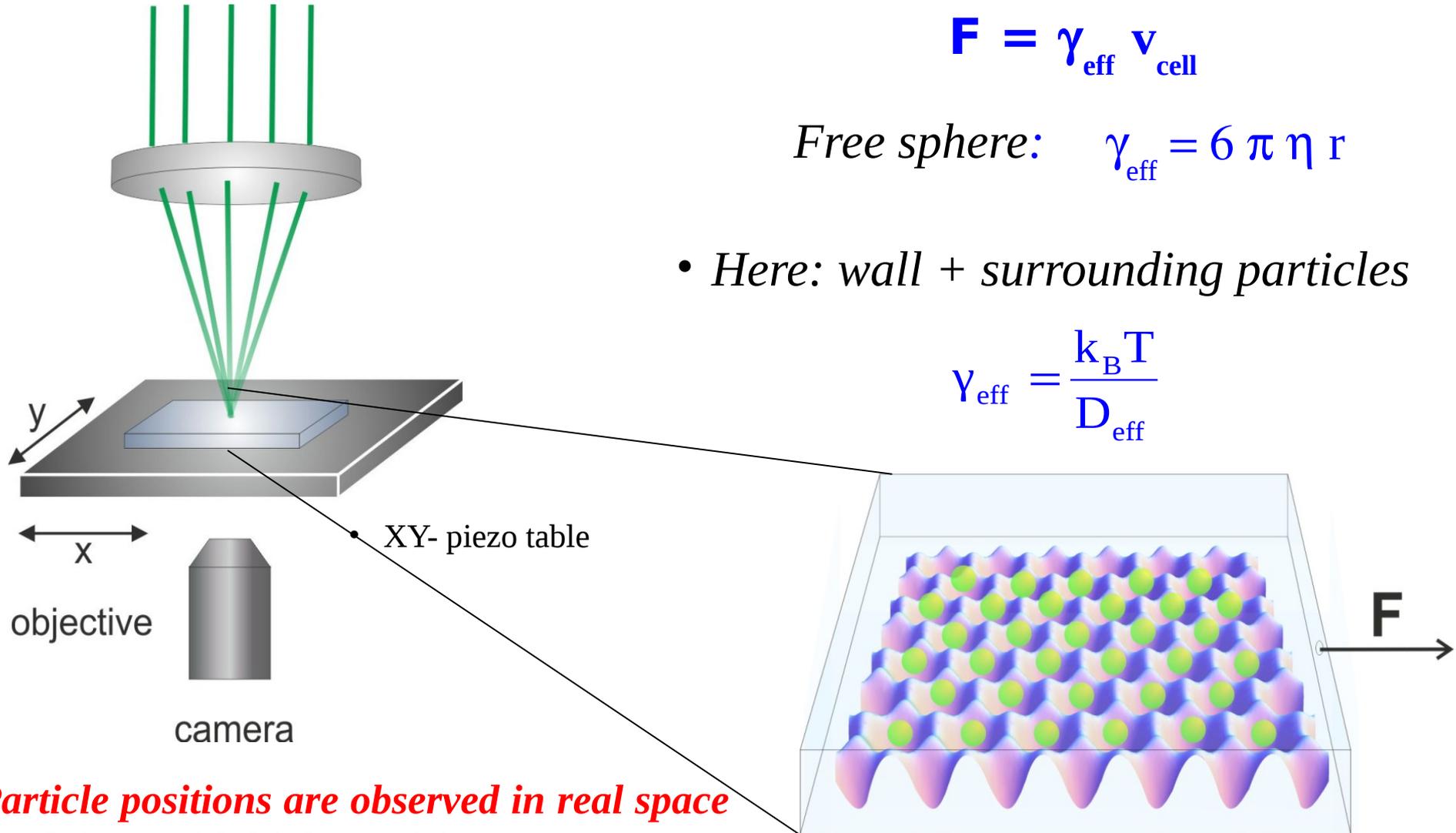
Translation of sample cell \rightarrow lateral force

$$\mathbf{F} = \gamma_{\text{eff}} \mathbf{v}_{\text{cell}}$$

Free sphere: $\gamma_{\text{eff}} = 6 \pi \eta r$

- Here: wall + surrounding particles

$$\gamma_{\text{eff}} = \frac{k_B T}{D_{\text{eff}}}$$



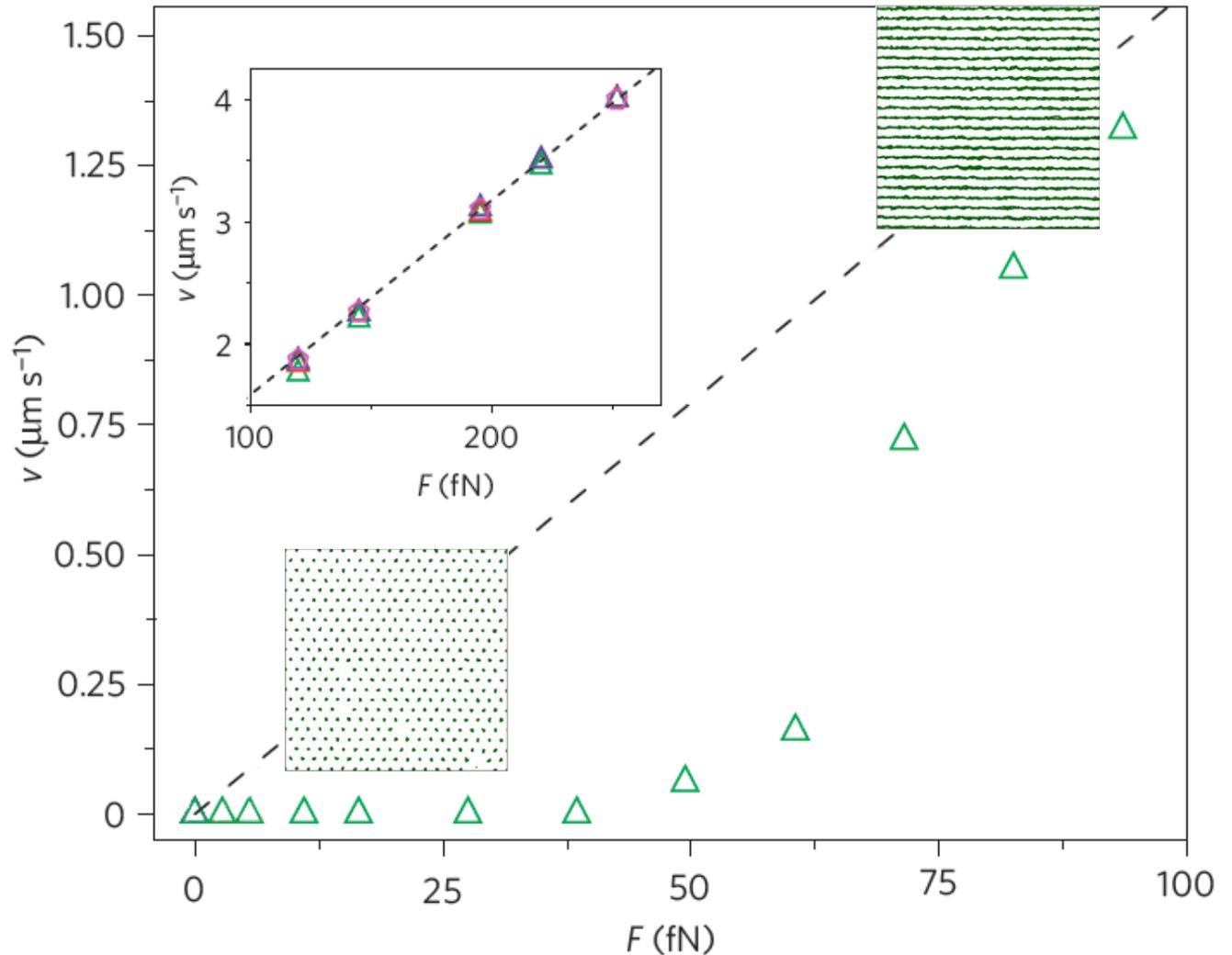
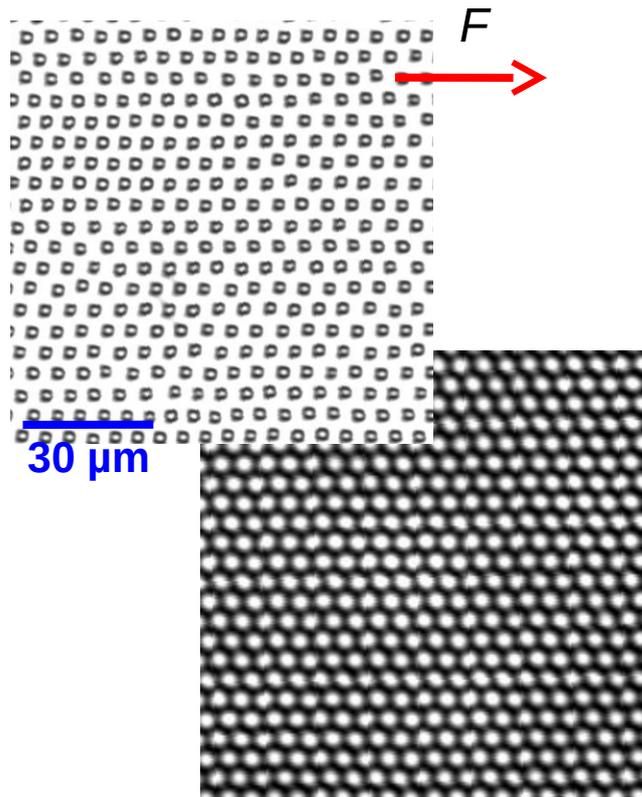
Particle positions are observed in real space (and time) with high precision (20 nm)

adjustable strength, **geometry** and **length scale** of substrate potential !!

Experimental findings

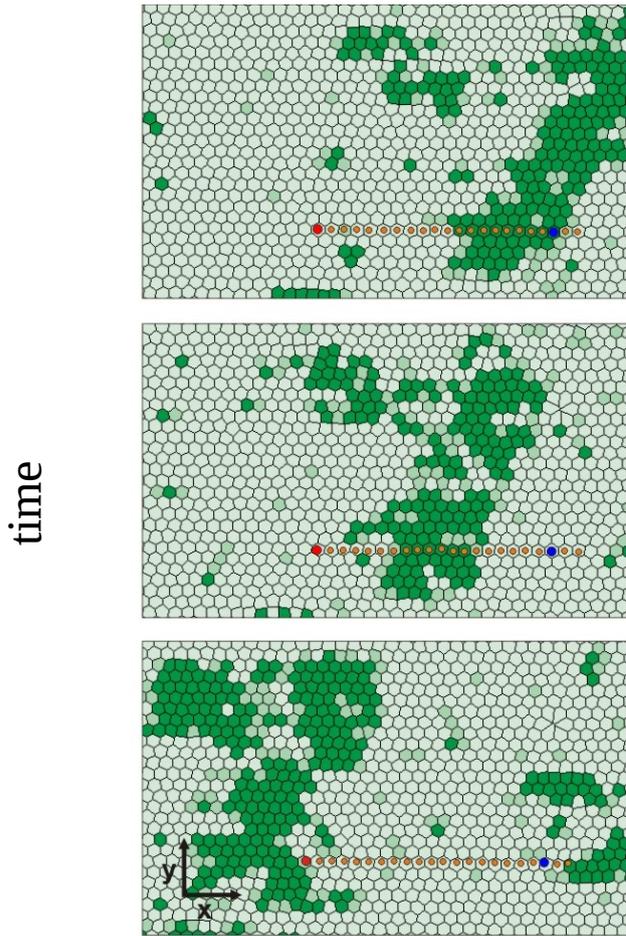
Friction of a colloidal crystal on a periodic substrate

commensurate case $a_{coll} = a_{sub}$ ($= 5.7 \mu\text{m}$)



Experimental findings

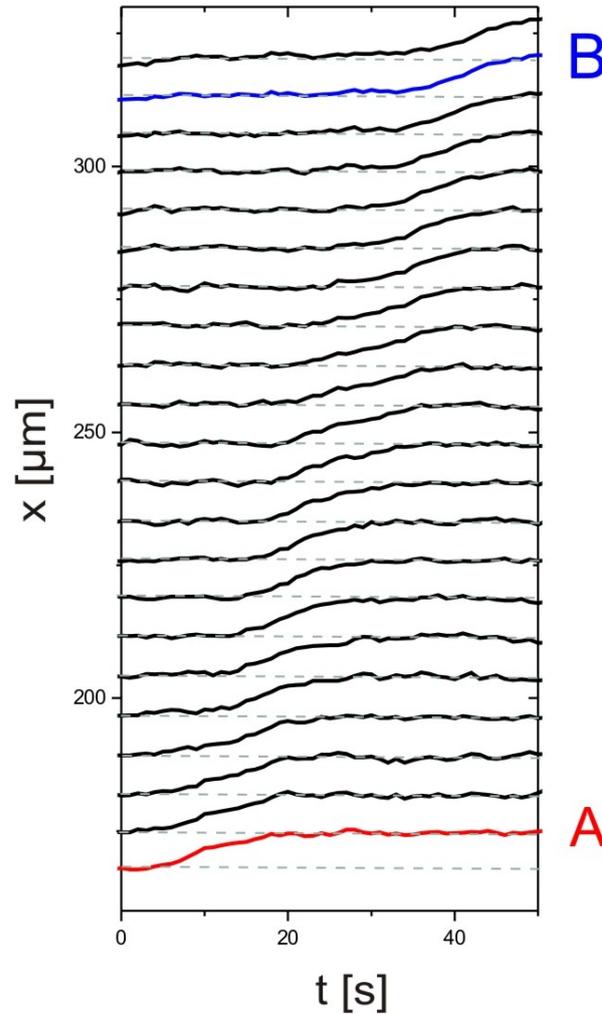
just above the **depinning transition...**



A

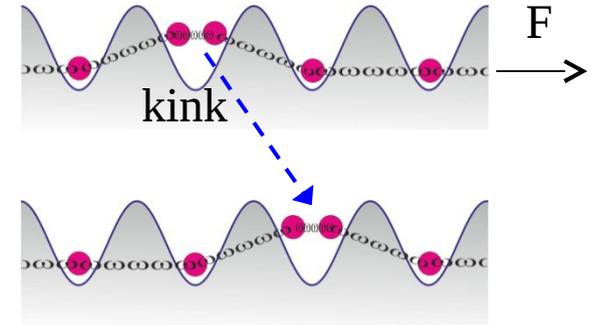
B

fast particles coincide with compressed areas

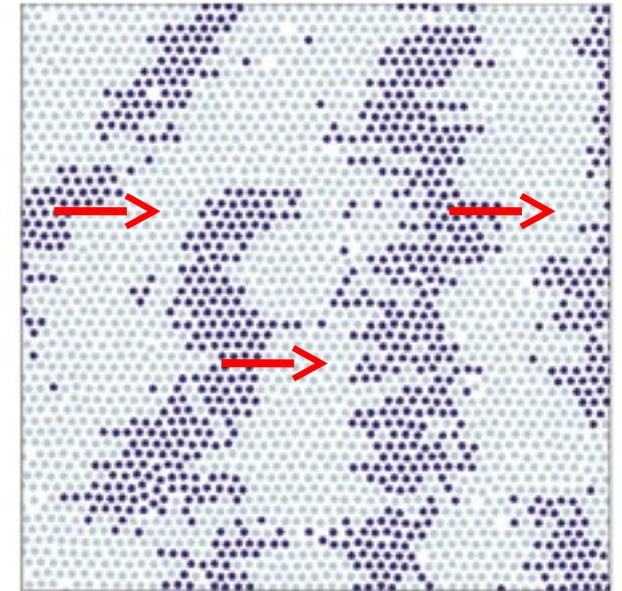


B

A



mass transport occurs via the translation of kinks



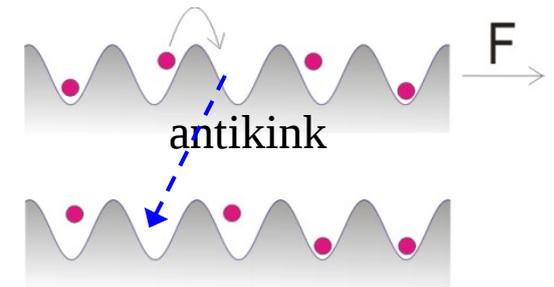
...at **higher driving**

Why kinks at a commensurate interface ???

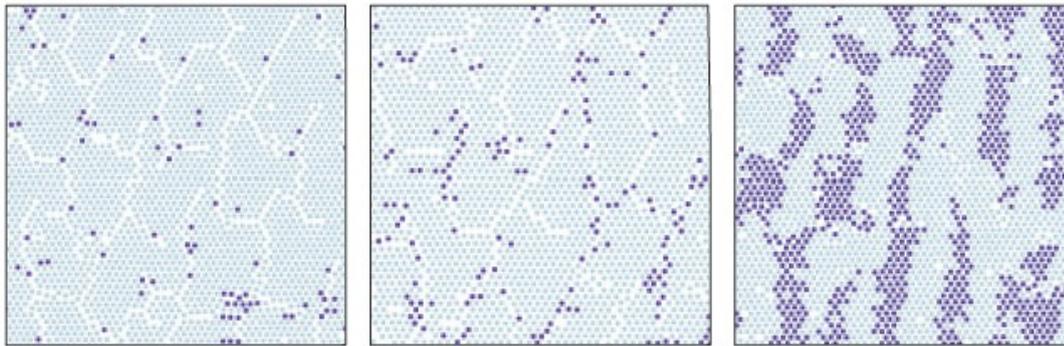
Experimental findings

Friction of a colloidal crystal on a periodic substrate

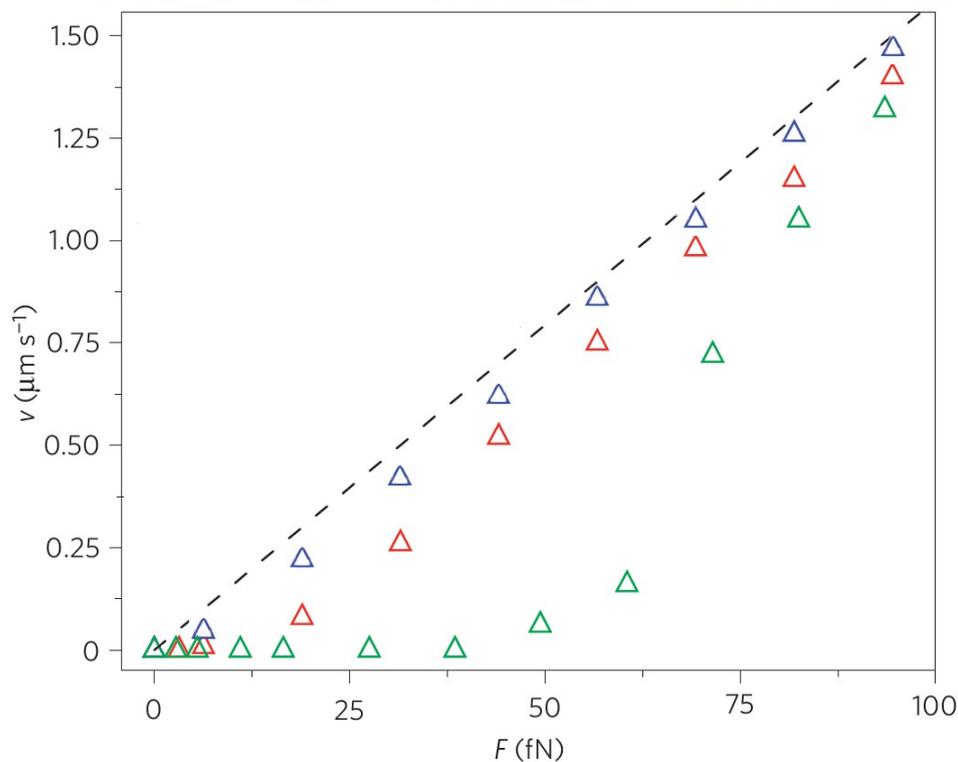
incommensurate case $a_{coll} > a_{sub}$



Increasing driving force



Fast particles coincide with expanded areas



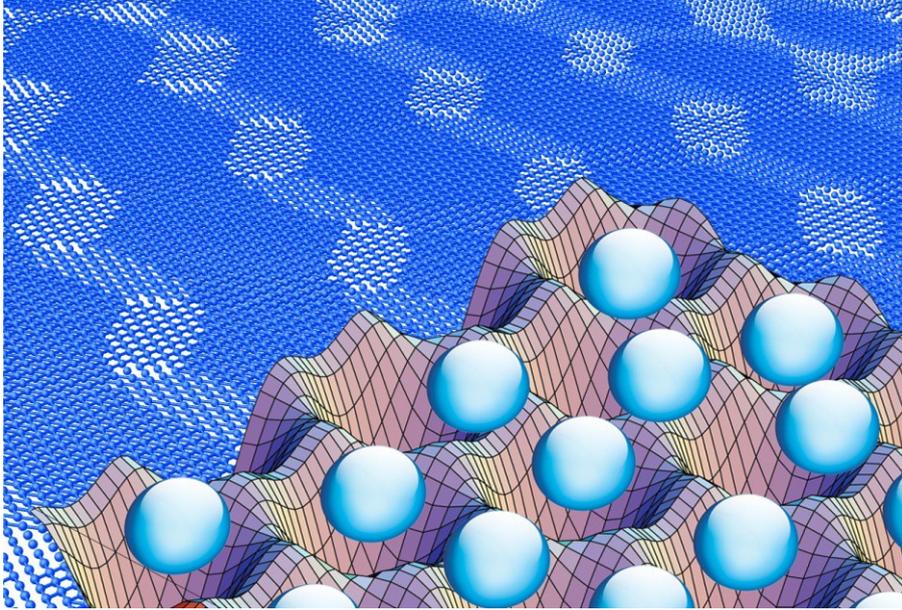
Static friction is largely reduced due to preformed antikinks

$$a_{coll} = 5.7 \mu\text{m}$$

$$a_{sub} = 5.7 \mu\text{m} \quad a_{sub} = 5.2 \mu\text{m} \quad a_{sub} = 4.8 \mu\text{m}$$

 toward *superlubricity*

MD modeling



- modelled as **charged point particles undergoing overdamped 2D dynamics under an external force** applied to each colloid
- $V(r_{ij}) = Q/r_{ij} \exp(-r_{ij}/\lambda_D)$
screened Coulomb repulsion with λ_D substantially smaller than the mean particle distance
- $F = \eta v_d$ (**fluid effective viscosity and velocity**)
- $-\eta v_i$ (**Stokes viscous force**)

- colloids are immersed in a Gaussian-shaped overall confining potential

$$G(|\mathbf{r}|) = -A_c \exp(-r^2/\sigma^2). \quad (\text{laser spot})$$

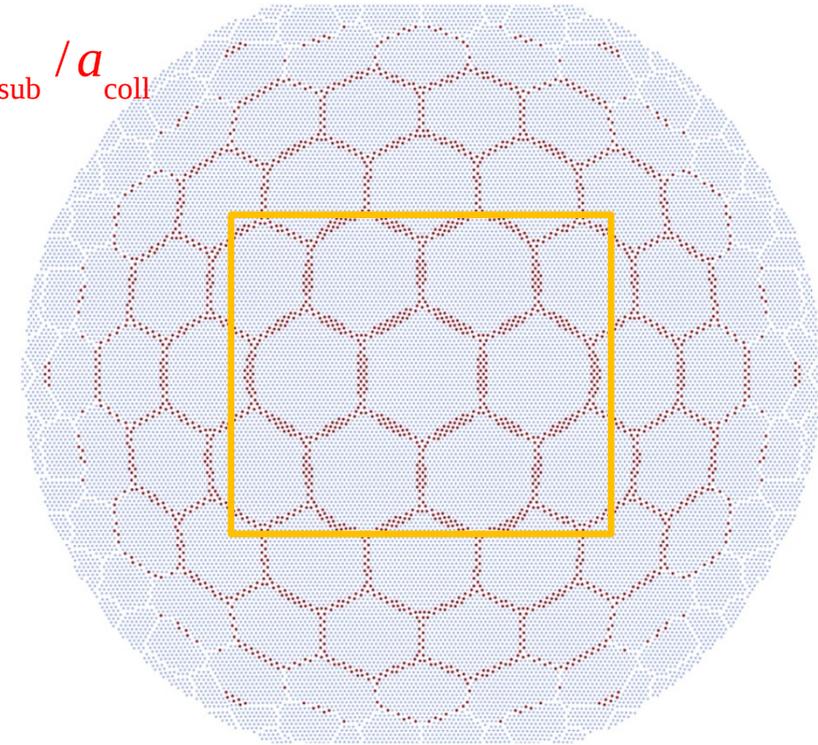
and in a triangular-lattice periodic potential

$$W(\vec{r}) = -\frac{2}{9} U_0 \left[\frac{3}{2} + 2 \cos \frac{2\pi r_x}{a_{\text{sub}}} \cos \frac{2\pi r_y}{\sqrt{3}a_{\text{sub}}} + \cos \frac{4\pi r_y}{\sqrt{3}a_{\text{sub}}} \right] \quad (\text{substrate corrugation})$$

MD modeling

typical **simulation size** $N \simeq 30,000$

- $U_0 = 0$, 2D **triangular colloidal lattice island** at rest (confining and repulsion energy balance)
- balance setting so that the **average** $a_{\text{coll}} = 1$
- by **changing** $a_{\text{sub}} = 1$, variety of mismatched ratios $\rho = a_{\text{sub}} / a_{\text{coll}}$
 - 3 representative cases:
 - **underdense**, $\rho = 0.95$ (AI)
 - **nearly commensurate**, $\rho \simeq 1.0$ (CO)
 - **overdense**, $\rho = 1.05$ (SI)



MD modeling

typical **simulation size** $N \simeq 30,000$

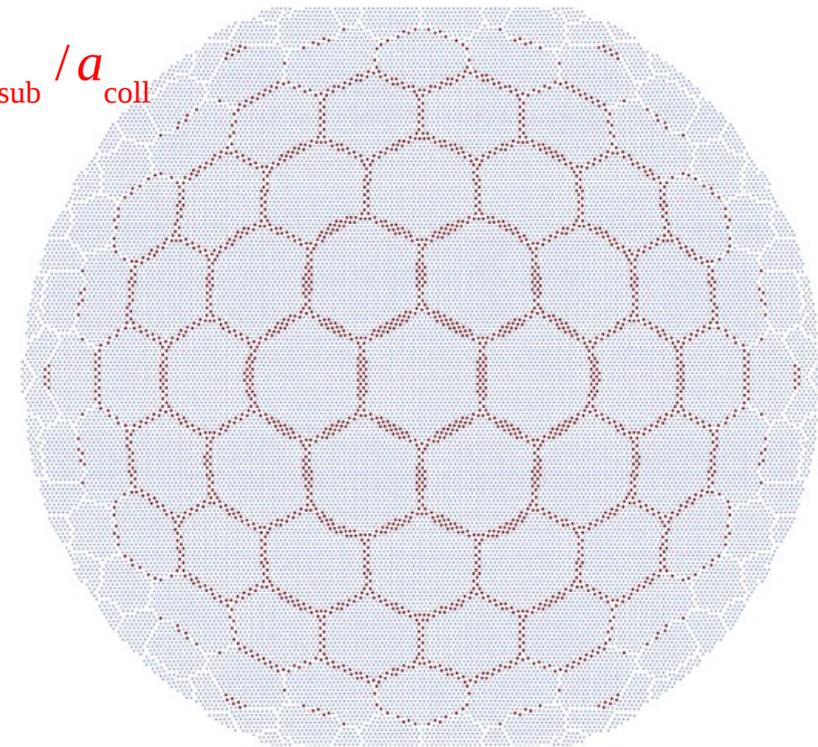
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➤ 3 representative cases:

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- **overdense**, $\rho = 1.05$ (SI)

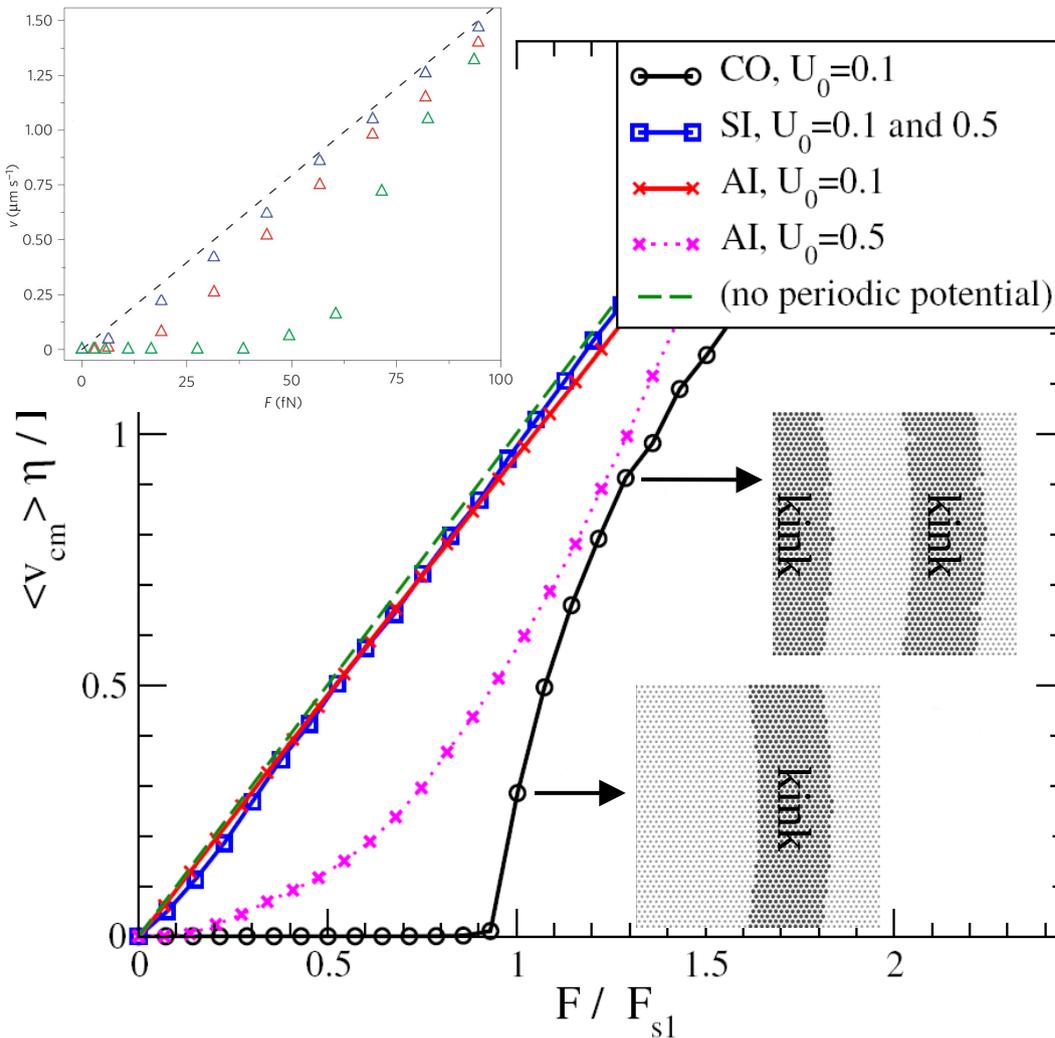
- In order to:
 - mimic the experiment,
 - prevent solitons from leaving the finite-size sample,

the **external force F** is **ramped adiabatically alternating in sign** (back and forth).



MD results

force-velocity characteristics



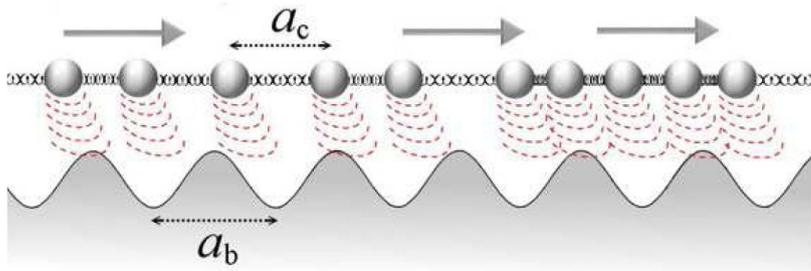
- **large static friction force** for $\rho \approx 1$ CO
- for **moderate corrugation U_0 and 5% lattice mismatch**, static friction drops essentially to zero, and a nearly free viscous sliding is realized (**superlubricity**)
- by **increasing U_0** , the AI mobility drops to zero at small force, and **pinning reemerges despite AI incommensurability**
- by contrast, **SI configurations remain superlubric** up to much larger U_0 .

- snapshots of the central region of the initially commensurate colloid during motion, illustrating **sliding-generated solitons**, whose **density increases as F is increased**.

Note: colloids located at repulsive spots of the corrugation potential [$W(r) > -U_0/2$] are drawn as dark points, while colloids nearer to potential minima [$W(r) \leq -U_0/2$] are light.

General theory: recall the Aubry transition

- The *1D Frenkel-Kontorova model*, harmonically interacting atoms subject to a sinusoidal potential



$$H = \frac{m}{2} \sum_i \dot{x}_i^2 + \sum_i \left[\frac{K}{2} (x_{i+1} - x_i - a_c)^2 + \frac{\mathcal{E}}{2} \left(1 - \cos \frac{2\pi}{a_b} x_i \right) \right],$$

undergoes, for *incommensurate configurations* (a_b/a_c *irrational*) and fixing the amplitude \mathcal{E} , the famous *Aubry transition* at a critical value K_c of the interatomic interaction.

Above the transition ($K > K_c$)

- ▶ no forbidden regions over the substrate potential for the values x_i
- ▶ incommensurate ground states described by an analytic hull function
- ▶ zero static friction (*superlubricity*)

Below the transition ($K < K_c$)

- ▶ particles trapped close to the minima of the substrate potential, forbidden regions arise
- ▶ incommensurate ground states described by a non-analytic hull function
- ▶ finite static friction (*pinning*)

Peyrard and Aubry, J. Phys. C: Solid State Phys. 16, 1593 (1983).

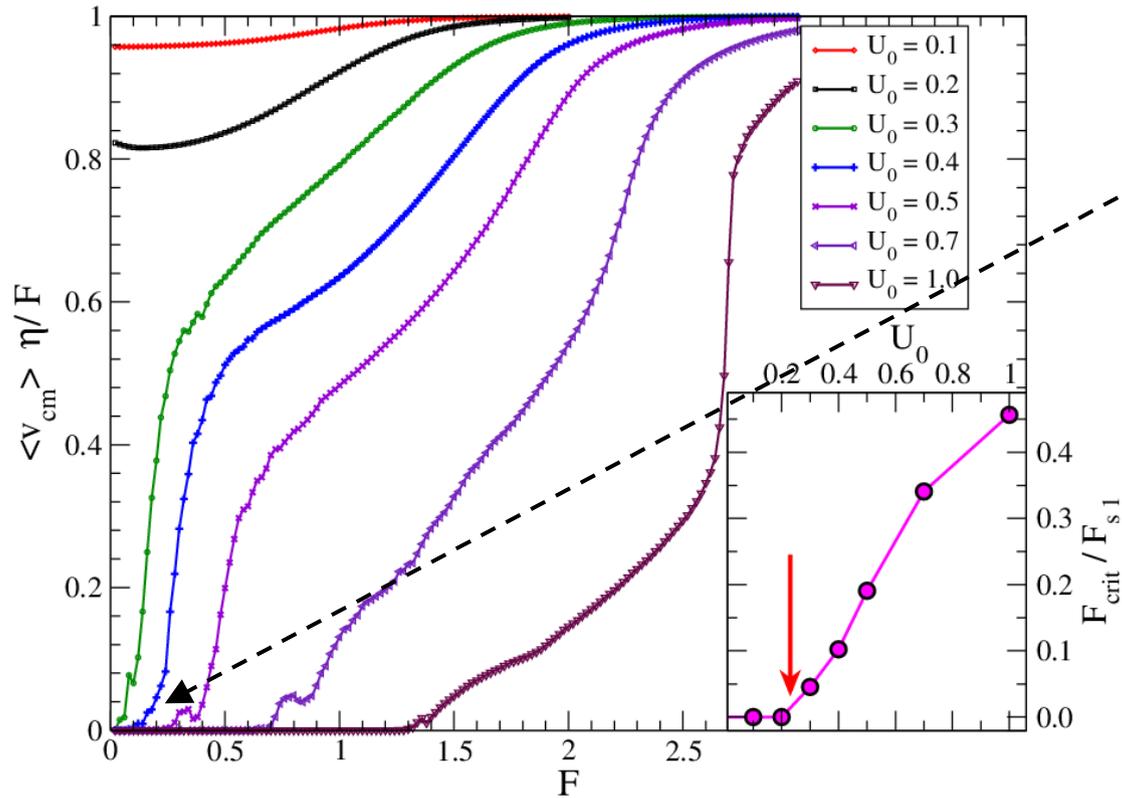
Braun and Kivshar, The Frenkel-Kontorova Model (Springer, Berlin, 2004).

Vanossi and Braun, J. Phys.: Condens. Matter 19, 305017 (2007).

MD results: the Aubry transition

Even in our 2D case, it is expected that **incommensurate colloids**, underdense ($\rho \lesssim 1$) or overdense ($\rho \gtrsim 1$), **undergo an Aubry-like superlubric-to-pinned transition for increasing U_0** .

mobility vs applied force for $\rho = 0.95$ (AI) [infinite-size colloid system]



*appearance of pinning
just above $U_0 = 0.2$*

*normalized static friction F_{crit} vs U_0
the arrow indicating the critical
Aubry corrugation*

This **ρ -dependent critical U_0** is **much larger for overdense SI** than for underdense AI colloids

The **soliton-antisoliton asymmetry** arises from the intercolloid effective spring constant

$$\frac{V''(a \pm \delta)}{V''(a)} \simeq \exp(-\delta/\lambda_D)$$

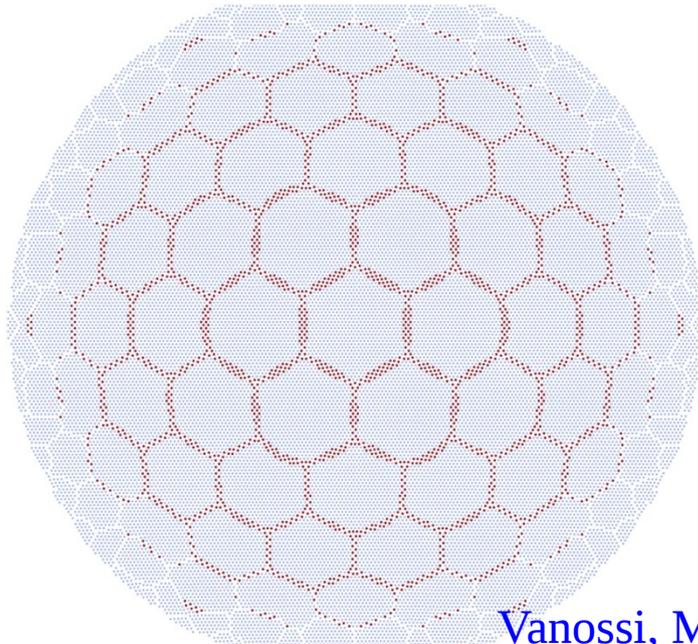
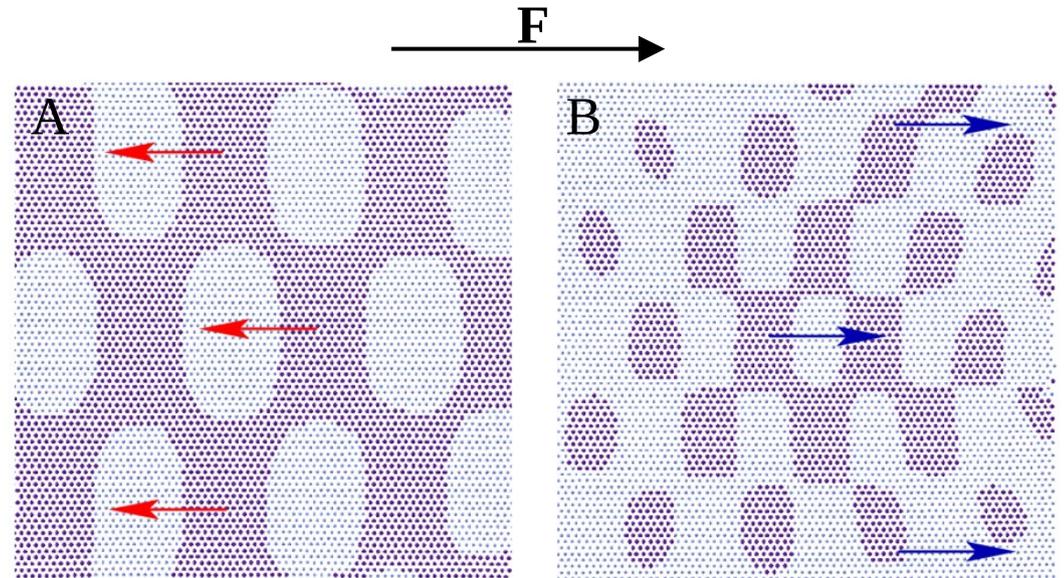
MD results

incommensurate colloid: sliding states

- The evolution of solitons/antisolitons (comparable with experiment) is of immediate interest. **With increasing F , their arrangements elongate into a stripe-like pattern perpendicular to the driving direction.**

(A) For underdense colloid ($\rho = 0.95$), preformed antisolitons **fly backward** antiparallel to the rightward force.

(B) For overdense colloid ($\rho = 1.05$), preformed solitons **fly rightward**, parallel to the force.



Dropping the back-and-forth driving protocol,

- **antisolitons** are eventually absorbed at the left edge boundary, while new ones spawn at the right edge, sustaining a steady-state mobility;
- **solitons** instead are not automatically spawned at the boundary, owing to the decreasing density.

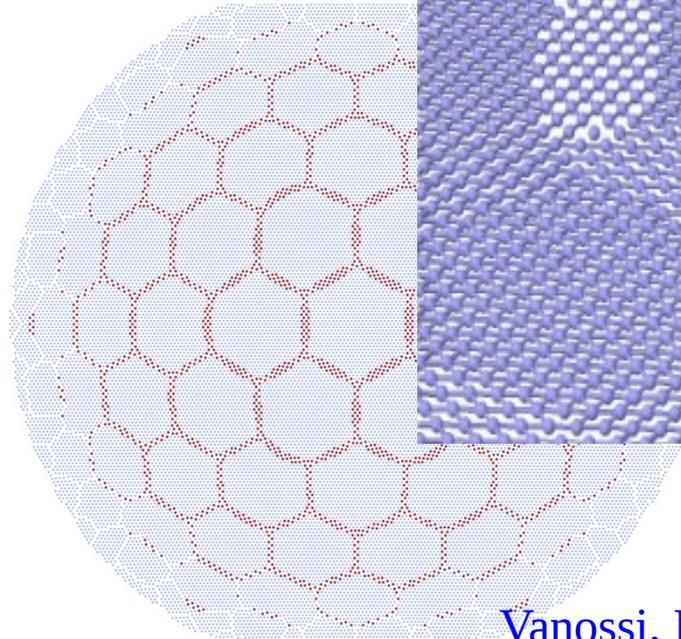
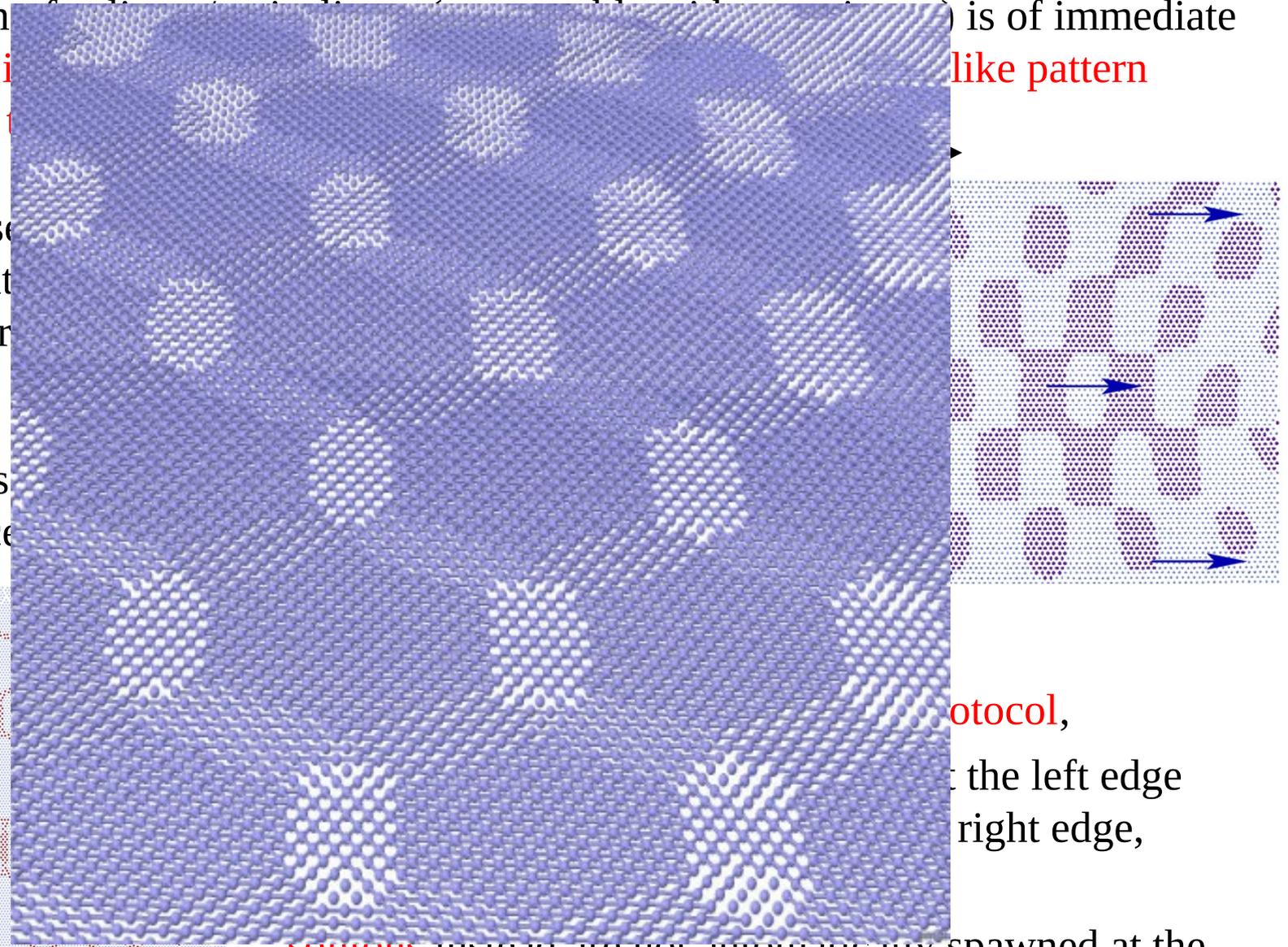
MD results

incommensurate colloid: sliding states

- The evolution of the system (under overdense conditions) is of immediate interest. **With incommensurate sliding states perpendicular to the force**

(A) For underdense conditions, preformed antisolitons are antiparallel to the force

(B) For overdense conditions, preformed solitons are parallel to the force



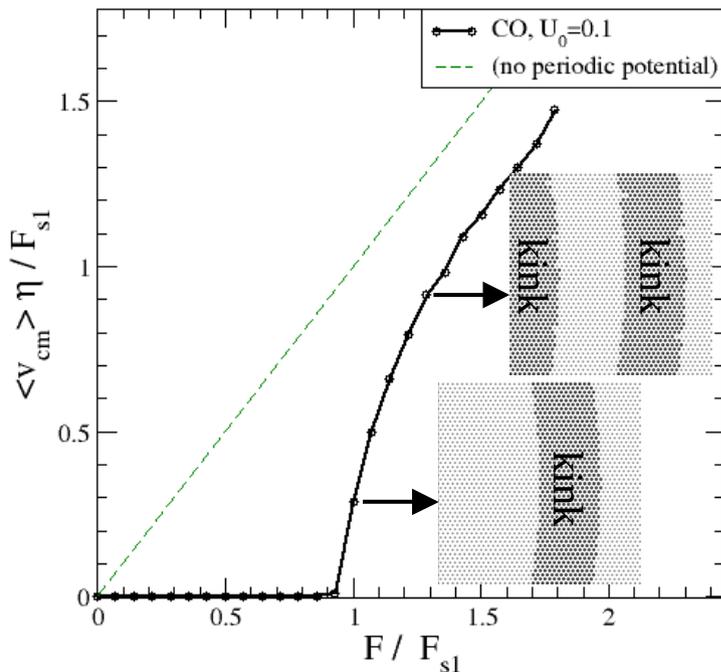
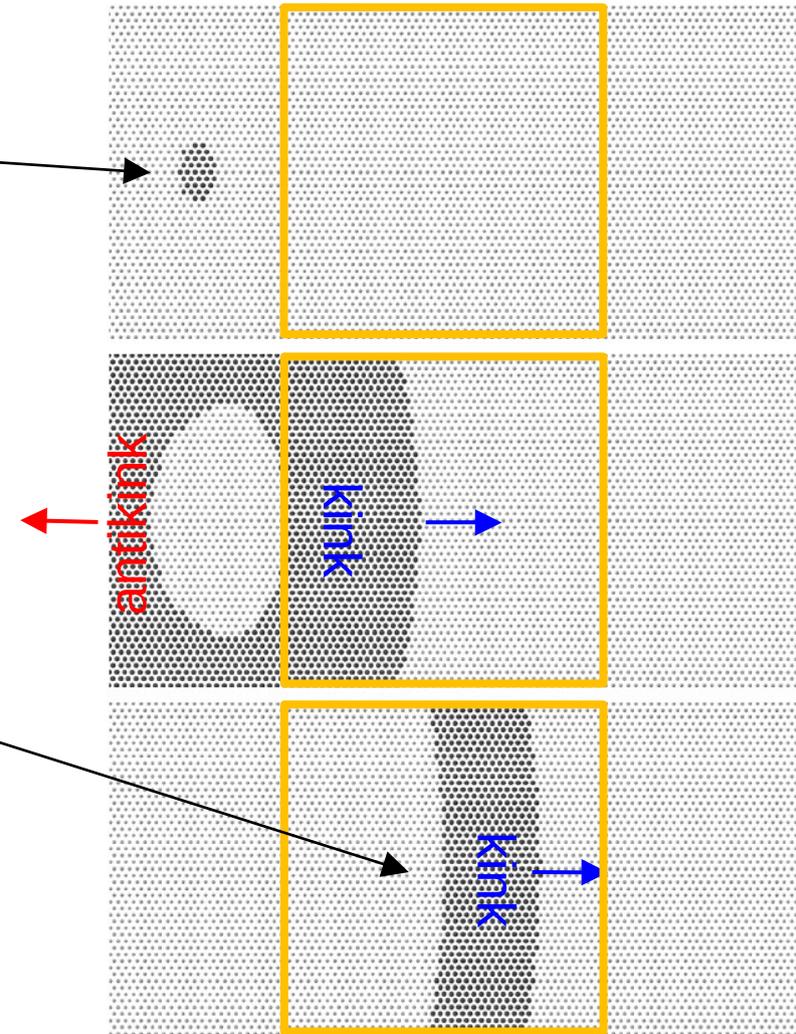
protocol,
at the left edge
right edge,

- **SOLITONS** instead are not automatically spawned at the boundary, owing to the decreasing density.

MD results

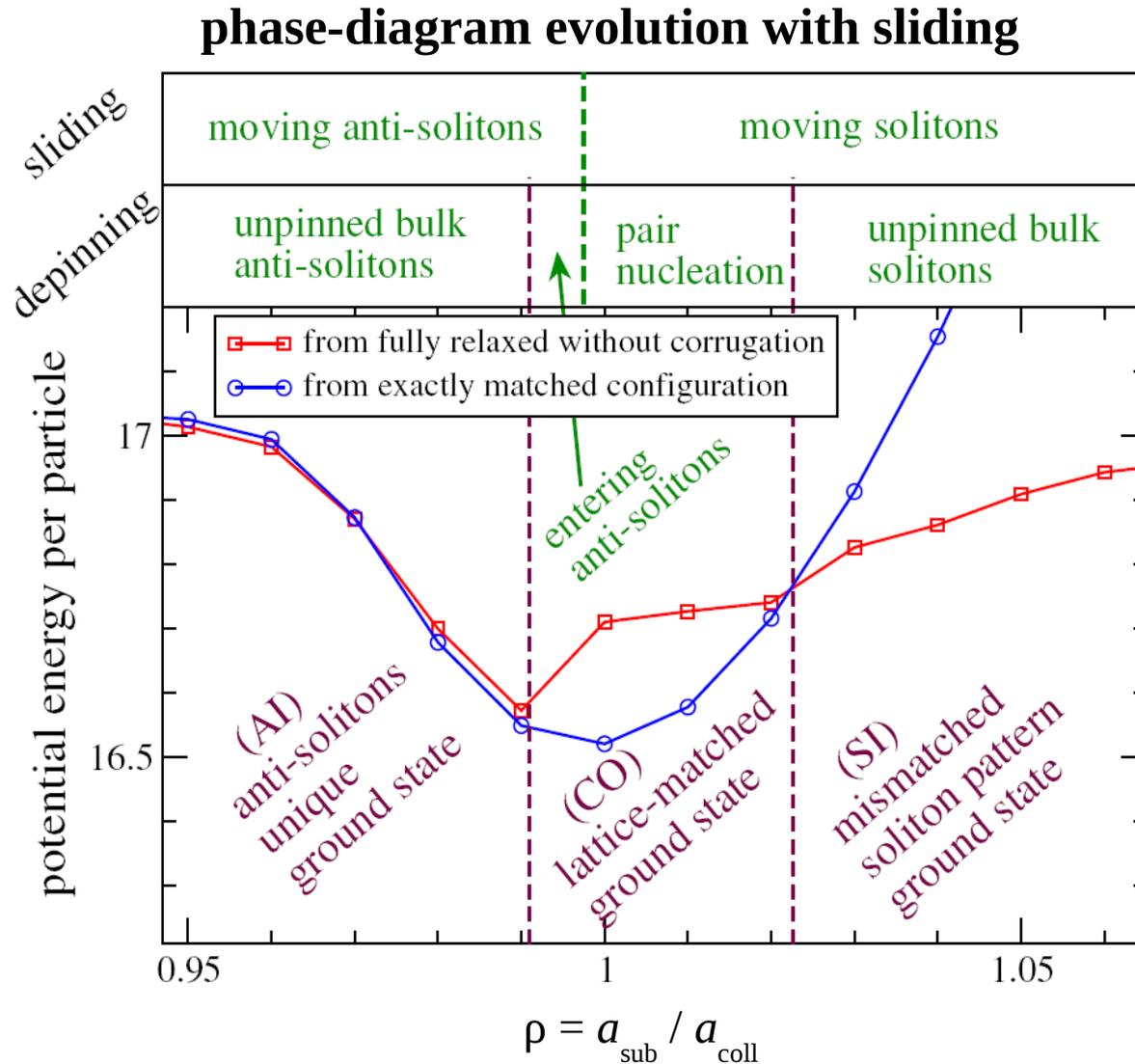
commensurate colloid: sliding states

- the **colloid only moves** after static friction is overcome
- **motion initiates by nucleation of soliton–antisoliton pairs** inside the bulk -**close to the left edge** because the central region tends to be slightly overdense
- **antisolitons flow leftwards** and **become undetectable** to the optically monitored central part of the colloid, where **only solitons transit**, as seen in experiment



- for pinned CO colloid the **soliton density**, initially zero, actually **increases with increasing driving force**

MD results



- With a nominal $\rho \approx 1$, but not exactly commensurate, the monolayer can realize (depending on U_0) a static arrangement with fully lattice-matched CO state.
- Under the external force, sliding may tilt the balance in favor of the 'natural' slightly mismatched arrangement, populating the former static CO phase with solitonic structures.

MD results

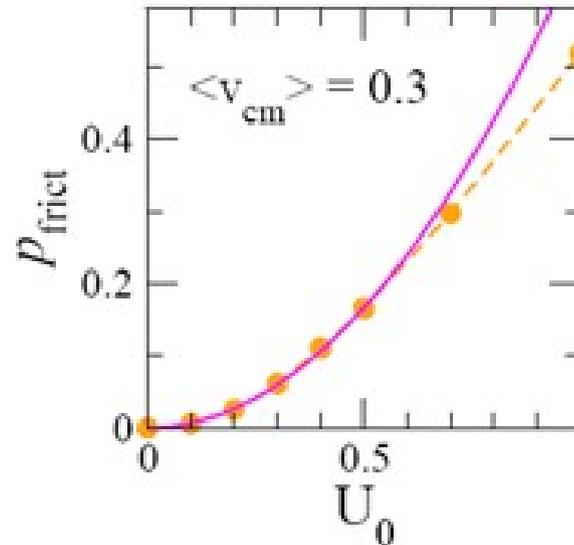
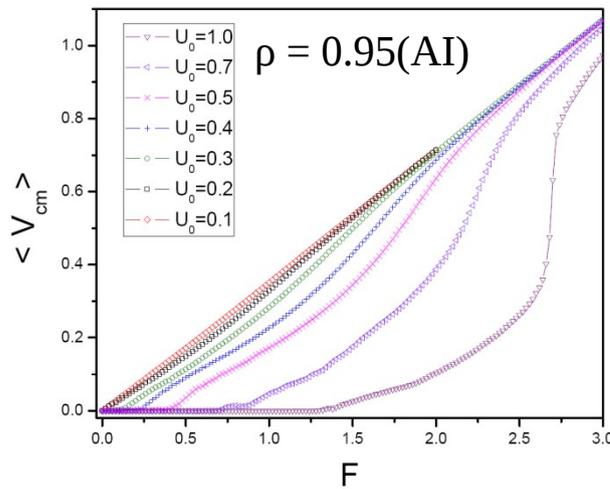
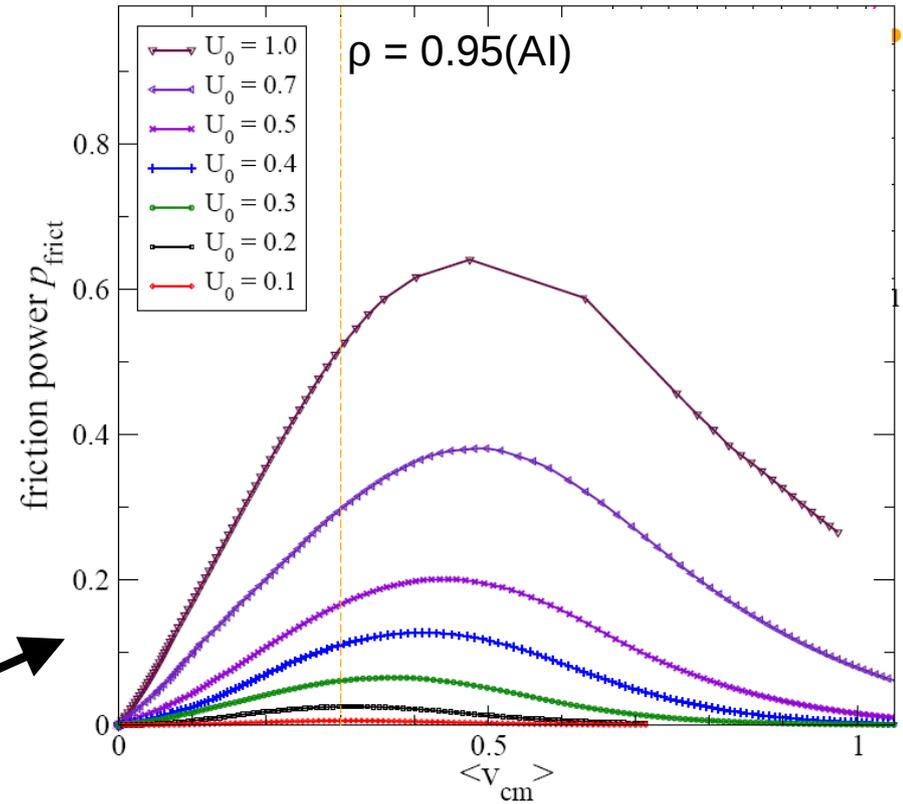
- Under steady sliding, the time-averaged overall power balance

$$\begin{aligned}
 P_{\text{tot}} &= \sum_i \eta \langle (\mathbf{v}_d - \mathbf{v}_i) \cdot \mathbf{v}_i \rangle \\
 &= (N\mathbf{F} \cdot \langle \mathbf{v}_{\text{cm}} \rangle - \eta \langle |\mathbf{v}_{\text{cm}}|^2 \rangle) - \eta \sum_i \langle |\mathbf{u}_i|^2 \rangle \\
 &= P_{\text{frict}} - P_{\text{kin}}, \quad (\mathbf{u}_i = \mathbf{v}_i - \mathbf{v}_{\text{cm}})
 \end{aligned}$$

vanishes ($P_{\text{tot}} = 0$), and the effective friction power is exactly balanced by an internal kinetic energy excess rate.

$$p_{\text{frict}} = \frac{P_{\text{frict}}}{N} \simeq \mathbf{F} \cdot \langle \mathbf{v}_{\text{cm}} \rangle - \eta |\langle \mathbf{v}_{\text{cm}} \rangle|^2$$

friction dissipation

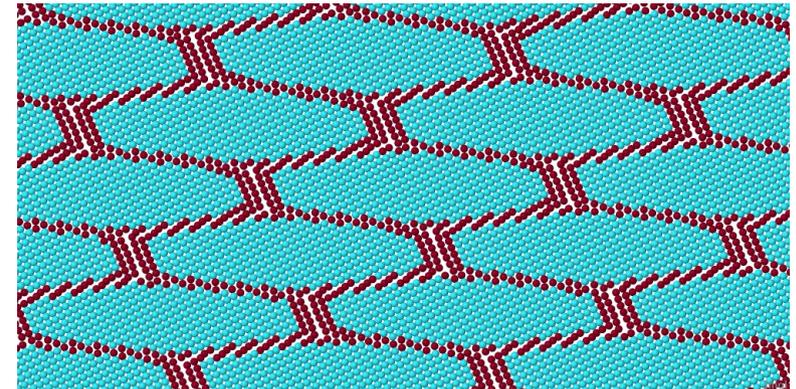


friction increase with U_0 , for a chosen speed, is found quadratic at weak corrugation, gradually turning to linear for larger U_0 values

Summary

Driven colloid systems offers the attractive possibility:

- to **change parameters** (symmetries, lattice spacings, corrugation amplitudes) **freely**
- to **compare directly experiment with simulations**, testing theoretical predictions
- to **visualize in real-time** in simple cases the intimate mechanisms of sliding friction, relating the overall tribological response to the detailed particle dynamics



Outlook

This work opens several lines of present & future research:

- trapping-and-driving method to **introduce stick-slip**
- friction tuning by **oscillating substrate** potentials
- dependence of friction on **contact size**
- sliding on **peculiar substrate geometries**
- large colloidal crystal sizes to address **mesoscopic complexity**

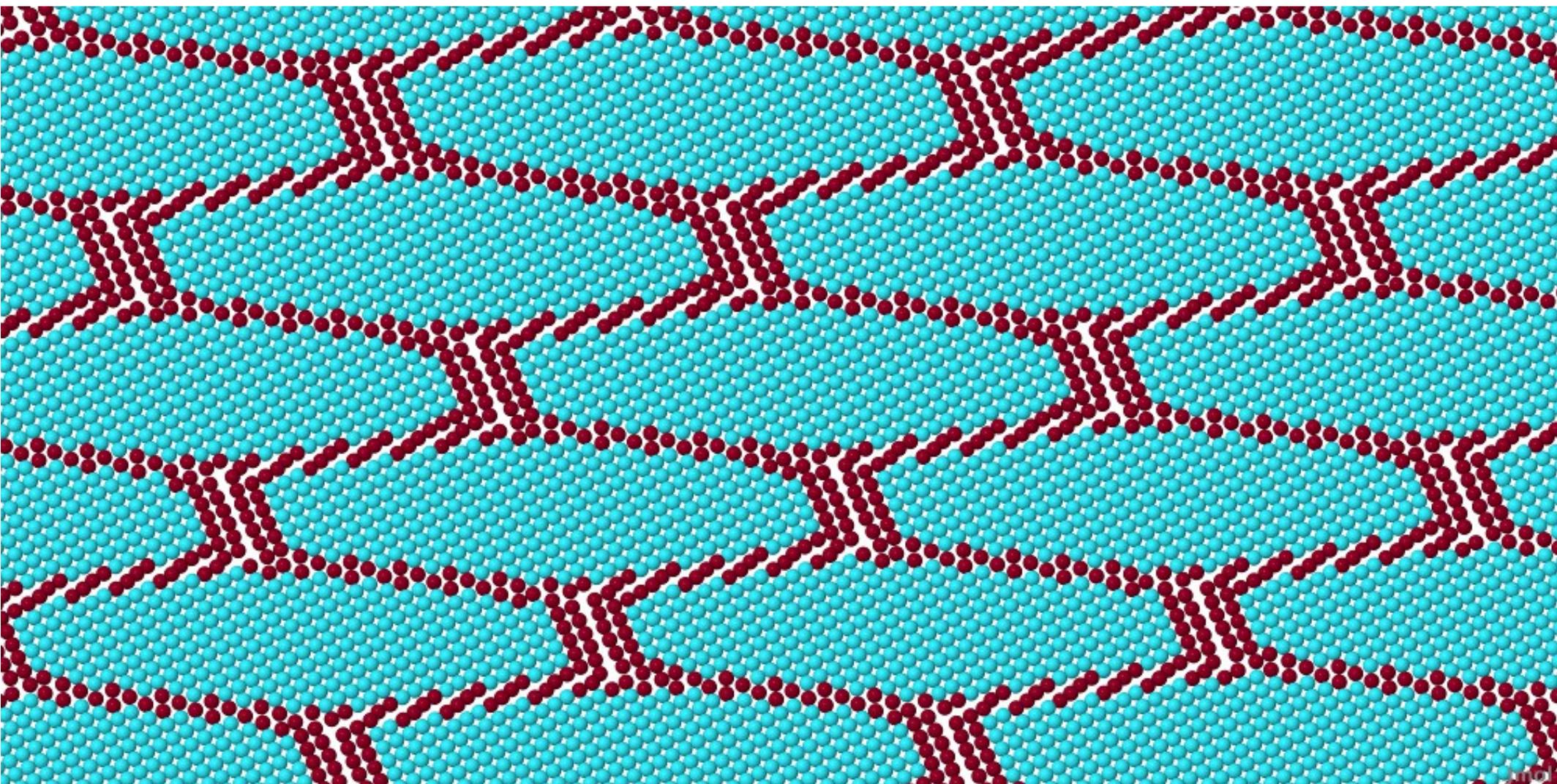


Table S2. Basic units for various quantities in our model, with typical values appropriate for the setup by Bohlein et al. 1.

Physical quantity	Model expression	Typical value
Length	a_{coll}	5.7 μm
Force	$F_0 = 9F_{s1}/(8\pi)$	18 fN
Viscosity coefficient	η	6.3×10^{-8} kg/s
Energy	$F_0 a_{\text{coll}}$	1.0×10^{-19} J
Time	$\eta a_{\text{coll}}^2 / U_0$	20 s
Mass	$\eta^2 a_{\text{coll}} / F_0$	1.3×10^{-6} kg
Velocity	F_0 / η	0.284 $\mu\text{m/s}$
Power	F_0^2 / η	5.1×10^{-21} W

Table S3. Numerical parameters adopted in the simulation, Eqs. S3, S5, S6, and S7, expressed in model units, to be scaled according to Table S2. L_x and L_y are the sides of the rectangular simulation supercell, respectively.

	η	N	Q	λ_D	A_c	σ	n	U_0	L_x	L_y
Cluster	1.4	28,861	10^{13}	0.03	1,200	1,200	3	0.1	500	500
Bulk	1.4	28,080	10^{13}	0.03	0.0	1,200	3	0.1	156	$90\sqrt{3}$