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## The refinement of a meteorological preprocessor for the urban environment

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**Abstract:** The meteorological preprocessor used routinely at the Finnish Meteorological Institute (FMI) has been modified in order to better represent urban conditions. We have re-evaluated the roughness length, introduced the zero-displacement height and divided the surface layer into a roughness sublayer and an inertial sublayer. The friction velocity and Monin-Obukhov length are evaluated using an empirically developed exponential Reynolds-stress profile in the roughness sublayer. The effect of these modifications has been studied by computing the dispersion parameters used in the urban dispersion modelling system UDM-FMI and comparing the revised parameters with the previous model computations.

**Keywords:** meteorological preprocessor, urban environment, dispersion

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### 1 Introduction

Short-range atmospheric dispersion models require input data on the state of the atmospheric boundary layer. These models need estimates of at least the mean plume transport velocity, the lateral and vertical components of turbulent energy, the vertical stability parameter and the mixing depth. Not all of these parameters are routinely observed, and it is therefore necessary to estimate them in terms of the routinely observed variables, using a so-called meteorological preprocessor.

The meteorological preprocessor applied in combination with the regulatory atmospheric dispersion models in Finland (Karppinen et al., 1997) was originally designed for rural areas only. This paper describes the modifications of the meteorological preprocessor in order to account for urban conditions. The atmospheric surface layer is divided into two parts: a roughness sublayer of height  $z^*$  and an inertial sublayer. Monin-Obukhov similarity laws are expected to be valid only in the inertial sublayer (Rotach, 1996). Close to the ground surface, the local Reynolds stress profile is used to recalculate the relevant turbulence parameters.

The key parameter in order to characterise vertical turbulence, the Monin-Obukhov length  $L$ , can be assumed to be equal to the depth of the mechanically well-mixed layer

(for instance, Stull, 1988); this can be identified as the roughness sublayer. In stable conditions we therefore set the minimum value for  $L$  to be equal to  $z^*$  ( $L \geq z^* \equiv L_{\min}$ ).

The influence of these modifications has been analysed by computing the dispersion parameters used in the UDM-FMI dispersion modelling system, and comparing the revised parameters with the previous "non-urban" model computations.

## 2 Description of the meteorological pre-processor

The meteorological pre-processing model is based on the method developed originally by van Ulden and Holtslag (1985). This method evaluates the turbulent heat and momentum fluxes in the atmospheric boundary layer (ABL) from synoptic weather observations. The parameterization of the ABL height is based on boundary layer scaling, utilizing meteorological sounding data.

The four main scaling parameters of this method are: the roughness height  $z_o$ , the friction velocity  $u_*$ , the temperature scale  $\theta_*$  and the boundary layer height  $z_i$ . The friction velocity  $u_*$  determines the shear production of turbulent kinetic energy at the surface. According to surface-layer similarity theory, the wind speed  $\bar{U}(z)$  is related to  $u_*$  by

$$\bar{U}(z) = \frac{u_*}{k} \left[ \ln \left( \frac{z}{z_o} \right) - \psi_m \left( \frac{z}{L} \right) + \psi_m \left( \frac{z_o}{L} \right) \right] \quad (1)$$

The influence function  $\psi_m$  can be evaluated from (van Ulden and Holtslag, 1985):

$$\psi_m = \left( 1 - 16 \frac{z}{L} \right)^{1/4} - 1 \quad \text{for unstable stratification (} L < 0 \text{)} \quad (2)$$

$$\psi_m = -17 \left( 1 - \exp \left( -0.29 \frac{z}{L} \right) \right) \quad \text{for stable stratification (} L > 0 \text{)} \quad (3)$$

The Monin-Obukhov length  $L$  is defined by the velocity and temperature scales as

$$L = \frac{T_2 u_*^2}{k g \theta_*} \quad (4)$$

where  $T_2$  is the air temperature at the height of 2 m, and  $k$  is the von Karman constant. The scaling temperature  $\theta_*$  can be written in terms of the turbulent kinematic heat flux at the surface  $Q_o$  and the friction velocity, i.e.:  $\theta_* = -Q_o/u_*$ .

The mixing height  $h$  is defined as the mean height to which turbulence extends vertically. In unstable conditions, scalar quantities (eg. temperature, moisture) are generally well-mixed up to this height.

### 3. The dispersion parameters

The turbulence dispersion parameters in the UDM-FMI dispersion model (Karppinen et al., 1998) are written in terms of the turbulence intensities as (Hanna, 1985):

$$\begin{aligned} \sigma_{ry} = i_y f_y x, \quad i_y = \frac{\sigma_v}{\overline{U}(z)}, \quad f_y = [1 + B_y x]^{-1/2} \\ \sigma_{rz} = i_z f_z x, \quad i_z = \frac{\sigma_w}{\overline{U}(z)}, \quad f_z = [1 + B_z x]^{-1/2} \end{aligned} \quad (5)$$

where  $i_y$  and  $i_z$  are the lateral and vertical turbulence intensities,  $f_y$  and  $f_z$  are functions of the downwind distance  $x$ ,  $\sigma_v$  and  $\sigma_w$  are the standard deviations of the turbulent velocity fluctuations in the lateral and vertical direction, and  $\overline{U}(z)$  is the average wind speed at height  $z$ .

In this paper we investigate only the effect of “urban” scaling on the parameters  $\sigma_v$  and  $\sigma_w$ , although in the modelling system the parameter  $B_z$  also is a function of the roughness length and Monin-Obukhov length (and therefore stability) as follows:

$$B_z = \begin{cases} 0, & p_q \leq -0.5, (unstable) \\ 0.0003 + 0.0006 p_q, & -0.5 < p_q < 2.0, (neutral) \\ 0.0015, & p_q \geq 2.0, (stable) \end{cases} \quad (6)$$

where the dimensionless stability parameter  $p_q$  is calculated from :

$$p_q = \frac{L}{|L|} \left\{ \frac{(14.6 - 0.167z_o)}{|L|} + [1.6 + 0.2 \ln(z_o)] \left[ 1 - \exp\left(\frac{47.8 + 178.5z_o}{|L|}\right) \right] \right\} \quad (7)$$

This equation represents a functional relationship between Monin-Obukhov length  $L$  and roughness length  $z_o$  for various Pasquill stability classes (Karppinen et al., 1998). In equation (5) for unstable situations  $B_z = 0$ , which means that  $f_z \equiv 1$ .

The standard deviations of the turbulent velocity fluctuations  $\sigma_v$  and  $\sigma_w$  for point and area sources are evaluated at the average dispersion height  $H_{eff}$  as follows. In stable conditions ( $L > 0$ ),

$$\begin{aligned} \sigma_v = u_* 2.0 \left( 1 - \frac{H_{eff}}{z_i} \right) \quad \text{and} \\ \sigma_w = u_* 1.6 \left| 1 - \frac{H_{eff}}{z_i} \right| \end{aligned} \quad (8)$$

and in unstable conditions ( $L < 0$ ),

$$\sigma_v = u_* \left( 0.36 \left| -\frac{z_i}{kL} \right|^{2/3} + 4.0 \left( 1 - \frac{H_{eff}}{z_i} \right)^2 \right)^{1/2}, \text{ and} \quad (9)$$

$$\sigma_w = u_* \left( 1.54 \left( -\frac{z_i}{kL} \right)^{2/3} \left( \frac{H_{eff}}{z_i} \right)^{2/3} \exp \left( -\frac{2H_{eff}}{z_i} \right) + 2.56 \left( 1 - \frac{H_{eff}}{z_i} \right)^2 \right)^{1/2}$$

These equations can be derived based on Wratt (1987), Arya (1984) and Caughey et al. (1979); as presented by Karppinen et al. (1998).

#### 4. Modifications in order to allow for urban conditions

In order to allow for the influence of urban conditions, we have re-evaluated the roughness height  $z_0$  and introduced the zero-displacement height  $d$ , using a computational method discussed by Rotach (1997). The quantities  $z_0$  and  $d$  were determined for the Helsinki metropolitan area. We have also divided the surface layer into a roughness sublayer and an inertial sublayer.

In stable conditions, we have used the height of the roughness sublayer  $z^*$  as a lower limit for the Monin-Obukhov length  $L$ , as  $L$  can be interpreted as the depth of the mechanically well-mixed layer. It is therefore plausible to assume that the Monin-Obukhov length  $L \geq z^* \equiv L_{min}$ , since the roughness sublayer height  $z^*$  is the height, at which the urban roughness elements are generating a more intense turbulence by definition.

#### 5. Application to the Helsinki metropolitan area

The roughness length and zero-displacement height are evaluated by utilizing an estimate of the proportion of built-up area:  $A_R/A \approx 15\%$ . This value is based on the roughness element density and the average building height  $h$  of 10 m in the Helsinki metropolitan area (City of Helsinki, 1997). Using these values in the formula of Counihan (1971), estimates can be obtained for the roughness length and displacement height:  $z_0 \approx d \approx 0.2 h$  ( $\approx 2$  m). These values are similar with the roughness length estimates reported commonly for suburban areas (e.g. Seinfeld & Pandis, 1998). The following computations are based on these estimates for  $z_0$  and  $d$ .

A more accurate estimate of the displacement height and roughness length, based on measurements from a meteorological mast, yielded similar values for  $z_0$  as the above-mentioned. However, based on the mast measurements, the displacement height was re-estimated to be  $d \approx 6$  m; this value is better in agreement with corresponding estimates in the literature (e.g. Stull, 1988). This revised value of  $d$  would correspond to the

proportion  $A_R/A \approx 50\%$ , which is reasonable, if one takes into account the combined effect of buildings, trees and other obstacles in the area.

Utilizing wind measurements from the Helsinki-Vantaa airport, we can estimate the friction velocity in the inertial sublayer (Rotach, 1997), yielding  $u_*^{IS} \approx 1.08 u_*$ , where the friction velocity of the non-urban computations is denoted by  $u_*$  and the subscript IS refers to inertial sublayer.

The height of the roughness sublayer can be determined by several methods (e.g., Raupach, 1993). We have adopted the value  $z^* = 30$  m, which is in the range from 3 to 5 times the average building height.

Using the exponential Reynolds stress profile, suggested by Rotach (1993), and requiring that  $u_*(z^*) = 0.99 u_*^{IS}$ , we obtain

$$u_*(z') = \sqrt{u_1' u_3'(z')} = u_*^{IS} (1 - e^{-0.117 z'})^{1/3} \quad (10)$$

where  $z'$  is the elevation from the zero-displacement level  $d$ .

We assume that the turbulent heat flux is constant throughout the roughness sublayer (Rotach, 1997). The profiles of the Monin-Obukhov length and temperature scale in the roughness sublayer can now be computed using equation (4). However, in stable conditions, if the computed Monin-Obukhov length is less than the lower limit of  $L$ , we apply the  $L_{\min}$ -value for  $L$ , and recompute the values of the friction velocity and temperature scale.

## 6. Comparison of dispersion parameters for urban and rural conditions

Figures 1 and 2 show the ratios of the re-evaluated (urban) and original (rural) dispersion parameters. Figures 1 and 2 correspond to unstable, and neutral and stable atmospheric stratification, respectively. The results are based on meteorologically preprocessed data in the Helsinki Metropolitan Area in 1993. The effective source height is assumed to be low ( $= 3$  m), compared with the mixing height, as the change in dispersion parameters affects mainly the concentrations near the ground level.

In unstable conditions, the urban vertical dispersion parameters are approximately half of the corresponding rural values, at an effective dispersion height near the zero-plane displacement. Clearly, the urban roughness elements give rise to enhanced turbulence above the roof top level and one would therefore expect the urban dispersion parameters to be larger within this layer, compared with the corresponding non-urban parameters. However, the introduction of the displacement height and the exponentially decreasing Reynolds stress result numerically in clearly smaller values of turbulence parameters in the layer between roof top level and displacement height. This effect can be seen to be consistent with the generally accepted picture of turbulent flow changing to laminar flow close to a surface. In this case we can consider the urban roughness sublayer as a layer within which the spatial average of Reynolds stress increases from zero to its value in the inertial sublayer (Rotach, 1993).

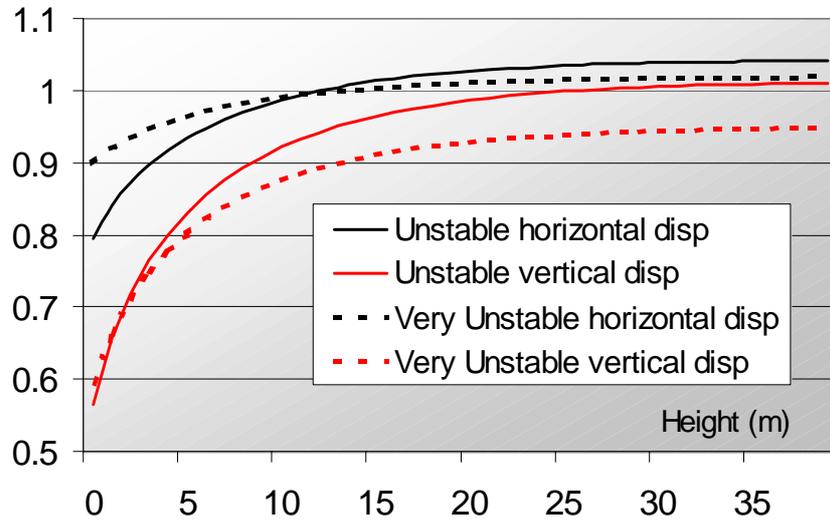


Figure 1. The ratio of urban and rural dispersion parameters in unstable conditions.

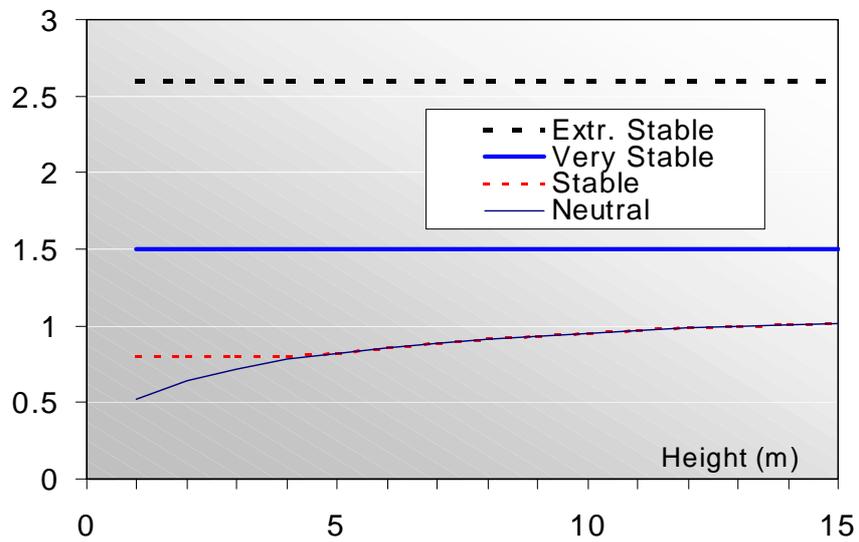


Figure 2. The ratio of urban and rural dispersion parameters in stable and neutral conditions

In neutral conditions, the variation of the curve is similar, compared with the unstable cases. However, in stable conditions the imposed limit of the Monin-Obukhov length substantially changes the situation. In extremely stable conditions, the urban dispersion parameters exceed the corresponding rural values with a large margin; the key factors influencing this ratio are stability and height of the roughness sublayer.

Figure 3 shows the effect of the modified dispersion parameters on the computed concentration distribution. The highest concentrations, which commonly correspond to extremely stable situations, are lower and more realistic in the new (urban) calculations. The concentrations in the range from 10 to 70  $\mu\text{g}/\text{m}^3$ , which typically correspond to neutral or unstable situations, are only marginally higher in the urban calculations.

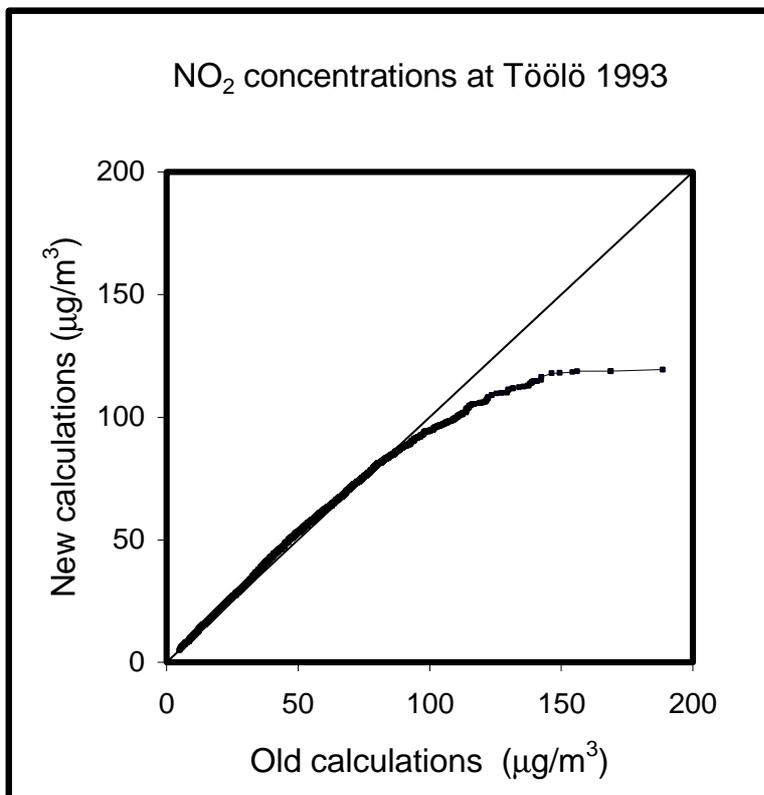


Figure 3. The calculated cumulative  $\text{NO}_2$  concentration distributions at the monitoring station of Töölö, Helsinki in 1993.

Figure 4 shows that the effect of the model modifications on monthly average concentrations is fairly small.

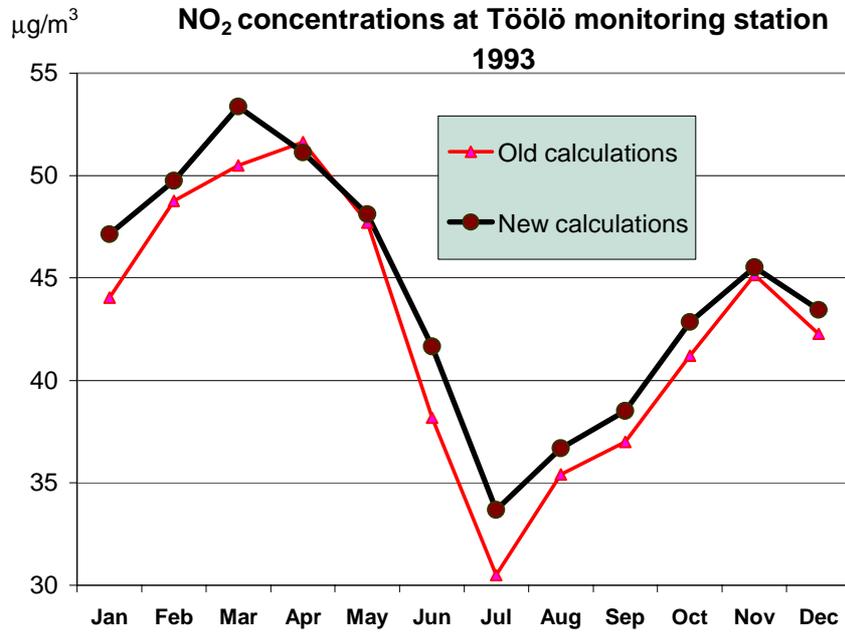


Figure 4. The calculated monthly average NO<sub>2</sub> concentrations at the monitoring station of Töölö, Helsinki 1993.

## 7. Conclusions

The meteorological preprocessor developed at our institute has been modified in order to better represent urban conditions. We have re-evaluated the roughness length, introduced the zero-displacement height and divided the surface layer into a roughness sublayer and an inertial sublayer. The friction velocity (Reynolds stress) and Monin-Obukhov length are re-evaluated using an empirically developed exponential Reynolds-stress profile in the roughness sublayer.

The influence of these modifications has been investigated, by computing the dispersion parameters used in the UDM-FMI dispersion modelling system, and comparing the revised parameters with the corresponding previous "non-urban" parameters. These modifications can have a substantial influence on the computed concentrations for the ground level or near the ground level sources (e.g., traffic). The re-evaluated friction velocity and dispersion parameters result in clearly lower concentrations in stable atmospheric stratification, and slightly higher concentrations in neutral and unstable atmospheric stratification, respectively.

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