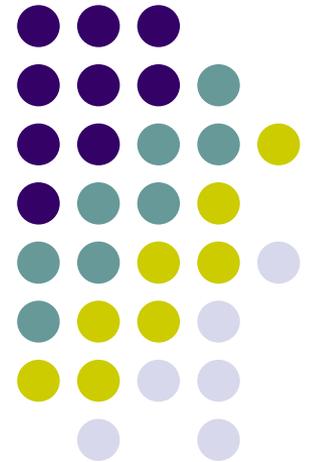


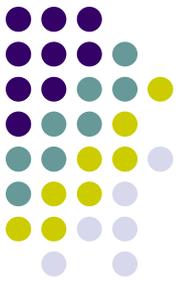
# Modeling and Automated Containment of Worms

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# Introduction

- Self-Propagating Worms
  - Spreads itself automatically by using a scanning strategy to find vulnerable hosts to infect.
  - Examples: Code Red, SQL Slammer
- Countermeasures:
  - Prevention, treatment, and containment
  - Countermeasures must be taken automatically during the early phase of worm propagation



# Our Contribution

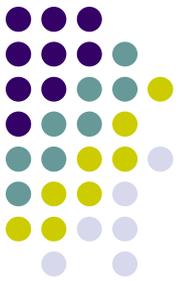
- Provide a means to accurately model the early phase of propagation of uniform scanning worms
- Proposed an automated mechanism for containing worm spreads
  - Effective for both fast and slow worms
  - No need for the worm signature in advance
  - No need to detect the worm
  - Non-intrusive - little impact on legitimate traffic

# Related Work

- Modeling
  - RCS Model - by Staniford et al.
  - Two Factor - Worm Model by Zou et al.
  - AAWP Model - by Chen et al.
- Detection
  - Kalman filter - by Zou et al.
  - DIB:S/TRAFEN - by Liljenstan et al.
- Virus Throttling
  - Restricting scan rate - by M. M. Williamson
- Worm Quarantine:
  - Requirements - by Moore et al.
  - Dynamic Quarantine - by Zou et al.

# Outline of this Talk

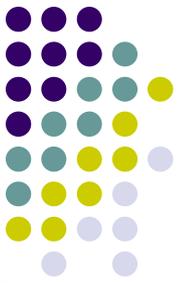
- Modeling
  - Branching Process Model for worms
  - Worm extinction probability
  - Probability distribution of total infections
- Automated Worm Containment Strategy
- Simulation Result
- Conclusion and Future Work



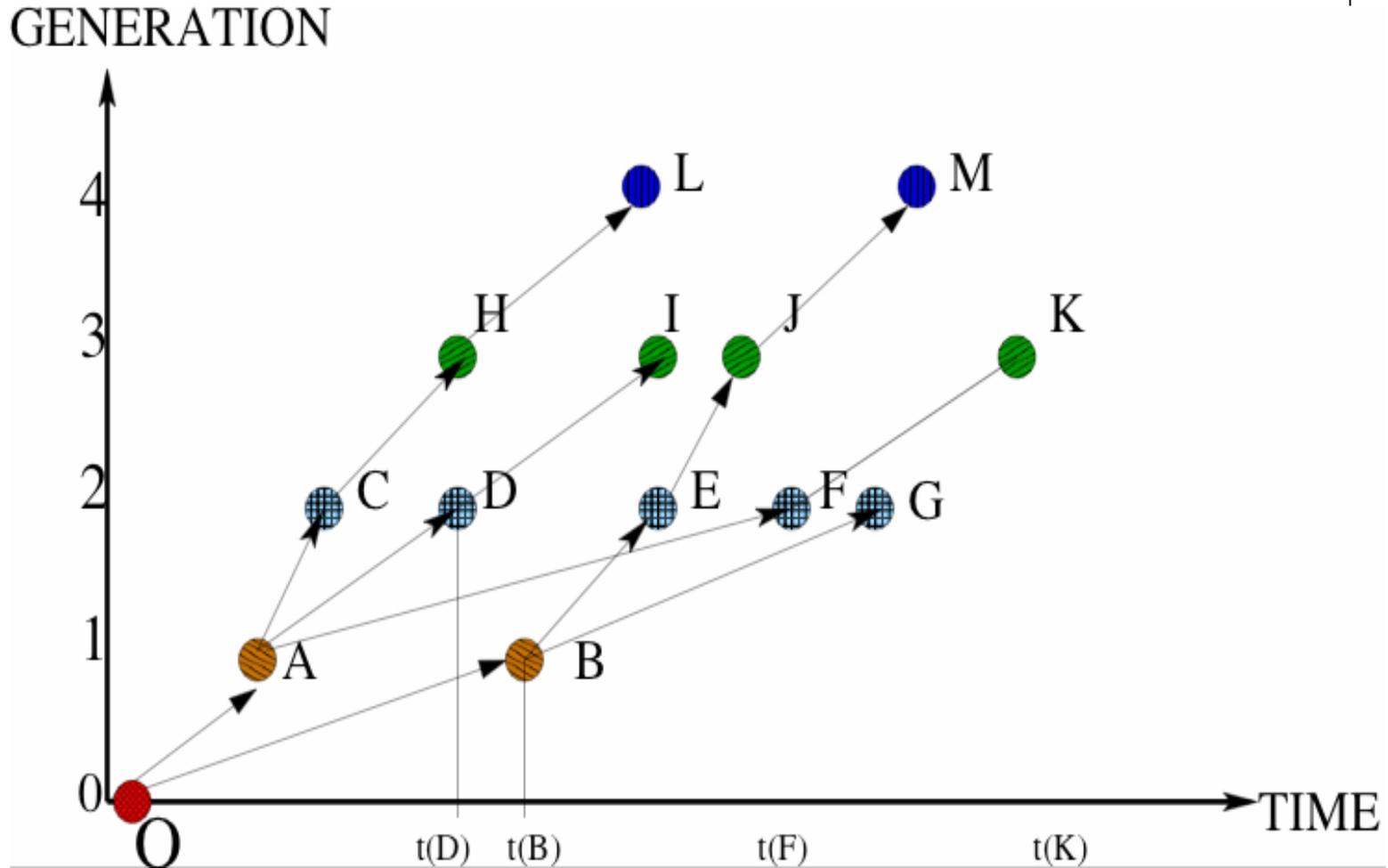
# Branching Process Overview

- Branching Process models a population in which each individual in generation  $n$  *independently* produces some random number of individuals (  $\xi$  ) in generation  $n+1$ , according to a *fixed* probability distribution:

$$P\{\xi = k\} = p_k$$



# Generation-wise Evolution of Worms



# Branching Process Model

- $p$ : the vulnerability density.
- $M$ : the total number of scans each infected host may perform.
- $\xi$ : the number of off-springs of one infected host scanning  $M$  times.

$$P\{\xi = k\} = \binom{M}{k} p^k (1 - p)^{M-k}$$

- During the early stage, the spread of the infected hosts in each generation forms a **branching process**.



# Extinction Probability

- $I_n$ : Number of  $n^{\text{th}}$  generation infected hosts
- $\xi_k^{(n)}$ : Number of offsprings by the  $k^{\text{th}}$  host of the  $n^{\text{th}}$  generation

$$I_{n+1} = \sum_{k=0}^{I_n} \xi_k^{(n)}$$

- $\pi$ : extinction probability

$$\pi = P\{I_n = 0, \text{ for some } n\}$$

# Extinction Probability

- **Branching Process Theorem:**

The extinction probability  $\pi$  is 1 if and only if the mean number offspring per individual is no more than 1, i.e.  $E\{\xi\} \leq 1$ .



# Worm Extinction Probability

- **Proposition:** If the density of the vulnerable hosts is  $p$ , and the total scans per host is  $M$ , Then  $\pi=1$  if and only if  $M \leq 1/p$ .

$$\text{Recall: } P\{\xi = k\} = \binom{M}{k} p^k (1 - p)^{M-k}$$
$$\text{So, } E\{\xi\} = M \times p$$

# Practical Implications

- Code Red:  $V = 360,000$ 
  - $p = 8.5 \times 10^{-5}$
  - Worm extinction probability is 1 iff  $M \leq 11930$
- SQL Slammer:  $V=120,000$ 
  - $p = 2.83 \times 10^{-5}$
  - Worm extinction probability is 1 iff  $M \leq 35791$



## Total Number of Infected Hosts

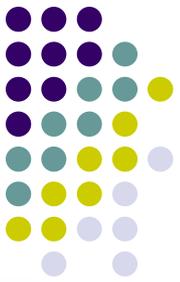
- The probability distribution of the total number of infected hosts ( $I = \sum_{n=0}^{\infty} I_n$ ) follows the Borel-Tanner Distribution:

$$P\{I = k\} = \frac{I_0}{k(k-I_0)!} (k\lambda)^{(k-I_0)} e^{-k\lambda},$$

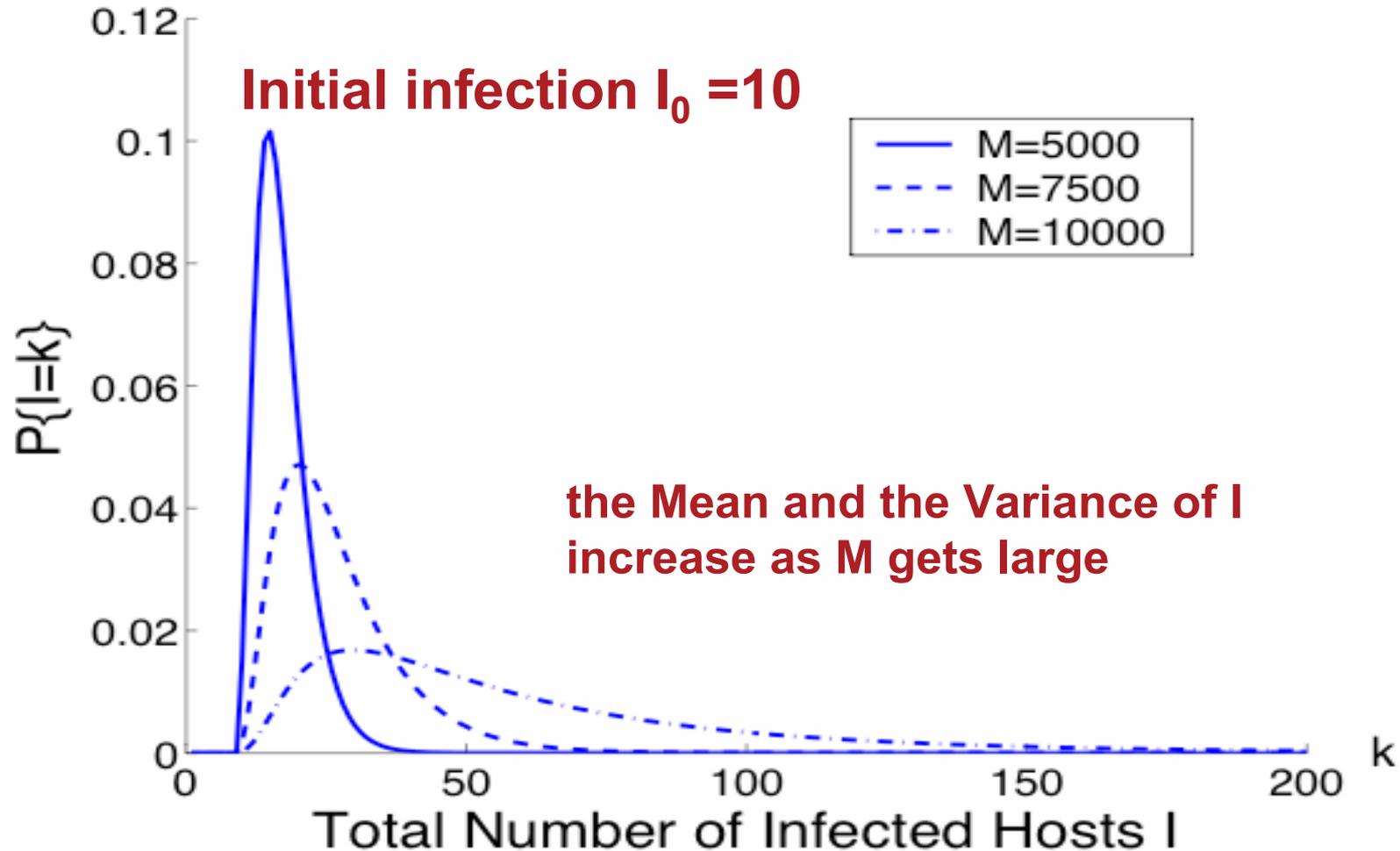
$$k = I_0, I_0 + 1, \dots$$

where  $\lambda = Mp$

$$E(I) = \frac{I_0}{1-\lambda} \quad VAR(I) = \frac{I_0}{(1-\lambda)^3}$$

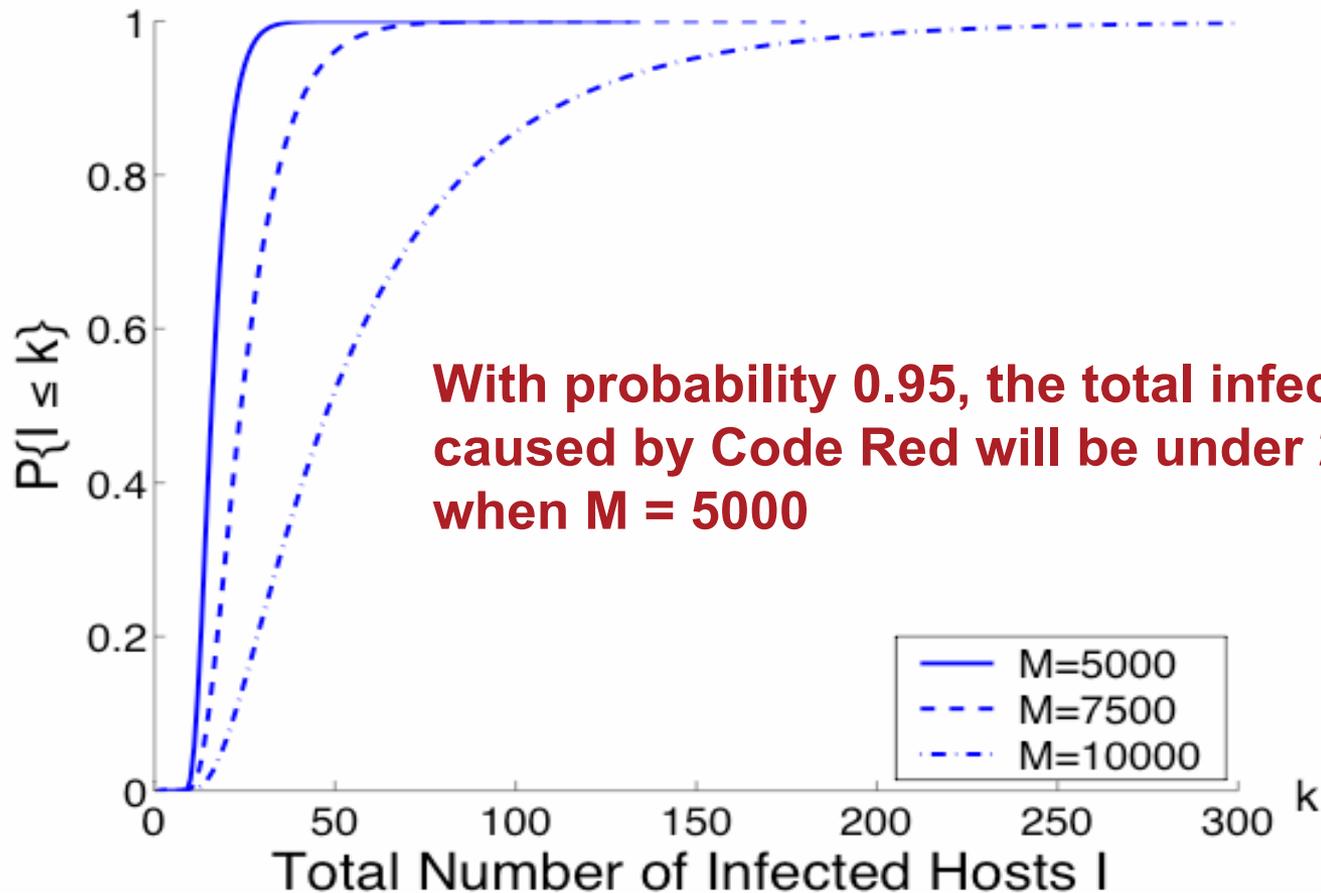


# Probability Density of I





# Cumulative Distribution for I

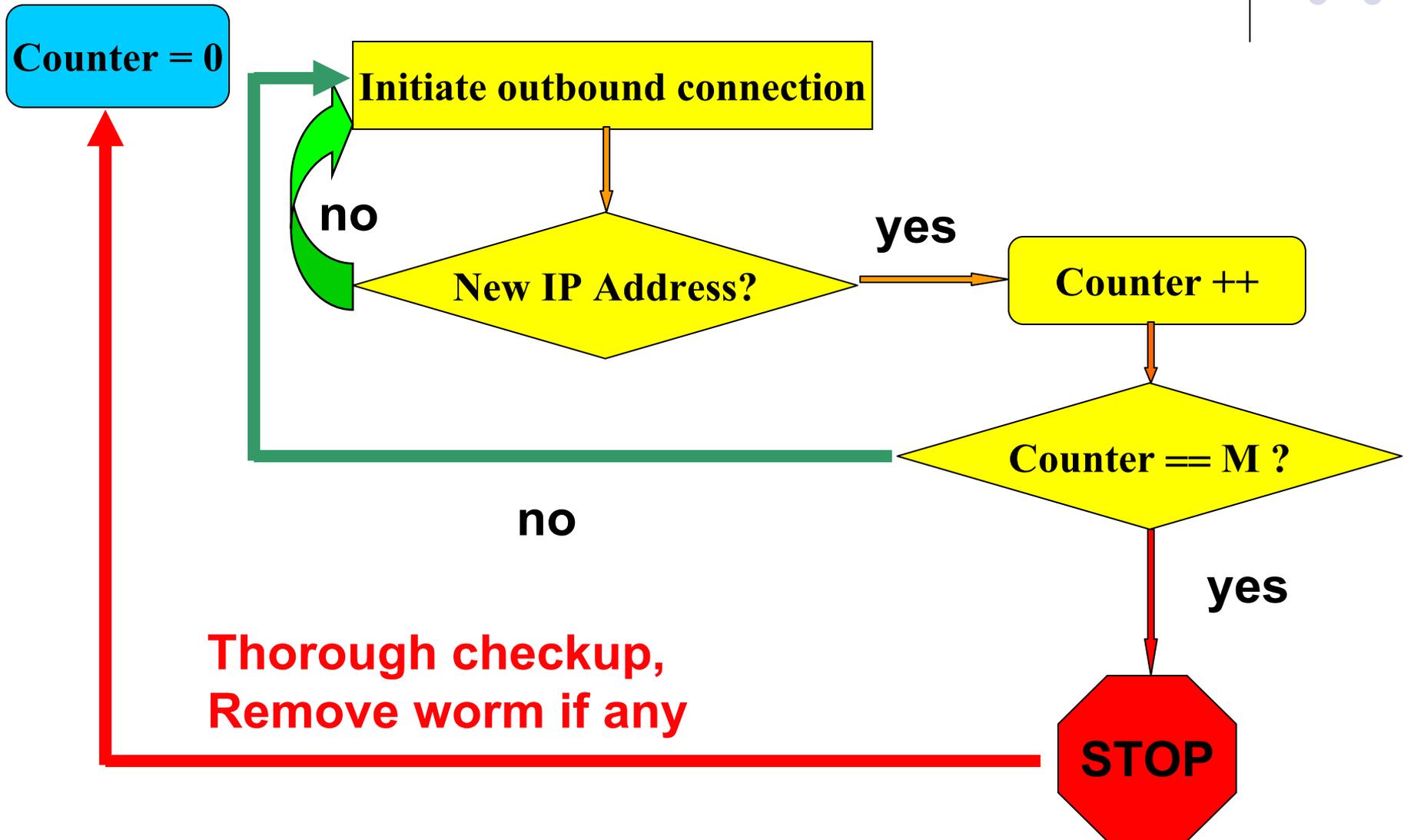


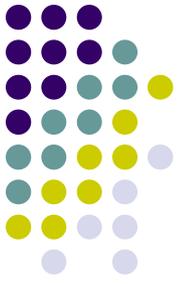
# Worm Containment System

- Host based system
- Containment cycle
  - Relative long period of time, on the order of weeks.
  - Can be obtained through a learning process, based on the hosts' normal scanning characteristics.
  - All hosts will be checked for infections at the end of the cycle.
- Policy: Each host is allowed to contact no more than M distinct IP addresses.
- Hosts that reach this maximum will be disconnected from the network and undergo a thorough checkup.



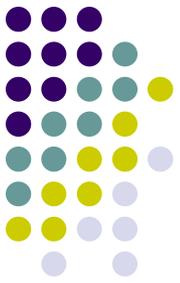
# Worm Containment System



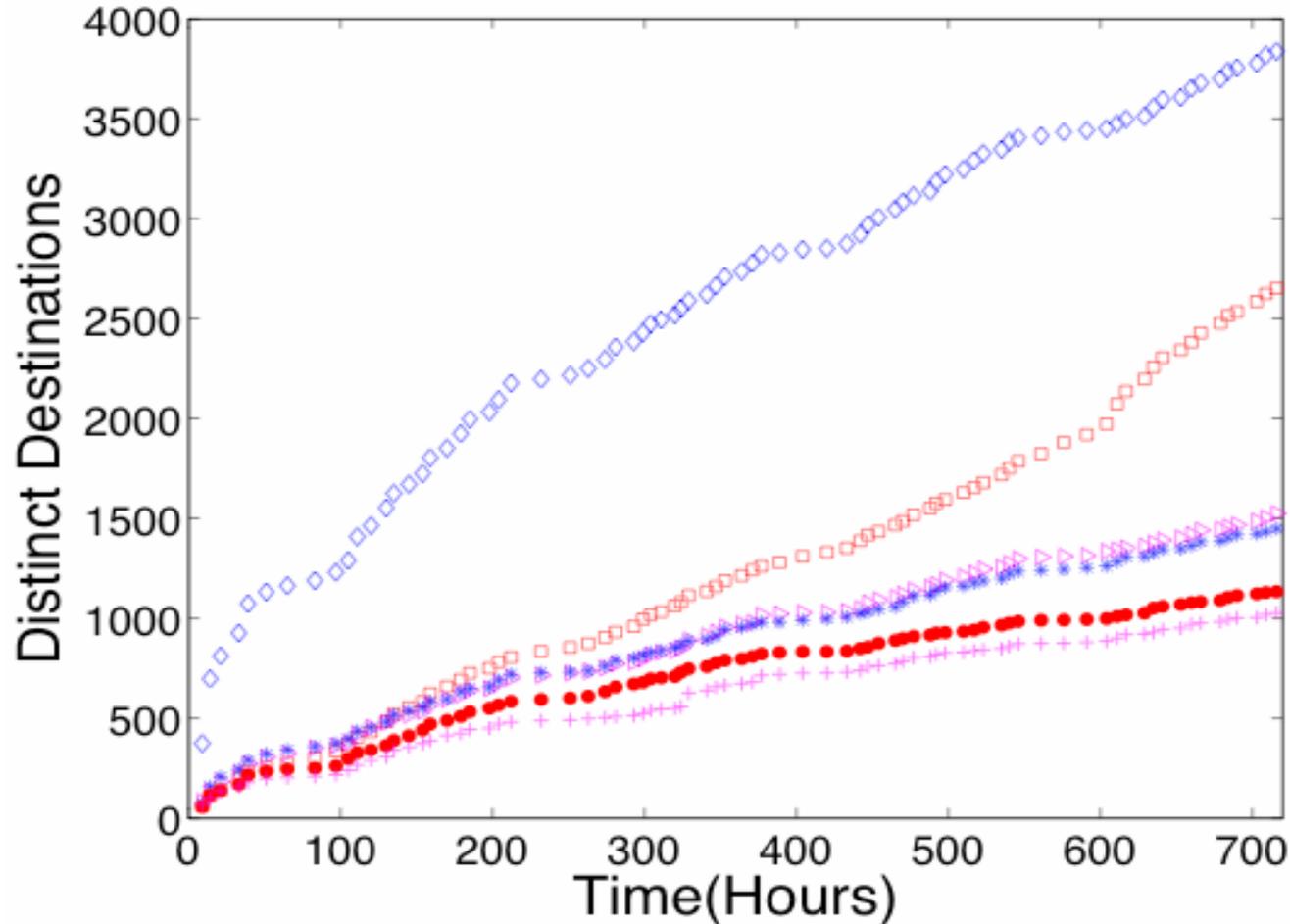


# Comparison with Virus Throttling

- Virus Throttling:
  - Rate limit of outgoing connections to 1 scans/sec
  - Slow worms will elude detection
- Worm Containment:
  - Limit the *total number* of outgoing connections to a predefined limit  $M$  over a *long period of time*
  - Do not need instantaneous rate control, thus less intrusive
  - Slow worms will be contained



# Six Most Active Hosts over 30 days





# Deployment Scenarios

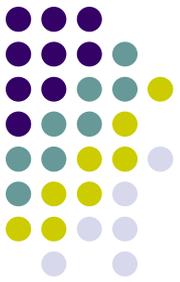
- Host Based
  - Each individual host monitors its outgoing connections to distinct IP addresses
  - Disconnect self from the network when the number of scans exceeds the pre-defined limit  $M$
  - Compared to virus throttling, our scheme is non-intrusive and also effective against slow scan worms
- May be deployed on edge routers
- Not be suitable for deployment at core routers

# Performance (Code Red)

- Our Containment System ( $M = 7500$ ):
  - Host based
  - With high probability (0.95), the total infections will be less than 50 hosts (0.015%).
- DIB/TRAN Detection:
  - Implemented on a set of carefully chosen routers
  - Detect worm activities when there are 0.03% of total infections (108 infected hosts).

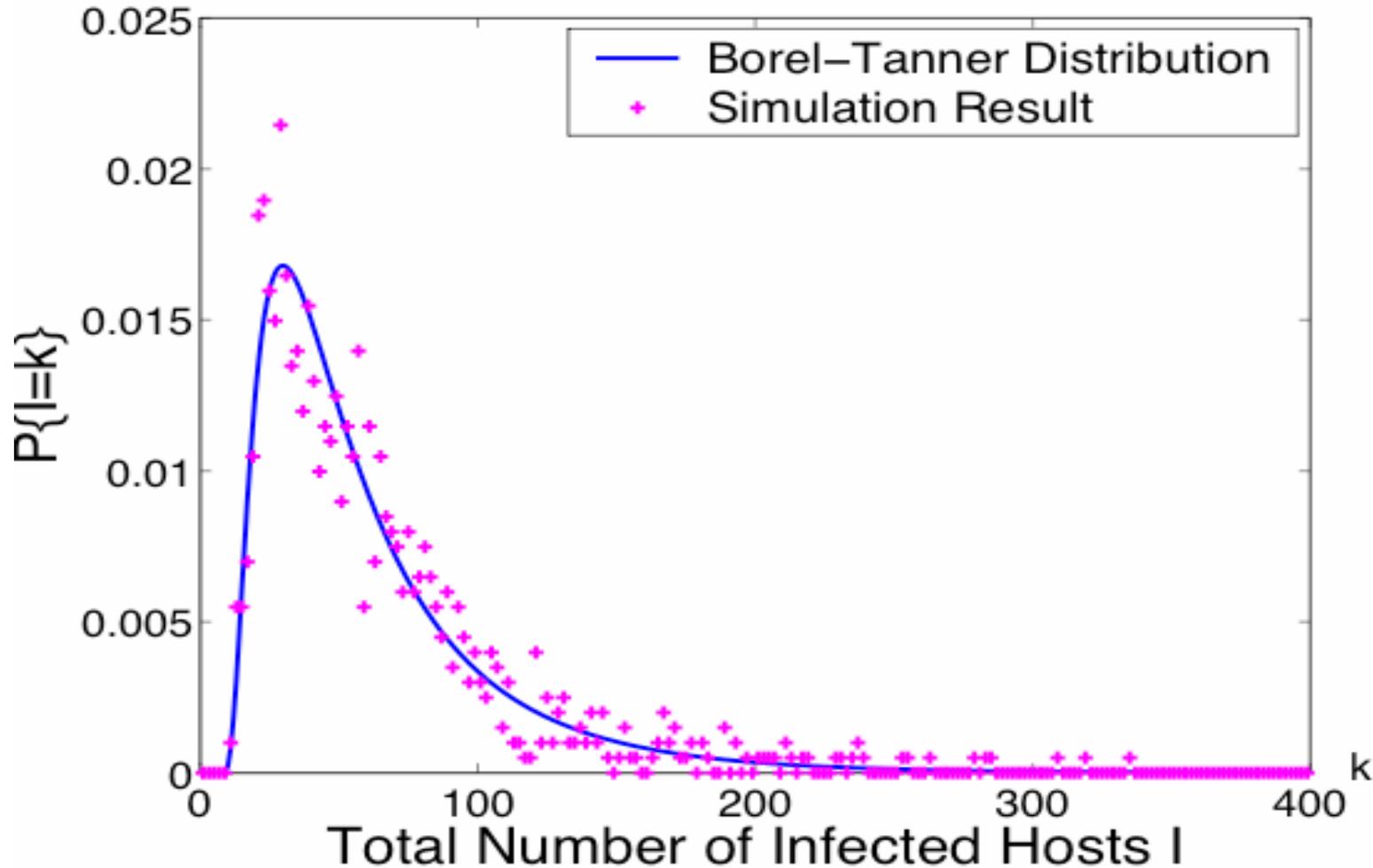
# Simulation

- Discrete Event Simulator
  - Input Parameters:
    - $V$ : vulnerable population size
    - $I_0$ : number of initial infected hosts
    - $M$ : maximum number of scans an infected host perform before it is removed.
  - Output Parameters:
    - Total number of infected hosts
    - Number of active infected hosts, removed hosts, accumulated total number of infected hosts.
- Simulations runs: 1000



# Simulation Results

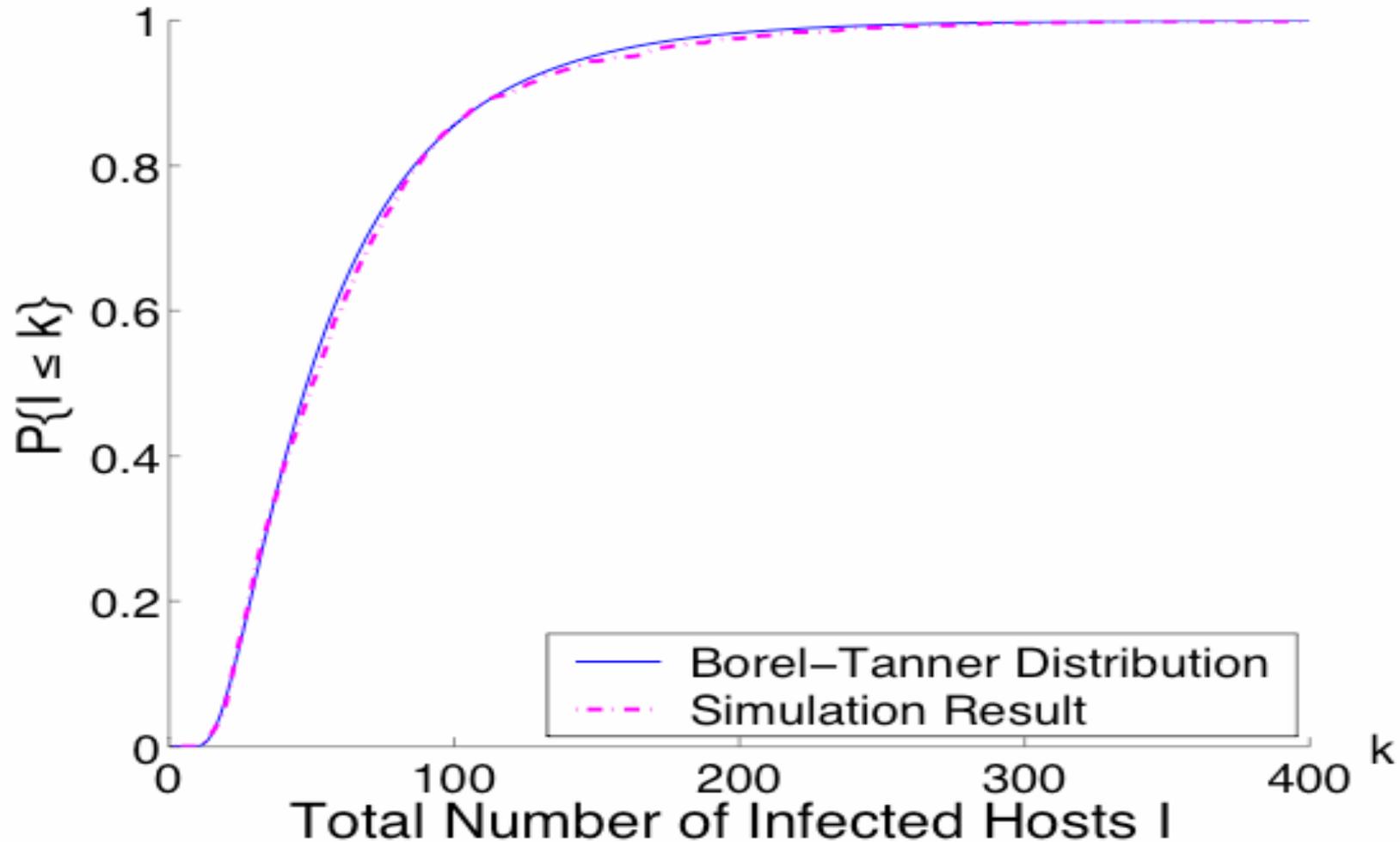
Code Red with  $M=10000$





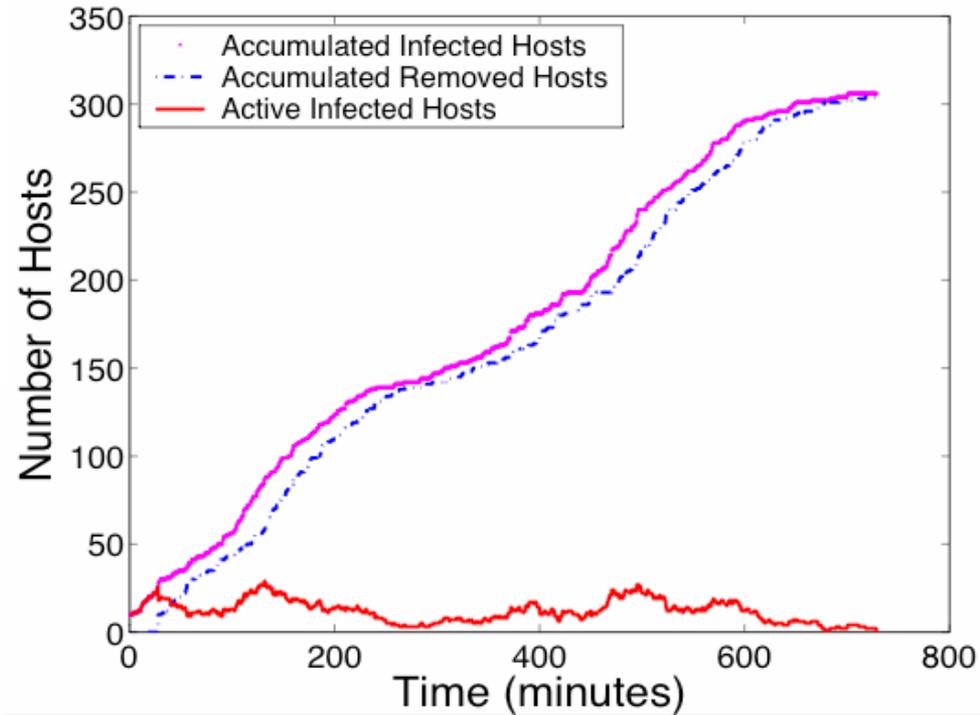
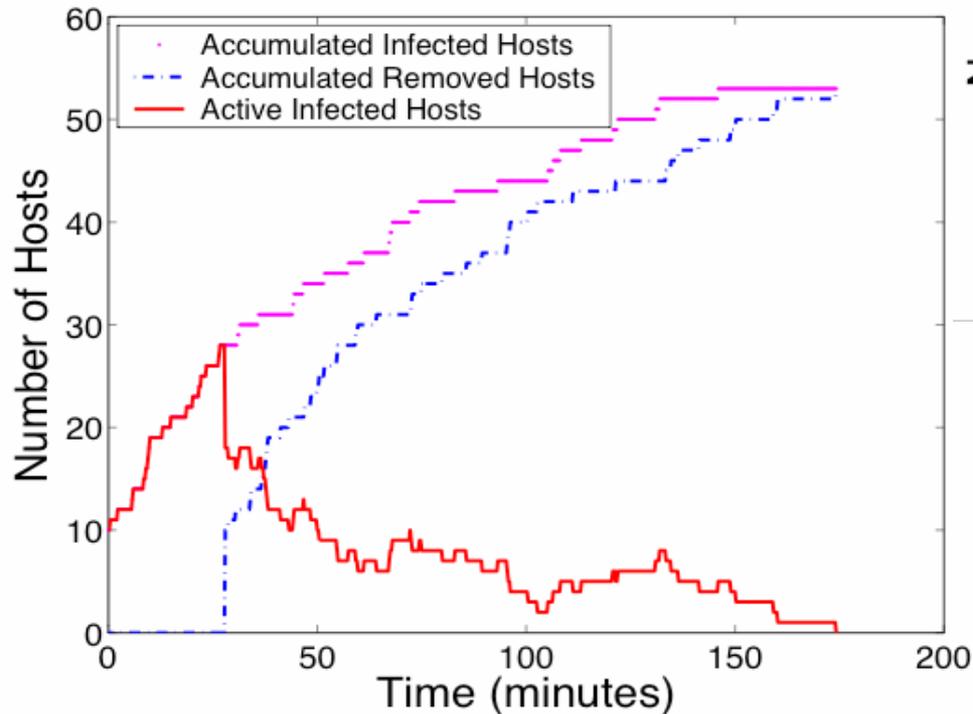
# Simulation Results

Code Red with  $M=10000$





# Sample Paths



# Conclusion

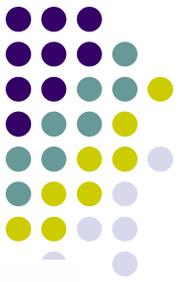
- Developed a branching process model to characterize the early phase propagation of scanning worms
  - Provide a precise bound  $M$  on the total number of scans that determines whether the worm will eventually die out.
  - Obtained probability that the total number of hosts that worm infects below a certain level

# Conclusion

- Developed an effective and automatic worm containment strategy.
  - Non-intrusive - legitimate traffic will not be affected.
  - Can contain both fast worms and slow worms
  - No need to know the worm signature in advance
  - No need to explicitly detect the worm

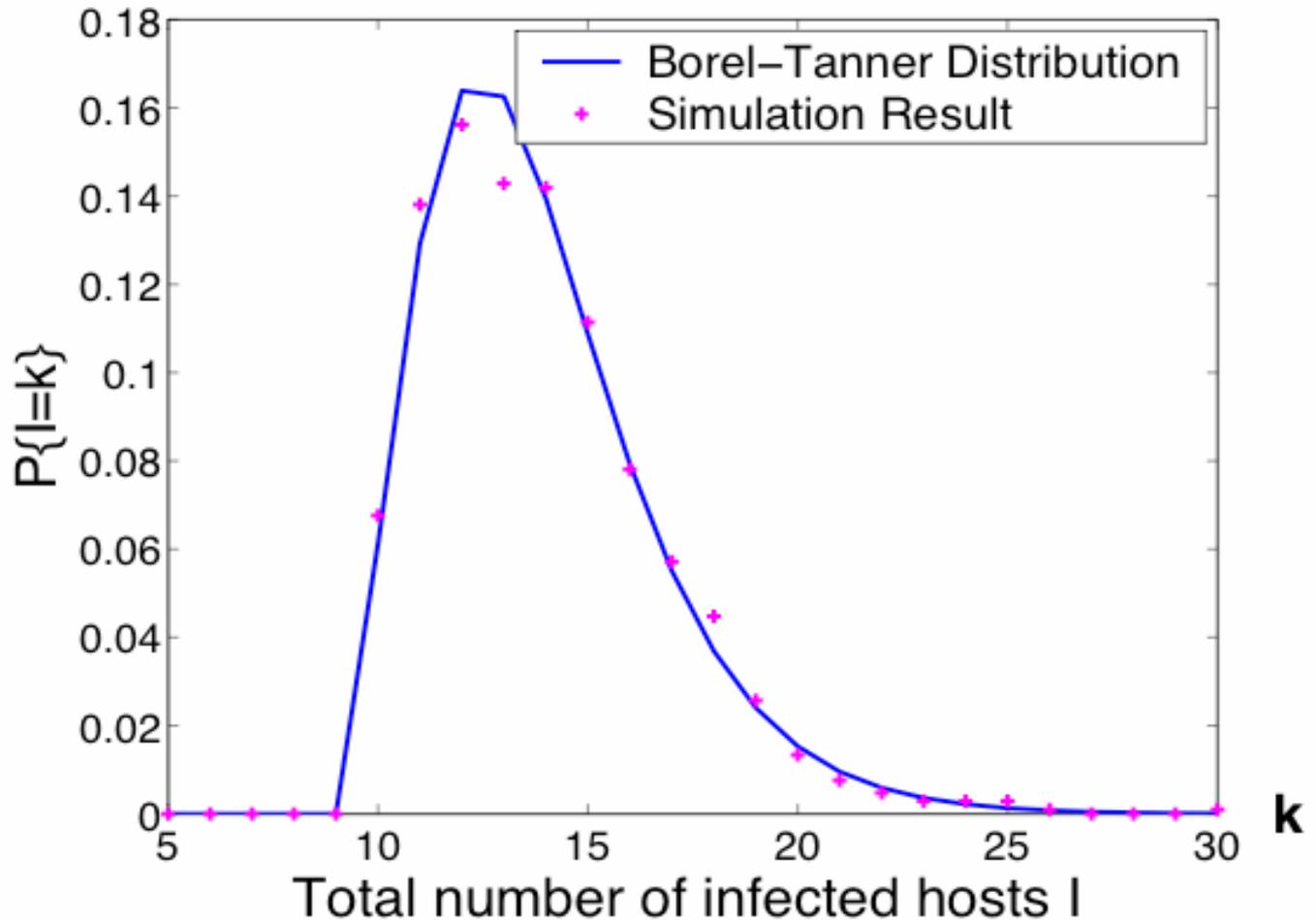
# Future Work

- Extend our strategy to model and contain preference scanning worms
- Incremental deployment of the worm containment strategy



# Back Up Slide

SQL Slammer with  $M=10000$





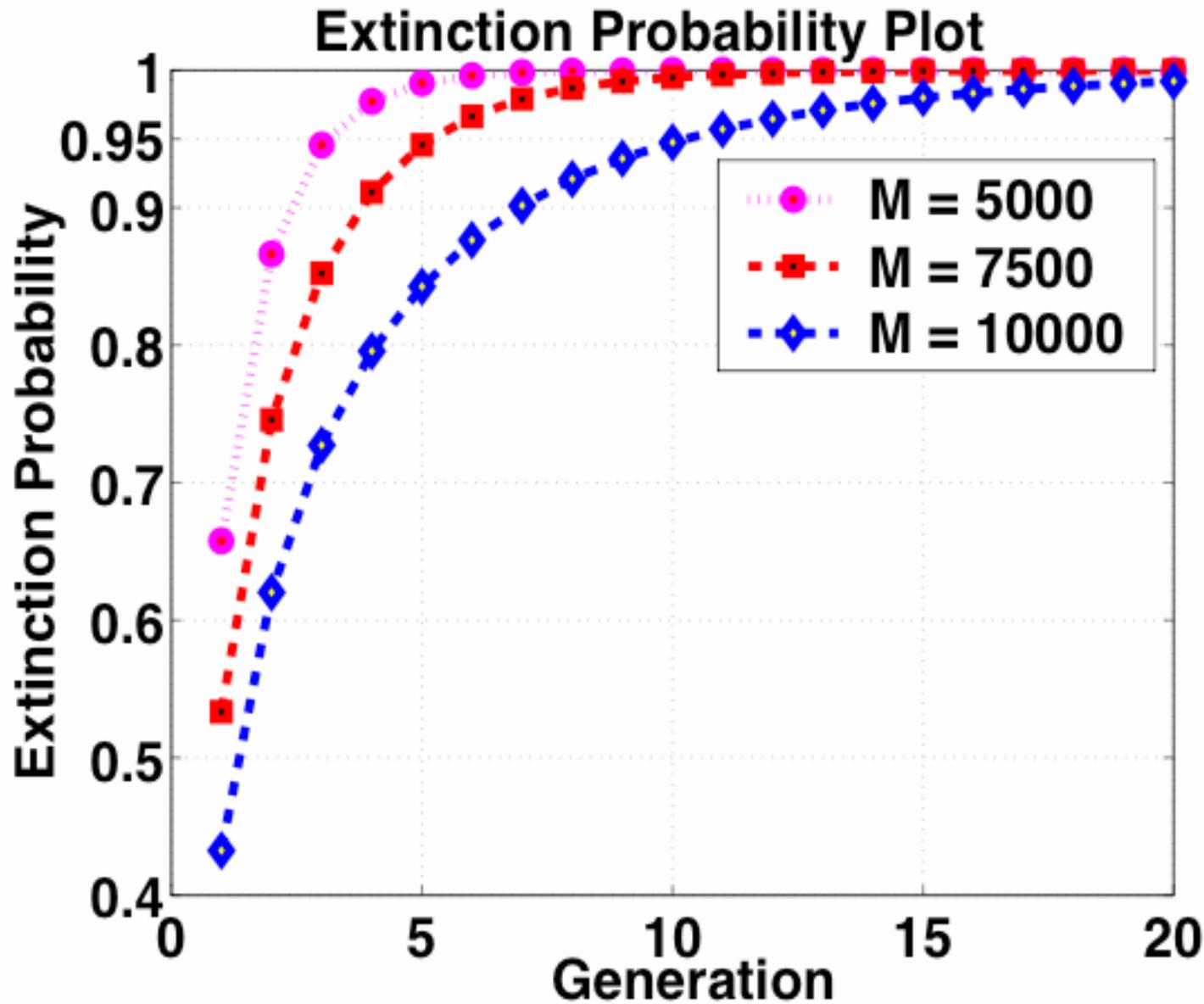
# Notations for Reference

Symbol	Explanation
$V$	The size of the vulnerable hosts
$p$	$p = \frac{V}{2^{32}}$ , the density of the vulnerable hosts
$M$	The total number of scans by each infected host
$\xi$	Random number of offsprings generated by each infected host
$\xi_k^{(n)}$	Number of offsprings produced by $k^{th}$ host in $n^{th}$ generation
$I_0$	Number of initial infected hosts
$I_n$	Number of $n^{th}$ generation infected hosts
$I$	Total number of all infected hosts [ $I = \sum_{n=0}^{\infty} I_n$ ]
$\pi$	Extinction probability
$P_n$	Extinction probability at $n^{th}$ generation



# Our Goals

- Develop an accurate model for the early phase of worm propagation
  - Provides insights for controlling the worm spread
  - Existing deterministic models are not adequate
- Develop a robust automatic worm containment strategy
  - Non-intrusive - legitimate traffic not affected
  - Contain both fast scanning worms and slow scanning worms



# Performance (SQL Slammer)

- SQL Slammer with  $I_0 = 10$ 
  - If  $M = 10,000$ , with high probability, no more than 10 additional hosts will be infected.
  - If  $M = 5000$ , with high probability, no more than 4 additional hosts will be infected
- DIB/TRAN detection: 0.005% (6 infections)