

# Addressing Delayed Feedback for Continuous Training with Neural Networks in CTR prediction

SI Ktena, A Tejani, L Theis, P Kumar Myana,  
D Dilipkumar, F Huszár, S Yoo, W Shi



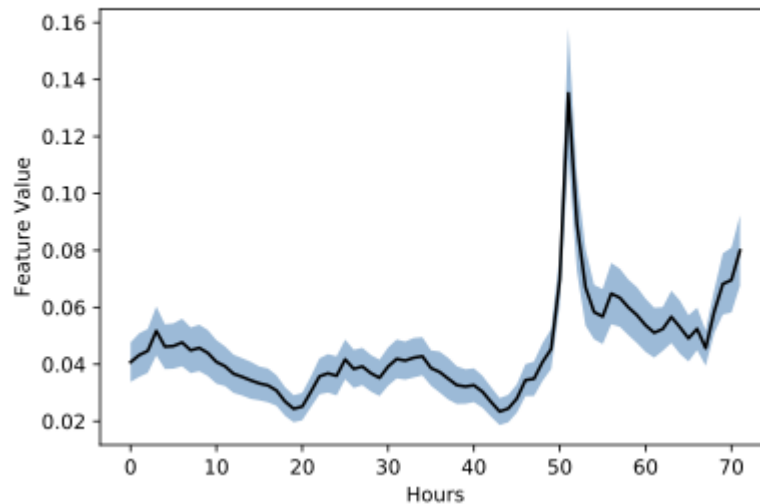
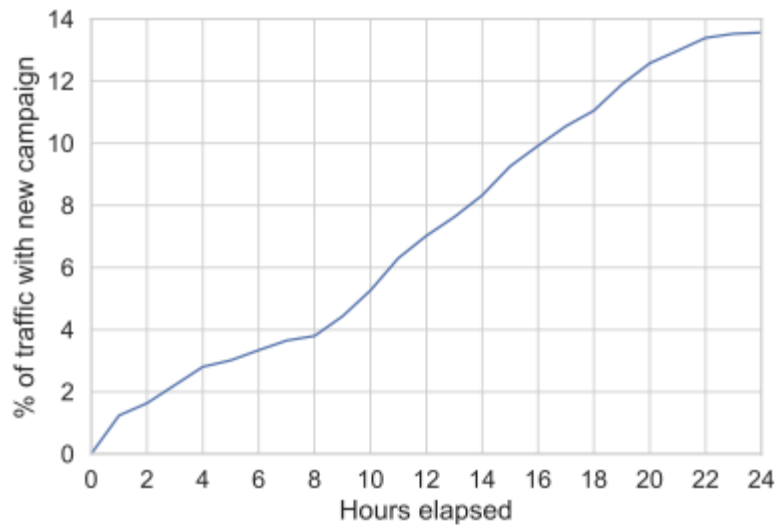
# Why continuous training?



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# New campaign IDs + non-stationary features





# Challenge: Delayed feedback

## Fact:

Users may click ads after  
1 second  
1 minute  
or 1 hour





# Challenge: Delayed feedback

Why is it a challenge?

**Should we wait?** → Delays model training



**Should we not wait?** How do we decide the label?





# Solution: accept “fake negative”

	Event	Label	Weight
Time ↓	(user1, ad1, t1)	imp	1
	(user2, ad1, t2)	imp	1
	(user1, ad1, t3)	click	1






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	Event	Label	Weight		
Time ↓	(user1, ad1, t1) imp		1	 same	
	(user2, ad1, t2) imp		1		 features
	(user1, ad1, t3) click		1		






# Solution: accept “fake negative”

	Event	Label	Weight	
Time ↓	(user1, ad1, t1) imp		1	← same features
	(user2, ad1, t2) imp		1	
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Assume X #Clicks out of Y #Impressions

**Works well when CTR is low**, where  $X/Y \approx X/(X+Y)$

# Delayed feedback models



# Delayed feedback models



## Delayed feedback models

- The probability of click is not constant through time [*Chapelle 2014*]



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- Assume an exponential distribution or other non-parametric distribution



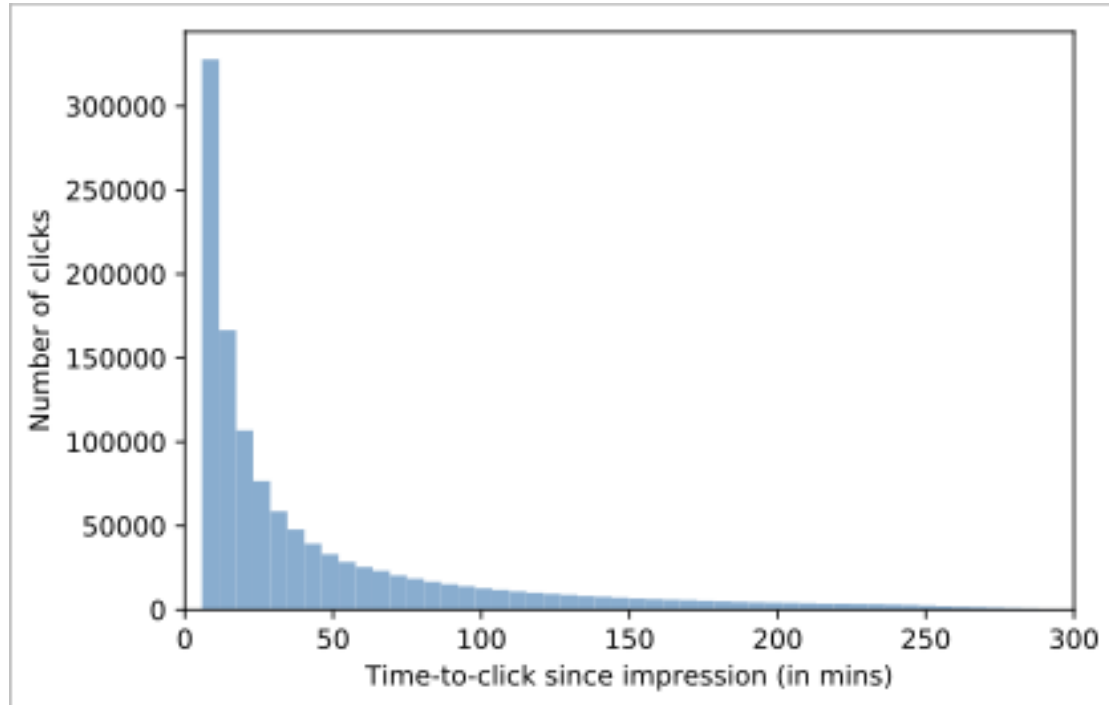
## Delayed feedback models

- The probability of click is not constant through time [*Chapelle 2014*]
- Second model similar to **survival time analysis** models captures the delay between impression and click
- Assume an exponential distribution or other non-parametric distribution

$$P(d|\mathbf{x}, \mathbf{c} = 1) = \lambda(\mathbf{x}) \exp(-\lambda(\mathbf{x})d)$$



## Delayed feedback models



# Our approach



## Importance sampling

- $p$  is the actual data distribution
- $b$  is the biased data distribution

$$\mathcal{L}(\theta) = -\mathbb{E}_p[\log f_\theta(y|\mathbf{x})] = -\sum_{\mathbf{x}, y} p(\mathbf{x}, y) \log f_\theta(y|\mathbf{x})$$

$$\mathbb{E}_p[\log f_\theta(y|\mathbf{x})] = \mathbb{E}_b\left[\frac{p(\mathbf{x}, y)}{b(\mathbf{x}, y)} \log f_\theta(y|\mathbf{x})\right]$$

Importance weights  $w(\mathbf{x}, y) = \frac{p(\mathbf{x}, y)}{b(\mathbf{x}, y)}$



- Continuous training scheme -> potentially wait **infinite** time for positive engagement
- Two **models**
  - Logistic regression
  - Wide-and-deep model
- Four **loss functions**
  - Delayed feedback loss [*Chapelle, 2014*]
  - Positive-unlabeled loss [*du Plessis et al., 2015*]
  - Fake negative weighted
  - Fake negative calibration



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- ➔ both rely on importance sampling



## Delayed feedback loss

Assume exponential distribution for time delay

$$\lambda(\mathbf{x}) = \exp(\mathbf{w}_d \cdot \mathbf{x})$$

$$\arg \min_{\theta, \mathbf{w}_d} \mathcal{L}_{DF}(\theta, \mathbf{w}_d) + \alpha(\|\theta\|_2^2 + \|\mathbf{w}_d\|_2^2)$$





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$$\begin{aligned} \mathcal{L}_{DF}(\theta, \mathbf{w}_d) = & - \sum_{\mathbf{x}, y=1} \log f_{\theta}(\mathbf{x}) + \log \lambda(\mathbf{x}) - \lambda(\mathbf{x})d \\ & - \sum_{\mathbf{x}, y=0} \log[1 - f_{\theta}(\mathbf{x}) + f_{\theta}(\mathbf{x}) \exp(-\lambda(\mathbf{x})e)] \end{aligned}$$



## Fake negative weighted & calibration

$$\mathcal{L}_{IS}(\theta) = - \sum_{\mathbf{x}, y} b(y = 1|\mathbf{x})(1 + p(y = 1|\mathbf{x})) \log f_{\theta}(\mathbf{x}) + \\ b(y = 0|\mathbf{x})p(y = 0|\mathbf{x})(1 + p(y = 1|\mathbf{x})) \log f_{\theta}(y = 0|\mathbf{x})$$

Don't apply any weights on the training samples, only calibrate the output of the network using the following formulation

$$p(y = 1|\mathbf{x}) = \frac{b(y = 1|\mathbf{x})}{1 - b(y = 1|\mathbf{x})}$$



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# Experiments



## Criteo data

- Small dataset & public
- Training - 15.5M / Testing: 3.5M examples

Logistic regression - Criteo data			
Loss function	Loss	RCE	PR-AUC
Log loss	0.3963	17.26	<b>0.5081</b>
Delayed feedback loss	0.3970	<b>17.32</b>	0.5080
PU loss	0.4065	15.10	0.5048
FN weighted	0.4008	16.30	0.5037
FN calibration	<b>0.3961</b>	17.29	0.4983



**RCE:** normalised version of cross-entropy (higher values are better)

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## Twitter data

- Large & proprietary due to user information
- Training: 668M ads w. FN / Testing: 7M ads

Wide & deep - Twitter data			
Loss function	Loss	RCE	PR-AUC
Log loss	0.5953	7.81	0.5872
Delayed feedback loss	0.5781	12.11	0.5781
PU loss	0.5567	13.57	<b>0.5927</b>
FN weighted	0.5568	13.54	0.5925
FN calibration	<b>0.5566</b>	<b>13.58</b>	0.5923



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## Online (A/B test)

Wide & deep - Online experiment			
Loss function	Pooled RCE	RPMq	Monetized CTR
Log loss	7.68	100.00	100.00
PU loss	<i>12.27</i>	<i>137.00</i>	<i>118.59</i>
FN weighted	<b>13.39</b>	<b>155.10</b>	123.01
FN calibration	13.37	154.37	<b>123.19</b>

**Pooled RCE:** RCE on combined traffic generated by models

**RPMq:** Revenue per thousand requests



## Conclusions

- Solve problem of delayed feedback in continuous training by relying on importance weights
- **FN weighted** and **FN calibration** proposed and applied for the first time
- Offline evaluation on large proprietary dataset and online A/B test



## Future directions

- Address catastrophic forgetting and overfitting
- Exploration / exploitation strategies



# Questions?

<https://careers.twitter.com>

@s0f1ra

