The shuttle radar topography mission (SRTM), was flown on space shuttle endeavour in February 2000, with the objective of acquiring a digital elevation model of all land between 60° north latitude and 56° south latitude, using interferometric synthetic aperture radar (InSAR) techniques. The SRTM data are distributed at horizontal resolution of 1 arc-second (~30 m) for areas within the USA and at 3 arc-second (~90 m) resolution for the rest of the world. A resolution of 90 m can be considered suitable for the small or medium-scale analysis, but it is too coarse for more detailed purposes. One alternative is to interpolate the SRTM data at a finer resolution; it will not increase the level of detail of the original digital elevation model (DEM), but it will lead to a surface where there is the coherence of angular properties (i.e. slope, aspect) between neighbouring pixels, which is an important characteristic when dealing with terrain analysis. This work intents to show how the proper adjustment of variogram and kriging parameters, namely the nugget effect and the maximum distance within which values are used in interpolation, can be set to achieve quality results on resampling SRTM data from 3” to 1”. We present for a test area in western USA, which includes different adjustment schemes (changes in nugget effect value and in the interpolation radius) and comparisons with the original 1” model of the area, with the national elevation dataset (NED) DEMs, and with other interpolation methods (splines and inverse distance weighted (IDW)). The basic concepts for using kriging to resample terrain data are: (i) working only with the immediate neighbourhood of the predicted point, due to the high spatial correlation of the topographic surface and omnidirectional behaviour of variogram in short distances; (ii) adding a very small random variation to the coordinates of the points prior to interpolation, to avoid punctual artifacts generated by predicted points with the same location than original data points and; (iii) using a small value of nugget effect, to avoid smoothing that can obliterate terrain features. Drainages derived from the surfaces interpolated by kriging and by splines have a good agreement with streams derived from the 1” NED, with correct identification of watersheds, even though a few differences occur in the positions of some rivers in flat areas. Although the 1” surfaces resampled by kriging and splines are very similar, we consider the results produced by kriging as superior, since the spline-interpolated surface still presented some noise and linear artifacts, which were removed by kriging.

Keywords: RTM; DEM; kriging; Geostatistics; Nugget value; Variogram; Interpolation
1. Introduction

The shuttle radar topography mission (SRTM), a joint project of the National Aeronautics and Space Administration (NASA), the National Geospatial-Intelligence Agency (NGA-DoD) and the German Aerospace Centre (Deutsches Zentrum für Luft- und Raumfahrt – DLR), was flown on space shuttle endeavour in February 2000, with the objective of acquiring a digital elevation model of all land between 60° north latitude and 56° south latitude, using interferometric synthetic aperture radar (InSAR) techniques (Farr and Kobrick 2000, van Zyl 2001, Rabus et al. 2003, Farr et al. 2007). The data are distributed as regular-grid digital elevation models (DEMs), at horizontal resolution of 1 arc-second (~30 m) for areas within the conterminous USA and at 3 arc-second (~90 m) for the rest of the world.

The SRTM data have been widely used as the source for DEMs. As a resolution of 90 m can be considered suitable for small to medium-scale analysis (e.g. 1:100,000 or smaller), it is too coarse for more detailed purposes. If no data are available with higher detail, one alternative is to interpolate the SRTM data at a finer resolution. This operation will not increase the level of detail of the original DEM, but it will lead to a surface with the higher coherence of angular properties (i.e. slope, aspect) between neighbouring pixels (Valeriano et al. 2006), which is an important characteristic when dealing with digital terrain analysis.

This work intents to show how the proper adjustment of variogram and kriging parameters (namely the nugget effect and the maximum distance within which values are used in interpolation – hence short distance-low nugget kriging) can be set to achieve quality results on resampling SRTM data from 3” to 1” resolution. Examples are presented for a test area in western USA and include different adjustment schemes (changes in nugget effect value and in the interpolation radius) and comparisons with the original 1”, with the national elevation dataset (NED) DEMs, and with other interpolation methods (splines and inverse distance weighted (IDW)).

The basic concepts for using kriging to resample terrain data, which will be discussed in the following sections, are as follows:

(i) working only with the immediate neighbourhood of the predicted point, due to the high spatial correlation of the topographic surface and omnidirectional behaviour of variogram in short distances;
(ii) adding a very small random variation to the coordinates of the points prior to interpolation, to avoid punctual artifacts generated by predicted points (pixels) with the same location than original data points;
(iii) using a small value of nugget effect, to avoid smoothing that can obliterate terrain features.

2. Materials and methods

2.1 Study area

Selection of the study area was based on the availability of 1” and 3” SRTM data – which limits the possibilities to the conterminous USA – on the morphological characteristics, such as the presence of hills and flatlands, and on lack of urban features, which could introduce bias in the analysis. The test area is located in southeastern California, close to the western limit of the Mojave Block, delimited by the San Andreas and Garlock Faults (figure 1). The main geomorphological units
are the southern Sierra Nevada north of the Garlock Fault, the Transverse Ranges west of the San Andreas Fault and the flatlands of the western Mojave Desert. According to Dibblee Jr. (1967), the area is composed mainly of crystalline pre-Tertiary rocks, Tertiary sedimentary and volcanic rocks and Quaternary sediments and local basaltic flows.

2.2 Dataset preparation

All kriging calculations were made using the R statistical language (Ihaka and Gentleman 1996, Grunsky 2002) as the basic system and the gstat package (Pebesma 2004) for geostatistical functions. Since the present version of gstat cannot deal properly with data in Latitude-Longitude format, the DEM was exported as points in [x,y,z] format. These points were projected to UTM coordinate system (zone 11, Northern Hemisphere) and then imported into the R workspace for variogram modelling and kriging. GRASS-GIS (geographical information system) (GRASS Development Team 2007, Neteler and Mitasova 2004) was used for raster/vector conversion and coordinate system projection.

One should avoid using a projected raster DEM as input data for resampling (instead of points in [x,y,z] format) because the coordinate projection process will create linear artifacts due to pixel shifting and cell size adjustment, which can be seen in figure 2. The area depicted corresponds to the larger inset in figure 6B. The left image is a shaded relief map of the 1” SRTM DEM projected to UTM using the nearest neighbours resampling, to preserve the original values, and the right image was generated by converting the Latitude-Longitude data into vector points, projecting these points to UTM, and converting them back to raster format. White areas in figure 2B correspond to ‘no data’ pixels. It is clear that the light grey lines running in a NE–SW direction in figure 2A were introduced by the coordinate projection, to fill the ‘linear voids’. These artifacts are expected to occur systematically and to be more closely spaced with increasing latitudes.

2.3 Variogram modelling

The variogram is a tool that allows to describe quantitatively the variation, in space, of a regionalised phenomenon. Elevation data are usually expected to be highly spatial dependent (high similarity of data at short distances) and often have variograms with a region of low slope near the zero distance, which can be best
modelled by a Gaussian model (Burrough 1987). Variograms calculated with linear trend residues of topographic data usually have adequate fits to classical variogram models, which present a clear and defined sill (Valeriano 2002); residues of the trend surface analysis are used to guarantee geostationarity of data being modelled.

Exploratory analysis of the test area with variograms in four directions (0°, 45°, 90° and 135°) shows that when the whole area is considered (figure 3A), the variograms have different ranges and sills, but when only the initial part of the curve is taken into account (figure 3B), the curves are very similar, which allows the use of a omnidirectional variogram for kriging, if only short distances from the origin are used.

According to Valeriano et al. (2006), the noise present in such data, that is, low similarity of data at distances close to the grid size, can be evaluated as the rate of
The nugget effect in variograms. This value can be calculated from the vertical error of SRTM elevation data, which have a theoretical vertical accuracy of $\pm 16$ m (van Zyl 2001, Rabus et al. 2003), and an absolute error of 9.0 m for North America (Rodriguez et al. 2006). The reported absolute error represents a 90% error in Gaussian statistics, so the standard deviation (which represents approximately 68% of the values) will be 1.69 times smaller than the 90% error (Waltham 1995), that is, 5.32 m. Since the nugget effect is a measure of the [semi]variance of data, its value will be the square of the standard deviation, that is, 28.3 m$^2$. This value was rounded to 30 m$^2$ in our tests.

Due to the high spacial dependence of terrain data, it is needed to limit the area within which observations are used for prediction, to work with small data variance and save computational cost. This can be done by limiting the maximum number of neighbouring points used by the interpolation function or by limiting the search radius of the function. In this work, we decided to constrain the number of neighbouring points, since the effect of this operation is similar to defining a square window around each point, except for the edges of the area.

Kriging honours the data values at their locations, so if a point to be estimated coincides with the location of a point in the original data, the predicted surface will have the same value as the original one at that location (Deutsch and Journel 1992). This can create punctual artifacts in the resampled surface, where some pixels have the same value of the original DEM and the surrounding ones have interpolated values (figure 4). Even if we consider that the 3” DEM was created by decimation of the 1” data (also known as thinning, that is, each value of the 3” DEM corresponds to the value of the central pixel in a 3×3 window of the 1” data) this situation should be avoided, because kriging is known to smooth the overall range of the data and it will also filter some of the noise present in SRTM models, so the resampled surface should be similar to the 1” surface, but not exactly equal. This problem can be solved by adding a very small random variation to the coordinates of the points prior to interpolation.

One point that must be taken into account is the presence of voids in SRTM data; these voids can be successfully filled by other techniques such as the Delta-Surface...
method of Grohman et al. (2006). One drawback of our method is that voids larger than the distance to the most distant point in the neighbourhood will not be filled, and will remain as artifacts in the resultant surface.

3. Results and discussion

To test the influence of nugget effect and the number of neighbouring points in the final results, we performed tests with nugget values of 10, 30, 50 and 100 m$^2$, and neighbourhoods of eight ($3 \times 3$ window), 24 ($5 \times 5$ window), 99 ($10 \times 10$ window) and 399 ($20 \times 20$ window) points. The complete variogram of the area and the variogram adjusted to the initial portion of the graphic, used for interpolation, are presented in figure 5.

The 3” data points were also gridded in GMT (Wessel and Smith 1991, 1998), using continuous curvatures splines in tension (Smith and Wessel 1990) and IDW. These methods are widely used and can be found in most GIS packages, what makes them suitable to be used for comparison with the kriging approach. To compare the interpolated surfaces with DEMs created by different methods, we selected the 1” NED, produced from vectorised contour lines (Gesch et al. 2002).

Examples of the analysis that were carried out are presented in figures 6 and 7. For a better visualisation of the effects of changing variogram parameters in the interpolated surface, DEM images are shown as shaded relief maps with lighting positioned at N315° and with 30° of inclination, no vertical exaggeration.

The original 1” SRTM data are presented in figure 6A and the original 3” data in figure 6B, both with artifacts created by the coordinate projection process. The larger inset in figure 6B corresponds to the area enlarged in figures 2 and 7 and the smaller inset to the area of figure 4. The surface interpolated with kriging (30 m resolution), is shown in figure 6C, and the surface interpolated with continuous curvatures splines in tension, in figure 6D. It is possible to see on the kriged surface that the coordinate projection artifacts are not present, that the noise was removed and that essentially all topographic features observed in the original 1” image can be identified. Although the surface produced by splines in tension is very similar to the kriging result, one can note the presence of noise and that the coordinate projection artifacts are still present.

In figures 7A–D, the results of changing the nugget effect values are presented. Figure 7A is a subset of the final interpolated surface with nugget = 10 m$^2$, figure 7B has nugget = 30 m$^2$, figure 7C has nugget = 50 m$^2$ and figure 7D has nugget = 100 m$^2$. It

![Figure 5. A) Variogram for the whole area; B) variogram adjusted to the initial portion of the graphic.](image-url)
can be seen how the changes in this value lead to a smoother surface, with less topographical information.

The effects of changing the number of neighbouring points ($n_{max}$) are presented in figures 7E–H; figure 7E has $n_{max}=8$, figure 7F has $n_{max}=24$, figure 7G has $n_{max}=99$ and figure 7H has $n_{max}=399$. These parameters not only influence the smoothness of the kriged surface, but also strongly determine the computational time involved, since the size of covariance matrices grows up exponentially.
According to Guth (2006), SRTM 1'' data compare much more closely with simulated 2'' NED than with 1'' NED. Following his methodology, we created a simulated 2'' NED DEM by decimating the 1'' data and used a plot of mean slope value versus elevation to compare the DEMs in this study. In figure 8, curves plot according to four groups, from left to right: (i) original 3'' SRTM (black dashed line) and 1'' SRTM resampled with IDW (grey solid line); (ii) 1'' SRTM resampled with kriging (black solid line) and with splines (grey dot-dashed line); (iii) simulated 2'' NED (grey solid line) and original 1'' SRTM (black dot-longdashed line); and (iv) original 1'' NED (black dotted line).

The original 1'' SRTM data follow the observations made by Guth (2006), and plots almost atop the curve for the simulated 2'' NED, while the original 1'' NED plots far to right (higher mean slopes). The curve for 3'' SRTM data plots far to the left (lower mean slopes), accompanied by the interpolated 1''-IDW data, which shows that IDW resulted in an underestimation of slopes, thus it should not be used to resample DEMs to higher resolutions. Both the curves for SRTM data interpolated by kriging and by splines plot very closely, and between the curves for 3'' SRTM and 1'' SRTM, which shows a clear improvement of the DEM.

As a last comparison between the original and resampled DEMs, the drainage network was derived from all surfaces, using the A⁺ least-cost search algorithm (implemented in GRASS in the r.watershed command, Ehlschlaeger 1989). A threshold value of 100 cells was used for surfaces with 1'' resolution and 33 cells for the 3'' SRTM, which should represent approximately the same area. Figure 9 shows...
the calculated streams in two subsets of the study area, one in a region of higher slopes (the same area of figures 2 and 7) and one in a region of lower slopes, where the noise present in SRTM data is more likely to induce errors in the hydrologic modelling. The ‘reference’ drainage was derived from 1” NED (which is filtered for
artifact removal) and is presented as grey scale raster backgrounds overlaid by the vectorised streams of each DEM.

Drainages derived in the hilly area (figures 9B–E) are similar for all 1” surfaces and have a good agreement with the network derived from the 1” NED, although the streams for the IDW surface are not as ‘clean’ as the others, with duplicated and less smooth channels (central region of figure 9E, for instance). In the low relief area, the main streams are represented in all surfaces, but not even the original 1” SRTM data could delineate the watersheds in the same way that the 1” NED. It is possible to see a large trunk river that was incorporated to the adjacent watershed to east (central-lower region of figure 9G). These two watersheds were correctly identified in the surfaces resampled by kriging and splines, although some differences in the position of the main river, were some streams in the splines surface follow more closely the reference ones.

4. Conclusions

In this paper we propose the use of kriging interpolation to resample DEM to a higher resolution. Resample of DEMs with kriging interpolation may be a laborious task, since it involves variogram modelling prior to interpolation and care must be taken on all steps of the process, but the quality of final results was considered satisfactory.

Using of few neighbouring points allows the user to perform a good adjust of the variogram model just on the initial part of the curve, but voids larger than the distance to the most distant point in the neighbourhood will become anomaly areas or will remain unfilled; on the other hand, a larger number of points will dramatically increase computational time and produce a smoother surface, obliterating small terrain features. The nugget effect will also act as a smoothing factor; in our tests, a value of 10 m$^2$ was sufficient to eliminate noise.

The method presented here is capable of producing surfaces with well-defined peaks and ridges, without noise, and also remove linear artifacts sometimes present in original SRTM data, but it is not suitable for void filling. In case of large voids in the data, one good approach is to first fill in the voids and then resample.

The curves of mean slope versus elevation show that IDW resulted in an underestimation of slopes, thus it should not be used to resample DEMs to higher resolutions. The curves for SRTM data resampled by kriging and by splines plot
between the curves for 3'' SRTM and 1'' SRTM, which shows an improvement of the DEM.

Drainages derived from the surfaces interpolated by kriging and by splines have a good agreement with streams derived from the 1'' NED, with correct identification of watersheds, even though a few differences occur in the positions of some rivers in flat areas.

Although the 1'' surfaces resampled by kriging and splines are very similar, we consider the results produced by kriging as superior, since the spline-interpolated surface still presented some noise and linear artifacts, which were removed by kriging.

Acknowledgements
This study was supported by Brazil’s Ministry of Education (Grant No. CAPES/PDDE-BEX 5176/06-9) and State of São Paulo Research Foundation (Grant No. FAPESP 04/06260-5). We are thankful to the anonymous reviewers of the original manuscript, Mike Smith, Roger Bivand, Claudio Riccomini and Rômulo Machado. This study was presented in earlier versions at the International Symposium on Terrain Analysis and Digital Terrain Modelling, held at Nanjing Normal University (Nanjing, China), and at the statGIS Conference 2007, held at Klagenfurt University (Klagenfurt, Austria).

References


FARR, T.G. and KOBRIK, M., 2000, Shuttle Radar Topography Mission produces a wealth of data. EOS (Transactions, American Geophysical Union), 81, pp. 583–585.


