Dynamic analysis of a needle insertion for soft materials: arbitrary
Lagrangian-Eulerian-based three-dimensional finite element analysis

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Abstract

Background: Our goal was to develop a three-dimensional finite element model that enables dynamic analysis of needle insertion for soft materials. To demonstrate large deformation and fracture, we used the arbitrary Lagrangian-Eulerian (ALE) method for fluid analysis. We performed ALE-based finite element analysis for 3% agar gel and three types of copper needle with bevel tips.

Methods: To evaluate simulation results, we compared the needle deflection and insertion force with corresponding experimental results acquired with a uniaxial manipulator. We studied the shear stress distribution of agar gel on various time scales.

Results: For 30, 45, and 60 degrees, differences in deflections of each needle between both sets of results were 2.424, 2.981, and 3.737 mm, respectively. For the insertion force, there was no significant difference for mismatching area error ($p<0.05$) between simulation and experimental results.

Conclusions: Our result have a potential to be stepping stone to develop pre-operative surgical planning to estimate an optimal needle insertion path for MR image-guided microwave coagulation therapy and for analyzing large deformation and fracture in biological tissues.
Keywords: dynamic analysis, needle insertion, finite element analysis, arbitrary Lagrangian-Eulerian method, MR-guided microwave coagulation therapy
Introduction

Hepatocellular carcinoma (HCC) is the fifth most common cancer and the second leading cause of cancer deaths in men [1]. Magnetic resonance (MR) image-guided microwave coagulation therapy of liver tumors is minimally invasive and has many advantages for both patients and surgeons compared to open surgery [2]. Surgeons are required to insert a needle tip precisely into a targeted location such as a tumor. However, even for expert surgeons, this is not easy because the needle deflection depends on the shape of the needle tip [3, 4].

Several researchers have developed ways to put tip of a needle into a target tumor precisely not only in MR image-guide microwave coagulation therapy of liver tumors but also a number of percutaneous interventions in anesthesia, biopsy, and brachytherapy. Their works can be categorized as modeling insertion force [3, 5-7], tissue deformation [8, 9], and needle deflection [10, 11]; and developing instruments to guide and steer the needle [8, 12-14]. In the modeling insertion force, Okamura, et al. have proposed a model of needle insertion force for the bovine liver [3]. However, they concluded that a more complete model of forces will require a combination of empirical and analytical modeling, with one approach being finite element analysis (FEA). On the
other hand, by extending FEA, Dimaio et al. have developed an interactive virtual needle insertion simulation based on measured planar tissue deformations and needle insertion forces [15]. In addition, they have also proposed the concept of needle steering and formulated a needle manipulation Jacobian based on numerical needle insertion models that include the amounts of needle deflection and soft tissue deformation [16]. Moreover, Alterovitz, et al. have developed a planning system for sensorless needle insertion to reduce the needle insertion error [9].

However, these results have never been clinically applied for human liver tissues [17]. One reason is complex physical phenomena such as fracture involved in large deformation in biological human tissues. Therefore, both clinicians and patients need new approaches. In this respect, time-dependent dynamic fracture analysis in FEA has a potential to solve this issue but it is especially difficult because mesh elimination techniques are required for representing it. In general, FEA with mesh elimination techniques is known as Lagrangian-based FEA for structural analysis. However, a stable calculation is difficult because the finite element mesh needs to flip the shape or release some nodes when the fracture occurs. Thus, we use an arbitrary Lagrangian-Eulerian (ALE) method for fluid analysis that is also suitable for large deformation and fracture
in the continuum model [18].

In this study, we develop a three-dimensional finite element model that enables dynamic analyses of needle insertion with ALE-based FEA using a soft tissue model and three types of needles with bevel tips. To evaluate simulation results, we compared the amount of deflection during needle insertion and the corresponding force along the needle axis with experimental results acquired with a uniaxial manipulator. In addition, we confirmed the shear stress distribution around the needle in simulation results.
Materials and Methods

Characterization of mechanical properties of agar gel

As a phantom study by assuming the use of MR image-guided microwave coagulation therapy in open-MRI [19-21], we used 3 % agar gel (Agar 010-15815, Wako Pure Chemical Industries, Osaka, Japan) instead of liver tissue as an isotropic and nonlinear elastic material [8]. To acquire a nominal stress and nominal strain curve of the agar gel, we performed a uniaxial compression test and three-points bending test using a compact tabletop universal tester (EZ Test, Shimadzu, Kyoto, Japan). In general, the nominal stress and nominal strain curve is generated from results of the uniaxial compression and tension tests. However, for agar gel, it is difficult to perform a tension test because of its wetness. So, as the first step, a bending elastic modulus and a bending strain were calculated by the three-points bending test following ISO 178. Then, a nominal strain combining the nominal strain of the bending test (positive) and the compression test (negative) was used as input data to calculate a nominal stress according to the strain energy function $W$ which is a function of the relative volume, $J^{[22]}$. 
\[ W^* = \sum_{i=1}^{3} \sum_{j=1}^{n} \frac{\mu_j}{\alpha_j} \left( \lambda_i^{*}\alpha_j - 1 \right) + K(J - 1 - \ln J) \]  

(1)

where the asterisk (*) indicates that the volumetric effects have been eliminated from the principal stretches, \( \lambda_j^* \). The number of terms, \( n \), may vary from 1 to 8 inclusive, and the bulk modulus is \( K \). The jth shear modulus and exponent are \( \mu_j \) and \( \alpha_j \), respectively. In this study, we used \( n = 3 \) as the number of terms. Finally, we manually estimated six parameters until correct nominal stress was obtained by demonstrating displacement-force curve similar to both the compression and three-points bending tests through Lagrangian-based FEA with commercial software (ANSYS LS-DYNA Ver. 971 R6.0 single, Livermore Software Technology, CA, USA), iteratively. We prepared ten test pieces for the test (compression test: 60×20×4 mm, three-points bending test: 60×20×20 mm, cross-head speed: 2 mm/sec). Young’s modulus and Poisson’s ratio of the copper needle C1100 (Custom-made, Umihira, Kyoto, Japan) used were 117 GPa and 0.33 respectively. The copper is used as one of MR compatible materials [23].

Needle insertion experiment

To evaluate this model, we performed an experiment to measure needle deflection and reaction force with a uniaxial insertion device (Custom-made, Umihira, Kyoto,
Japan) (Fig. 1) by 8000 Hz sampling rates. The sizes of the needle and agar were φ1.6 × 150 mm based on MR compatible 14-G puncture needle [2]) and 150 × 40 × 200 mm, respectively. The angles of the bevel needle tip were 30, 45, and 60°. The needle was inserted into the agar gel at constant velocity 2 mm/sec with a penetration depth of 100 mm by assuming an application with open-MRI robot [23]. After insertion, we took photos from the lateral side with a digital camera (IXY Digital 2000IS, Canon, Ota-ku, Japan) to measure the needle deflection with image processing software (Image J, NIH, Bethesda, MD, USA) (n = 5).

**ALE-based finite element analysis**

We developed ALE-based FEA models as shown in Fig. 2A. The model consists of the agar fixed on the lower surface. The displacement 100 mm along the z-axis was applied to the rigid part (Yellow part of Fig. 2A) of the needle. The frictional coefficient 0.01 was empirically set as the contact condition between the needle and the agar. The same geometries as the experimental model were adopted for the sizes of the needle and agar, and the angles of the bevel needle tip. Also, the needles have no tubular structure because an outer needle was inserted into liver with an inner coagulation probe as one
needle. We generated the needle mesh using rectangular elements as a shell, and generated the meshes of the agar with hexahedral elements as a solid (Fig. 2B, 2C). The number of meshes totaled 297,014 elements. The size of the smallest mesh was 0.375 mm in all models. We performed standard ALE-based FEA including ANSYS LS-DYNA. Material models of the needle and the agar gel applied linear elastic material (MAT_001) and isotropic elastic-plastic material (MAT_124) applying a nominal stress and nominal strain curve estimated via the above procedure, respectively.

Statistical analysis

We statistically compared between the simulation and experimental results of acquired force and displacement curve using a two-factor ANOVA ($p<0.05$). An average curve was generated among experimental results for each bevel angle. We calculated the mismatching area by subtracting a domain bounded by the acquired force and displacement curve of simulation results from that of experimental results.
Results

Mechanical properties of agar gel

Fig. 3 shows mechanical properties of the agar gel. A nominal stress and nominal strain curve shows different trends for compression and tension.

Needle deflection

A comparison of needle deflections between the experimental and simulation results were shown in Fig. 4. For 30, 45, and 60 degrees, differences in mean deflections of each needle between both sets of results were 2.424, 2.981, and 3.737 mm, respectively. Fig. 5 shows photos from the vertical direction for lateral side of the 30-degree needle at 0, 20, 40, 60, 80, and 100 mm, respectively.

Needle insertion force

A comparison of needle insertion forces was shown in Fig. 6. For experimental and simulation results, the mismatching areas were 189, 238, and 222; and 246, 294, and 317, respectively (Fig. 7). The needle reaction forces showed no significant difference between simulation and experimental results ($p>0.05$). In addition, the
post-puncture force gradually increased in all cases.

Shear stress distribution

The shear stress distribution in a cross-sectional surface along the x-z plane from steps 0 to 100 for every 20th step for 30 degree was shown in Fig. 8. Shear stresses in each model had different distributions affecting the needle tip shape (S1, S2, and S3).

For 30, 45, and 60 degrees, the maximum shear stresses in last step were 0.0267, 0.0347, and 0.0350 MPa, respectively. The maximum shear stress appeared near the needle tip for all time scales and all cases.
Discussion

In this study, we developed a three-dimensional finite element model for dynamic fracture analysis of needle insertion through ALE-based FEA using an acquired nominal stress and nominal strain curve of agar gel. Applying an ALE method to fluid analysis makes it possible to do structure analysis with large deformation and fracture. Our results help to predict the needle deflection, insertion force, and shear stress distributions during needle insertion as pre-operative surgical planning in silico. In addition, it can help design new shapes of clinical needles to reduce the burden on patients.

For the nominal stress and nominal strain curve, it is clear that the agar gel has different compression and tension properties. Thus, in this study, we used an isotropic elastic-plastic material (MAT_124 that is the material number in ANSYS/LS-DYNA). For the different compression and tension properties, one should apply Ogden (MAT_77O) or Mooney-Rivlin (MAT_27) material, which can exhibit hyper-elastic rubber properties [24]. However, both hyper-elastic rubber models in ANSYS/LS-DYNA were supported for only low strain range. Thus, by following the Ogden equations (1), the nominal stress and nominal strain were estimated and applied
into MAT_124 that can use a different stress/strain curve for compression and tension.

While the differences of needle deflection were 2.42, 2.98, and 3.73 mm, respectively (Fig. 4), the size of a typical target tumor is about 30 mm [25-27]. These results suggest that our simulation results are in the allowable range for clinical applications such as pre-operative surgical planning. However, these error rates of the mismatching errors for 30, 45, and 60 degrees were 23, 19, and 30 %, respectively and these results seem inaccurate even given the allowable range for clinical applications. One of reasons is the material property of the agar gel that can vary time-dependently in terms of the room temperature. Also, the agar gel has difficult to generate it as a complete isotropic material. As one of solutions, we are investigating generation of samples using a magnetic stirrer. In addition, our simulations used a great deal of time, about 70 hours to finish analysis. At this time, we can say with fair certainty that real-time simulation of intra-operative surgical navigation or virtual reality training to train hand skill is difficult; the research may be useful for pre-operative surgical planning instead. As one solution for this issue, the general purpose graphics processing unit (GPGPU) [28] has been developed and has accelerated the use of various commercial software in recent years. In other words, real-time ALE-based FEA will
appear soon.

For the insertion force (Fig. 6), there was no peak during needle puncture compared to a result obtained by Okamura et al [3]. It is for this reason that we eliminate the thin membrane on top of the surface of agar gel before the experiment and have absolutely no membrane in the finite element model. Actually, in MR image-guided microwave coagulation therapy, an incision line by surgical instruments is marked out on abdominal skin to reduce renitences of the needle insertion. In both simulation and experimental results, the increase of insertion force in post-puncture is due to the influence of friction between the agar gel and the needle. Also, the oscillation of the curve (Fig. 6) caused a stick-slip effect due to friction [3, 15, 29, 30].

Finally, shear stress in the agar gel is distributed along the needle and seems generally undulating. This reason is, as mentioned above, also due to the influence of the stick-slip effect. In addition, one of the reasons for gradually rising of maximum shear stress is that the shape of the needle tip becomes increasingly similar to a cylindrical solid as the bevel angle increases. In this study, a maximum shear stress was adopted to confirm the stress distributions because the maximum shear stress is located as a safe side in comparison with the maximum principal stress and maximum strain.
energy.

For more clinical situation, the estimation of stress and strain curve of bovine liver tissue as isotropic and nonlinear elastic material [8] and ALE-based FEA are ongoing to investigate availability of our approach. Within the limitations of finite element study, these solutions may become a strong tool for understanding the mechanisms of various complex biological phenomena such as mosquito needle insertion into human skin [31-33] and cell injection [34, 35].
Conclusion

In this study, we developed a three-dimensional finite element model that enables dynamic analysis of needle insertion by applying the ALE-based three-dimensional FEA. Our result have a potential to be stepping stone to develop pre-operative surgical planning to estimate an optimal needle insertion path for MR image-guided microwave coagulation therapy and for analyzing large deformation and fracture in biological tissues.
Acknowledgments

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Author Contributions

Conceived and designed the experiments: SY, KT, KS, SM. Performed the experiments: SY, KS. Performed the simulations: SY, KT. Analyzed the data: SY. Contributed reagents/materials/analysis tools: SY, KS, SM, YS. Wrote the paper: SY. Administrative support: YS, HT.
References


[23] Hata N, Tokuda J, Hurwitz S, Morikawa S, MRI-compatible


Summary

Hepatocellular carcinoma (HCC) is the fifth most common cancer and the second leading cause of cancer deaths in men. Radiofrequency ablation (RFA) therapy of liver tumors is minimally invasive and has many advantages for patients such as minimal pain and scarring and quick recovery compared to open surgery. Surgeons are required to insert a needle tip precisely into a targeted location such as a tumor. However, even for expert surgeons, this is not easy because the needle deflection depends on the shape of the needle tip.

Our goal was to develop a three-dimensional finite element model that enables dynamic analysis of needle insertion for soft materials. To demonstrate large deformation and fracture, we used the arbitrary Lagrangian-Eulerian (ALE) method for fluid analysis. We performed ALE-based finite element analysis for 3% agar gel and three types of copper needle with bevel tips by assuming to apply MR image-guided microwave coagulation therapy in Open-MRI.

To evaluate simulation results, we compared the amount of deflection during needle insertion and the corresponding force along the needle axis with experimental results acquired with a uniaxial manipulator. In addition, we confirmed the shear stress
distribution around the needle in simulation results.

For 30, 45, and 60 degrees, differences in deflections of each needle between both sets of results were 2.424, 2.981, and 3.737 mm, respectively. For the insertion force, there was no significant difference for mismatching area error ($p<0.05$) between simulation and experimental results.

In this study, we developed three-dimensional finite element model that enables dynamic analysis of needle insertion by applying the ALE-based three-dimensional FEA. Our result shows that it is useful for pre-operative surgical planning for liver cancer surgery by radiofrequency ablation therapy and for analyzing large deformation and fracture in biological tissues. For the future, ALE-based FEA will become widely used to explain fracture mechanisms in biological tissues.
Figure 1
Figure 3
Figure 4

![Bar chart showing needle deflection (mm) at different angles.

- **Experiment**: Bars with solid shading.
- **Simulation**: Bars with dotted shading.

<table>
<thead>
<tr>
<th>Angle of needle tip (deg)</th>
<th>Needle deflection (mm)</th>
</tr>
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<tbody>
<tr>
<td>30</td>
<td>6.252</td>
</tr>
<tr>
<td>45</td>
<td>5.602</td>
</tr>
<tr>
<td>60</td>
<td>3.274</td>
</tr>
</tbody>
</table>
Figure 5
Figure 6

Z force (N) vs. Insertion depth (mm) for 30deg experiment and 30deg simulation.
Figure 7

![Diagram showing area comparison between experiment and simulation for 30deg, 45deg, and 60deg angles.](image)

- **30deg**
- **45deg**
- **60deg**

Legend:
- Experiment
- Simulation
**Figures legends**

Figure 1. Uniaxial manipulator.

Figure 2. Finite element model for needle insertion analysis. (A) Whole image (B) Solid model (C) Meshed model.

Figure 3. Nominal stress and nominal strain curve of agar gel.

Figure 4. Comparison of needle deflection at 100mm in depth between results of experiment and simulation.

Figure 5. Needle deflection (30 deg). (A) 0mm, (B) 20mm, (C) 40mm, (D) 60mm, (E) 80mm, (F) 100mm.

Figure 6. Comparison of reaction force between results of experiment and simulation.

Figure 7. Comparison of mismatching area between results of experiment and simulation.

Figure 8. Shear stress distributions (30 deg). (A) step 0, (B) step 20, (C) step 40, (D) step 60, (E) step 80, (F) step 100.

S1. Shear stress distributions for 30 deg.

S2. Shear stress distributions for 45 deg.
S3. Shear stress distributions for 60 deg.