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Electric Vehicle Powertrain Architecture and Control Global Optimization

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Abstract

The design of a full electric vehicle (or battery electric vehicle (BEV)) requires the development and optimization of a complete electric powertrain, including battery, power electronics, electric machine, sensors and control system.

When designing an electrical platform, from the very beginning of the V-cycle, it is mandatory to rely on modelling and simulation tools in order to drive the main choices and then to optimize the system. This paper presents an electric powertrain simulation platform developed with Matlab-Simulink, dedicated to multiphysic optimization of the system.

As an example, the basic electrical powertrain architecture first considered in this paper includes a battery, an inverter, a dc-dc buck converter supplying motor inductor and a wound rotor synchronous machine (WRSM). The purpose is to show how simulation tools can help in comparing different powertrain control strategies.

The present simulation platform is also useful to study physics architecture. To illustrate this point, another electrical architecture is also presented, including a dc-dc boost converter between battery and inverter. This structure must be considered here as an example only in order to show how to optimize control laws taking into account various criteria, including architecture ones. Simulation results are compared for both architectures in terms of powertrain performances and range.

Keywords: Electric powertrain, simulation platform, powertrain control strategies, architecture optimization

1 Introduction

When designing an electrical platform, from the very beginning of the V-cycle, it is mandatory to rely on modeling and simulation tools in order to drive the main choices and then to optimize the system.

The paper is organised as follows. The section 2 presents an electrical powertrain simulation platform developed with Matlab-Simulink. Main

models and equations are described in order to introduce different optimization strategies with criteria on performances and on powertrain losses in section 3. Optimization is performed with a powertrain architecture with three degrees of freedom. As the aim is to expose methodologies and to show typical results, the results presented in this paper are related to typical study cases, and not to an industrial one.

Ω : Motor speed (rad/s)

C_e : Motor torque (N.m)

Parameters:

p : Pole-pair number

R_s, R_f : Stator and rotor resistances (Ω)

L_d, L_q, L_f : Stator and rotor inductances (H)

M_f : Mutual inductance (H)

The electrical equations of stator and rotor are given in [3].

Motor torque equation is as follows:

$$\text{Torque: } C_e = \frac{3 \cdot p}{2} (i_q \cdot \Phi_d - i_d \cdot \Phi_q) \quad (1)$$

Magnetic saturations are taken into account: L_d, L_q, L_f, M_f depend on stator and rotor currents through non-linear complex equations.

Each inductance parameter is function of three currents (i_d, i_q, i_f). To determine these relations, we use steady-state maps of magnetic fields Φ_d, Φ_q, Φ_f depending on (i_d, i_q, i_f).

Figure 3 shows magnetic field Φ_d according to (i_d, i_q) for different constant values of i_f :

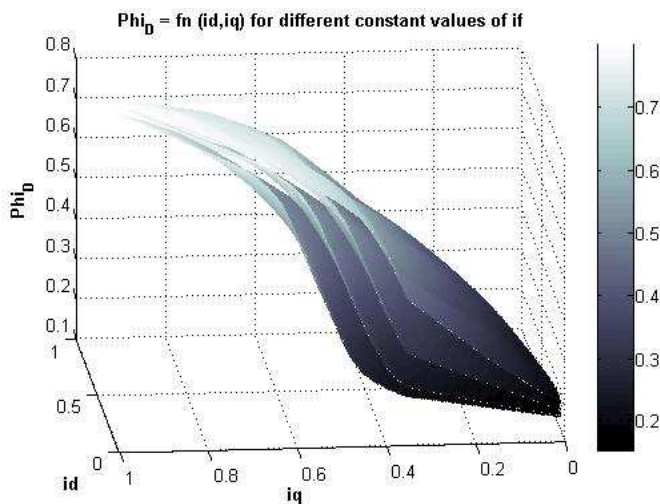


Figure 3: Stator magnetic field on axe d according to stator current (units = p.u.)

NB : Most figures in this paper are presented with per-unit axes (between 0 and 1).

To include magnetic saturation in Park equations, we proceed as follows:

- a map of $L_q(i_d, i_q, i_f)$ is obtained by dividing $\Phi_q(i_d, i_q, i_f)$ by i_q

- equation $\Phi_d = L_d i_d + M_f i_f$ is modified as follows:

$$\Phi_d = L_d i_d + M_f i_f + LM i_d i_f \quad (2)$$

with:

$$\circ L_d(i_d, i_q, i_f) = \frac{\Phi_d(i_d, i_q, i_f)}{i_d}$$

$$\circ M_f(i_d, i_q, i_f) = \frac{\Phi_d(i_d, i_q, i_f)}{i_f}$$

$$\circ LM(i_d, i_q, i_f) = \frac{\Phi_d - L_d i_d - M_f i_f}{i_d i_f}$$

The methodology is the same for rotor field $\Phi_f(i_d, i_q, i_f)$.

In addition to electrical equations, the mechanical part can be modelled by the following equation [4]:

$$J \cdot \frac{d\Omega}{dt} = C_e - C_r - C_l \quad (3)$$

with: J : Motor Inertia (kg.m²)

C_r : Resistive torque (N.m)

C_l : "Losses" torque (N.m)

A resistive torque C_l is added to classical mechanical equation $J \cdot \frac{d\Omega}{dt} = C_e - C_r$ to take into account some motor losses, such as core losses and mechanical losses. Losses expressions are presented in section 3.3.

To determine C_l expression, we solve the following equation with steady state relations:

$$P_{in} - P_{out} = P_{TOT} \quad (4)$$

with:

- $P_{in} = \frac{3}{2} (v_d i_d + v_q i_q) + v_f i_f$: input electric power

- $P_{out} = C_e \cdot \Omega$: output mechanic power

- $P_{motor} = P_{Copper} + P_{Core} + P_{Mec}$: motor losses (cf. section 3.3).

2.4 Converters models

Three-phase inverter

The inverter converts DC-voltage from battery to AC-voltage in order to supply stator of electric motor. This converter is made of six switches. Our model considers simplified IGBT/diode switches (Fig.4).

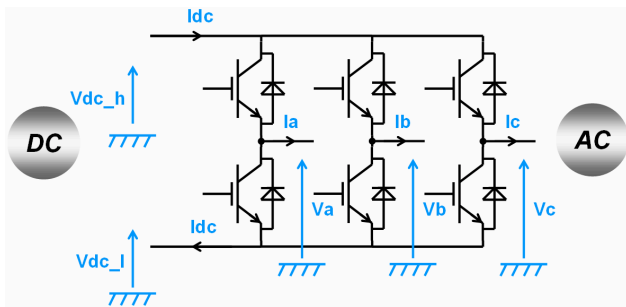


Figure 4: Three-phase inverter

Switching parameters are series resistors and threshold voltages for both IGBT and diodes.

Concerning inverter control, we use a classical Space Vector PWM: switches closed and open positions are deduced from a reference voltage vector [5].

To simulate complete driving cycles, we use a slow-transient model of inverter (or “first harmonic” model). Inputs are three-phased voltage references, AC current and DC voltage. Outputs are AC voltage and DC current. To take into account converter losses, output DC current is modified according to losses map inside Simulink model.

DC-DC converters

A classical buck converter is used between high-voltage battery and machine rotor. Both fast-transient and slow-transient models are realized in the same way as AC-DC converter.

3 Control Optimization

3.1 Low-level control structure

Powertrain architecture, presented in Figure 5, provides three degrees of freedom: two stator

currents i_d, i_q (hypothesis: $i_a + i_b + i_c = 0$) and rotor current i_f .

Let us briefly describe the powertrain control structure. From the motor torque reference $(C_e)_{ref}$ three currents references $(i_{d ref}, i_{q ref}, i_{f ref})$ are defined. Three controllers achieve currents regulation. Finally, controllers outputs are transformed in open / close switching positions for inverter (Space vector PWM is used) and for dc-dc buck converter [6]:

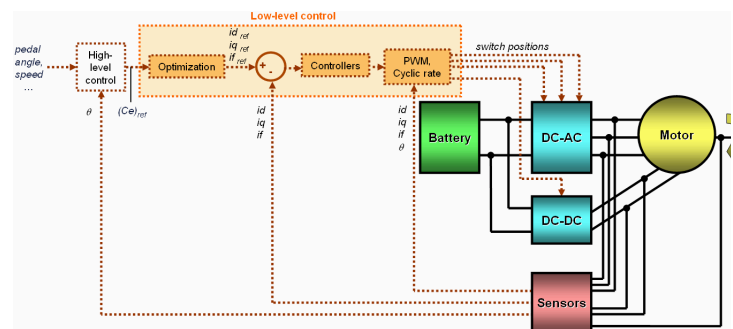


Figure 5: Electric Powertrain Control System

Electric powertrain global optimization is considered at three levels: the first step is the currents reference determination $(i_{d ref}, i_{q ref}, i_{f ref})$, the second step deals with controllers coefficients and the third step deals with switching control. This paper mainly focuses on the first step: $(i_{d ref}, i_{q ref}, i_{f ref})$ triplet optimization.

Many control strategies can be studied, considering one main objective (following torque motor reference $(C_e)_{ref}$) and three main degrees of freedom (i_d, i_q, i_f) . Optimization methods can thus be applied on variables (i_d, i_q, i_f) under torque constraint with vehicle range and performances objectives [7], [8], [9]. Constraints on maximal voltages and currents in battery, converters and machine must also be taken into account.

Figure 6 shows an example of simulation results obtained with a losses minimization control strategy (see section 3.3 for more details about this strategy):

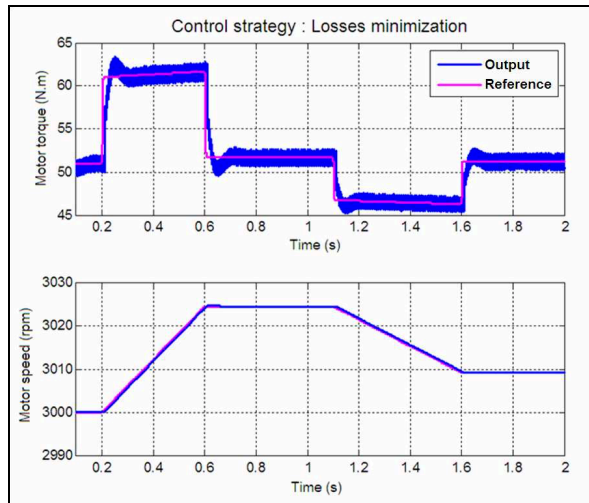


Figure 6: Example of power system simulation with a losses minimization control strategy: machine torque and speed (typical study case)

Two control strategies with criteria on performances (“torque maximization strategy”) and range (“losses minimization strategy”) are explained and compared in following sections.

3.2 Torque maximization

In a first time, we consider motor inductance parameters as constant. According to torque equation (3), to maximize C_e , we set rotor current at its maximum value: $i_f = i_{f_{\max}}$.

Concerning stator current, i_d and i_q are linked by the relation $I = \sqrt{i_d^2 + i_q^2}$. The idea is to find (i_d, i_q) that maximize C_e for any value of I . Considering constant inductance parameters, we compute C_e partial derivatives:

$$\frac{\partial C_e}{\partial i_q} = \frac{3 \cdot p}{2} \left(M_f i_f + (L_d - L_q) \left(i_d - \frac{i_q^2}{i_d} \right) \right) \quad (5)$$

$$\frac{\partial C_e}{\partial i_q} = 0 \rightarrow$$

$$i_d = \frac{-M_f i_f + \sqrt{M_f^2 i_f^2 + 8(L_d - L_q)^2 I^2}}{4(L_d - L_q)} \quad (6)$$

If $L_d = L_q$ (round rotor machine), $(i_d, i_q) = (0, I)$ corresponds to a maximum of torque equation.

To illustrate these results, we plot C_e for different values of I (Fig.7).

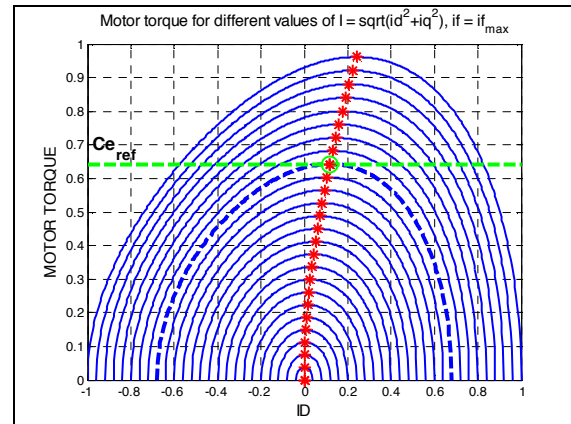


Figure 7: Motor torque according to stator current for maximum rotor current (units = p.u.)

Torque maximization control strategy consists in finding the curve for which $(C_e)_{ref} = (C_e)_{\max}$. Optimal operating points corresponding to torque maximum values are represented with stars (see Figure 7).

Figure 8 shows maximum motor torque versus (i_d, i_q) . For a given value of $(C_e)_{ref}$ corresponds a triplet $(i_d, i_q, i_{f_{\max}})$ maximizing torque.

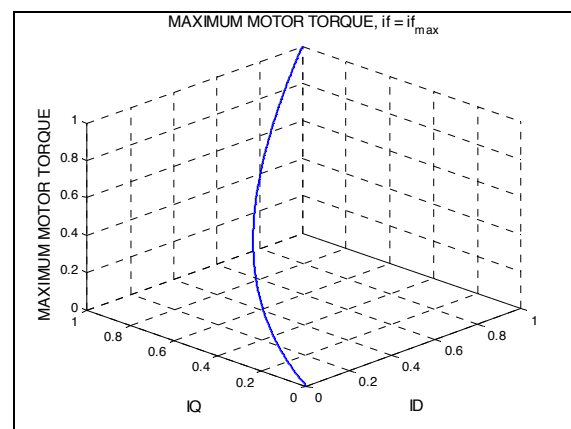


Figure 8: Maximum motor torque according to stator current (units = p.u.)

If we take into account magnetic saturation, results are similar, but the method is slightly different: partial derivatives of C_e equation cannot be easily calculated as previously. We use a gradient-based optimization method to find C_e maximum value for each value of I . The relation $i_f = i_{f_{\max}}$ remains unchanged.

Optimization problem:

- cost function to minimize:

$$J_{opt} = - \left| \frac{3 \cdot p}{2} \cdot (M_f \cdot i_f \cdot i_q + (L_d - L_q) i_d i_q) \right| \quad (7)$$

- variables : i_d, i_q

- constraint : $I = \sqrt{i_d^2 + i_q^2}$

We use a classical SQP (Successive Quadratic Procedure) to solve this optimization. Results are plotted on Figures 9 and 10.

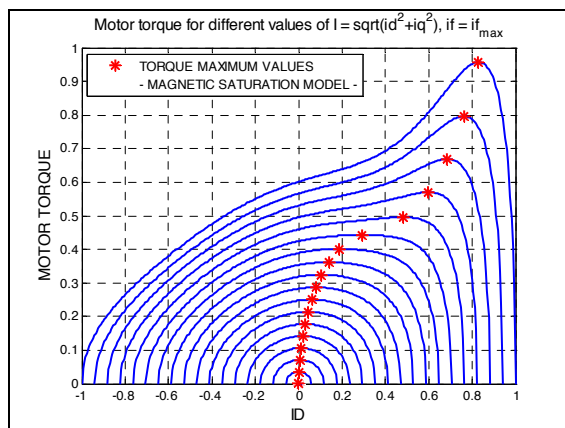


Figure 9: Motor torque according to stator current for maximum rotor current with a magnetic saturation model (optimal operating points = stars) (units = p.u.)

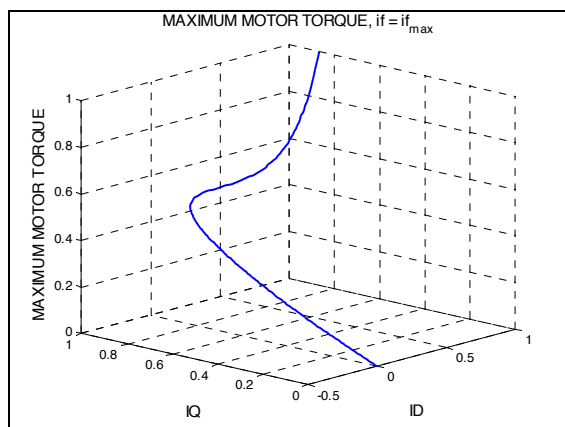


Figure 10: Maximum motor torque according to stator current with a magnetic saturation model (units = p.u.)

Finally, the Motor Torque Maximization methodology can be summarized in three steps:

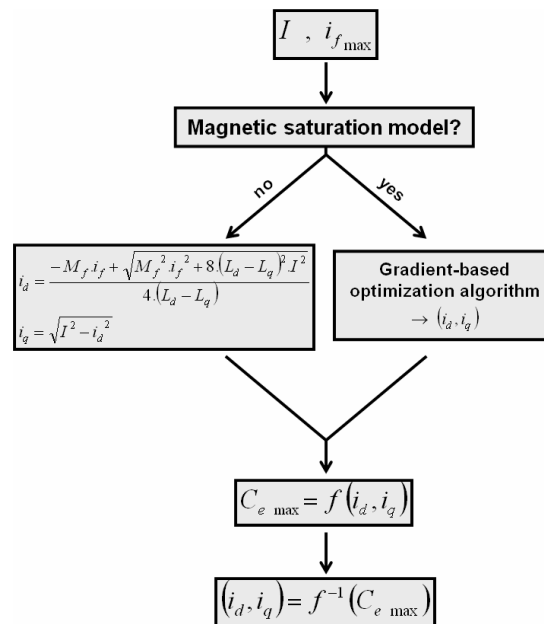


Figure 11: Motor torque maximization method

The result is a non analytic algebraic relation giving (i_d, i_q, i_f) from $(C_e)_{ref}$.

In order to take into account battery output voltage, a constraint on (v_d, v_q) is added:

inequality $\sqrt{v_d^2 + v_q^2} \leq V_{max}$ must be respected for all operating points (C_e, Ω) .

3.3 Losses minimization

The difficulty of a losses minimization strategy depends on the chosen approach:

- **approach 1** : to use a fine and complex model of motor losses (e.g. through losses maps from tests). Advantage is a high correlation between tests and simulation results. Major drawback concerns optimization method complexity: when the cost function to minimize is not an explicit function of optimization variables, simple and fast gradient-based methods can not be applied. More complex methods (such as heuristic algorithms) are required, with longer computation times.
- **approach 2** : to use simplified losses model, with explicit expressions of optimization variables. There are two advantages of this approach : first, the use of fast optimization methods is possible; secondly, it allows studying losses variations with motor parameters. Drawback is advantage of first approach (classical compromise between precision and computation times).

Approach 2 is used in this paper. For that purpose, simplified losses expressions are required.

The cost function to minimize represents global losses in powertrain (apart from battery losses).

Converters losses:

- **Conduction losses:**

$$P_{Cond} = A_C \cdot I^2 + B_C \cdot I \quad (8)$$

- **Switching losses:**

$$P_{Sw} = f_c \cdot (A_S \cdot I^2 + B_S \cdot I + C_S) \quad (9)$$

where the parameters are:

f_c : switching frequency (Hz)

A_C, B_C : Constant coefficients to determine A_S, B_S

I : Converter current:

- Stator AC-DC converter:

$$I \rightarrow \sqrt{i_d^2 + i_q^2}$$

- Rotor DC-DC converter: $I \rightarrow i_f$

Motor losses [10]:

- **Copper losses:**

$$P_{Copper} = R_f \cdot i_f^2 + \frac{3}{2} \cdot R_s \cdot (i_d^2 + i_q^2) \quad (10)$$

- **Core losses:**

$$P_{Core} = (\Phi_d^2 + \Phi_q^2) (k_h \cdot \Omega + k_e \cdot \Omega^2) \quad (11)$$

- **Mechanical losses** (dry friction, viscous friction and windage losses):

$$P_{Dry Friction} = k_{df} \cdot \Omega \quad (12)$$

$$P_{Viscous Friction} = k_{vf} \cdot \Omega^2 \quad (13)$$

$$P_{Windage} = k_w \cdot \Omega^3 \quad (14)$$

k_h, k_e, k_{df}, k_{vf} and k_w are constant coefficients to determine, respectively corresponding to hysteresis, eddy current and mechanical losses.

Coefficients determination

To determine A_C, B_C, A_S, B_S coefficients for stator and rotor converters, we apply linear regression to data maps. These maps represent converters global losses and motor current measures according to torque and speed.

Linear regression consists in approximating a linear equation $Y = A \cdot X$ with X a vector of unknown parameters, by a least square method ($\min_X \|Y - AX\|_2$),

where:

$$X = \begin{bmatrix} A_{C \text{ Stator}} \\ B_{C \text{ Stator}} \\ A_{S \text{ Stator}} \\ B_{S \text{ Stator}} \\ C_{S \text{ Stator}} \\ A_{C \text{ Rotor}} \\ B_{C \text{ Rotor}} \\ A_{S \text{ Rotor}} \\ B_{S \text{ Rotor}} \\ C_{S \text{ Rotor}} \end{bmatrix}$$

and Y and A contain data from measures.

X can be compute from the well known expression:

$$X = (A^T \cdot A)^{-1} \cdot A^T \cdot Y \quad (15)$$

Concerning motor losses coefficients determination, we use the same method applied to stator and rotor losses data with:

$$X = \begin{bmatrix} k_h \\ k_e \\ k_{df} \\ k_{vf} \\ k_w \end{bmatrix}$$

If stator and rotor resistance values are unknown parameters, linear regression can provide them by modifying Y, A and X so that:

$$X' = \begin{bmatrix} R_f \\ R_s \\ X \end{bmatrix}$$

(Using this vector is also a mean to check motor resistance values)

Figures 12 and 13 represent converters and motor losses from tests versus simulation results. Modelling error on converters losses is quasi-inexistent. Concerning motor, in low torque area, there is up to 20% error, certainly due to losses simplified model (e.g. stray losses are neglected).

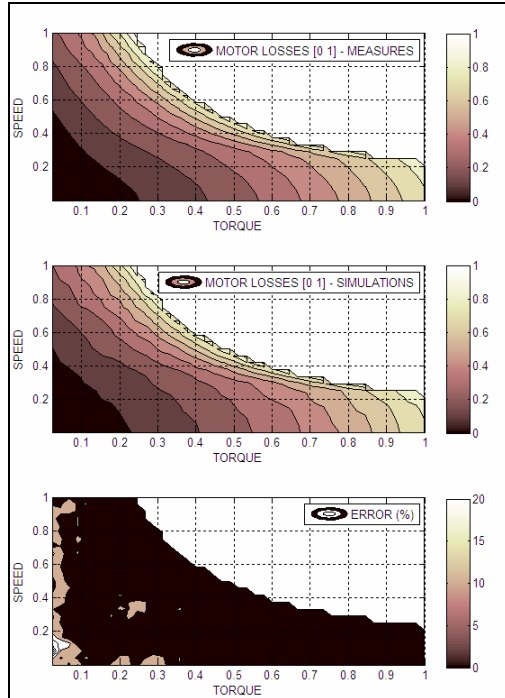


Figure 12: Motor losses measures vs. simulation results (units = p.u.)

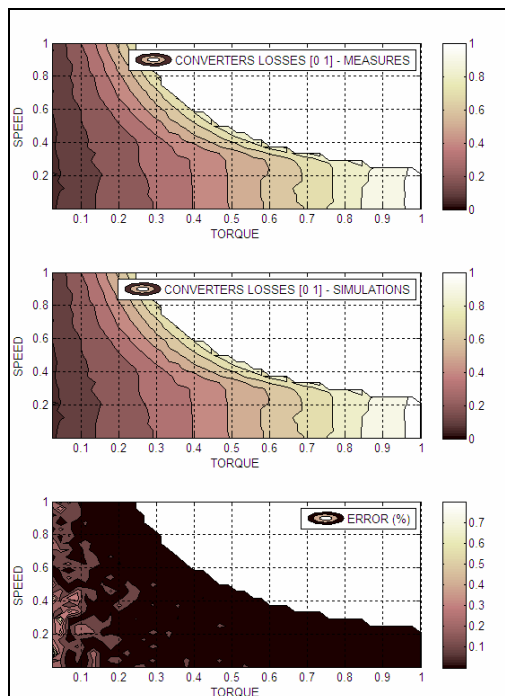


Figure 13: Converters losses measures vs. simulation results (units = p.u.)

Global losses:

$$P_{TOT} = P_{Copper} + P_{Core} + P_{Mec} + P_{Stator Sw} + P_{Stator Cond} + P_{Rotor Sw} + P_{Rotor Cond} \quad (16)$$

P_{TOT} is the cost function to minimize.

Optimization variables are i_d, i_q, i_f .

Constraint to respect concerns motor torque (eq.(3)): $C_e = (C_e)_{ref}$.

For each couple (C_e, Ω) , we find (i_d, i_q, i_f) that minimize P_{TOT} , verifying torque expression and respecting following constraints:

$$\begin{aligned} \sqrt{v_d^2 + v_q^2} &\leq V_{max} \\ \sqrt{i_d^2 + i_q^2} &\leq I_{max} \\ i_f &\leq I_{fmax} \end{aligned} \quad (17)$$

To achieve computation, we use as previously a SQP procedure.

To understand the importance of taking into account both losses in motor **and** converters for optimization (instead of motor losses only for example), we compare global efficiency with two control strategies (Fig.16) [11]:

- motor losses minimization (Fig.14)
- (motor+converters) losses minimization (Fig.15)

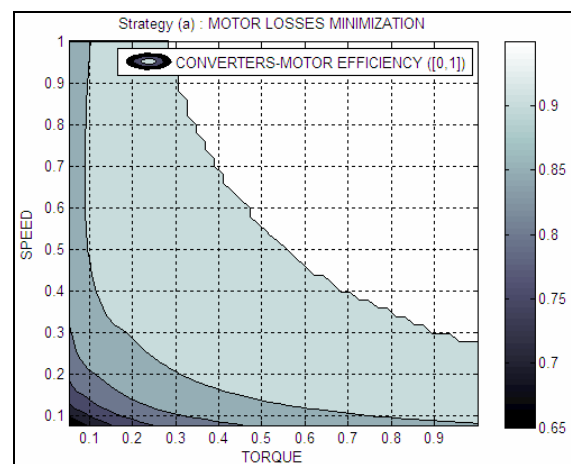


Figure 14: Powertrain efficiency with a strategy of motor losses minimization (units = p.u.)

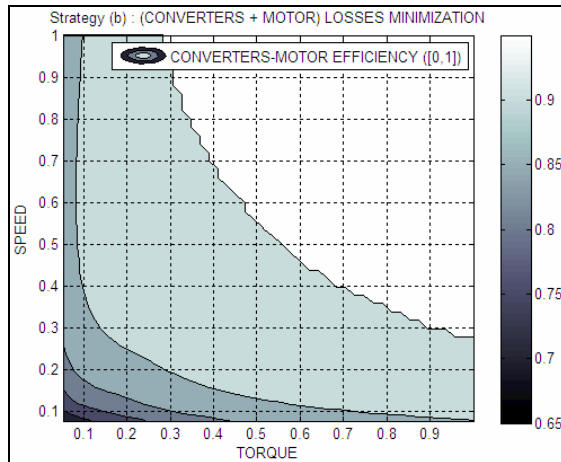


Figure 15: Powertrain efficiency with a strategy of global losses minimization (units = p.u.)

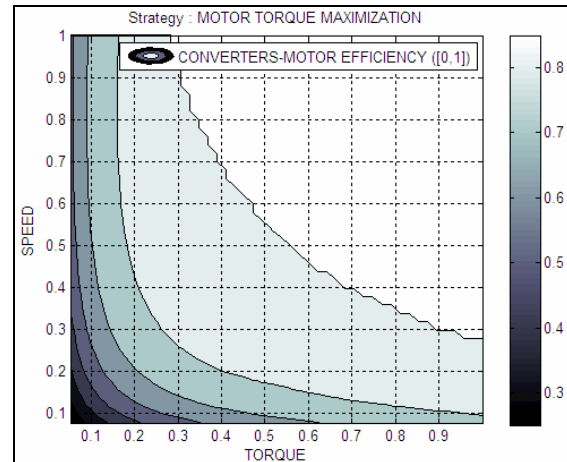


Figure 17: Global efficiency with a strategy of torque maximization (units = p.u.)

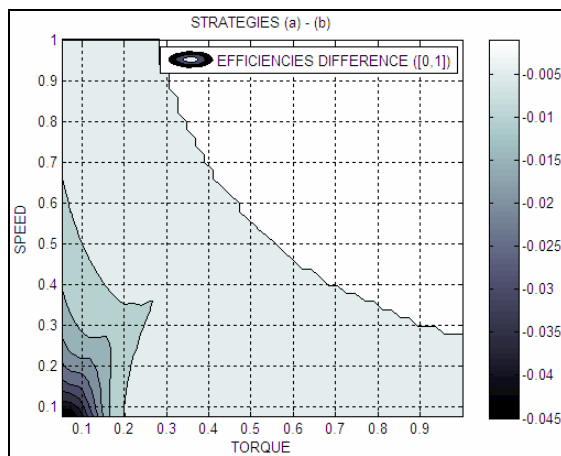


Figure 16: Powertrain efficiency gain with a strategy of global losses minimization vs. motor losses minimization (units = p.u.)

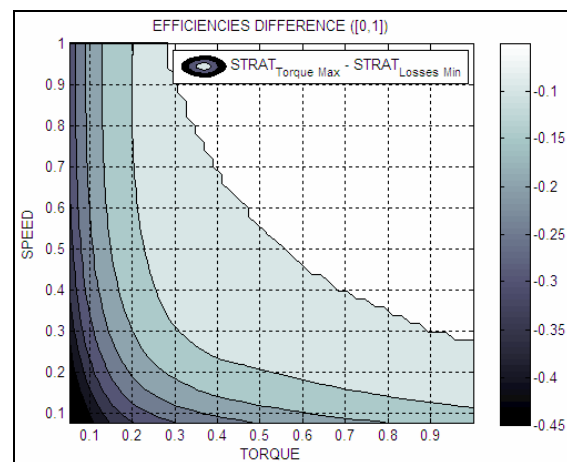


Figure 18: Global efficiency gain with a strategy of losses minimization vs. motor torque maximization (units = p.u.)

Efficiency gain does not exceed 5%. Indeed, in this study case, converter efficiency is much higher than motor efficiency.

3.4 Strategies comparison

Figure 17 shows a global efficiency map obtained with torque maximization strategy (previously presented and frequently used in literature [6]).

This strategy is compared with losses minimization strategy (Fig.18).

Losses minimization strategy allows increasing efficiency, especially for low torques area, where a maximal rotor current is not necessary.

4 Architecture Optimization

When dealing with powertrain performances, it is mandatory to take into account the way battery voltage changes with respect to the state of charge. This voltage value has a direct impact on (i_d, i_q, i_f) optimization.

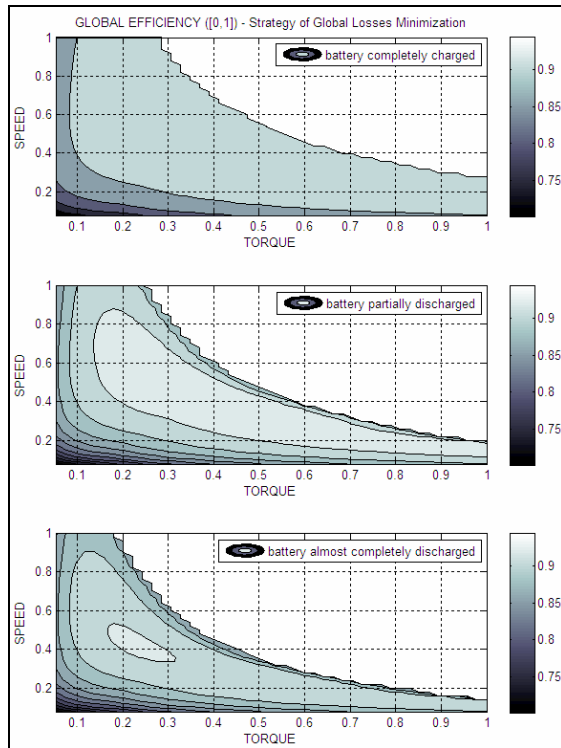


Figure 19: Global efficiency with losses minimization strategy for different battery voltages (units = p.u.)

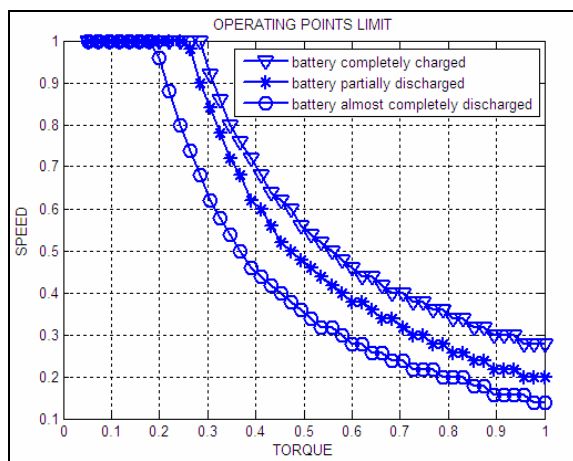


Figure 20: Operating points limits for different battery voltages (units = p.u.)

Figure 19 shows powertrain efficiencies according to battery state of charge. Results are obtained by losses minimization for three different constraints on (v_d, v_q) .

As well as global efficiency differences, we observe variations of operating points limit due to optimization constraints (Fig.20). Battery voltage has an impact on both efficiency and performances.

4.1 DC-DC Boost converter

The electrical architecture of the powertrain may have a great influence on battery voltage variations impact. For example, introducing a dc-dc converter between the battery and the inverter can change the behaviour of the system. The function of this converter is to stabilize as much as possible the inverter dc voltage whatever the battery state of charge is [12].

To study the efficiency of this architecture, a dc-dc boost converter model with IGBT has been integrated in the simulation platform (Fig. 21).

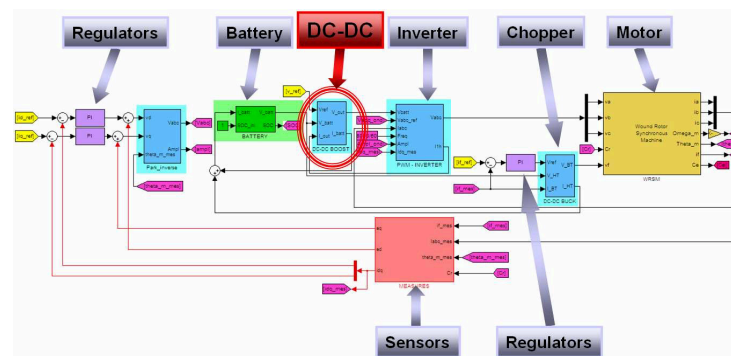


Figure 21: Electric Powertrain with dc-dc boost converter

4.2 Low-level control with four degrees of freedom

With this new powertrain architecture, four degrees of freedom are now potentially available: (i_d, i_q, i_f) currents as previously presented and dc-dc voltage reference. When optimizing powertrain control, output battery voltage constraints can thus be partly relaxed (especially when the battery state of charge is low).

4.3 Architectures comparison

Figure 22 shows various results with and without dc/dc converter.

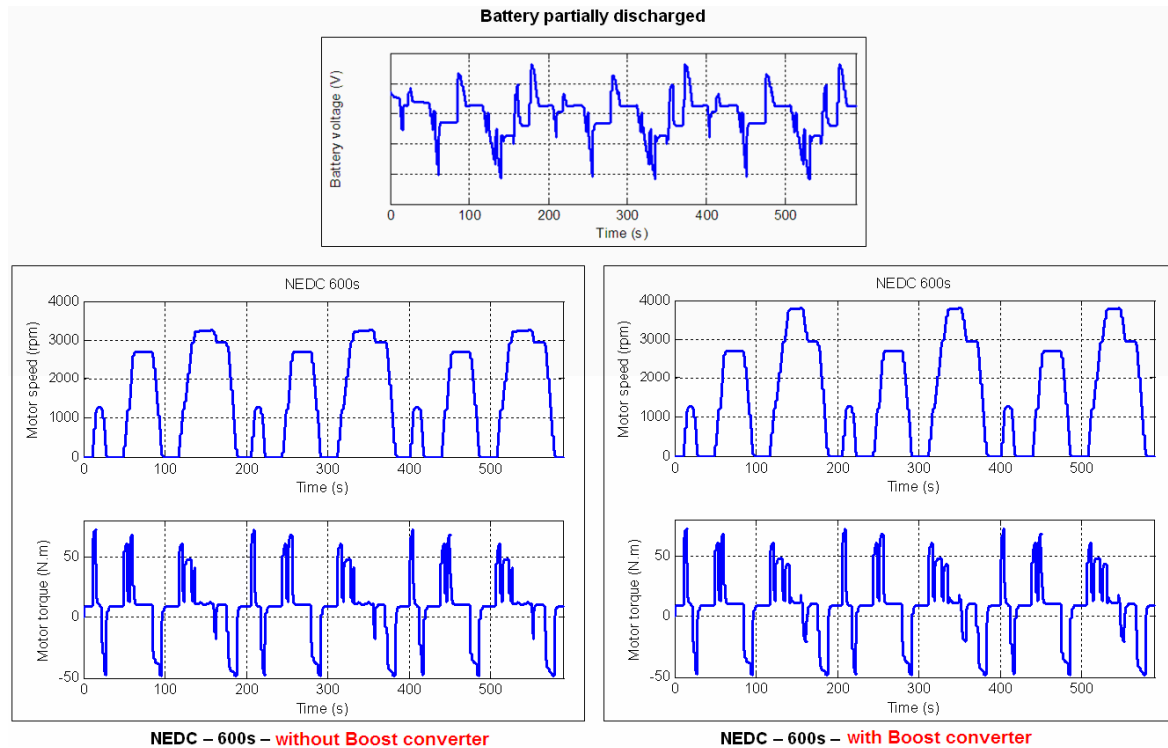


Figure 22: Example of simulation results comparison with and without dc-dc boost converter (typical case study)

5 Conclusion

A platform for Electric Vehicle Powertrain has been presented in this paper. Battery, converters and traction motor are modelled with the intention of optimizing performances and powertrain efficiency (highly linked with vehicle range). Consequently, models are as much simplified as possible. Further, explicit formulations depending on degrees of freedom are preferred.

In a second step, we have presented two powertrain control strategies resulting from a “software” optimization: we have used a classic electric powertrain architecture and shown how performances and efficiencies can be different depending on control laws.

Finally, we have studied an example of “hardware” optimization by introducing an additional degree of freedom with a dc-dc boost converter between battery and inverter. Comparison results have been obtained with the simulation platform. This platform has proven its efficiency and has brought much more than satisfactory results for the deep understanding of proposed optimized control laws and architectures.

Acknowledgments

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