GPU Acceleration of Regular Expression Matching for Large Datasets: Exploring the Implementation Space

Xiaodong Yu and Michela Becchi
University of Missouri - Columbia
xymt3@mail.missouri.edu, becchim@mail.missouri.edu

ABSTRACT
Regular expression matching is a central task in several networking (and search) applications and has been accelerated on a variety of parallel architectures, including general purpose multi-core processors, network processors, field programmable gate arrays, and ASIC- and TCAM-based systems. All of these solutions are based on finite automata (either in deterministic or non-deterministic form) and mostly focus on effective memory representations for such automata. More recently, a handful of proposals have exploited the parallelism intrinsic in regular expression matching (i.e., coarse-grained packet-level parallelism and fine-grained data structure parallelism) to propose efficient regex-matching designs for GPUs. However, most GPU solutions aim at achieving good performance on small datasets, which are far less complex and problematic than those used in real-world applications.

In this work, we provide a more comprehensive study of regular expression matching on GPUs. To this end, we consider datasets of practical size and complexity and explore advantages and limitations of different automata representations and of various GPU implementation techniques. Our goal is not to show optimal speedup on specific datasets, but to highlight advantages and disadvantages of the GPU hardware in supporting state-of-the-art automata representations and encoding schemes, approaches that have been broadly adopted on other parallel memory-based platforms.

Categories and Subject Descriptors
C.2.0 [Computer Communication Networks]: General – Security and protection (e.g., firewalls).

General Terms

Keywords
CUDA; GPGPU; deep packet inspection; finite automata; regular expression matching.

1. INTRODUCTION
Regular expression matching is an important task in several application domains (bibliographical search, networking, and bioinformatics) and has received particular consideration in the context of deep packet inspection. Deep packet inspection is a fundamental networking operation, employed most notably at the core of network intrusion detection systems (NIDS). Some well-known open-source applications, such as Snort and Bro, fall into this category; in addition, all major networking companies are offering their own network intrusion detection solutions (e.g., security appliances from Cisco, Juniper Networks and Huawei Technologies). A traditional form of deep packet inspection consists of searching the packet payload against a set of patterns. In NIDS, every pattern represents a signature of malicious traffic. As such, the payload of incoming packets is inspected against all available signatures, and a match triggers pre-defined actions on the interested packets. Because of their expressive power, which can cover a wide variety of pattern signatures, regular expressions have been adopted in pattern-sets used in both industry and academia. In recent years, datasets used in practical systems have increased in both size and complexity: as of December 2011, over eleven thousand rules from the widely used Snort contain Perl-compatible regular expressions.

To meet the requirements of networking applications, a regular expression matching engine must both allow parallel search over multiple patterns and provide worst-case guarantees as to the processing time. An unbounded processing time would in fact open the way to algorithmic and denial of service attacks. To allow multi-pattern search, current implementations represent the pattern-set through finite automata (FA) [4], either in their deterministic or in their non-deterministic form (DFA and NFA, respectively). The matching operation is then equivalent to a FA traversal guided by the content of the input stream. Worst-case guarantees can be met by bounding the amount of per-character processing. Being the basic data structure in the regular expression matching engine, the finite automaton must be deployable on a reasonably provisioned hardware platform. As the size of pattern-sets and the expressiveness of individual patterns increases, limiting the size of the automaton becomes challenging. As a result, the exploration space is characterized by a trade-off between the size of the automaton and the worst-case bound on the amount of per-character processing.

Previous work [5-18] has focused on accelerating regular expression matching on a variety of parallel architectures: general purpose multi-core processors, network processors, FPGAs, ASIC- and TCAM-based systems. In all these proposals, particular attention has been paid to providing efficient logic- and memory-based representations of the underlying automata (namely, DFAs, NFAs and equivalent abstractions). Because of their massive parallelism and computational power, in recent years GPUs have been considered a viable platform for this application [19-23].

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1 http://www.snort.org
2 http://www.bro-ids.org
5 http://www.huaweisymantec.com
However, existing work has mostly evaluated specific solutions on small datasets consisting of a few tens of patterns.

In general, there is disconnect between the richness of proposals (in terms of the automata and their memory representation) that have emerged in the context of other memory-centric architectures [5-15, 24], and their evaluation on GPU platforms, especially on large and complex datasets which are relevant to today’s applications. Besides leaving the suitability of GPUs to real-world scenarios unclear, this lacuna tends to allow proposals focusing on trivial datasets with little practical relevance and presenting automata abstractions that appear innovative but are essentially equivalent to existing solutions. In this work, we target this problem. Our contributions can be summarized as follows.

- We present an extensive GPU-based evaluation of different automata representations on datasets of practical size and complexity.
- We show three simple schemes to avoid some of the limitations of a recent NFA-based design [22].
- We discuss the impact of state-of-the-art memory compression schemes [5, 10] on DFA solutions.
- We evaluate the use of software managed caches on GPU.

The rest of this paper is organized as follows. In Section 2, we provide some more background and discuss related work on regular expression matching. In Section 3, we present different regular expression matching engine designs for GPUs based on NFAs and DFAs. In Section 4, we provide an experimental evaluation of all the proposed schemes on a variety of pattern-sets. In Section 5, we conclude our discussion.

2. BACKGROUND & RELATED WORK

Regular expression matching is implemented using finite automata, and their exploration space is characterized by a trade-off between the size of the automaton and the worst-case bound on the amount of per-character processing. NFAs and DFAs are at the two extremes in this exploration space. In particular, NFAs have a limited size but can require expensive per-character processing, whereas DFAs offer limited per-character processing at the cost of a possibly large automaton. To provide intuition regarding this fact, in Figure 1 we show the NFA and DFA accepting patterns \(a'bc\), \(bcd'\) and \(cde\). In the two diagrams, states active after processing text \(aabc\) are colored gray. In the NFA, the number of states and transitions is limited by the number of symbols in the pattern-set. In the DFA, every state presents one transition for each character in the alphabet \(\Sigma\). Each DFA state corresponds to a set of NFA states that can be simultaneously active [4]; therefore, the number of states in a DFA equivalent to an \(N\)-state NFA can potentially be \(2^N\). In reality, previous work [6, 9, 12, 14, 24] has shown that this so-called state explosion happens only in the presence of complex patterns (typically those containing bounded and unbounded repetitions of large character sets). Since each DFA state corresponds to a set of simultaneously active NFA states, DFAs ensure minimal per-character processing (only one state transition is taken for each input character).

From an implementation perspective, existing regular expression matching engines can be classified into two categories: memory-based [5-15, 24] and logic-based [7, 16-18]. In the former, the FA is stored in memory; in the latter, it is stored in (combinatorial and sequential) logic. Memory-based implementations can be (and have been) deployed on various parallel platforms: general purpose multi-core processors, network processors, ASICs, FPGAs, and GPUs; logic-based implementations typically target FPGAs. For the logic-based approaches, updates in the pattern-set require the underlying platform to be reprogrammed. In a memory-based implementation, the design goals are the minimization of the memory size needed to store the automaton and of the memory bandwidth needed to operate it. Similarly, in a logic-based implementation the design should aim at minimizing the logic utilization while allowing fast operation (that is, a high clock frequency). Memory-based solutions have been recently adapted and extended to TCAM implementations [25-27].

Existing proposals targeting DFA-based, memory-centric solutions have focused on two aspects: (i) designing compression mechanisms aimed at minimizing the DFA memory footprint; and (ii) devising novel automata to be used as an alternative to DFAs in case of state explosion. Alphabet reduction [5, 13, 28], run-length encoding [13], default transition compression [5, 10], and delta-FAs [15] are generally applicable mechanisms falling into the first category, whereas multiple-DFAs [12, 13], hybrid-FAs [6, 24], history-based-FAs [9] and XFAs [14] fall into the second one. All DFA compression schemes leverage the transition redundancy that characterizes DFAs describing practical datasets. Despite the complexity of their design, memory-centric solutions have three advantages: (i) fast reconfigurability, (ii) low power consumption, and (iii) limited flow state; the latter leads to scalability in the number of flows (or input streams).

In recent years GPUs have been widely used to accelerate a variety of scientific applications [29-31]. Most proposals have targeted NVIDIA GPUs, whose programmability has greatly improved since the advent of CUDA [32]. The main architectural traits of these devices can be summarized as follows. NVIDIA GPUs comprise a set of Streaming Multiprocessors (SMs), each of them containing a set of simple in-order cores. These in-order cores execute the instructions in a SIMD manner. GPUs have a heterogeneous memory organization consisting of high latency global memory, low latency read-only constant memory, low-latency read-write shared memory, and texture memory. GPUs adopting the Fermi architecture, such as those used in this work, are also equipped with a two-level cache hierarchy. The judicious use of the memory hierarchy and of the available memory bandwidth is essential to achieving good performance. With CUDA, the computation is organized in a hierarchical fashion, wherein threads are grouped into thread-blocks. Each thread-block is mapped onto a different SM, while different threads in that
block are mapped to simple cores and executed in SIMD units, called warps. Threads within the same block can communicate using shared memory, whereas threads from different thread-blocks are fully independent. Therefore, CUDA exposes to the programmer two degrees of parallelism: fine-grained parallelism within a thread-block and coarse-grained parallelism across multiple thread-blocks. Branches are allowed on GPU through the use of hardware masking. In the presence of branch divergence within a warp, both paths of the control flow operation are in principle executed by all CUDA cores. Therefore, the presence of branch divergence within a warp leads to core underutilization and must be minimized to achieve good performance.

Recent work [33] has considered exploiting the GPU’s massive hardware parallelism and high-bandwidth memory system in order to implement high-throughput networking operations. In particular, a handful of proposals [19-23] have looked at accelerating regular expression matching on GPU platforms. Most of these proposals use the coarse-grained block-level parallelism offered by these devices to support packet- (or flow-) level parallelism intrinsic in networking applications.

Gnort [19, 20], proposed by Vasiliadis et al, represents an effort to port Snort IDS to GPUs. To avoid dealing with the state explosion problem, the authors process on GPU only a portion of the dataset consisting of regular expressions that can be compiled into a DFA, leaving the rest in NFA form on CPU for separate processing. As a result, this proposal speeds up the average case, but does not address malicious and worst case traffic. Gnort represents the DFA on GPU memory uncompressed, and exploits parallelism only at the packet level (i.e., it does not leverage any kind of data structure parallelism to further speed up the operation).

Smith et al [21] ported their XFA proposed data structure [14] to GPUs, and compared the performance achieved by an XFA- and a DFA-based solution on datasets consisting of 31-96 regular expressions. They showed that a G80 GPU can achieve a 10-11X speedup over a Pentium 4, and that, because of the more regular nature of the underlying computation, on GPU platforms DFAs are slightly preferable to XFAs. It must be noted that the XFA solution is suited to specific classes of regular expressions: those that can be broken into non-overlapping sub-patterns separated by \( \cdot \) or \( \cdot \) terms. However, these automata cannot be directly applied to regular expressions containing overlapping sub-patterns or \( [c_i..c_j]^* \) terms followed by sub-pattern containing any of the \( c_i, ..., c_k \) characters.

More recently, Cascaran et al [22] proposed iNFAnt, a NFA-based regex matching engine on GPUs. Since state explosion occurs only when converting NFAs to DFAs, iNFAnt is the first solution that can be easily applied to rule-sets containing any of the \( \cdot \) or \( \cdot \) terms. However, this work, to our knowledge, the only GPU-oriented proposal which presents an evaluation on large, real-world datasets (from 120 to 543 regular expressions). The main disadvantage of iNFAnt is its unpredictable performance and its poor worst-case behavior. In Section 3.2, we will discuss this solution in more detail.

Zu et al [23] proposed a GPU design which aims to overcome the limitations of iNFAnt. The main idea is to cluster states into compatibility groups, so that states within the same compatibility group cannot be active at the same time. The main limitation of this method is the following. The computation of compatibility groups requires the exploration of all possible NFA activations (this fact stems from the definition of compatibility groups itself). This, in turn, is equivalent to subset construction (i.e., NFA to DFA transformation). As highlighted in previous work [6, 9, 12, 14, 24], this operation, even if theoretically possible, is practically feasible only on small or simple rule-sets that do not incur the state explosion problem. Not surprisingly, the evaluation proposed in [23] is limited to datasets consisting of 16-36 regular expressions. Further, the transition tables of these datasets are characterized by a number of distinct transitions per character per entry \( \leq 4 \) (although they are not systematically built to respect this constraint). This proposal is conceptually very similar to representing each rule-set through four DFAs, which is also feasible only on small and relatively simple datasets. As a consequence, we believe that the comparison with iNFAnt is unfair. A comparison with a pure DFA-based approach would be more appropriate. However, given its nature, the proposal in [23] is likely to provide performance very similar to a pure DFA-based solution.

In this work, we evaluate GPU designs on practical datasets (with size and complexity comparable to those used in [22]). In contrast to [23], our goal is not to show optimal speedup of a given solution on a specific kind of rule-set. Instead, we want to provide a comprehensive evaluation of automata representations, memory encoding and compression schemes that are commonly used in other memory-centric platforms. We hope that this analysis will help users to make an informed selection among the plethora of existing algorithmic and data structure proposals.

3. GPU IMPLEMENTATION

In all our regular expression engine designs, the FA traversal, which is the core of the pattern matching process, is fully implemented in a GPU kernel. The implementations presented in this proposal differ in the automaton used, and, as a consequence, in the memory data structures stored on GPU and in the FA traversal kernel. However, the CPU code is the same across all the proposed implementations. We first describe the CPU code and the computation common to all implementations (Section 3.1), and then our NFA and DFA traversal kernels (Section 3.2 and 3.3, respectively).

3.1 General Design

Like previous proposals, our regular expression matching engine supports multiple packet-flows (that is, multiple input streams) and maps each of them onto a different thread-block. In other words, we support packet-level parallelism by using the different SMs available on the GPU. The size of the packets \( P_{size} \) is configurable and set to 64KB in all our experiments. The number of packet-flows processed in parallel \( N_{pf} \) is also configurable: if it exceeds the number of SMs, multiple packet-flows will be mapped onto the same SM. Packet-flows handled concurrently may not necessarily have the same size: we use an array of flow identifiers to keep track of the mapping between the packets and the corresponding packet-flows. When a packet-flow is fully processed, the corresponding thread-block is assigned to a new flow.

The FA is transferred from CPU to GPU only once, at the beginning of the execution. Then, the control-flow on CPU consists of a main loop. The operations performed in each iteration are the following. First, \( N_{PF} \) packets – one per packet-flow - are transferred from CPU to GPU and stored contiguously on the GPU global memory. Second, the FA traversal kernel is invoked, thus triggering the regex matching process on GPU. The result of the matching operation is transferred from GPU to
CPU at the end of the flow-traversal. The state information, which must be preserved in order to detect matches that occur across multiple packets, can be kept on GPU and does not need to be transferred back to CPU. However, such information must be reset before starting to process a new packet-flow.

We use dual buffering to hide the CPU-GPU packet transfer time. To this end, on GPU we allocate two buffers of \( N_{P} \) packets each: one buffer stores the packets to be processed in the current iteration, and the other the ones to be processed in the next iteration. The FA-traversal corresponding to iteration \( i \) overlaps with the packet transfer related to iteration \( i+1 \). The function of the two buffers is swapped from iteration to iteration.

### 3.2 NFA-based Engines

The advantage of NFA-based solutions is that they allow a compact representation for datasets of arbitrary size and complexity. Given a set of regular expressions, it is always possible to build an NFA with a number of states which is less than or equal to that of characters in the pattern-set. In this section, we consider NFA solutions that are applicable to arbitrary pattern-sets and that rely on NFAs with a minimal number of states. As mentioned in Section 2, the \( iNFAnt \) design [22] is the most efficient and broadly applicable GPU-based NFA proposal. In fact, while [23] provides better performance than \( iNFAnt \), it implicitly requires a full analysis of the potential NFA activations and is not applicable to arbitrary NFAs.

#### 3.2.1 \( iNFAnt \)

In the \( iNFAnt \) proposal, the transition table is encoded using a symbol-first representation: transitions are represented through a list of (source, destination) pairs sorted by their triggering symbol, whereby source and destination are 16-bit state identifiers. An ancillary data structure, records, for each symbol, the first transition within the transition list. Persistent states (i.e., states with a self-transition on every character of the alphabet) are handled separately using a state vector. These states, once activated, will remain active for the whole NFA traversal. The \( iNFAnt \) kernel operates as shown in the pseudo-code below, which is adapted from [22]. For readability, in all the pseudo-code reported in this paper, we omit representing the matching operation occurring on accepting states.

```plaintext
kernel iNFAnt
1: \textbf{current} \leftarrow \textbf{initial}
2: \textbf{while} \textbf{input.empty} \textbf{do}
3: \textbf{c} \leftarrow \textbf{input.first}
4: \textbf{input} \leftarrow \textbf{input.tail}
5: \textbf{future} \leftarrow \textbf{current} \& \textbf{persistent}
6: \textbf{while} \textbf{a transition on} \textbf{c} \textbf{is pending} \textbf{do}
7: \textbf{src} \leftarrow \textbf{transition source}
8: \textbf{dst} \leftarrow \textbf{transition destination}
9: \textbf{if} \textbf{current}[,\textbf{src}] \textbf{is set then}
10: \textbf{atomicSet}(\textbf{future}, \textbf{dst})
11: \textbf{current} \leftarrow \textbf{future}
end;
```

Besides the persistent state vector (\textbf{persistent}), \( iNFAnt \) uses two additional state vectors: \textbf{current} and \textbf{future}, which store the current and the future set of active states. All state vectors are represented as bit-vectors, and stored in shared memory. After initialization (line 1), the kernel iterates over the characters in the input stream (loop at line 2). The bulk of the processing starts at line 5, after character \textbf{c} is retrieved from the input buffer (lines 3-4). First, the future state vector is updated to include the active persistent states (line 5). Second, the transitions on input \textbf{c} are selected (lines 6-8), and the ones originating from active states cause \textbf{future} to be updated (lines 9-10). Finally, \textbf{current} is updated to the value of \textbf{future} (line 11). Underlined statements represent barrier synchronization points. As can be seen (line 10), an additional synchronization is required to allow atomic update of the future state vector.

Besides thread-block parallelism at the packet level, this kernel exploits thread-level parallelism in several points. First, the state vector updates at lines 1, 5 and 11 are executed in parallel by all threads. In particular, consecutive threads access consecutive memory words, thus ensuring conflict-free shared memory accesses. Second, the transition processing loop (lines 6-10) is also parallelized over the threads in a block, and the layout of the transition table allows coalesced global memory accesses during this operation. Note that the number of threads concurrently accessing the state vectors and the transition list is equal to the block size: in case of large NFAs, multiple iterations are required to perform a full scan of these arrays.

Since the state vectors are represented as bit-vectors and the transition table contains 16-bit state identifiers, a translation between a bit-vector and a short integer state identifier representation is required in lines 9 (for \textbf{src}) and 10 (for \textbf{dst}). This operation is relatively costly.

#### 3.2.2 Our optimized NFA-based design

We note that \( iNFAnt \) presents the following inefficiency. The loop at line 6 must scan all NFA transitions on a given symbol \textbf{c}. On large NFAs, such list can be very long and may require a large number of thread-block iterations. In every iteration, global memory is accessed to retrieve the transition information (line 6), and several translations of state identifiers into bit-vectors are required (line 9). The latter operation is performed even if the corresponding states are inactive. Therefore, with the exception of instruction 10, the cost of the loop at line 6 is independent of the size of the current state vector. This makes \( iNFAnt \)'s average-case processing time comparable to its worst-case. In the worst-case, instruction 10 is executed on all retrieved transitions.

The average-case processing can be improved by taking the following observations into consideration.

1. In most traversal steps, only a minority of the NFA states are active.
2. NFA states can be easily clustered into groups of states that cannot be active at the same time.

The second observation is also exploited by [23]. Differently from [23], we do not want to fully explore the compatibility between NFA states, because this would require a full exploration of all possible NFA activations, which is impractical on relatively large and complex datasets.

One of the advantages of \( iNFAnt \) is the simplicity of its implementation. We aim to introduce code modifications that maintain the simplicity of the original design. Ad-hoc solutions targeting too specific situations can originate divergence during execution, and end up being not beneficial in the average case.

#### Optimization 1

The first consideration can be exploited as follows. If transitions on the same character are sorted according to the source state identifier, and the largest active state identifier \( SID_{MAX} \) is known, then the execution of loop 6 can be terminated when the first transition with source identifier greater than \( SID_{MAX} \) is encountered. In case of large NFAs, this can significantly reduce the number of iterations required to process...
the transitions on the current input symbol. We implement this optimization as follows. First, we store $SID_{MAX}$ in shared memory (and save it to global memory at the end of each packet). Second, we add the instruction $atomicMax(SID_{MAX}, dst)$ to the if-statement at line 9. This updates $SID_{MAX}$ whenever required (the update is performed in shared memory). Third, in implementing the loop at line 6, we check whether the last retrieved transition has source state identifier greater than $SID_{MAX}$, in which case we terminate the loop. More specifically, our implementation requires two versions of $SID_{MAX}$: a current and a future value. These variables are handled similarly to the current and future version of the active state vector.

**Optimization 2:** The second observation can be exploited as follows. States can be grouped according to their incoming transitions. We define two or more states as compatible if they can potentially be active at the same time. For example, states that share at least one incoming transition (i.e., the symbol on that transition) are compatible. We perform the following state clustering. We distinguish states with a single incoming transition and states with multiple incoming transitions. States with a single incoming transition on character $c_i$ are grouped into $group_{c_i}$. The other states are grouped into a special group, that we call $overlap$. Clearly, the following holds. (i) States belonging to the same group are compatible. (ii) States belonging to different $group_{c_i}$ are incompatible. (iii) States belonging to $overlap$ are compatible with any other state. Compatibility groups will decrease in size (and increase in number) if a finer grained classification is made (for instance, if sequences of two or more incoming characters are considered in defining the compatibility groups). However, most of the NFA states have a single incoming transition, and we experimentally verified that a finer grained classification does not significantly affect the performance of our implementation.

We can take advantage of the above classification as follows. Loop 6 can be made more efficient by grouping transitions on the same input character according to the compatibility group of their source state. For simplicity, we will say that two transitions are compatible when their source states are such. At each iteration, rather than processing all transitions on the current input symbol, we can consider only the ones that are compatible with the current active states. Note that, because of our definition of compatibility, all the states in the active set (that is, in $current_{n}$) must be compatible: they must belong either to the same $group_{c_i}$ or to the $overlap$. The compatibility group of the current active set depends on the previously processed input character $c_{p}$. To summarize, when processing the current input character $c$, the traversal can be limited to two subsets of the transitions on $c$: those in $group_{overlap}$ and those in $group_{c_i}$. This can be easily achieved by sorting the transitions on the same character according to their compatibility group, and by using an ancillary array indicating the offset of each group within this hierarchical transition list.

**Optimization 3:** To combine the benefits of the two optimizations presented above, a proper numbering scheme for state identifiers must be adopted. We make three observations. First, persistent states and states with self-loops belong to the $overlap$. These states have a higher likelihood to be active during the traversal (and, once activated, they may be never or hardly deactivated). Second, states close to the NFA entry state are more likely to be traversed. Third, the benefits of optimization 1 will be higher if the state numbering scheme is such that states within the same compatibility group have similar identifiers. Given these considerations, we adopt the following state numbering scheme. First, we number the states according to a breadth-first traversal of the NFA. Second, we compute the compatibility groups. Third, we order the compatibility groups as follows. First, we consider the $overlap$. Then, we sort all $group_{c_i}$ according to the average frequency of character $c$ on publicly available packet traces. Finally, we assign the source identifiers in sequence starting from the first group. Within each group, we keep the priority dictated by the identifiers set in the first phase (thus preserving the breadth-first ordering of states within groups).

In Figure 2, we show an example. In particular, Figure 2(a) shows the original NFA, Figure 2(b) shows the state numbering assigned with breadth-first traversal (Orig. ID) and with the described state numbering scheme (New ID). Figure 2(c) shows the state compatibility groups, and reports the state identifiers in the original NFA of Figure 2(a), and those computed with our scheme. In Figure 3, we show the memory layout of the transitions on characters $a$, $b$ and $c$ for the NFA of Figure 2.
3.3 DFA-based Engines

The main weakness of NFAs is their non-deterministic nature. During NFA traversal, the number of active states can vary from iteration to iteration; and so does the amount of work performed in different phases of the traversal. On the other hand, thanks to their deterministic nature, DFAs can offer predictable and bounded per-character processing. As mentioned above, the presence of repetitions of wildcards and large character sets may lead to state explosion when transforming an NFA into DFA, making a DFA solution impractical. DFAs are never a viable solution in the presence of unanchored regular expressions containing bounded repetitions of character sets [12, 24]. Becchi & Crowley [24] proposed a counting automaton to tackle this kind of patterns. In this work, we do not take counting constraints in consideration: they can, however, be supported through our NFA-base design. The remaining problematic patterns, namely unbounded repetitions of wildcards and large character sets, can be handled by grouping regular expressions into clusters and by generating multiple DFAs [12, 34], one for each cluster. The pattern matching operation requires all these DFAs to be traversed on each input character, thereby causing memory bandwidth pressure.

There is no established optimal mechanism to cluster an arbitrary set of regular expressions. In this paper, we use the clustering algorithm proposed in [34]. The basic idea is the following: rather than statically determining the number of DFAs to generate, the user defines the maximum allowed DFA size. The generation process will try to cluster together as many regular expressions as possible so that the corresponding DFA size will not exceed the defined threshold. This is done by first attempting to generate a DFA accepting the whole pattern-set. If, during DFA generation, the maximum DFA size is reached, the regular expression set is automatically split in two. The algorithm proceeds recursively in a divide and conquer fashion, until all regular expressions have been processed. Typically this will lead to a small number of DFAs for small and simple datasets, and in a large number of DFAs for large and complex ones. In our experiments we set the maximum DFA size to 64K states, to allow the use of 16-bit state identifiers.

A naïve way to implement a DFA-based regular expression matching engine is to treat multiple DFAs as a single NFA (with a constant active set size). In other words, iNFAnt can be used to support multiple DFAs. Given the large number of DFA states, however, this implementation would be very inefficient. A better design exploits the fact that each DFA state has one and only one outgoing transition on any input character.

3.3.1 Uncompressed DFA-based solution

The bulk of the traversal of a set of uncompressed DFAs is represented in the pseudo-code below. Again, we assume that different thread-blocks are dedicated to different packet-flows (or input streams). Thread-level parallelism is exploited at a DFA granularity: each thread processes a different DFA.

```
kernelfunction uncompressed-DFA
1:  current, ← initial, [tid]
2:  while input.empty do
3:      c ← input.first
4:      input ← input.tail
5:      current, ← state_table[tid][current,][c];
6:  initial, [tid] ← current,
end
```

The underlying data structure consists of a bi-dimensional transition table per DFA (state_table in the pseudo-code), which stores the destination state identifier for every (source state, input character) pair. State tables corresponding to different DFAs are laid out next to one another in global memory. Each thread stores the information of the current active state in a local register (current, variable), which is initialized from global memory and copied back to it at the beginning and at the end of each packet’s processing (lines 1 and 6, respectively). In each iteration of the main loop (which starts at line 2), each thread performs a global memory access to query the state table on the input character (line 5). Note that such memory accesses are scattered and uncoalesced. The only way to hide the memory latency is to increase the global thread count by processing multiple packet-flows on the same SM. This is possible given the limited shared memory and register requirement of this simple DFA traversal kernel. Note that, in case of small datasets leading to a single or few DFAs, the code can be slightly modified so to make each thread-block process multiple packet-flows. For example, in the presence of 4 DFAs, a 32-thread block (sized to handle a full warp), can process 8 packet-flows in parallel. Since our design aims at evaluating generally applicable solutions on large and complex datasets, we do not consider this optimization in our experimental evaluation.

3.3.2 Compressed DFA-based solution

Uncompressed DFAs are characterized by one outgoing transition per character per state. In the presence of large alphabets and millions of states, this may lead to high memory requirements. This problem has been extensively studied. All existing DFA memory compression schemes exploit the transition redundancy inherent in these automata. Perhaps the most effective DFA compression mechanism has been proposed in [10] and improved in [5]. The basic idea is to connect pair of states $S_1$ and $S_2$ characterized by transition commonality through non-consuming directed default transitions. Then, all transitions common to $S_1$ and $S_2$ can be safely removed from the source state $S_1$. This mechanism leads to a processing overhead due to default transition traversal: the algorithm proposed in [5] minimizes such overhead and ensures a worst-case of $2N$ state traversals to process an input stream consisting of $N$ characters. Other compression mechanisms, such as alphabet reduction [5, 13], are mostly ineffective on large datasets.

```
kernelfunction compressed-DFA
1:  current, [tid,] ← initial, [tid,]
2:  idx[tid,] ← 0
3:  while (idx[tid,]=PACKET_SIZE) do
4:      future, [tid,] ← INVALID
5:      c ← input[idx[tid,]]
6:      tx_offset ← offset[current, [tid,]]
7:  while current states has unprocessed transitions
8:      symbol ← labeled tx[tid,][tx_offset][tx_offset+tid,x].char
9:      dst ← labeled tx[tid,][tx_offset][tx_offset+tid,x].dst
10:     if (symbol = c)
11:         future, [tid,] ← dst
12:         idx[tid,]++
13:     if (future, [tid,] = INVALID)
14:         future, [tid,] ← default tx[tid,][current, [tid,]]
15:  current, [tid,] = future, [tid,]
16:  initial, [tid,] ← current, [tid,]
end
```

The pseudo-code above represents a kernel implementing the multiple-DFA traversal in the presence of default transition
Figure 4: Exemplification of mapping of DFAs and input streams on the GPU in the compressed-DFA-based solution.

compression. In a default transition-compressed DFA, each state has a default transition and a variable number of labeled transitions. Default transitions can be stored in a one-dimensional array (default_tx) with as many entries as DFA states. Labeled transitions can be represented through a list of (input character, destination state) pairs, and an ancillary data structure (offset array) indicating, for each state, the offset in the transition list. In our implementation, to optimize the memory usage, we store labeled transitions in a one-dimensional array (labeled_tx) of 32-bit elements. For each element, 8 bits are used to represent the ASCII input character, and the remaining bits to store the state identifier. Note that this allows supporting DFAs with up to 16M states (well above the 64K threshold used in this work). These data structures are stored in global memory; the only exception being the frequently accessed initial state, which is stored in constant memory and accessed through the constant memory cache.

Thread-level parallelism is exploited in two ways: different threads process different DFAs and, within the same DFA, different labeled transitions. This is accomplished by using bi-dimensional thread-blocks. The logical mapping and partitioning is represented in Figure 4. As can be seen, different input streams are again mapped onto different thread-blocks. Threads within the same block are partitioned over multiple DFAs (using the y-dimension of the thread identifier). Within each partition, different threads process different labeled transitions (using the x-dimension of the thread identifier). The DFA data structures are laid out in memory next to one another.

The data structures stored in shared memory are the following:
(i) the active state vector current, initialized from global memory and restored to it at the beginning and at the end of each packet’s processing (lines 1 and 15, respectively); (ii) the future state vector future, with the same use as in the NFA implementation; and (iii) the vector idx, containing a pointer to the next character to be processed. Each of these arrays has one entry per DFA, which must be shared along the x-dimension by all threads processing the same DFA. For efficiency, variables c, tx_offset, symbol and dst reside in (per-thread) registers.

The bulk of the processing in the main loop (starting at line 3) can be summarized as follows. In lines 7-12, the labeled transitions are fetched from global memory by different threads. The corresponding memory accesses are coalesced. If the number of labeled transitions is larger than the x-dimension of the thread-blocks, this operation may require several iterations (“it_offset” represents the iteration offset). If a transition on the current input character is found (line 10), the future state vector is updated and the pointer idx is moved forward. Otherwise, the default transition is taken (lines 13-14).

As can be seen (lines 3 and 12), because of the use of default transitions, different DFAs may be processing different characters of the input stream at the same time. The use of the algorithm proposed in [5] minimizes the number of extra state traversals performed. However, default transitions may still lead to warp divergence and badly affect the performance. After default transition compression, more than 90% of the states are left with 4-5 labeled transitions. If the x-dimension of the block size is set to 32 (to equal the warp size), an iteration of the loop at line 7 is sufficient to process most input characters. However, such setting leads to warp underutilization.

3.3.3 Enhanced compressed DFA-based solution

We want to overcome the main limitations of our compressed-DFA design. Specifically, we want to reduce warp divergence and thread underutilization. Further, given that previous work [34] has shown that regular expression matching exhibits strong locality, we implement a software-managed caching scheme in shared memory.

To achieve these goals we reorganize the layout of the transition table in a more regular way. Specifically, we allow compressed states to consist of either 4 or 8 labeled transitions. All states with more than 8 transitions are represented in full and processed via direct indexing. States with less than 4 or with more than 4 but less than 8 labeled transitions are padded (by duplicating some existing transitions), as shown in Figure 5(a). In addition, for each DFA, we reorder and renumber the states so to accommodate states of the same kind contiguously. Each memory region is identified by a base_offset variable, which stores the identifier of the first state in that region, and is stored in a register for efficient access. For example, in Figure 5(b), base_offset4 = 1, base_offset6 = n+1 and base_offset32=n+m+1.

With this layout, processing compressed states requires a maximum of 8 CUDA threads and a single iteration of the loop at lines 7-12 in the pseudo-code above. We modify the thread-block organization so to have 8 threads along the x-dimension; we keep the size of the y-dimension equal to the number of DFAs. Each warp can now process 4 (rather than a single) DFAs. In this design, warp divergence can take place when, on
Datasets have been generated using the tool described in [34] and using tokens extracted from the backdoor rules. In particular, we generated nine synthetic pattern-sets: exact-match (or EM), range.5, range.1, dotstar.5, dotstar.1 and dotstar.2. As the names suggest, the exact-match set contains only exact-match patterns; in range.5 and range.1 50% and 100% of the patterns include character sets; in addition to that, the dotstar* datasets contain a varying fraction of unbounded repetitions of wildcards (5%, 10%, and 20%, respectively). All synthetic datasets consist of 1,000 regular expressions.

The packet traces used in the evaluation have been also synthetically generated using the tool described in [34]. This tool allows producing traces that simulate various amount of malicious activity. This is possible by tuning \( p_{mc} \), a parameter that indicates the probability of malicious traffic. In the generation, we used 15 probabilistic seeds and 4 \( p_{mc} \) values: 0.35, 0.55, 0.75, and 0.95. All traces have a 1 MB size. The packet size has been set to 64KB across all experiments. As detailed below, various numbers of packet-flows have been used.

### 4.2 Dataset Characterization

A characterization of the datasets and of their memory requirements on GPU using different automata representations is reported in Table 1. Because of their simplicity, the exact-match and range* datasets can be compiled into a single DFA, and do not require a compressed DFA representation. State explosion starts originating when considering pattern-sets with unbounded repetitions of wildcards (i.e., dotstar* datasets). As can be seen, the number of DFAs generated increases quickly with the fraction of dot-star terms in the pattern-set. The memory footprints are limited in case of NFAs and larger in case of DFAs (even in their default transition compressed form). For synthetic datasets, the uncompressed-DFA representation has 40-50 times the memory requirements of its compressed counterpart. The enhanced-DFA representation is slightly less memory efficient (by a factor ~1.5X) than the compressed one. The dotstar.2 datasets cannot fit the device memory when an uncompressed-DFA representation is used.

### 4.3 Performance evaluation

A performance evaluation of the proposed solutions on different datasets and packet traces is presented in Table 2. The missing data (i.e., cells with -) represent unnecessary or unsupported implementations. As mentioned above, simple pattern-sets (exact-match and range*) can be compiled into a single DFA with limited memory requirements and therefore do not require DFA compression; on the other hand, complex datasets (dotstar.2) do not fit the memory capacity of the GPU (1.5 GB) unless default transition compression is performed. The data show the performance achieved using the optimal number of packet-flows per SM in every implementation. This optimal number varies from case to case, as detailed in Table 3. For completeness, we show also the throughput obtained using the serial CPU implementation described in [8].

We recall that the uncompressed DFA (U-DFA) traverses exactly one state per input character, independent of the pattern-set and trace. The compressed DFA (C-DFA) performs between 1 and 2 state traversals per character due to the presence of non-
consumption. For example, the dotstar.2 dataset almost all datasets, and is more resilient to malicious traffic with complex pattern-sets including a fraction of rules with wildcards repetitions ≥ 2% (for example, the dotstar.2 dataset). E-DFA is a good compromise between U-DFA and C-DFA: it achieves a 3-5x speedup over C-DFA at the cost of ~1.5x its memory requirements. On synthetic datasets, the performance improvement increases with the complexity of the patterns (i.e., with the fraction of wildcard repetitions). As explained in Section 3.3.3, this performance gain is due to the more regular computation and better thread utilization of E-DFA over C-DFA. Further, E-DFA outperforms both NFA solutions on almost all datasets, and is more resilient to malicious traffic patterns. All DFA-based GPU implementations greatly outperform their CPU counterparts.

Our optimized NFA implementation (O-NFA) achieves a speedup over iNFAnt (NFA) by reducing the number of transitions processed on every input character. In our experiments, the number of iterations over the loop at line 6 in the iNFAnt pseudo-code is reduced up to a 5x factor. This reduction leads to a performance improvement, however, is not so dramatic. This is because the number of iterations is not the only factor that contributes to the matching speed. The additional atomic operation and the more complex control-flow are limiting factors to the speedup. Both NFA-based GPU implementations outperform their CPU counterpart by a factor varying from ~10x (for simple patterns and low $p_{M}$) to ~80X (for complex patterns and high $p_{M}$).

The optimal number of packet-flows per SM varies across the implementations, pattern-sets and traces. Our results are summarized in Table 3. Most implementations reach their peak performance at 4-5 flows/SM. However, in the case of complex datasets, C-DFA achieves best performances at 2-3 flows/SM. Recall that, in C-DFA, bi-dimensional thread-blocks are used. The block-size is equal to 32 along the x-dimension, and is equal to the number of DFAs along the y-dimension. In case of complex datasets, the large number of DFAs leads to large thread-blocks that fully utilize the SM. Therefore, further performance improvements cannot be achieved by increasing the flow-level parallelism beyond 2-3 flows/SM.

All data presented so far have been reported by allowing the GPU to automatically treat part of the shared memory as a hardware-managed cache. We now evaluate the effect of our software-managed cache design on the performance of E-DFA. Due to space limitations we show only the best results, which have been achieved by storing the tag information in registers, caching a maximum of 4 blocks per DFA, and setting the cache block size to the multiple of 128B which allows the maximum utilization of the shared memory (such size depends on the number of DFAs processed in parallel). Table 4 shows the evaluation in case of 1 flow/SM. As can be seen, for average traffic ($p_{M}=0.35$ and $p_{g}=0.55$), the miss rate is low and slight performance improvements are reported. However, malicious traffic ($p_{M}=0.75$ and $p_{g}=0.95$) leads to worse locality behavior and higher miss rate, and, as a consequence, to little-to-no performance gain. The complexity of the datasets also affects the

### Table 3: Effect of number of flows/SM on performance.

<table>
<thead>
<tr>
<th>Implementation</th>
<th>Optimal # flows per SM</th>
<th>Improvement over 1 flow per SM</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Min</td>
</tr>
<tr>
<td>U-DFA</td>
<td>5</td>
<td>1.72</td>
</tr>
<tr>
<td>C-DFA</td>
<td>5 (single-DFA) 2-3 (multi-DFA)</td>
<td>1.16</td>
</tr>
<tr>
<td>E-DFA</td>
<td>5</td>
<td>2.49</td>
</tr>
<tr>
<td>iNFAnt</td>
<td>4</td>
<td>1.81</td>
</tr>
<tr>
<td>Opt-iNFAnt</td>
<td>4</td>
<td>2.55</td>
</tr>
</tbody>
</table>

Table 2: Throughput (in Mbps) obtained with different implementations on different input traces.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>CPU NFA</th>
<th>DFA NFA</th>
<th>O-NFA NFA</th>
<th>U-DFA NFA</th>
<th>C-DFA NFA</th>
<th>E-DFA NFA</th>
<th>CPU DFA</th>
<th>DFA NFA</th>
<th>O-NFA NFA</th>
<th>U-DFA DFA</th>
<th>C-DFA DFA</th>
<th>E-DFA DFA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Backdoor</td>
<td>0.4</td>
<td>7.9</td>
<td>40.8</td>
<td>37.6</td>
<td>171.4</td>
<td>13.8</td>
<td>42.6</td>
<td>0.5</td>
<td>7.7</td>
<td>39.9</td>
<td>37.1</td>
<td>169.1</td>
</tr>
<tr>
<td>Spyware</td>
<td>0.9</td>
<td>4.0</td>
<td>40.1</td>
<td>46.4</td>
<td>168.2</td>
<td>11.5</td>
<td>31.8</td>
<td>0.9</td>
<td>4.1</td>
<td>37.5</td>
<td>43.5</td>
<td>170.9</td>
</tr>
<tr>
<td>E-M</td>
<td>3.9</td>
<td>40.3</td>
<td>14.3</td>
<td>27.3</td>
<td>235.6</td>
<td>-</td>
<td>-</td>
<td>3.6</td>
<td>38.8</td>
<td>11.4</td>
<td>26.3</td>
<td>228.7</td>
</tr>
<tr>
<td>Range.5</td>
<td>4.9</td>
<td>40.6</td>
<td>13.6</td>
<td>26.7</td>
<td>227.1</td>
<td>-</td>
<td>-</td>
<td>4.1</td>
<td>39.0</td>
<td>12.5</td>
<td>25.7</td>
<td>225.5</td>
</tr>
<tr>
<td>Range1</td>
<td>4.9</td>
<td>41.1</td>
<td>18.6</td>
<td>25.7</td>
<td>211.8</td>
<td>-</td>
<td>-</td>
<td>4.1</td>
<td>39.4</td>
<td>15.4</td>
<td>24.7</td>
<td>219.9</td>
</tr>
<tr>
<td>Dotstar.05</td>
<td>1.4</td>
<td>7.9</td>
<td>20.0</td>
<td>25.8</td>
<td>190.6</td>
<td>13.7</td>
<td>37.1</td>
<td>1.0</td>
<td>7.7</td>
<td>17.1</td>
<td>24.5</td>
<td>183.4</td>
</tr>
<tr>
<td>Dotstar.1</td>
<td>0.9</td>
<td>5.2</td>
<td>18.7</td>
<td>26.0</td>
<td>158.1</td>
<td>8.8</td>
<td>30.2</td>
<td>0.7</td>
<td>5.8</td>
<td>19.8</td>
<td>21.4</td>
<td>156.8</td>
</tr>
<tr>
<td>Dotstar.2</td>
<td>0.6</td>
<td>3.2</td>
<td>18.6</td>
<td>24.0</td>
<td>-</td>
<td>6.2</td>
<td>26.3</td>
<td>0.6</td>
<td>3.4</td>
<td>21.7</td>
<td>22.9</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 4: Evaluation in case of 1 flow/SM. As can be seen, for average traffic ($p_{M}=0.35$ and $p_{g}=0.55$), the miss rate is low and slight performance improvements are reported. However, malicious traffic ($p_{M}=0.75$ and $p_{g}=0.95$) leads to worse locality behavior and higher miss rate, and, as a consequence, to little-to-no performance gain. The complexity of the datasets also affects the...
performance: a higher number of DFAs leads to smaller cache blocks and consequently to more cache misses.

Finally, we verified the use of a software-managed cache does not improve the performance when increasing the number of flows mapped to the same SM. Recall that each flow is associated to a thread-block. Since, with the described caching scheme, each thread-block fully utilizes the share memory, the execution of multiple thread-blocks mapped onto the same SM is serialized by the warp scheduler. To allow concurrent execution of flows mapped onto the same SM it is necessary to reduce their shared memory requirement. This can be done by using small cache blocks (i.e., 128-byte blocks independently of the number of DFAs). Small cache blocks, however, lead to higher miss rates, and thus to negligible performance gains. In summary, even if regular expression matching exhibits good locality, the limited size of the shared memory does not make the use of ad-hoc caching schemes advantageous on GPUs. Higher performance gains can be achieved by exploiting flow-level parallelism rather than by making use of caching.

5. CONCLUSION

In this work, we have provided a comprehensive study of regular expression matching on GPUs. To this end, we have used datasets of practical size and complexity and explored advantages and limitations of different NFA- and DFA-based representations. Our evaluation shows that, because of the regularity of its computation, an uncompressed DFA solution outperforms other implementations and is scalable in terms of the number of packet-flows that are processed in parallel. However, on large and complex datasets, such representation may lead to exceeding the memory capacity of the GPU. We have shown schemes to improve a basic default-transition compressed DFA design so to allow more regular processing and better thread utilization.

6. ACKNOWLEDGMENTS

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7. REFERENCES

[31] V. W. Lee et al., “Debunking the 100X GPU vs. CPU myth: an evaluation of throughput computing on CPU and GPU,” in Proc. of ISCA 2010, pp. 451-460.