

Molecular motors

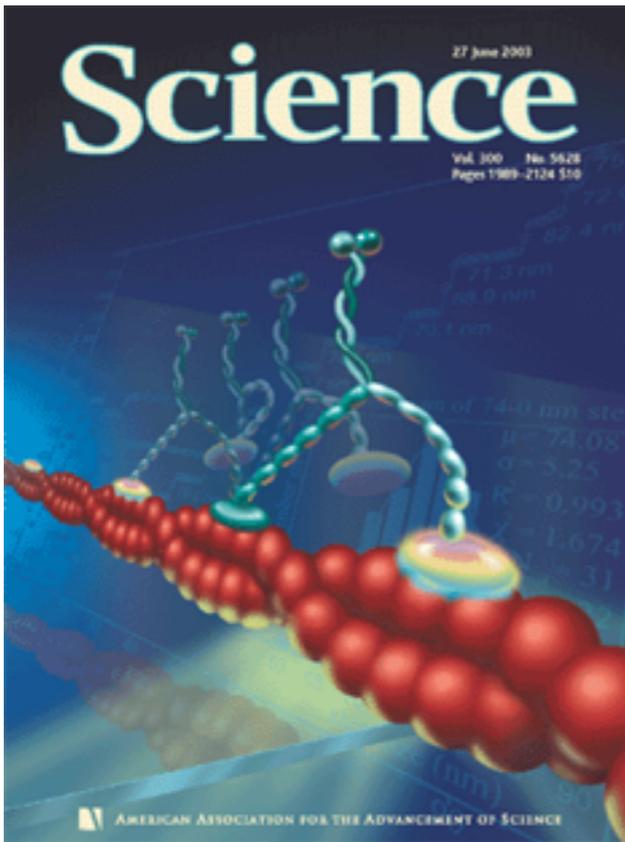


Figure 16.2a Physical Biology of the Cell, 2ed. (© Garland Science 2013)

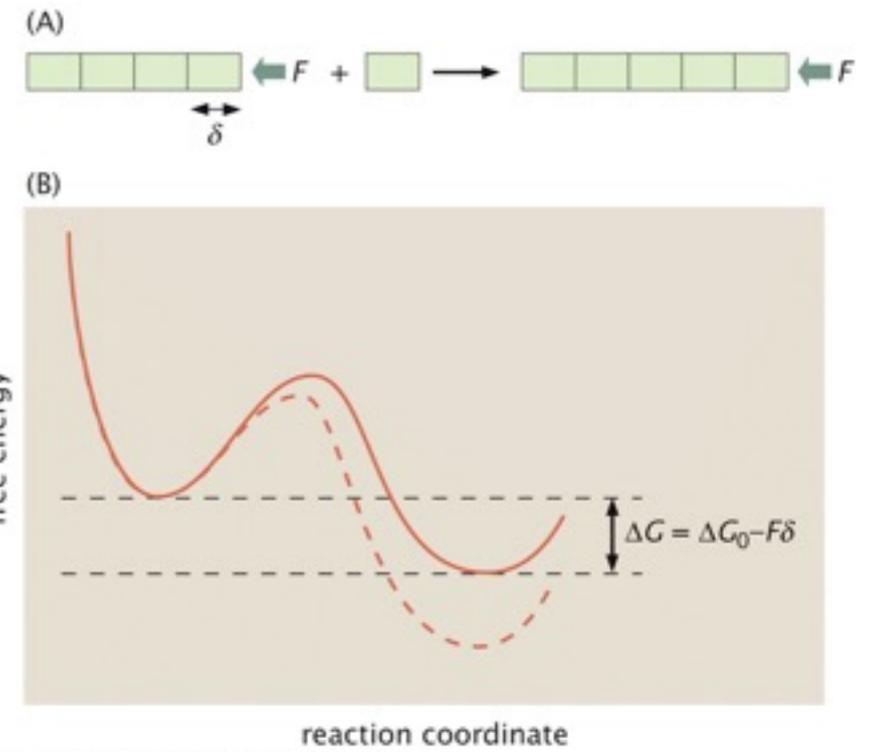


Figure 16.44 Physical Biology of the Cell, 2ed. (© Garland Science 2013)

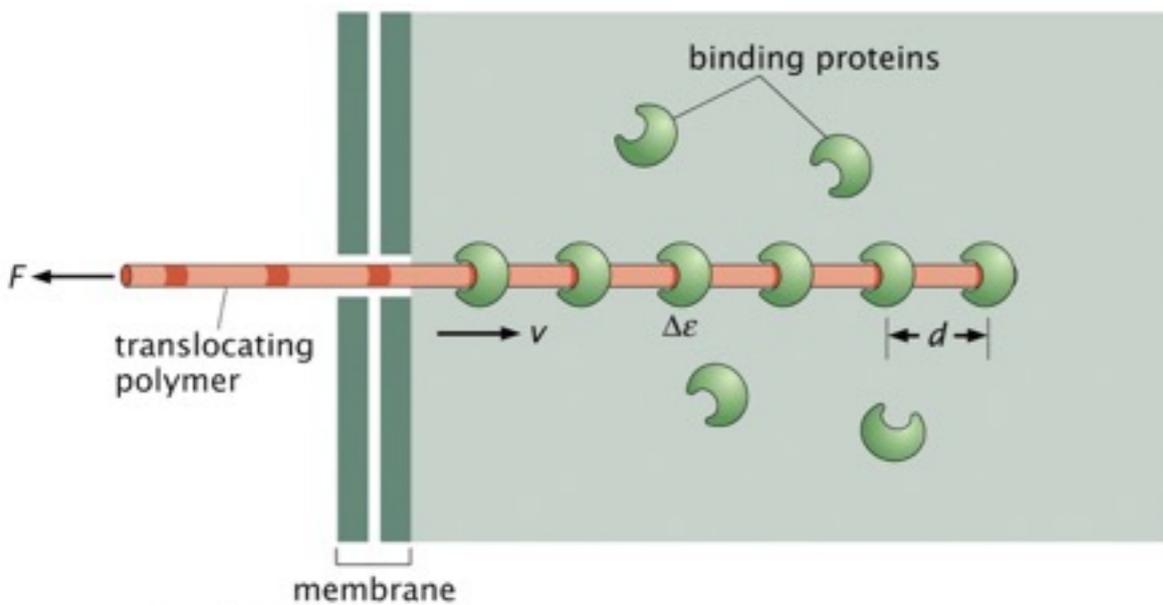
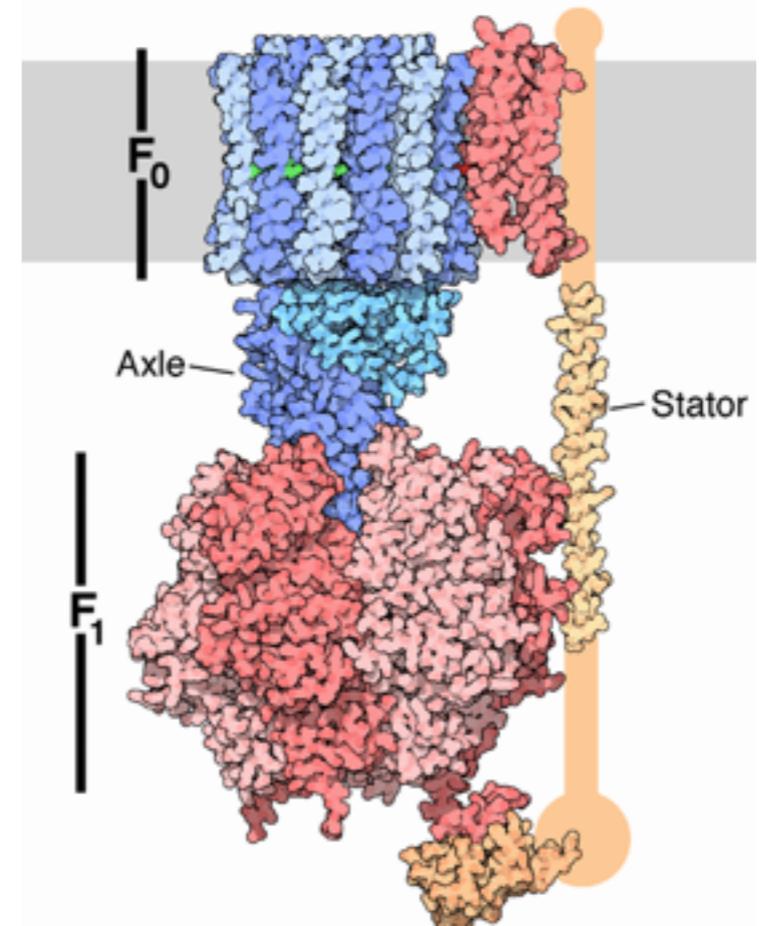


Figure 16.52 Physical Biology of the Cell, 2ed. (© Garland Science 2013)



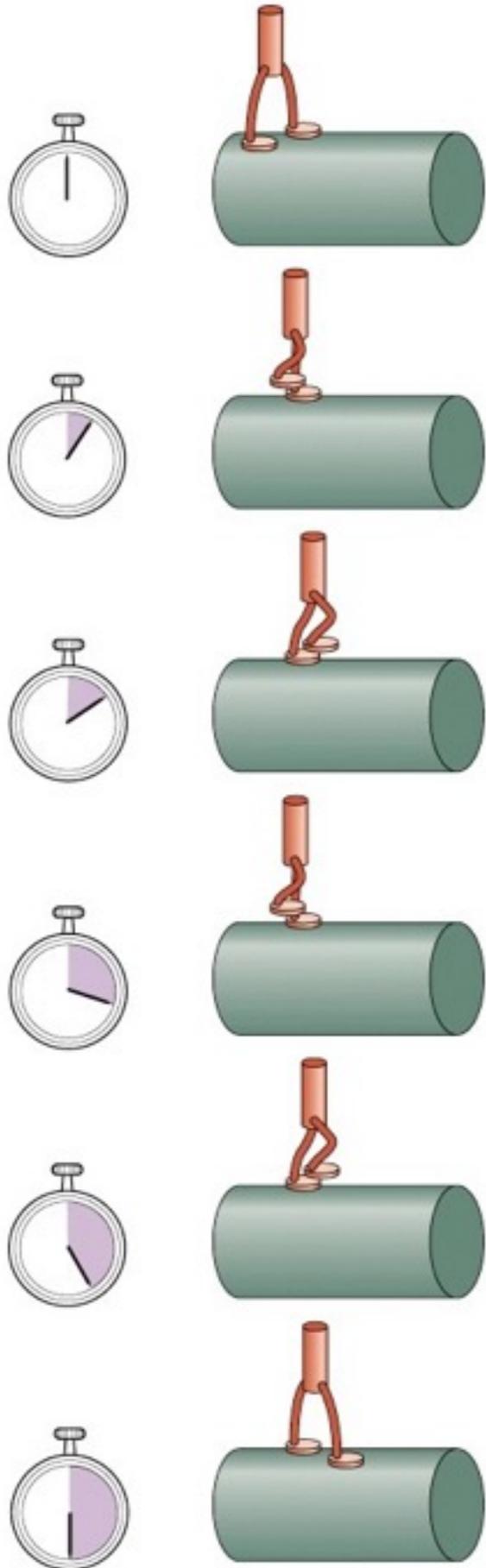
Molecular **motors**

molecular motors move in fits and starts, in contrast to **macroscopic** ones that appear to move continuously forward

ultimately, they are **stochastic**, due (as usual) to the large effect of thermal forces at molecular scales

biased random walkers, they use energy to **rectify** brownian motion (*driven diffusion*)

“two steps forward, one step back”



Four broad classes

Translational (ex. *myosin*)

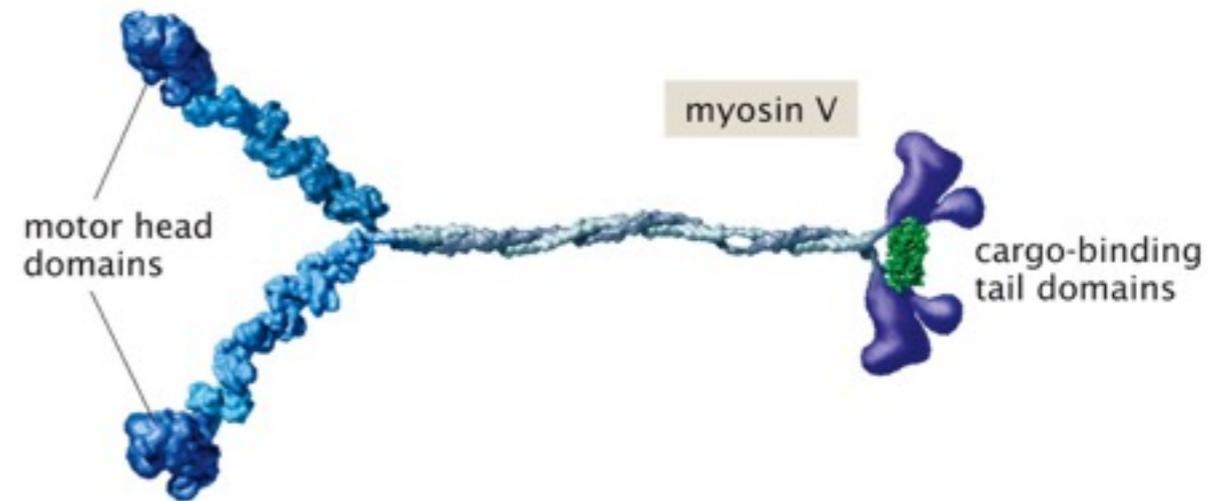
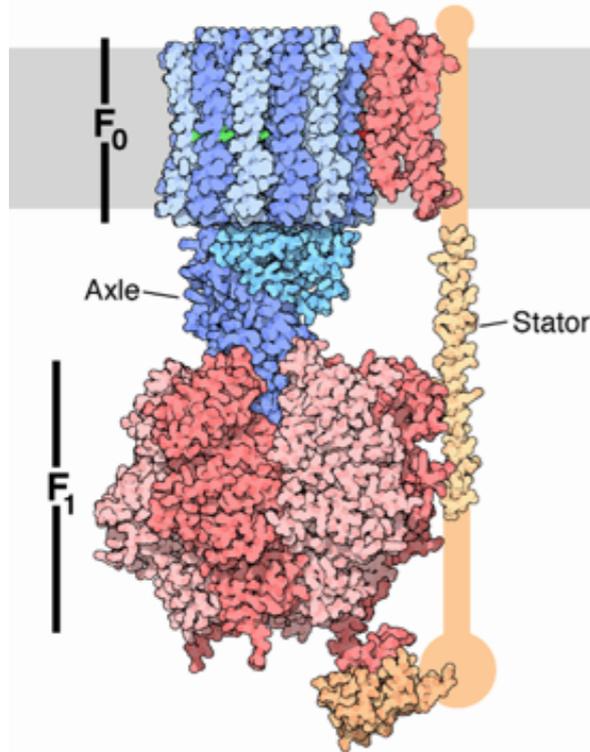


Figure 16.2a Physical Biology of the Cell, 2ed. (© Garland Science 2013)

Rotary (ex. *ATP synthase*)

Polymerization (ex. *actin*)
“pushing by growing”

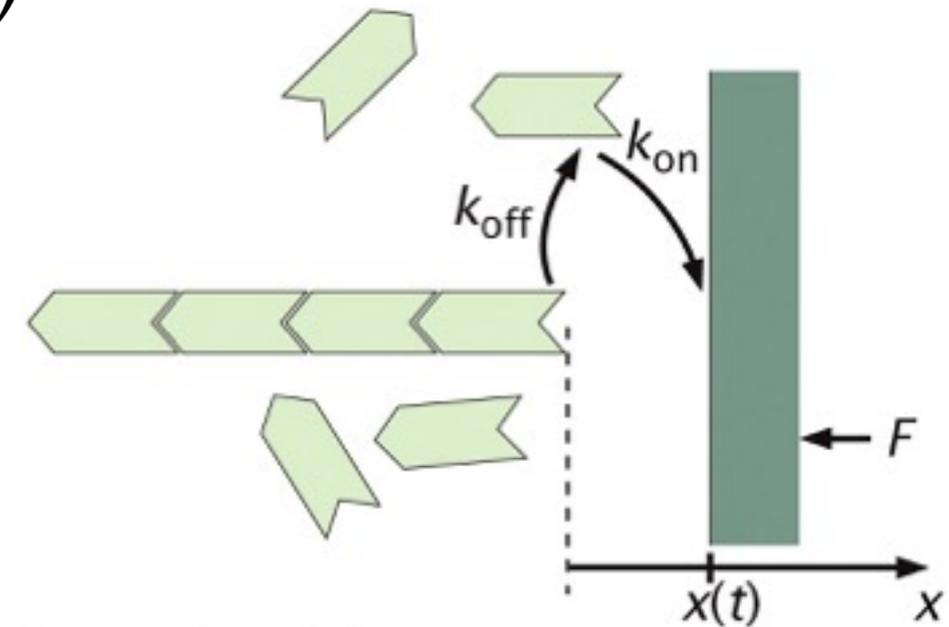
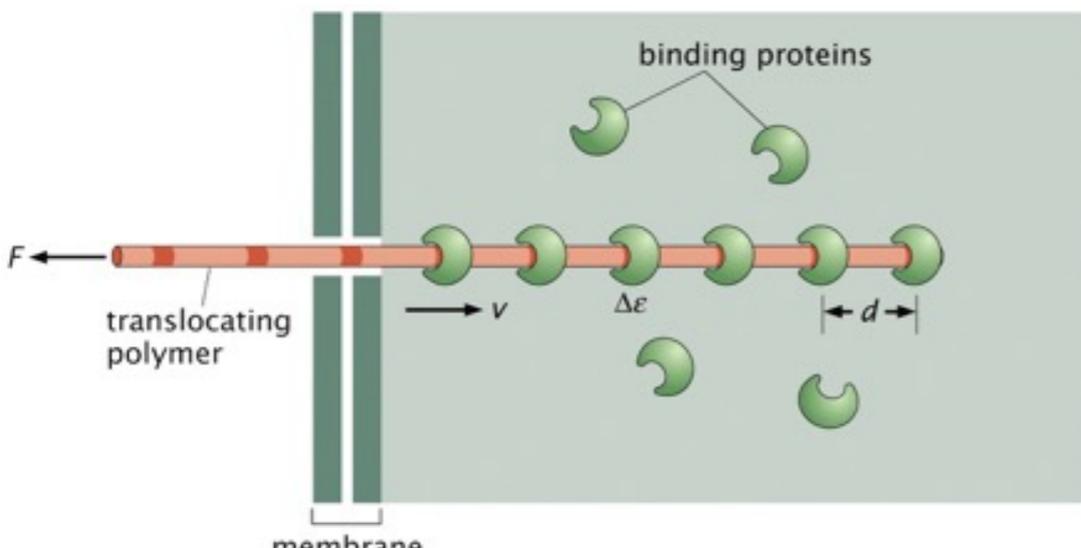
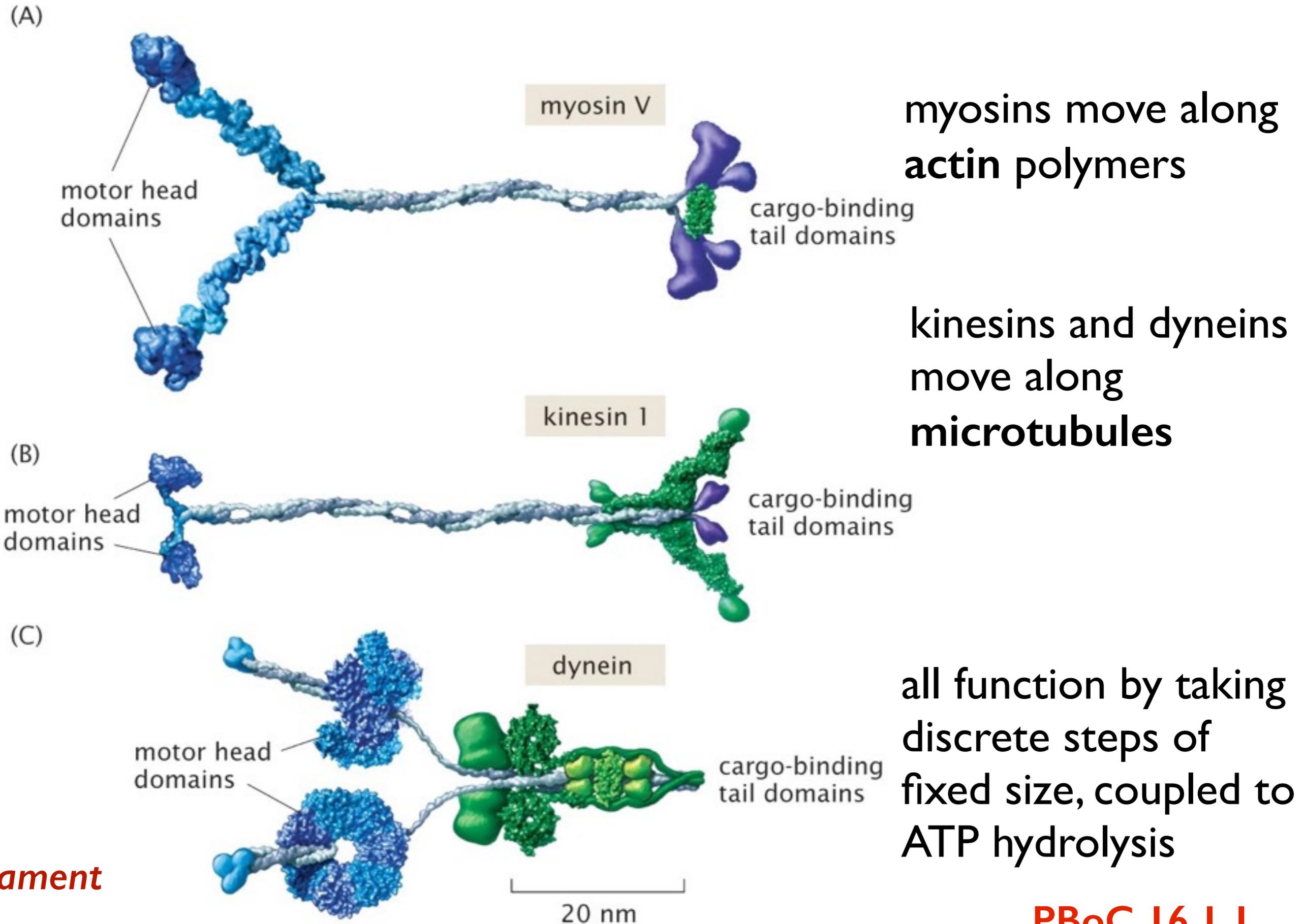


Figure 16.45 Physical Biology of the Cell, 2ed. (© Garland Science 2013)

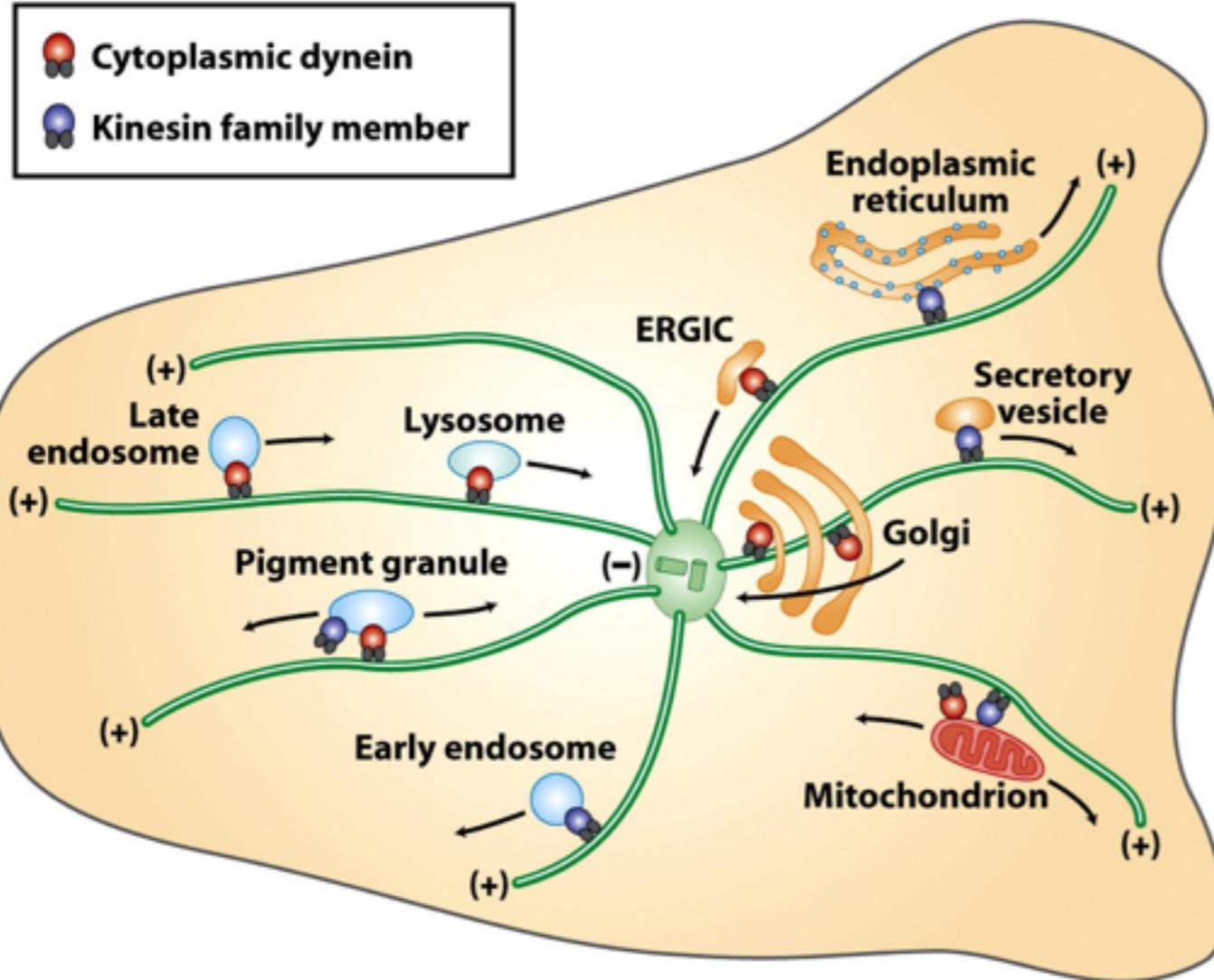


Translocation (ex. *BiP*)
“pushing by pulling”

Translational motors



Translational motors: dynein, kinesin



transport large cargos, e.g., vesicles, organelles along microtubules, also involved in cell division

kinesins are structurally similar to myosins, dyneins not

most kinesins walk toward plus end, i.e., from cell center to periphery

dyneins walk toward the minus end, i.e., toward the cell's center

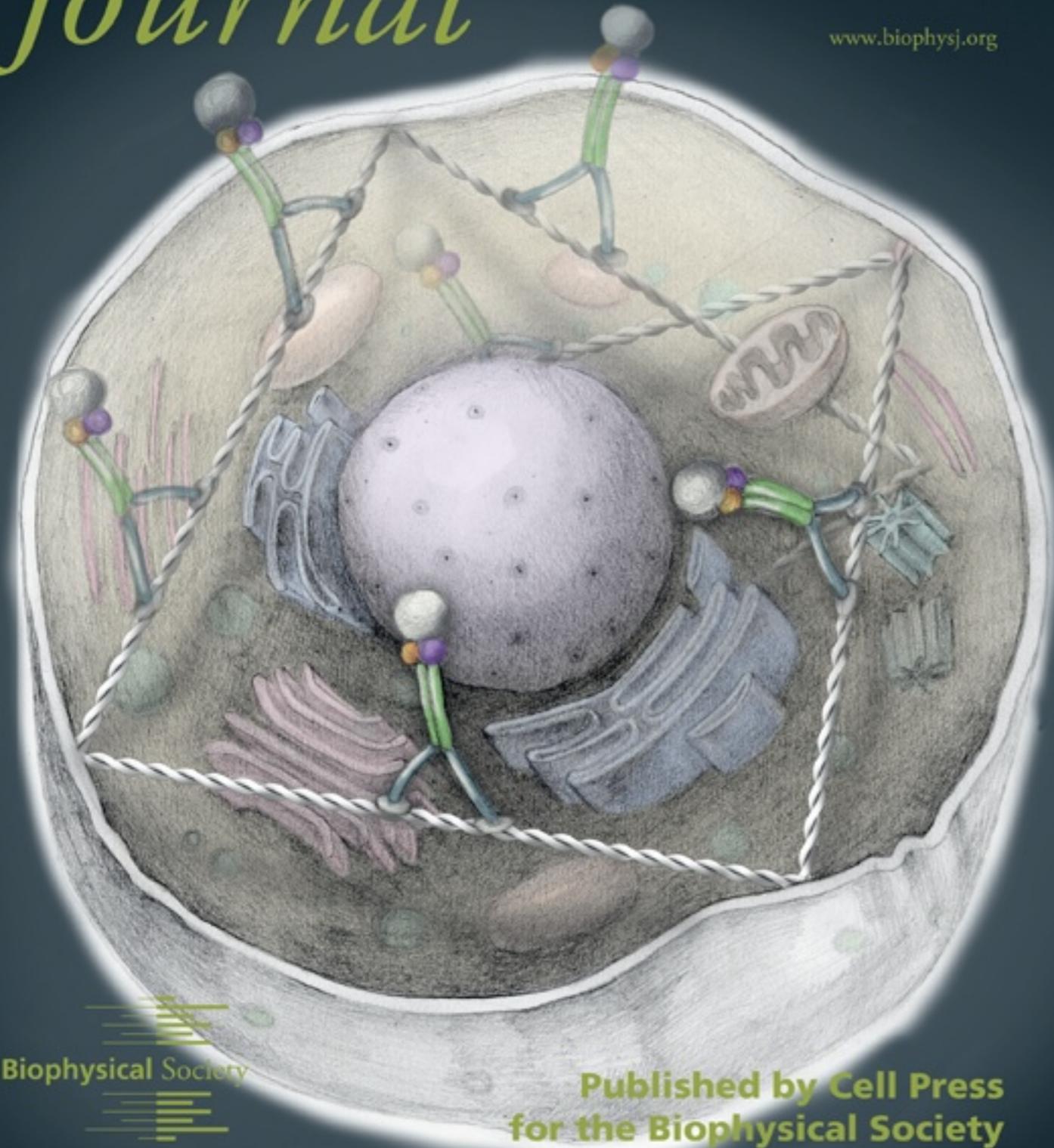
Biophysical Journal

Volume 100

Number 12

June 22, 2011

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for the Biophysical Society

*translational motor proteins
moving along tracks in the
cell*

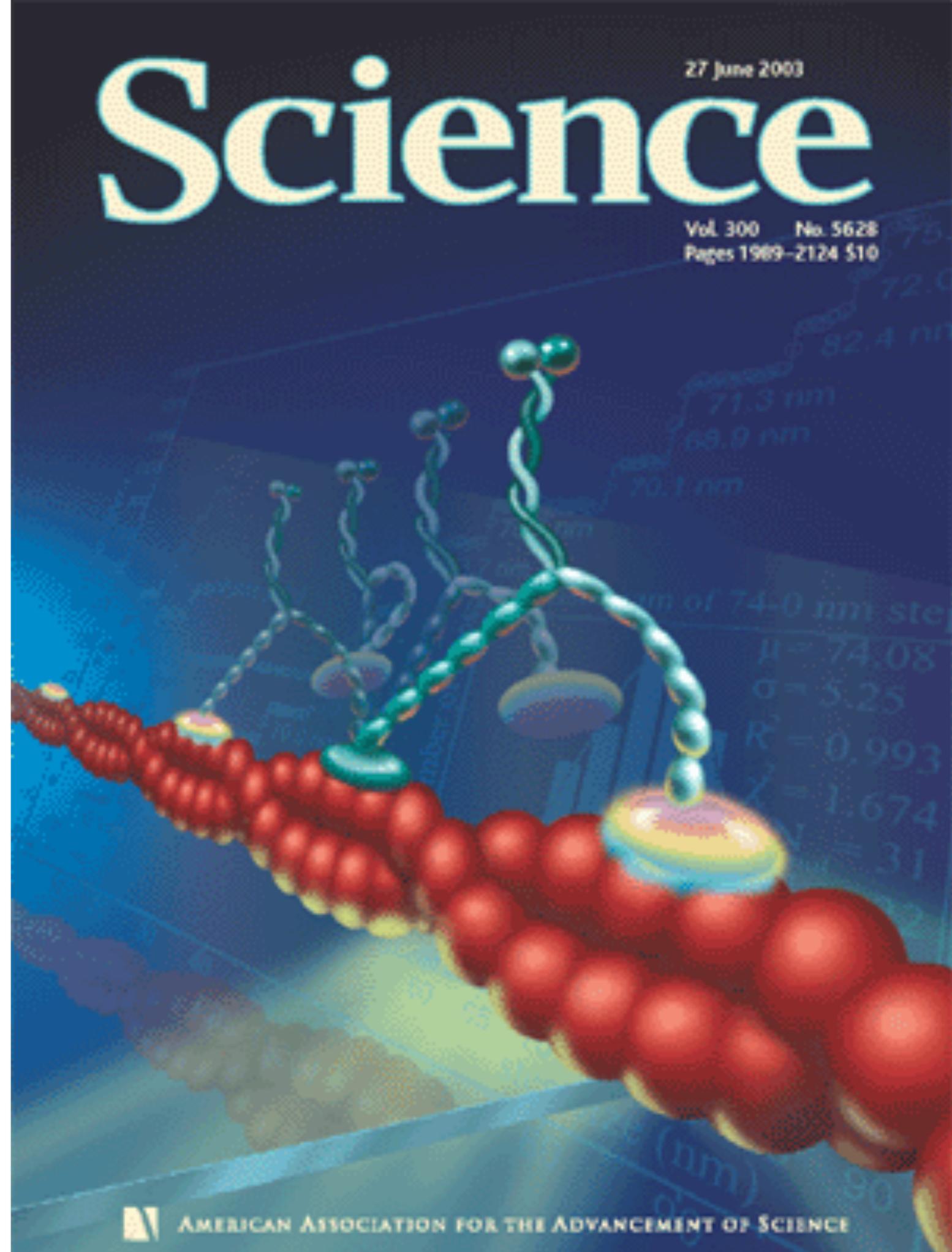
- **Extension of a three-helix bundle domain of myosin VI and key role of calmodulins.** Yanxin Liu, Jen Hsin, HyeongJun Kim, Paul R Selvin, and Klaus Schulten. *Biophysical Journal*, 100:2964-2973, 2011.

further evidence that motor proteins = attractive covers

Myosin V Walks Hand-Over-Hand: Single Fluorophore Imaging with 1.5-nm Localization

Ahmet Yildiz, Joseph N. Forkey, Sean A. McKinney, Taekjip Ha, Yale E. Goldman, and Paul R. Selvin

Science 27 June 2003: 2061-2065.

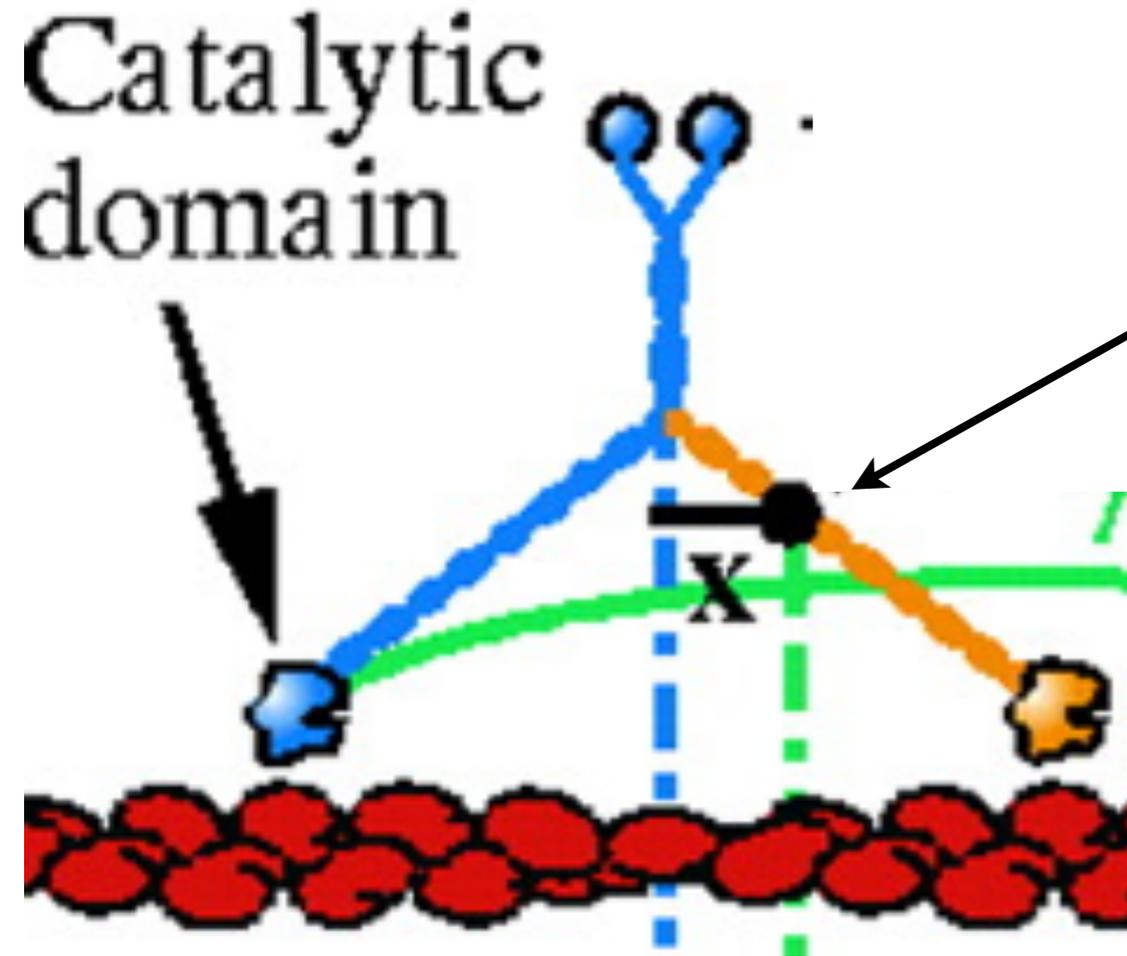


how myosin moves

black dot is fluorophore label

two models for how myosin moves along actin, **hand-over-hand** or **inchworm**

let's predict what they see...

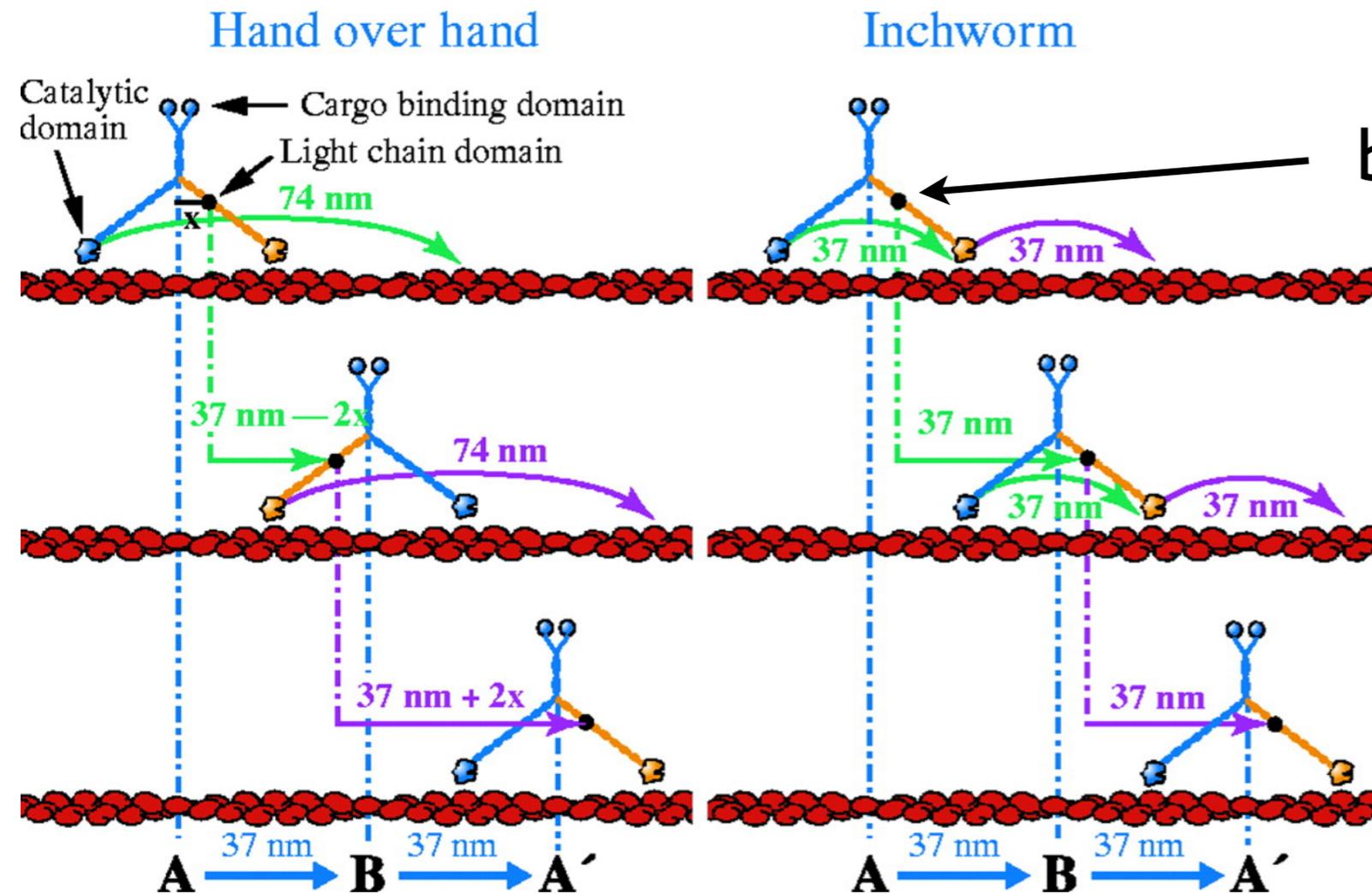


how myosin moves

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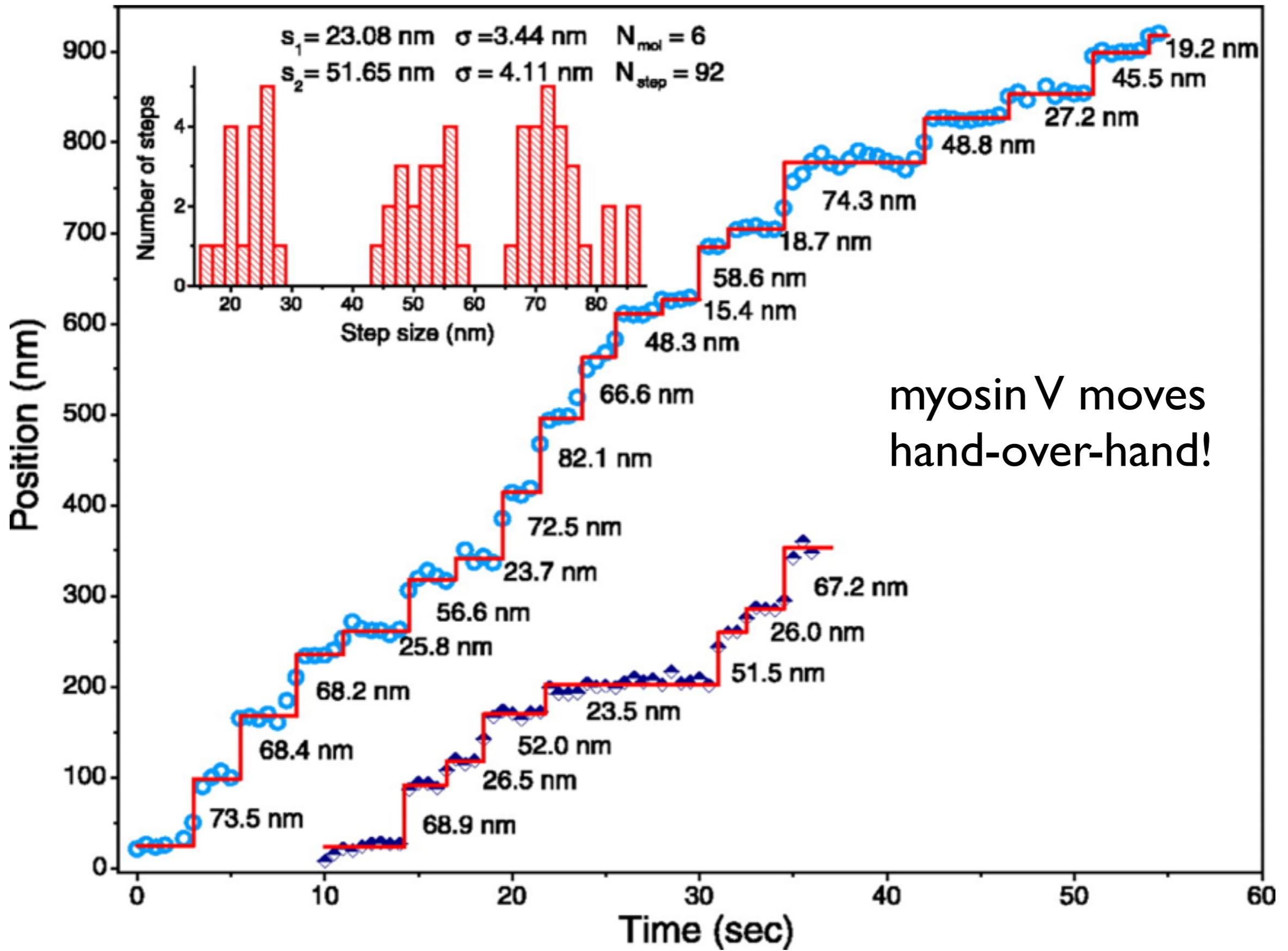


hand-over-hand predicts pairs of jumps that sum to 74 nm

inchworm model predicts separate jumps of 37 nm only

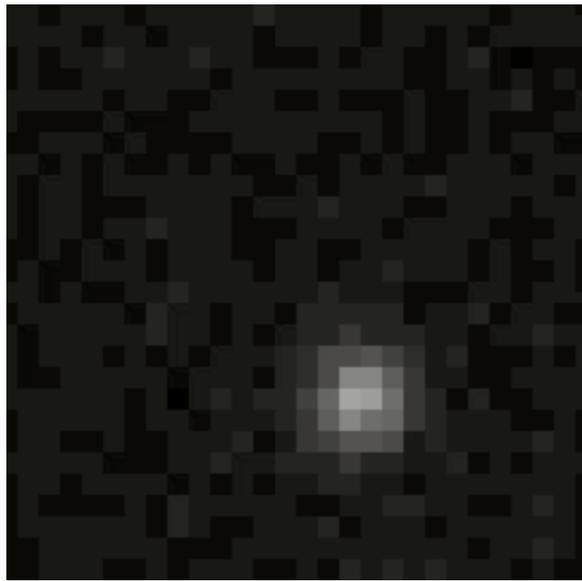
What do the experiments show?

how myosin moves



analyzing the experiments

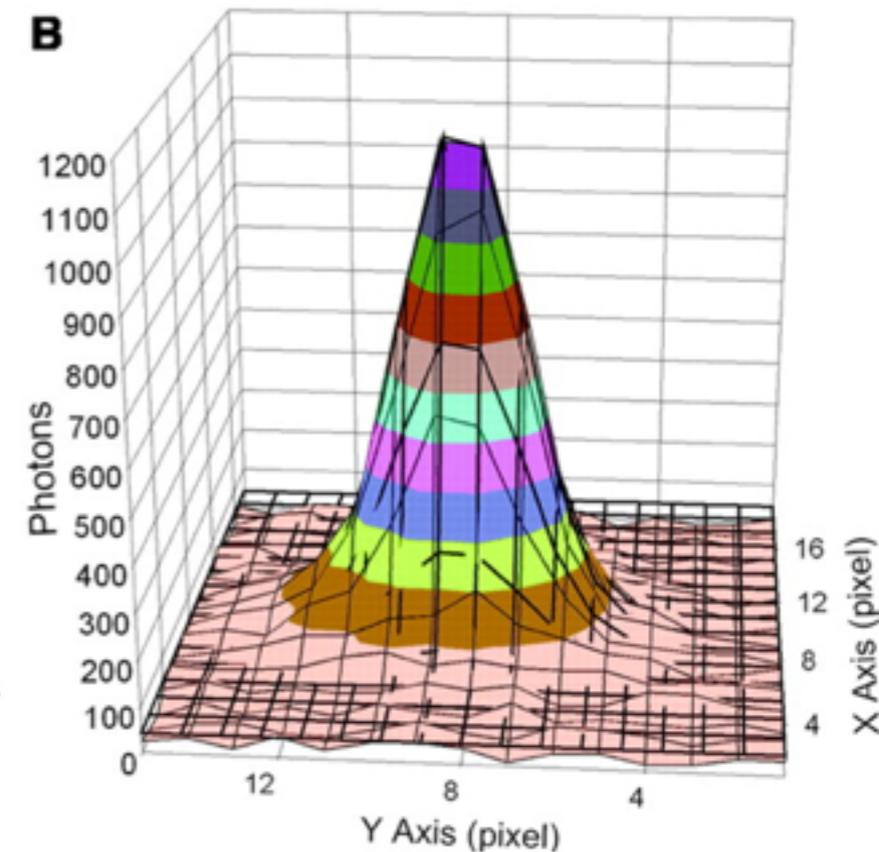
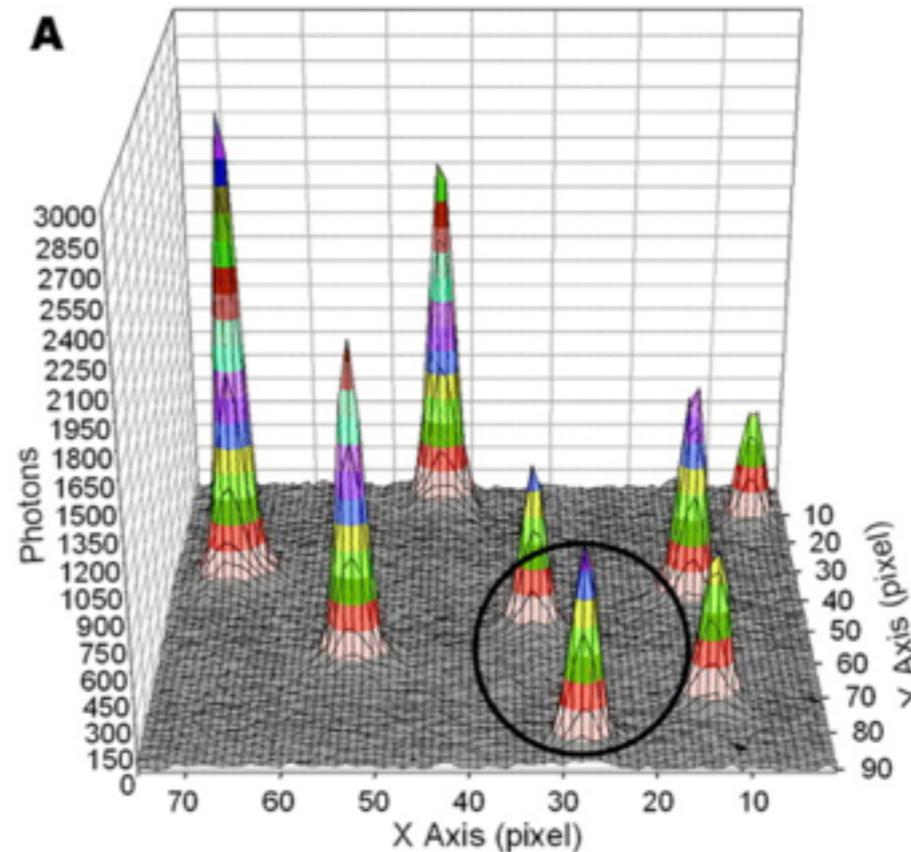
the actual data from the myosin V experiments



FIONA - Fluorescent Imaging with One-Nanometer Accuracy

fit image with a gaussian
(point-spread function)

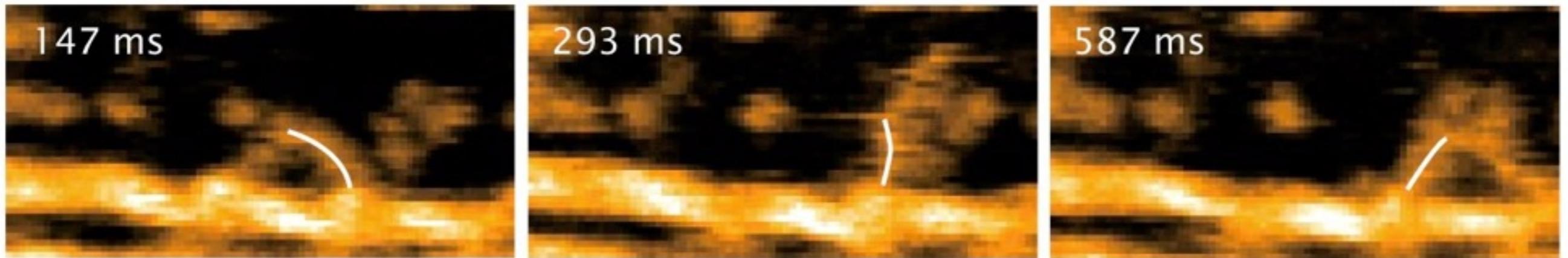
with enough photons,
accuracy is **unlimited**
(assuming the
distribution is correct)



*even for “real” experiments, everything is
rooted in modeling!!!*

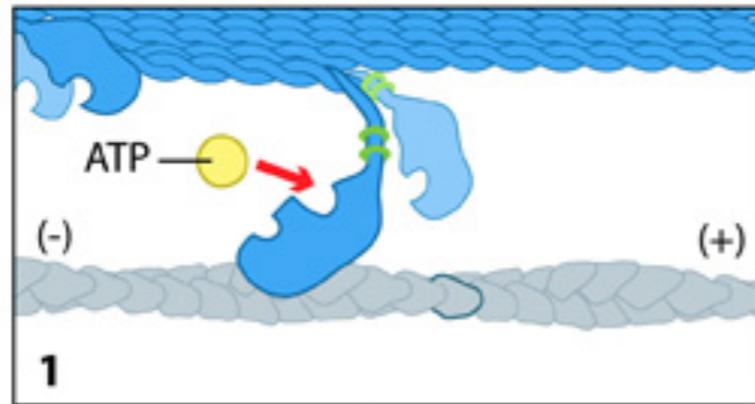
analyzing the experiments

High-speed AFM experiments - do you see the myosin?

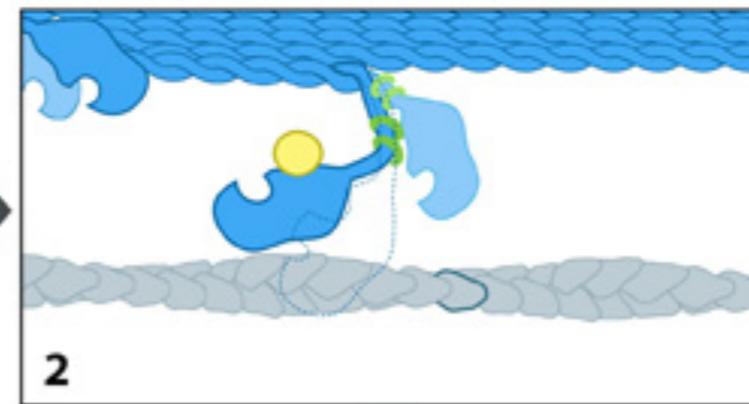


myosin motion involves distinct states

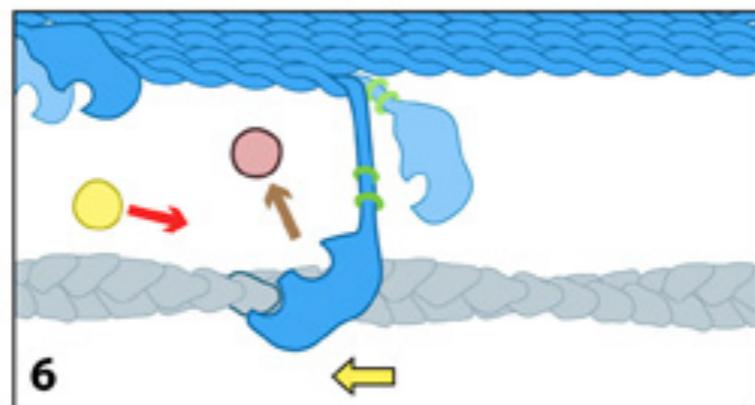
head is in rigor state (no ATP or products), bound to actin



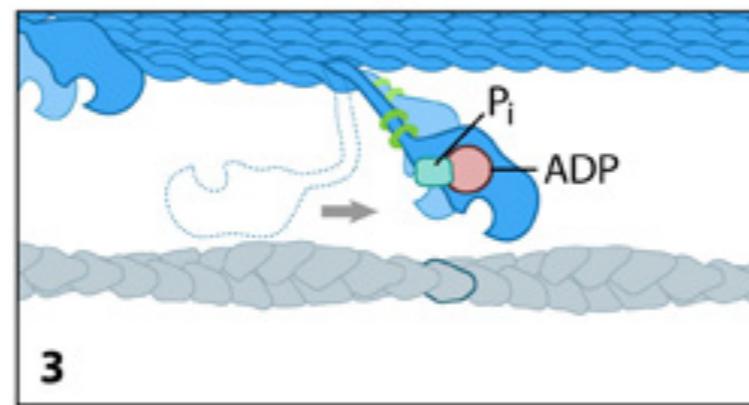
ATP binds, head releases and bends forward



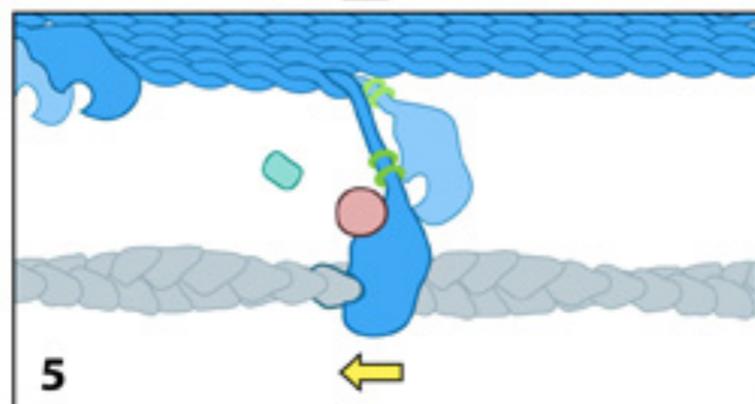
ADP is released



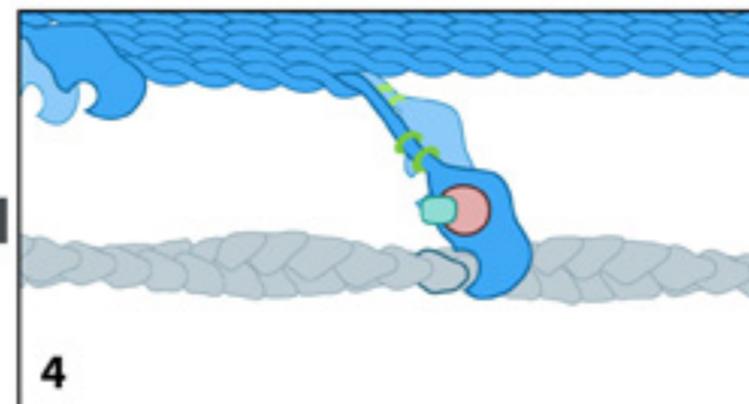
ATP is hydrolyzed



release of phosphate triggers "power stroke", head moves to original position

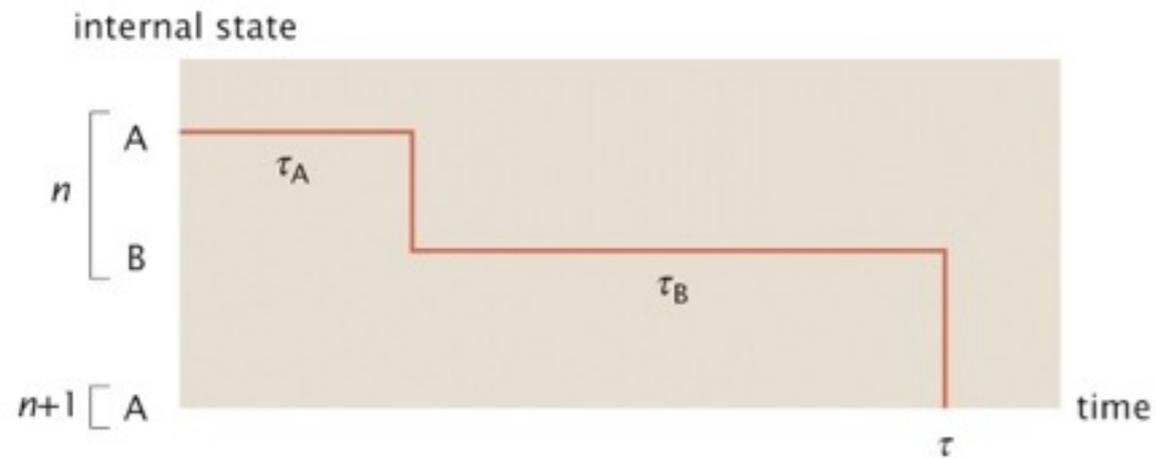


head contacts actin again



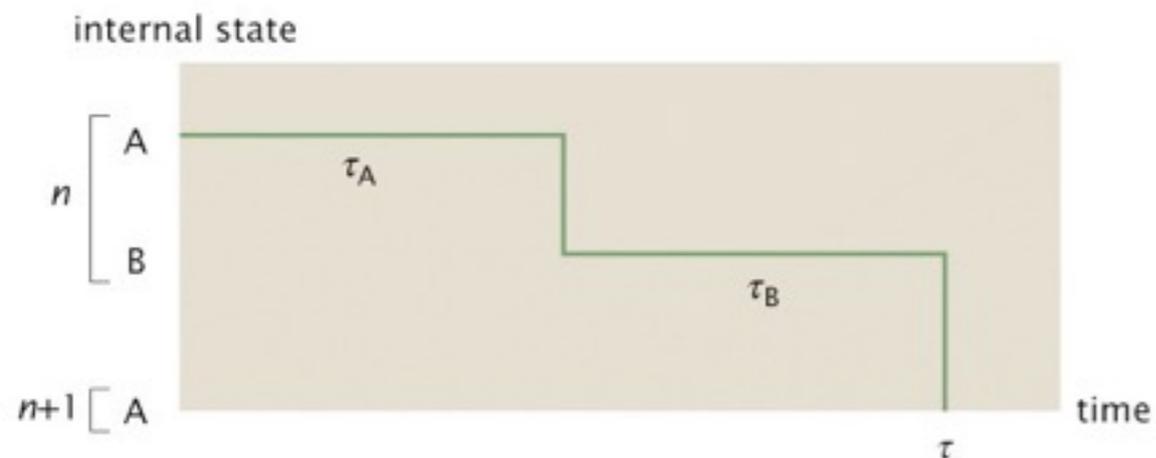
How many distinct states?

TRAJECTORY 1



each step is itself an independent stochastic process that takes an average time τ to occur, e.g., ATP binding, ADP unbinding, etc.

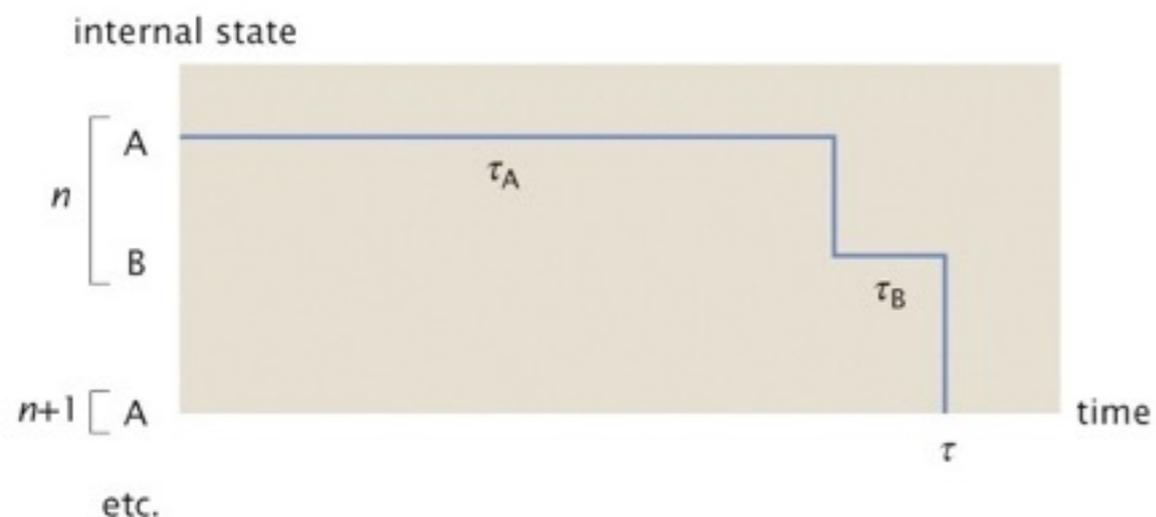
TRAJECTORY 2



For a single rate-limiting step:

$$p(t) = \frac{1}{\langle t \rangle} e^{-t/\langle t \rangle}$$

TRAJECTORY 3



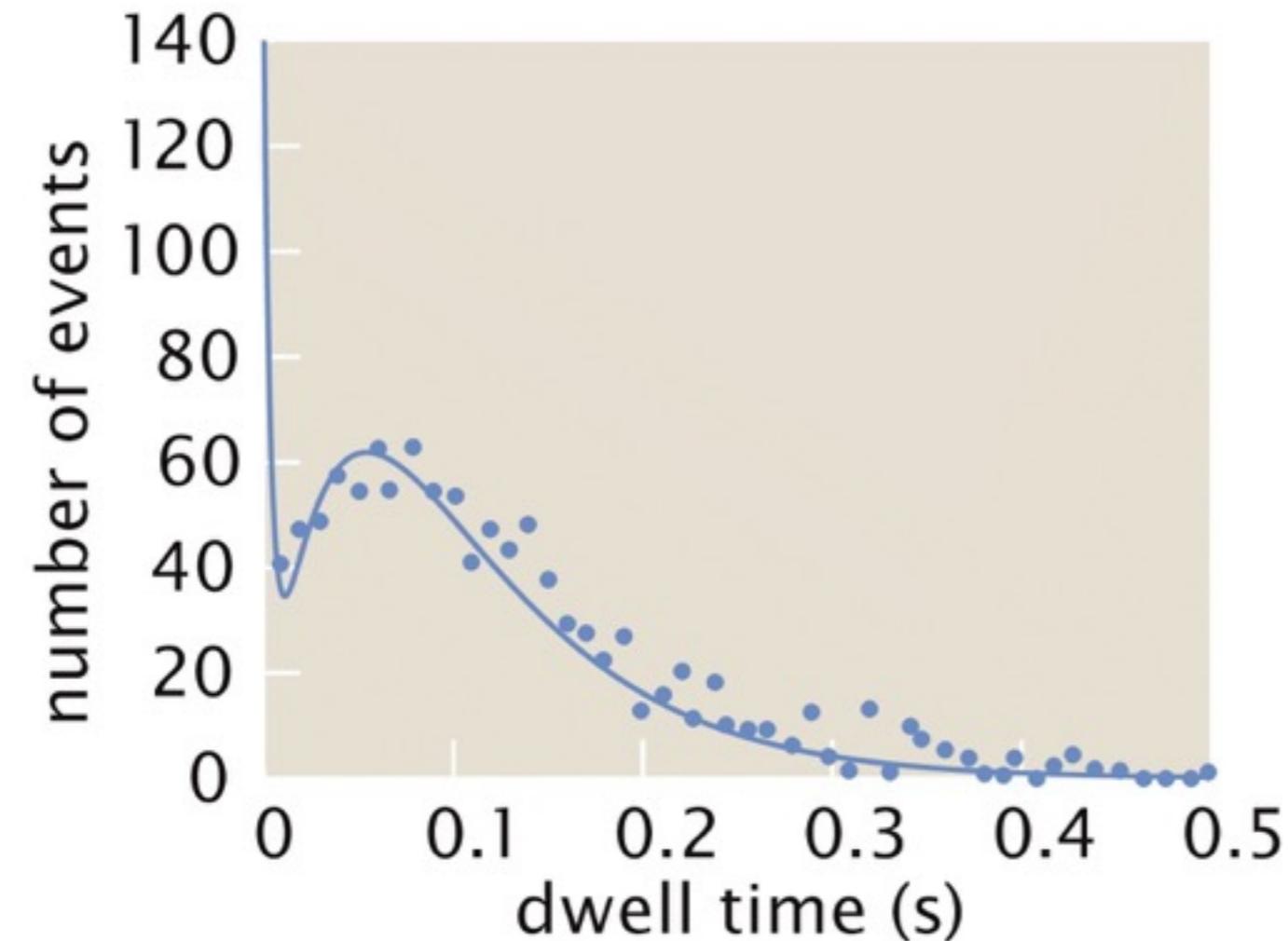
For two steps, $p(t)$ is the **convolution** of two independent probabilities

$$p(t) = \int_0^t p_A(\tau) p_B(t - \tau) d\tau$$

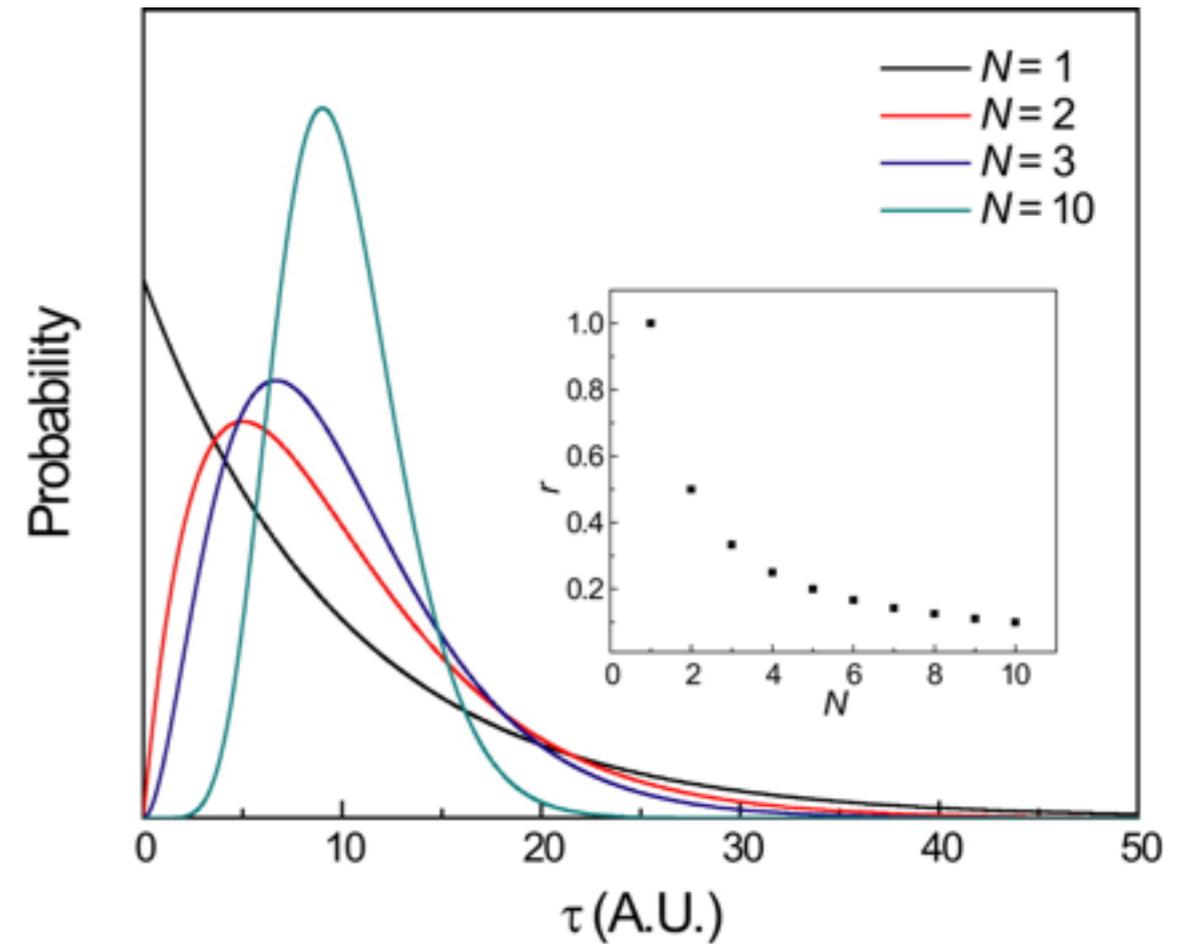
How many distinct states?

$$p(t) = \frac{1}{\tau_B - \tau_A} \left(e^{-t/\tau_B} - e^{-t/\tau_A} \right)$$

Shape of curve and resulting fit can reveal the number of intermediate states, even if hidden from direct observation



dwell time distribution for single-headed myosin V with two-state model fit

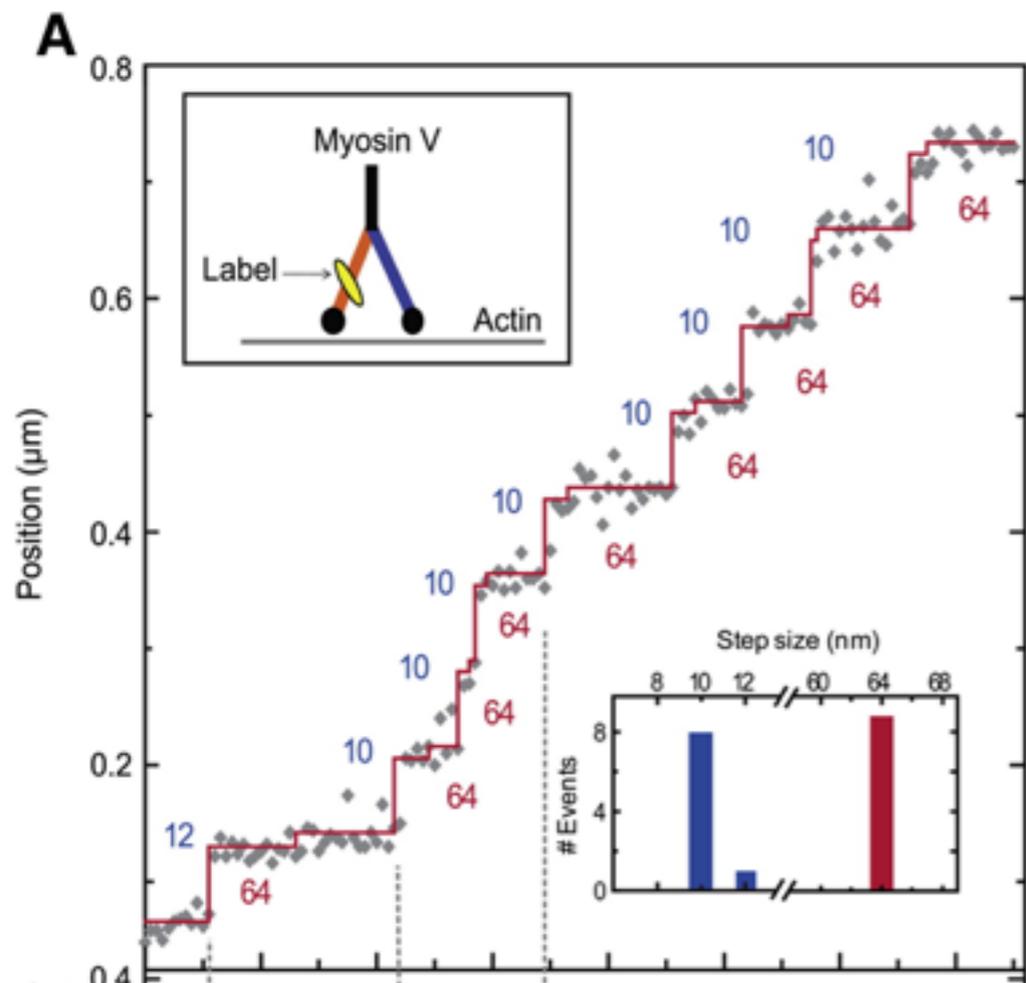
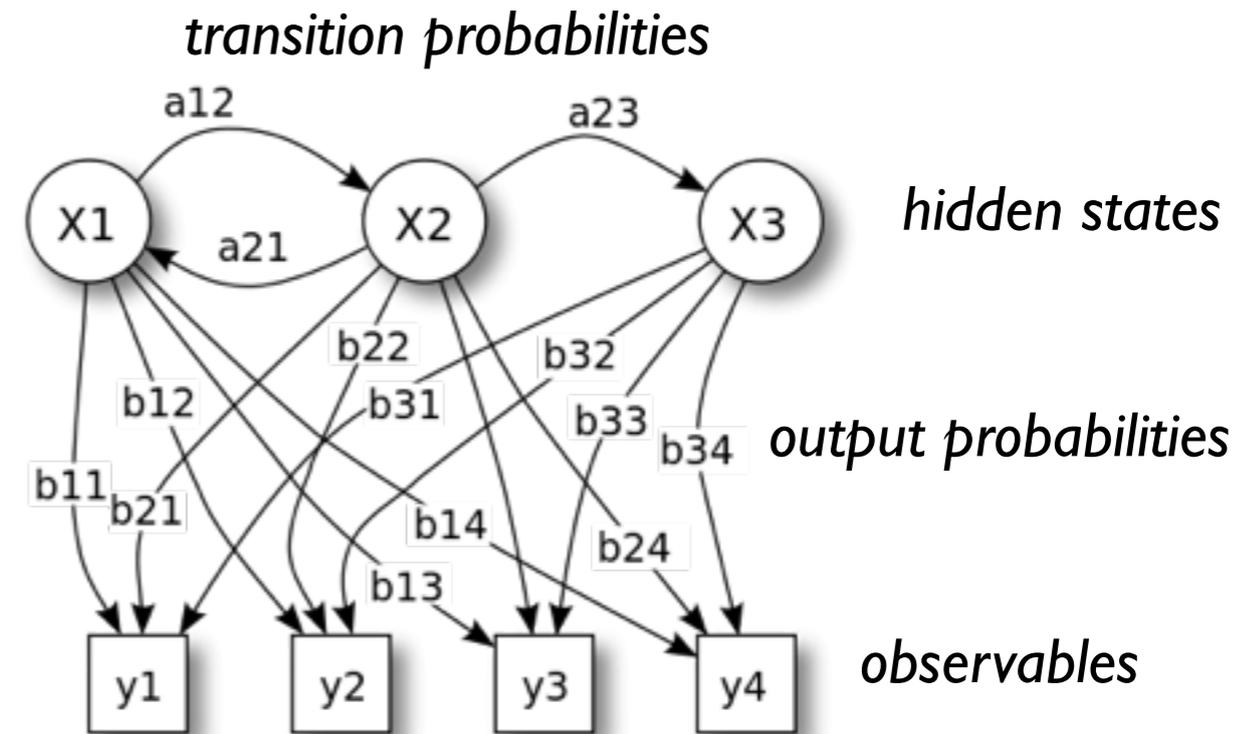


DL Floyd, SC. Harrison, AM van Oijen. Analysis of Kinetic Intermediates in Single-Particle Dwell-Time Distributions. (2010) *Biophys. J.* **99**:360-366.

hidden Markov models (HMM)

An HMM is a sequence of **hidden states** and corresponding probabilities underlying a connected sequence of observations

Goal is to solve for the most likely hidden states that explain the observed sequence

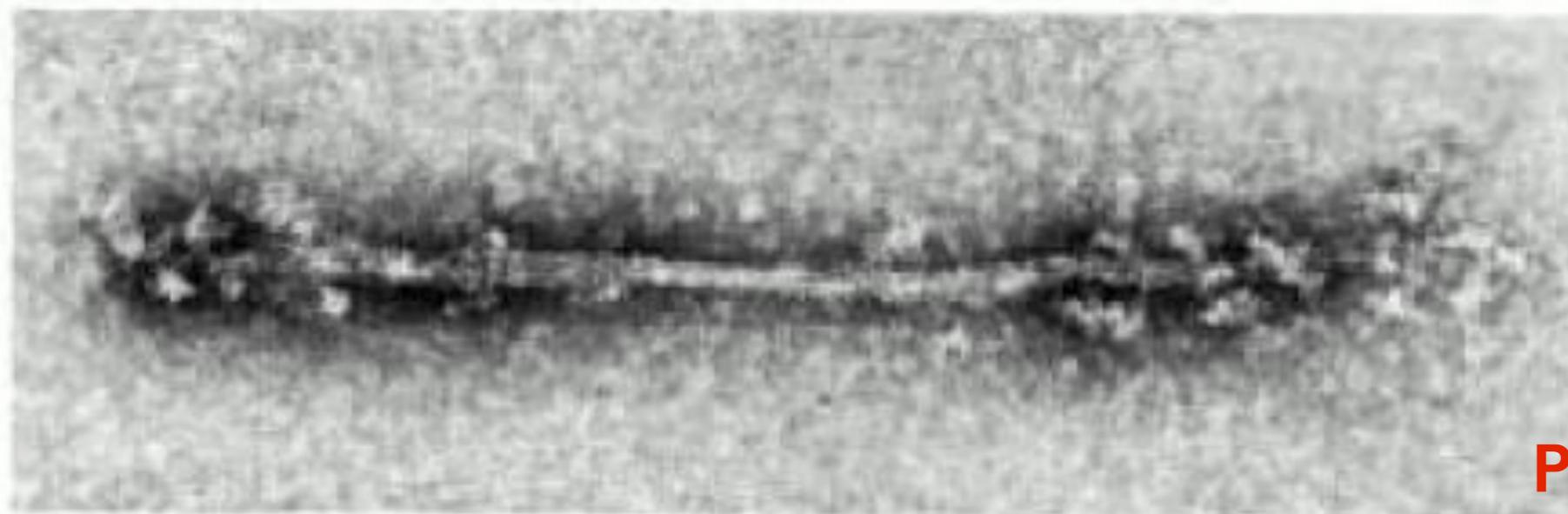
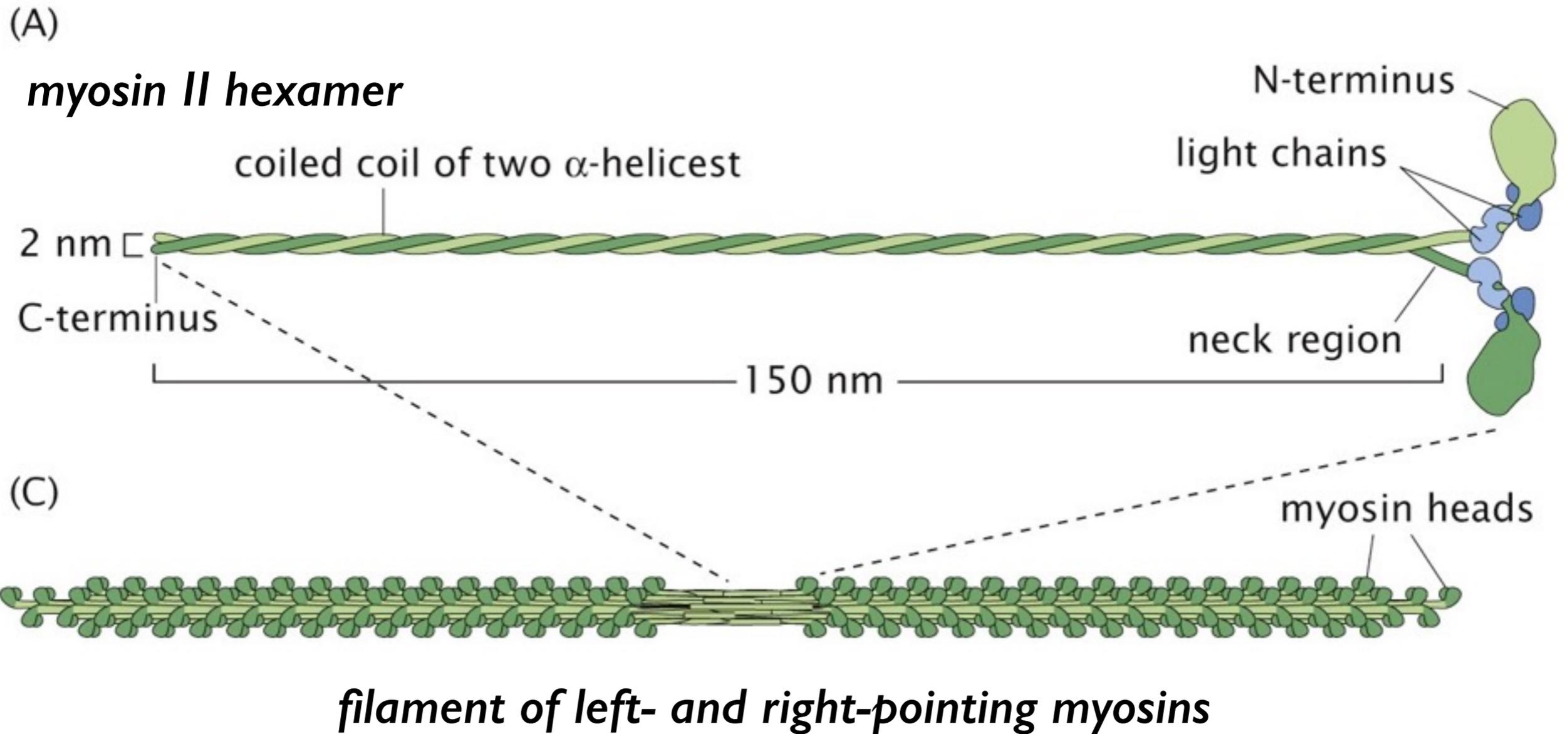


Ex: Myosin V stepping, don't know dwell times, have only trace of position vs. time

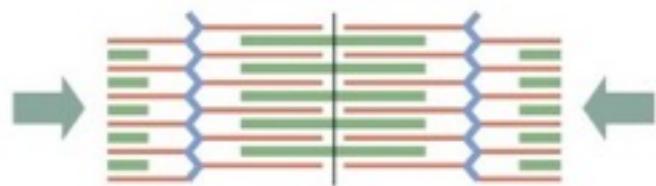
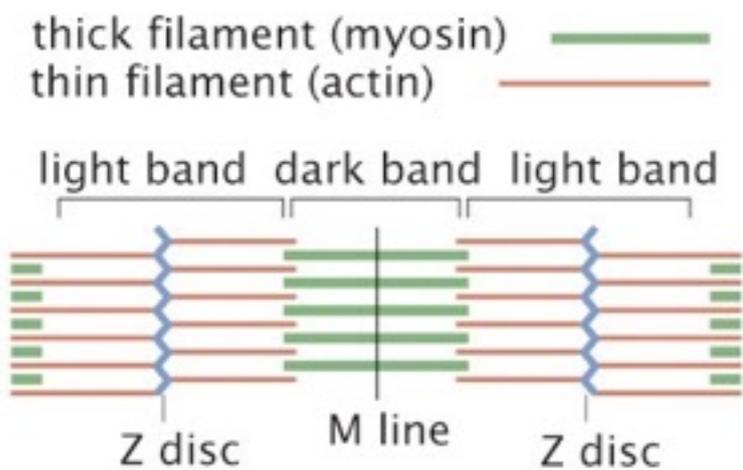
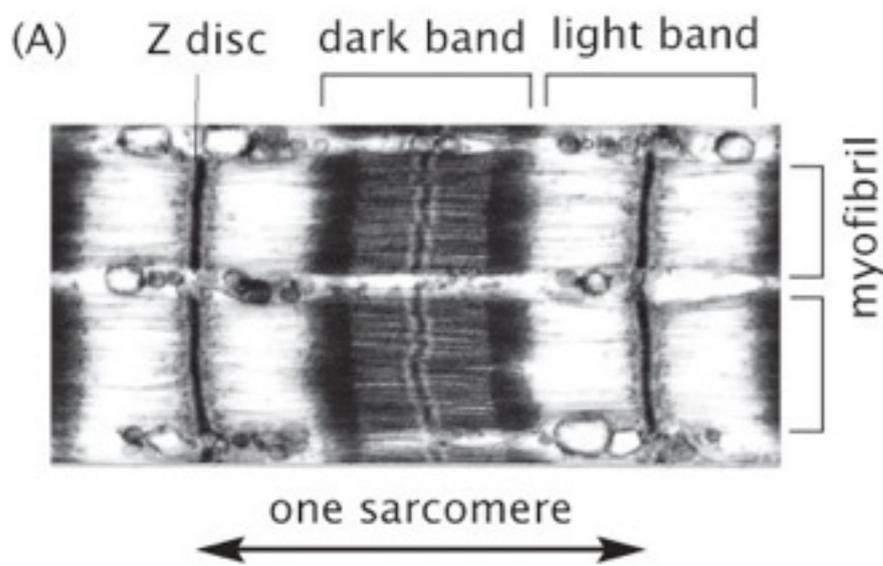
build a model parameterized by (1) n kinetic states (hidden) and (2) m step sizes

HMM solution reveals two discrete step sizes, allows reconstruction of noise-less trace w/dwell times (**red**)

muscle contraction



muscle contraction



contraction

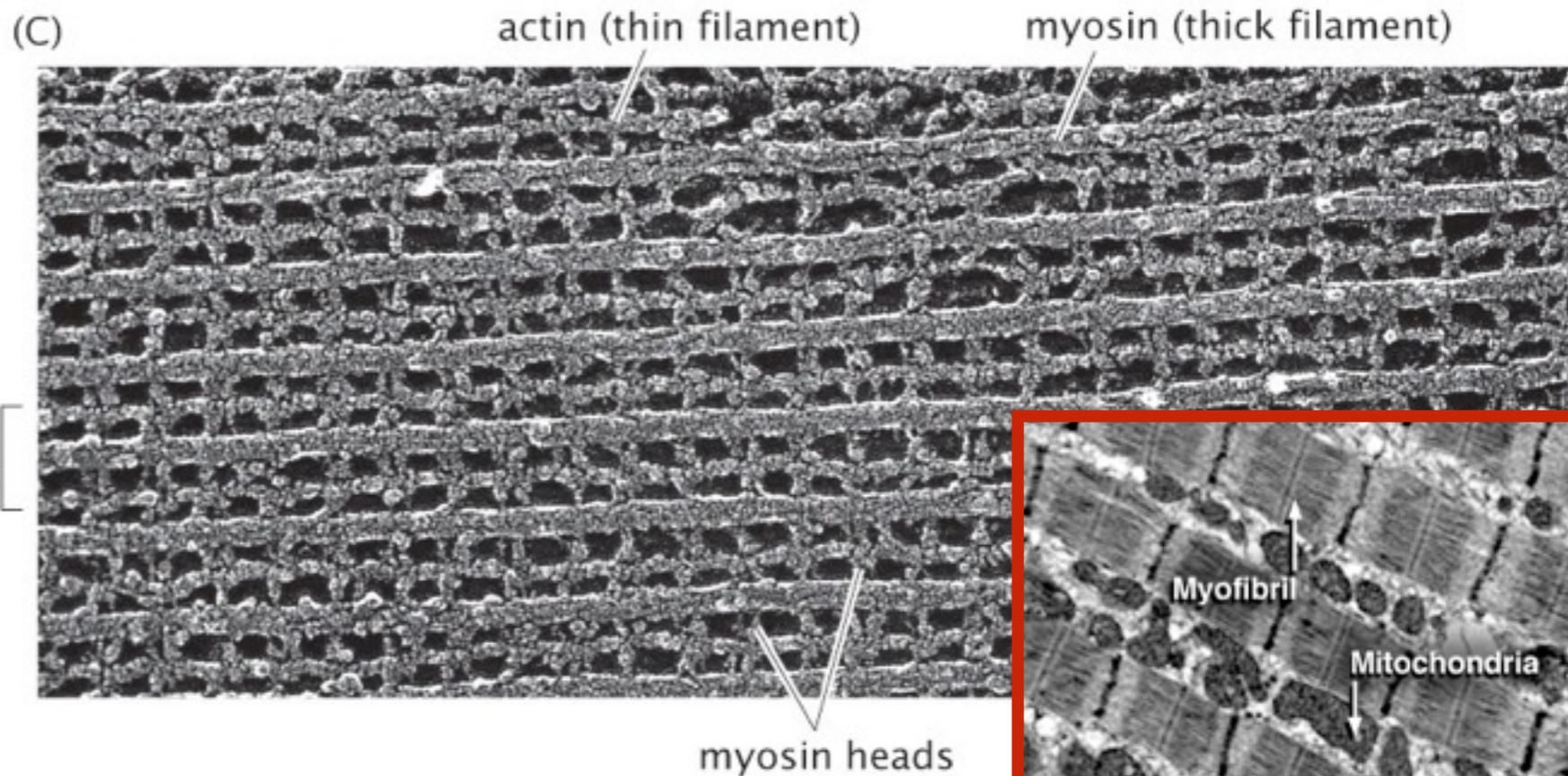
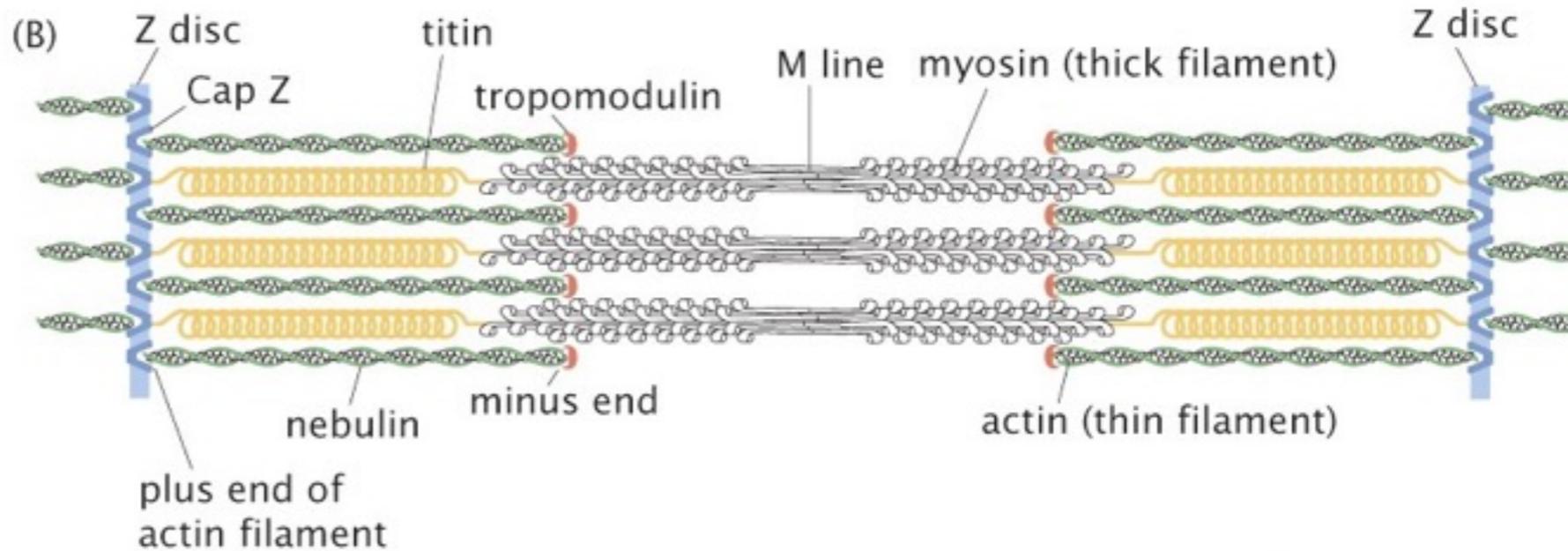
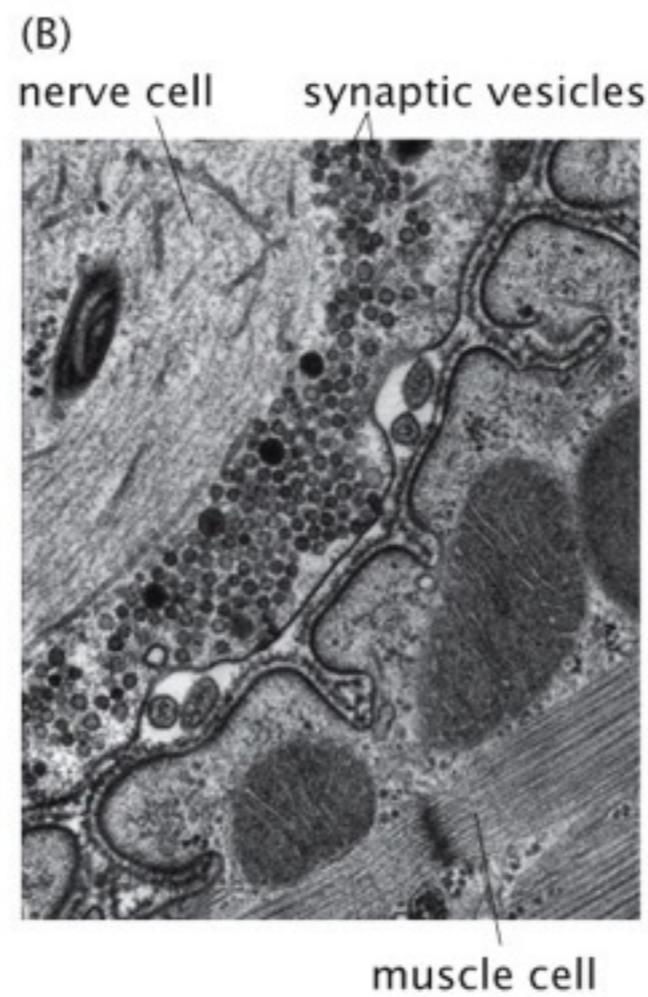
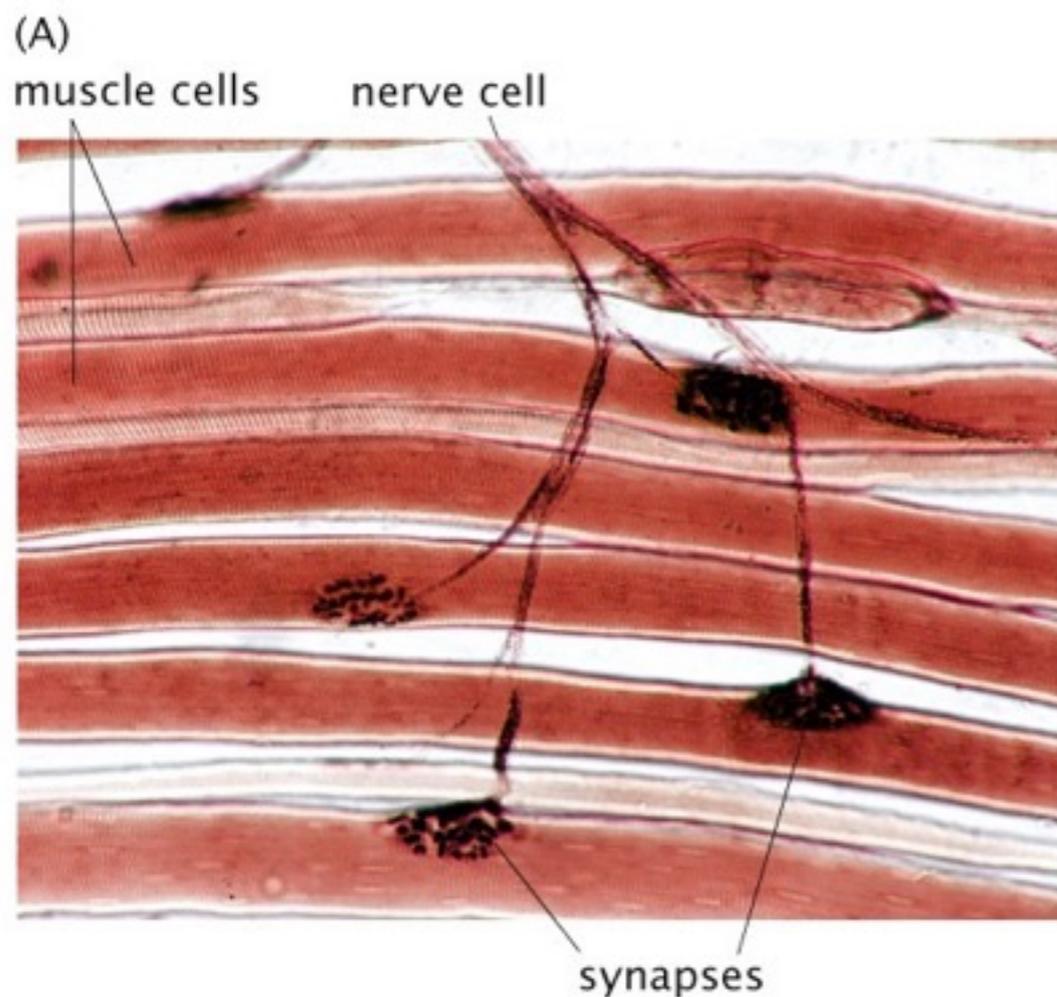


Figure 16.7 Physical Biology of the Cell, 2ed. (© Garland Science 2013)

mediated by three proteins: myosin + actin (**both** acting as filaments) and titin (spring)

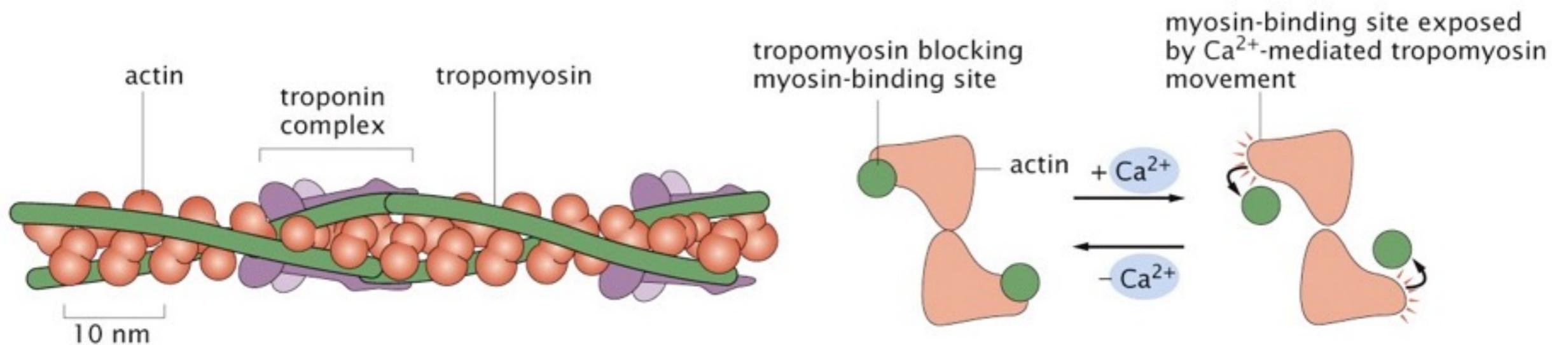
PBoC 16.1.1



coordinating the signal

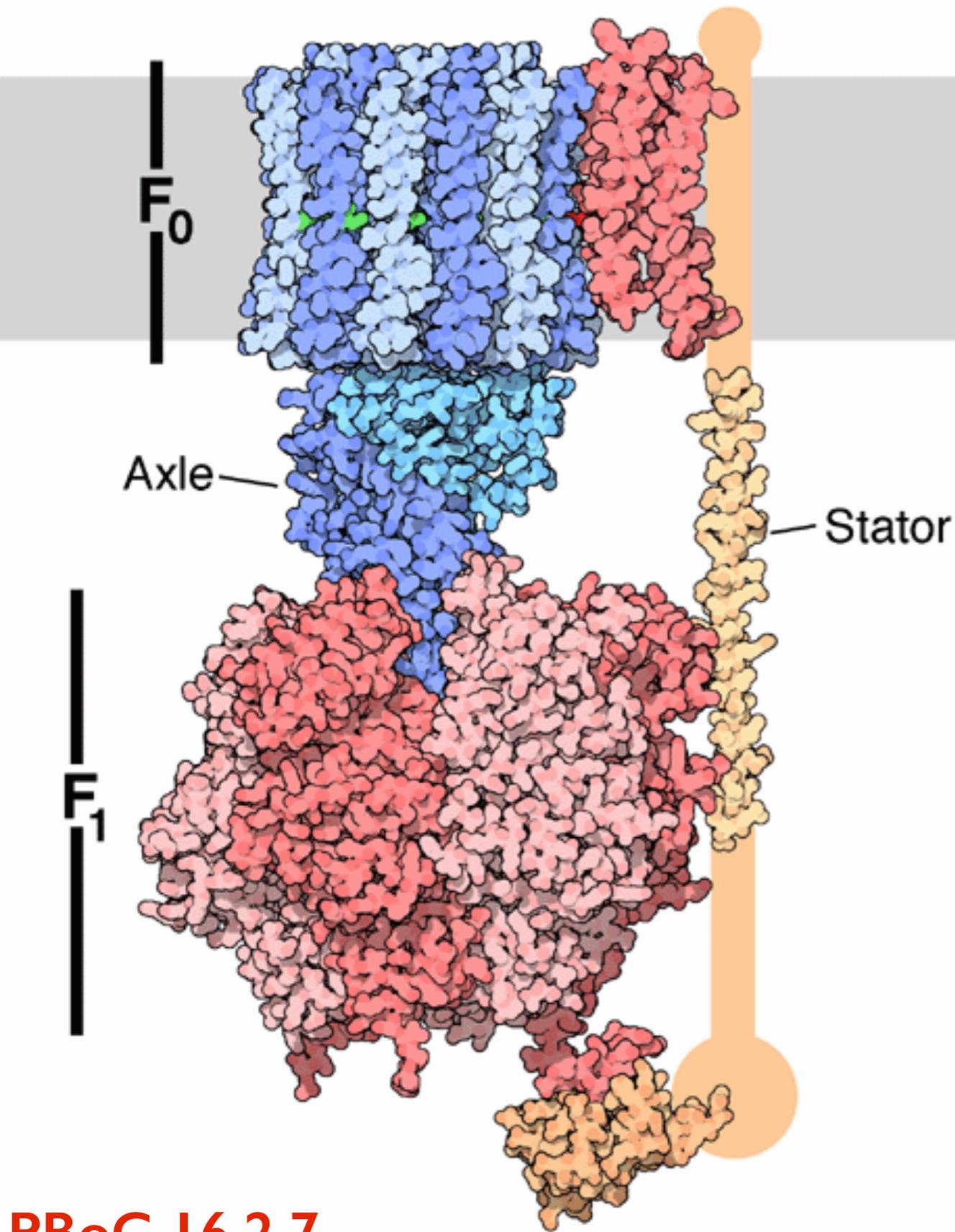
nerve cell releases acetylcholine-containing synaptic vesicles, causes Ca^{2+} channels to open

Ca^{2+} ions (the signal) cause tropomyosin to release from actin, exposing myosin-binding sites simultaneously!



Each myosin moves 11 nm at a rate of $\sim 5/s$ (55 nm/s), action of hundreds simultaneously increases rate to 8,000 nm/s

Rotary motors: ATP synthase



ATP is made by two **coupled** rotary motors known as ATP synthase, likely arose through modular evolution

one motor, F_0 , sits in the membrane and is driven by a proton gradient (similar to flagellar motor)

the other motor, F_1 , is in the cytoplasm and makes (or uses!) ATP (similar to DNA helicase)

the two motors are coupled by an **axle** (rotates) and a **stator** (stationary)

Each motor is *reversible*, one can drive the other!

F_o rotary motor

stator holds rotor in place until proton/ion enters from one side through salt bridge (+/- residues)

proton/ion neutralizes charge, rotor then can move freely after which proton/ion leaves to other side

rotation is thermally driven but *rectified* by proton transport across membrane, clockwise/ccw determined by which side proton comes from

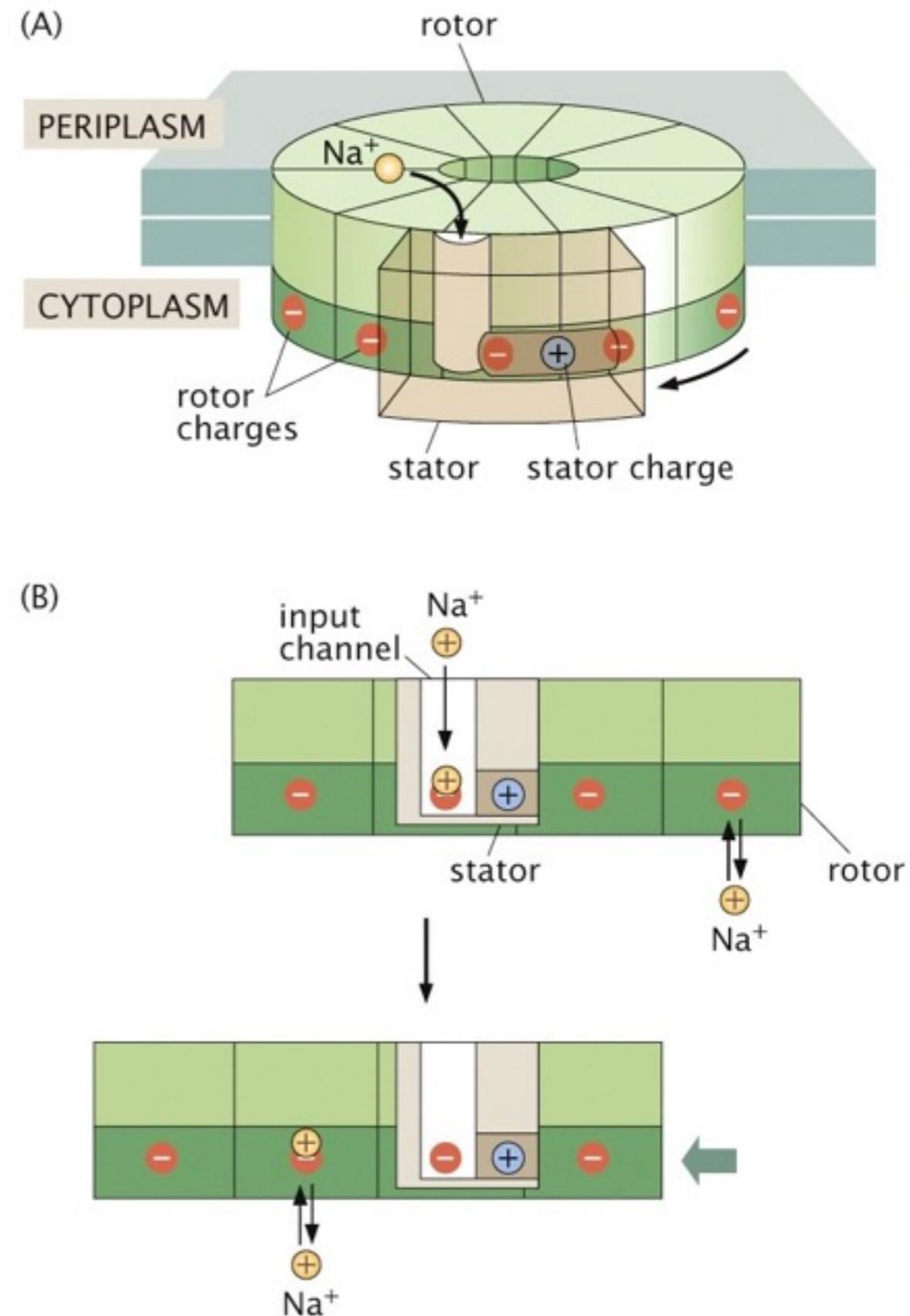
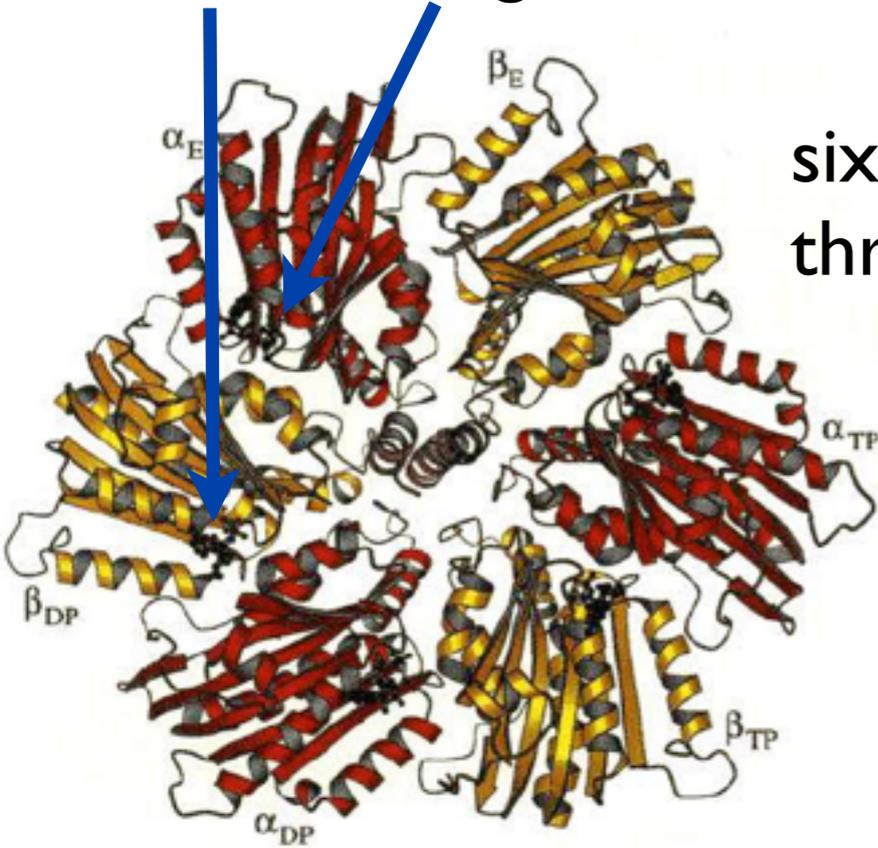


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ATP binding sites



six binding sites, only three (β) are catalytic

F₁ rotary motor

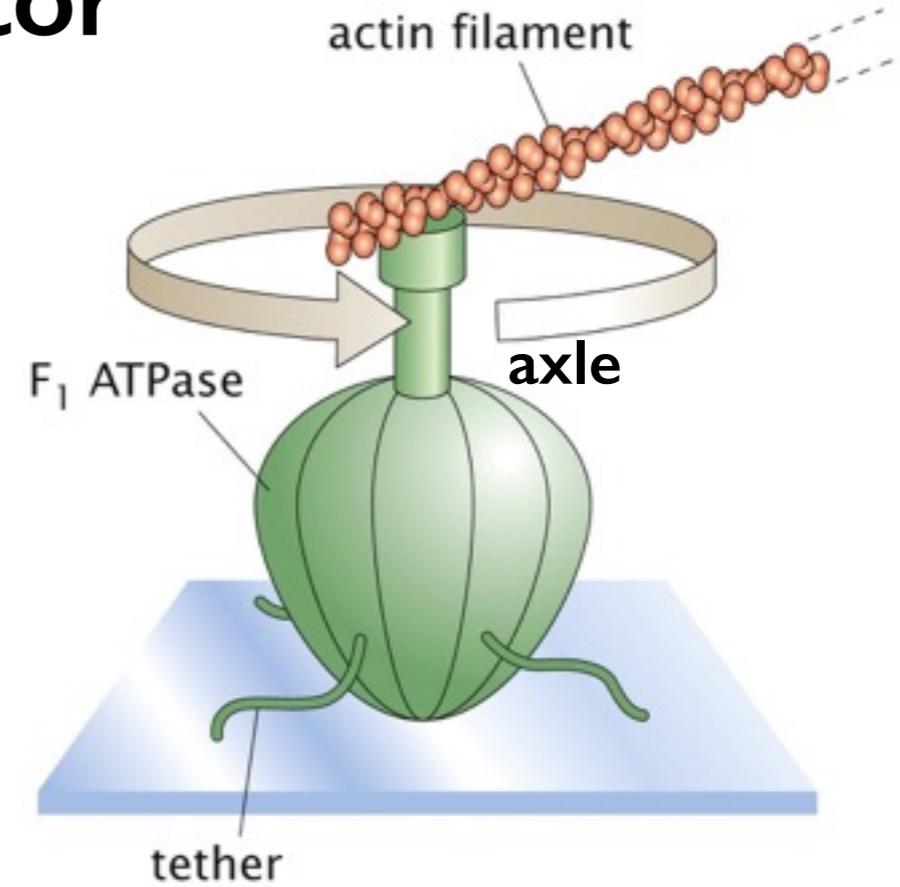


Figure 16.16a Physical Biology of the Cell, 2ed. (© Garland Science 2013)

b



Hiroyuki Noji, Ryohei Yasuda, Masasuke Yoshida & Kazuhiko Kinosita Jr. (1997) Direct observation of the rotation of F₁-ATPase. *Nature*, 386, 299 - 302.

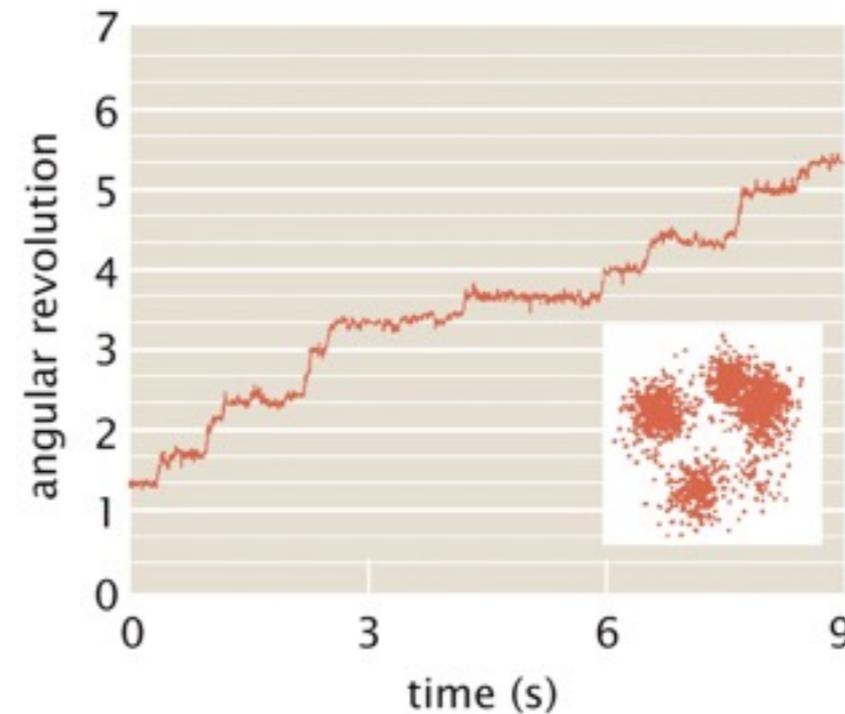


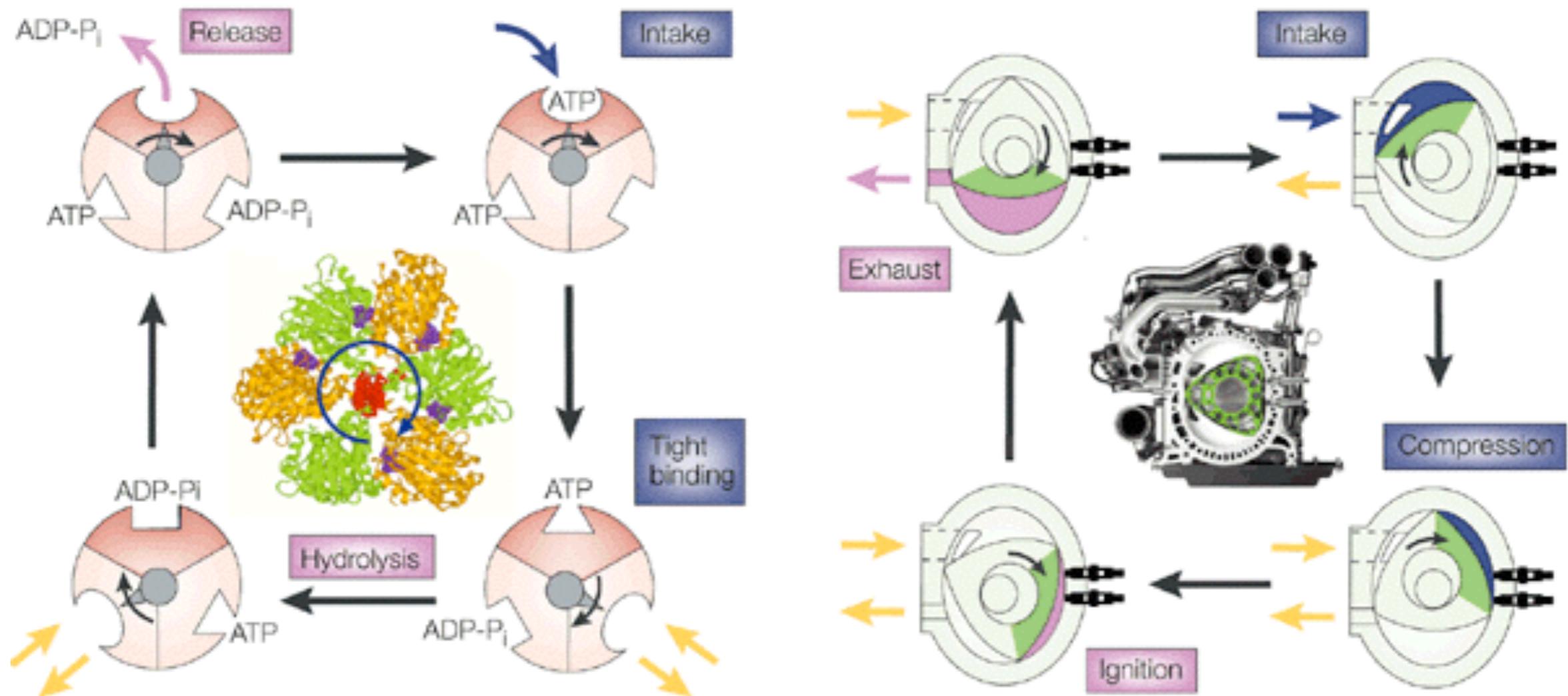
Figure 16.16c Physical Biology of the Cell, 2ed. (© Garland Science 2013)

First direct evidence F₁ rotates unidirectionally in discrete (3x) steps

F₁ rotary motor

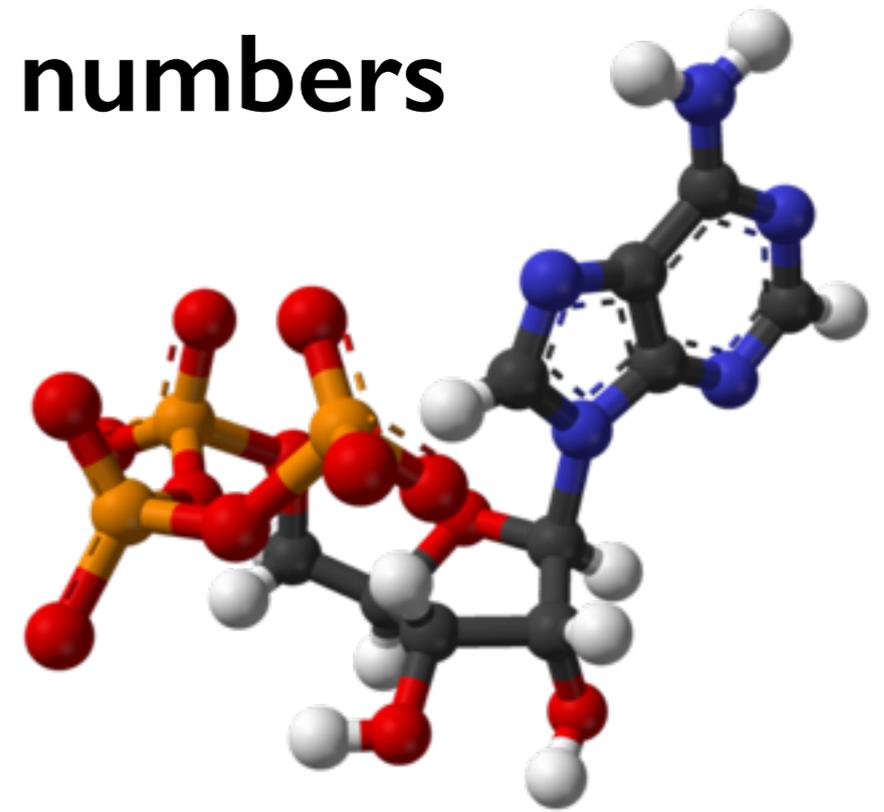
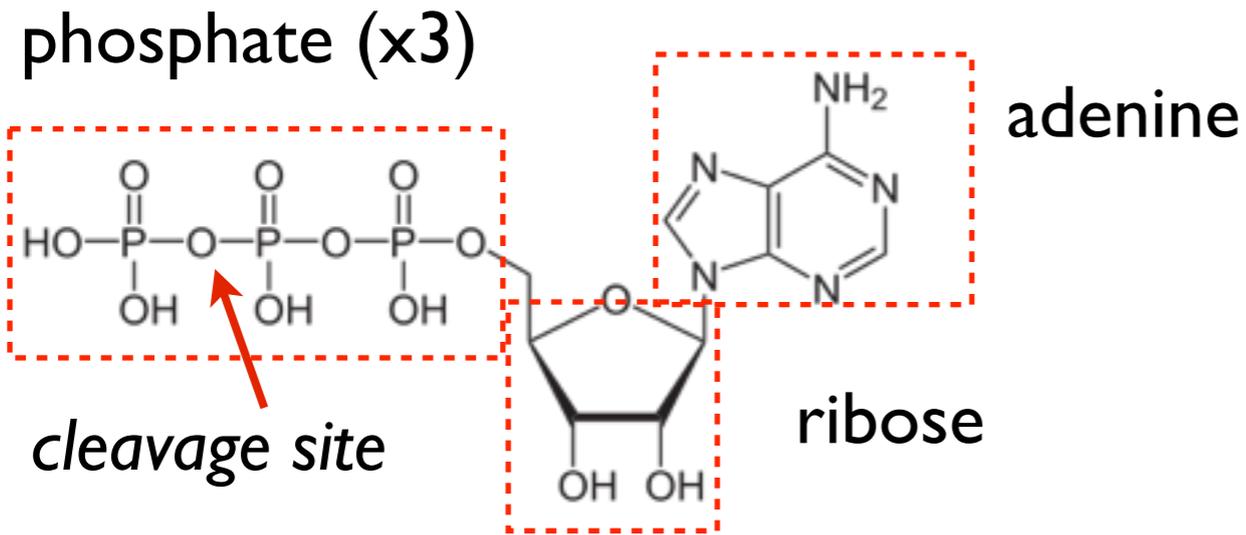
catalytic cycle just like a Mazda rotary combustion engine
(convergent evolution???)

difference is ATP synthase is almost 100% efficient!



Nature Reviews | Molecular Cell Biology

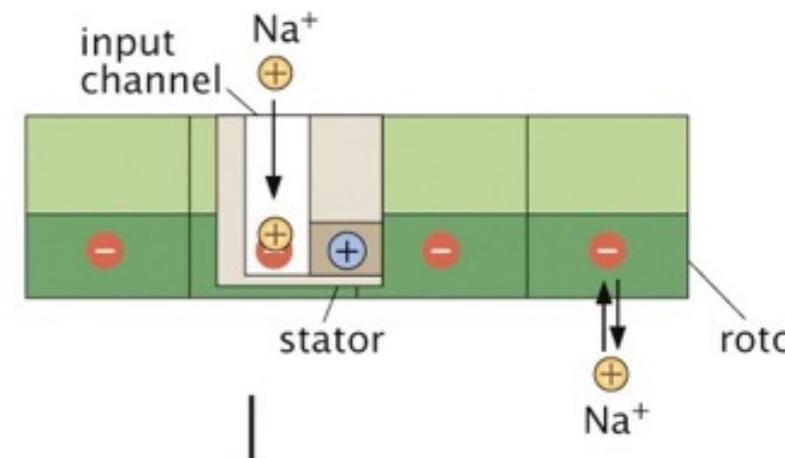
ATP synthase by the numbers



typical membrane potential $\sim 100 \text{ mV}$

energy gained by moving 1 ion/proton: $0.1 \text{ eV} = 4 \text{ kT}$

actual amount is **7 kT**, due to *chemical* (in addition to *electrical*) potential

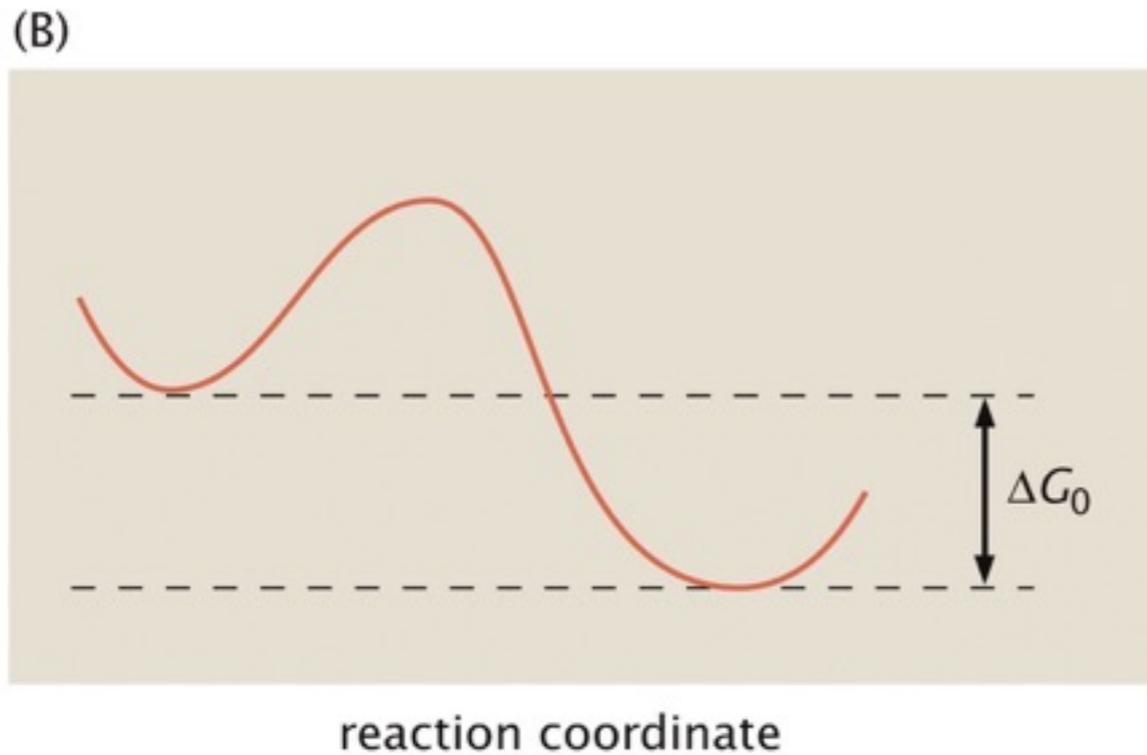


Each step of the turn (120 degrees) generates 1 ATP
 from the numbers above, need at least 3-4 protons to get 1 ATP
 and indeed, this is the case (F_o has ~ 12 subunits)
 ATP synthase is practically **100% efficient!!!**

Polymerization motors



even the tracks on which translational motors move are motors themselves (e.g., actin, microtubules)



addition of monomer to filament is energetically favorable

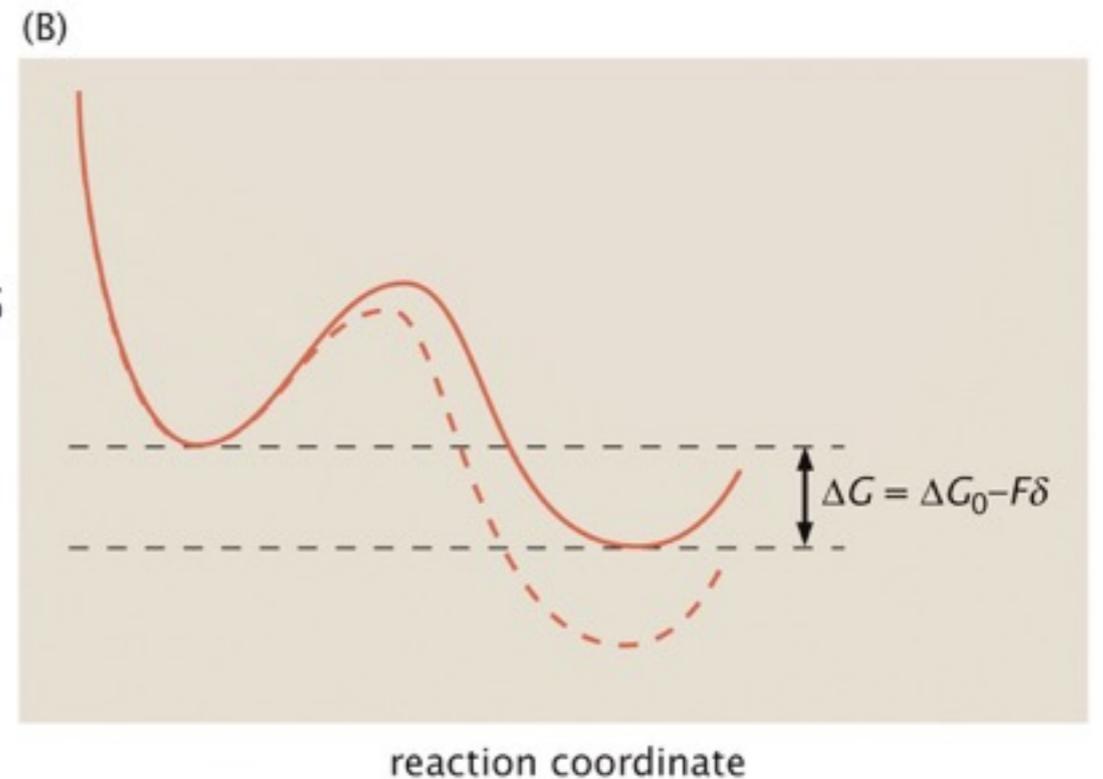
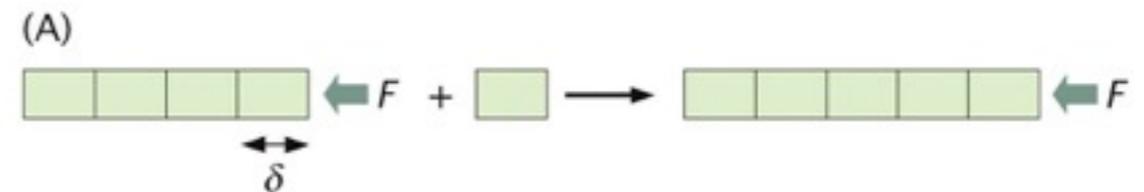


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Figure 16.44 Physical Biology of the Cell, 2ed. (© Garland Science 2013)

$$\Delta G = kT \ln \frac{m}{m^*} \quad m^* = \frac{\Omega}{V} e^{-\beta \Delta \epsilon}$$

m is monomer concentration, $m^* = K_d$ is concentration at equilibrium

this free energy can be harnessed to do useful mechanical work

Polymerization motors

random fluctuations of barrier or filament can allow a monomer to come in and bind

the force exerted by the barrier alters the off and on rates

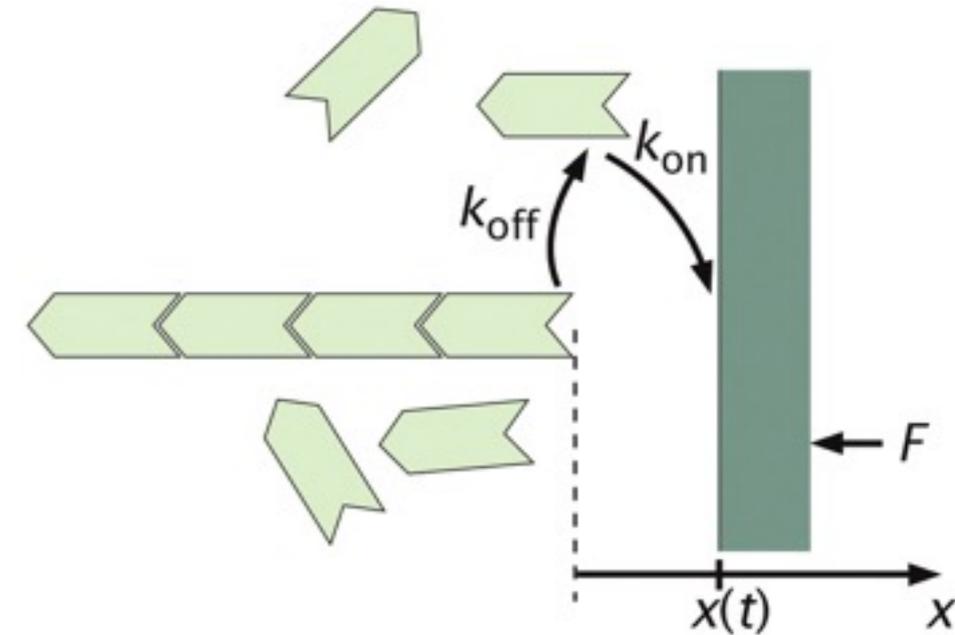
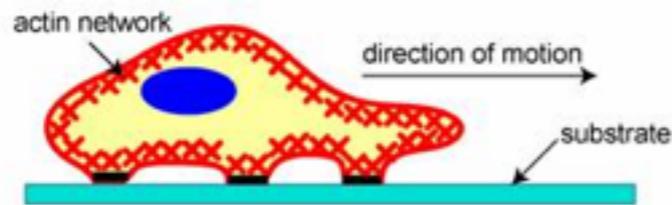
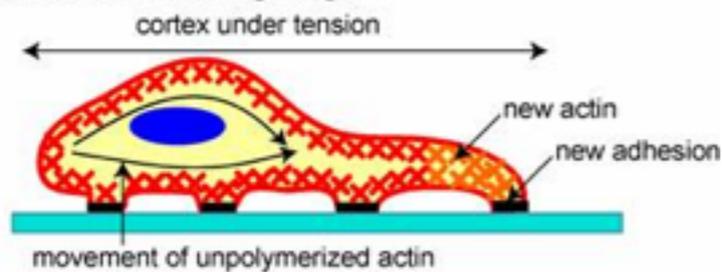


Figure 16.45 Physical Biology of the Cell, 2nd. (© Garland Science 2013)

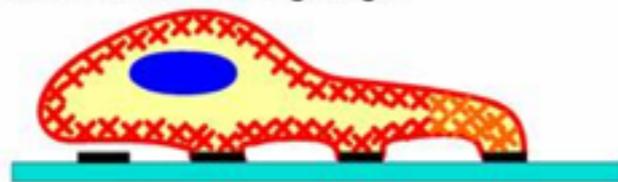
1) Protrusion of the Leading Edge



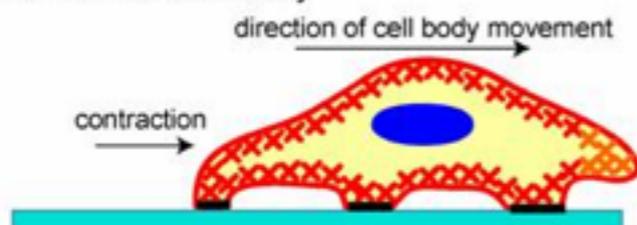
2) Adhesion at the Leading Edge



Deadhesion at the Trailing Edge



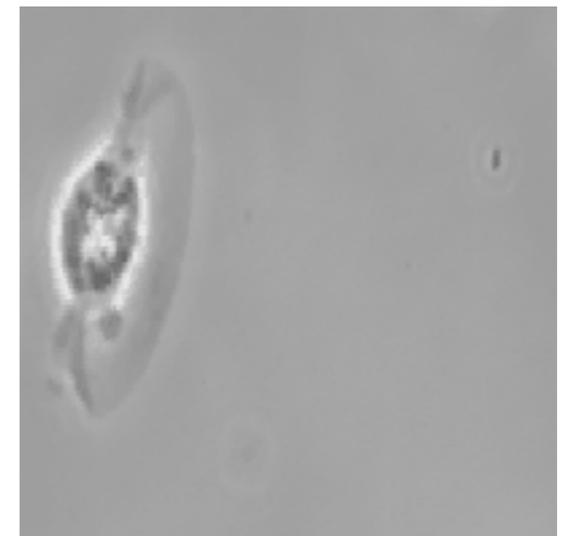
3) Movement of the Cell Body



$$F_{\max} = \frac{kT}{\delta} \ln \frac{m}{m^*}$$

estimates for single actin polymer around 5-7 pN

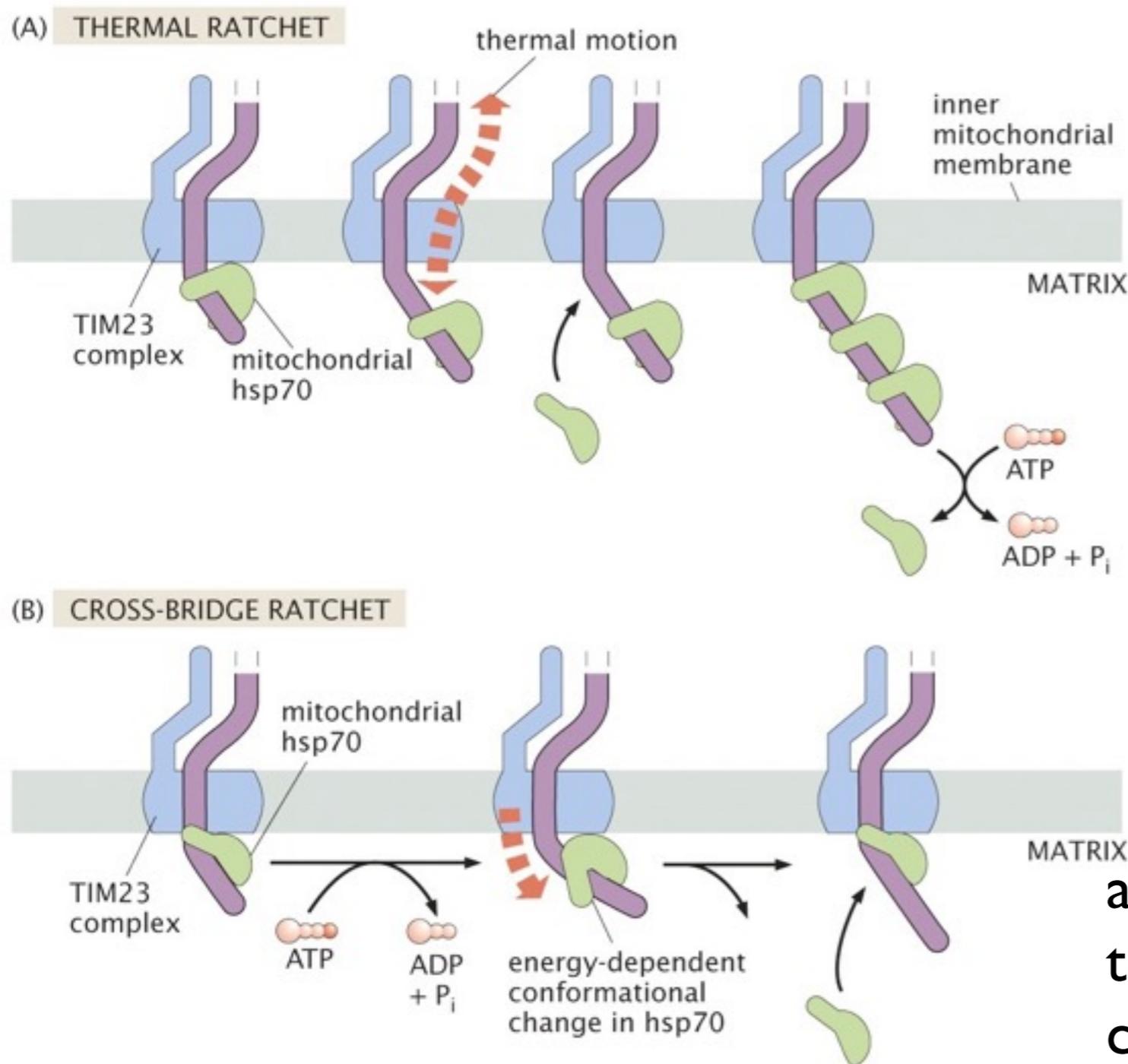
many cells move through actin polymerization forces!



keratocyte (from Julie Theriot lab)

Translocation motors

directed motion generated by ratcheting mechanism, used for, e.g., protein import/export across membranes



binding of proteins on one side prevents backsliding, energy is utilized to induce unbinding

alternatively, energy is used directly to pull protein through, tight hold in channel prevents backsliding

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Translocation motors

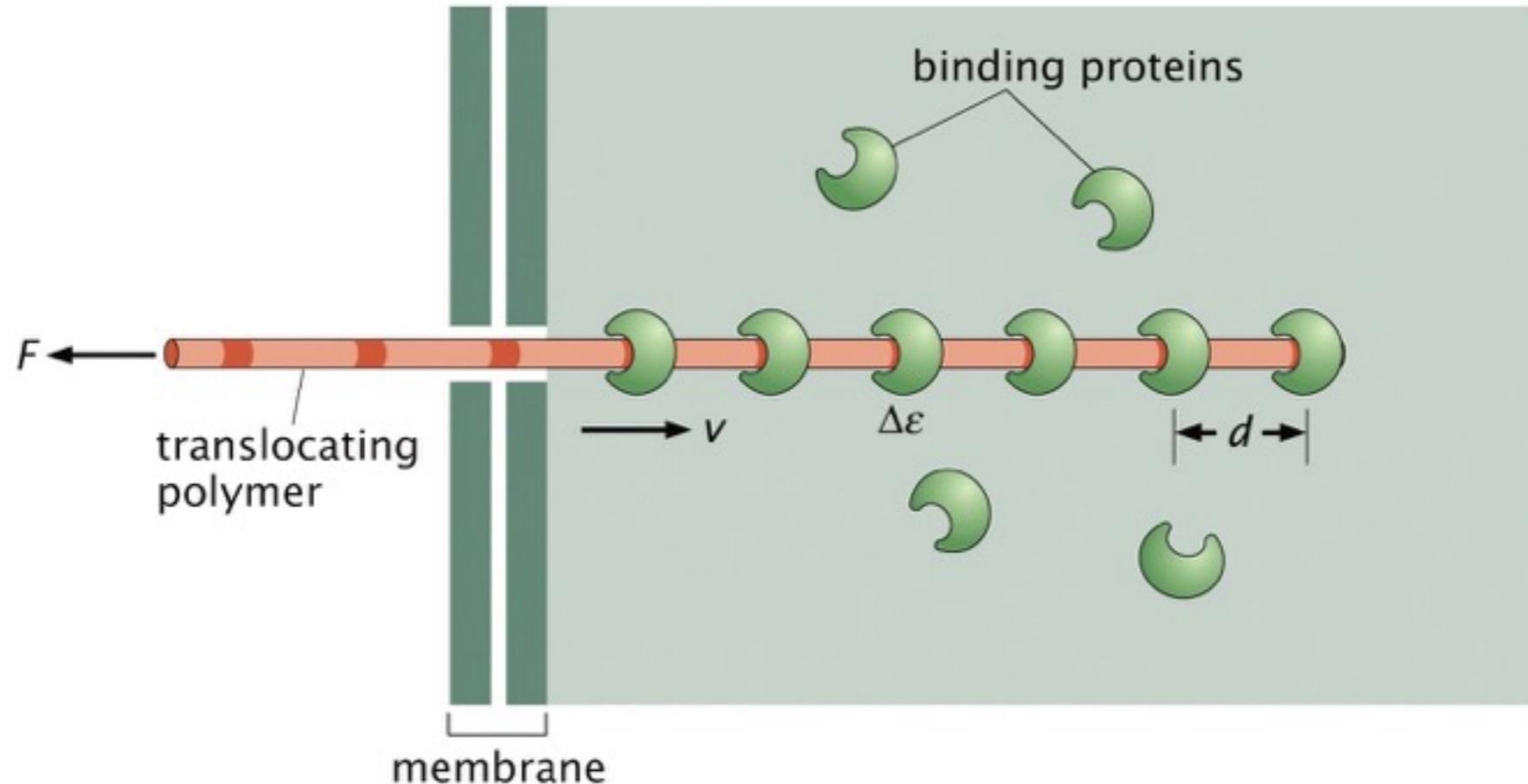


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through diffusion alone, polymer would spontaneously end up on other side in time $t_{\text{diff.}}$.

$$t_{\text{diff.}} = \frac{L^2}{D} = \frac{(nd)^2}{D}$$

$$\frac{t_{\text{trans.}}}{t_{\text{diff.}}} = \frac{1}{n}$$

with binding to prevent backsliding, time is reduced to $t_{\text{trans.}}$.

$$t_{\text{trans.}} = n \left(\frac{d^2}{D} \right)$$