Joint Correction of Ionosphere Noise and Orbital Error in L-Band SAR Interferometry of Interseismic Deformation in Southern California

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Abstract—The accuracy of L-band synthetic aperture radar (SAR) differential interferometry (InSAR) on crustal deformation studies is largely compromised by ionosphere path delays on the radar signals. The ionosphere effects cause severe ionospheric distortion such as azimuth streaking and long wavelength phase distortion similar to orbital ramp error. Effective detection and correction of ionospheric phase distortion from L-band InSAR images are necessary to measure and accurately interpret surface displacement. In this paper, we investigate the performance improvement of L-band InSAR interseismic deformation measurements in southern California through the joint correction of both ionosphere noise and orbital error. Our results show that this method can effectively remove orbit and ionosphere phase distortions. In comparison with in situ GPS measurements, the achieved InSAR measurement accuracy is improved from $\sim$30 mm to $\sim$10 mm by the proposed joint correction method. We show that, after the joint correction, the remaining atmosphere noise can be further mitigated through stacking, leading to an RMS error of $\sim$4.7 mm/year in resultant line-of-sight velocity, as compared with $\sim$11.3 mm/year before the correction. Our results demonstrate that the proposed joint correction technique provides a promising way to jointly correct orbital and ionospheric artifacts in L-band InSAR studies of crustal deformation.

Index Terms—ALOS PALSAR, interferometric SAR (InSAR), ionospheric correction, ionosphere noise, multiple-aperture interferometry (MAI), orbital error, synthetic aperture radar (SAR).

I. INTRODUCTION

SATELLITE synthetic aperture radar (SAR) differential interferometry (InSAR) is now a widely used technique for measuring relative surface displacements along the radar line-of-sight (LOS) direction between SAR acquisitions with accuracy of an approximately millimeter to centimeter level at a fine spatial resolution ($\sim$100 m or higher) over a large area [1]–[3]. The success and accuracy of this technique in measuring surface deformation are strongly affected by various noise sources inherent in InSAR measurements. These typically include orbital error, troposphere artifact, ionosphere phase delay, residual topography error, and decorrelation noise. For an L-band SAR system, one dominant noise source is the ionosphere effect due to the propagation of the SAR wave through the ionosphere. The ionosphere’s frequency-dependent refractive index leads to wave dispersion, inducing phase delays on radar pulses that are directly proportional to the total electron content (TEC) and inversely proportional to the radar frequency [4] and [5]. Ionosphere phase delay causes significant interferometric phase errors, including small-scale phase distortions due to ionosphere turbulence and long-wavelength phase artifacts that are similar to orbital error. The spatial and temporal variability of TEC associated with solar activity also cause heterogeneous effects of the propagation delay on a SAR image and result in considerable spatiotemporal interferometric phase variations [6].

The ionospheric influence on SAR, InSAR, and polarimetric SAR has been recently studied [4], [6], [7]. A number of approaches for the ionosphere correction have been proposed [4]. These approaches either exploit the ionosphere effect from the range and/or azimuth correction have been proposed [4]. These approaches either exploit the ionosphere effect from the range and/or azimuth correction, interferogram. It then exploits the linear relationship between the MAI phase and the azimuth
the MAI interferogram. Further analysis also demonstrates that the improved method can estimate TEC variation with accuracy better than $10^{-4}$ TEC units at 100 or more multilooking level and 0.5 coherence level, which is significantly better than other azimuth shift methods [11]. Because the method of [11] uses MAI [12] and [15] rather than the pixel offset from cross correlation of two SAR amplitude images [5] to estimate the interferometric phase due to azimuth displacement, it improves the accuracy of the measurement.

In this paper, we investigate the improvement of L-band InSAR interseismic deformation measurements from joint corrections of the ionosphere noise and orbital error. The measurements are from two Advanced Land Observation Satellite (ALOS) Phase Array L-band SAR (PALSAR) L-band InSAR pairs that cover the southern San Andreas-San Jacinto fault system. Both InSAR images are subject to severe ionosphere phase distortion with long wavelength features similar to deformation signals and orbital ramp errors. We show that the joint correction method allows the effective removal of large ionosphere and orbital artifacts. We also show that, after the joint correction, it is possible to further reduce remaining noise components such as atmosphere delay by resorting to conventional methods such as stacking or temporal filtering in InSAR time-series analysis.

II. METHOD

In the following, we describe the joint correction method of ionospheric noise and orbital error, including a brief description of the MAI-based ionosphere correction method for phase distortion. More details about the MAI-based ionosphere correction method can be referred to [11].

The ionosphere correction method exploits the linear relationship between the MAI phase and the azimuth gradient of ionosphere phase, which can be expressed as

$$\frac{\partial \phi_{\text{ion}}}{\partial x} = -\alpha \cdot \frac{l}{n\lambda} \cdot \phi_{\text{MAI}}$$

where $\phi_{\text{MAI}}$ is the MAI phase, $x$ is the azimuth, $\partial \phi_{\text{ion}}/\partial x$ is the azimuth derivative of the ionospheric phase, $\alpha$ is a system- and geometry-dependent factor, $l$ is the effective antenna length, $\lambda$ is the radar wavelength, and $n$ is a normalized squint that is a fraction of the full aperture width. Consequently, the ionospheric phase can be expressed by the integration of the MAI phase extending from A to B as $\phi_{\text{ion}} = -\alpha \cdot l/n\lambda \cdot \int_A^B \phi_{\text{MAI}} dx$. Furthermore, according to [11], the relationship between the InSAR phase and the MAI phase exists as

$$\frac{\Delta \phi_{\text{InSAR}}(x, r)}{\Delta_{az}} = \alpha \cdot \phi_{\text{MAI}}(x, r) + \beta$$

$$\Delta \phi_{\text{InSAR}}(x, r) = \phi_{\text{InSAR}}(x + 1, r) - \phi_{\text{InSAR}}(x, r)$$

where $\Delta_{az}$ is multilooked azimuth pixel spacing, $r$ is the range, and $\beta$ is the offset value used to calculate the reference phase of the MAI interferogram. $\phi_{\text{MAI}}(x, r)$ is the scaled MAI phase and defined as $\phi_{\text{MAI}}(x, r) = -(l/n\lambda)\phi_{\text{MAI}}(x, r)$. $\Delta \phi_{\text{InSAR}}/\Delta_{az}$ is the azimuth derivative of InSAR phase, and $\Delta \phi_{\text{InSAR}}(x, r)$ is the InSAR phase difference along the azimuth. Once parameters of $\alpha$ and $\beta$ are estimated using linear regression, the ionospheric phase $\phi_{\text{ion}}$ can be calculated as

$$\phi_{\text{ion}}(x, r) = \sum_{u=1}^{x} \left[ (\alpha \cdot \phi_{\text{MAI}}(u, r) + \beta) \cdot \Delta_{az} \right] + C(r)$$

where $C(r)$ is the integral constant that varies along the range direction. The integral constants can be estimated using the correlation between ionospheric and InSAR phase [11] and [16].

Jung et al. [12] found that the residual flat earth and topographic phase in MAI interferograms are approximate functions of the perpendicular baseline difference between forward- and backward-looking pairs, and the flat earth phase is generally much larger than the topographic phase. They also showed that a second-order polynomial model could be used to remove such phase distortions. However, the model does not work well for MAI interferograms that have severe ionosphere distortion since the ionosphere phase is much larger than the flat earth phase in the MAI interferograms. Thus, the insufficient correction of the MAI phase distortions could cause a nonlinear phase distortion in the ionospheric phase $\phi_{\text{ion}}$ calculated from the azimuth integration in (4). This phase distortion is more severe in azimuth direction and can be approximately modeled by a second-order polynomial in both azimuth and range directions. Note that, when the flat earth phase is very small, such phase distortion due to insufficient correction of the flat earth phase is negligible.

A polynomial fitting method has been used for the removal of the phase distortion induced by the orbital error, which is frequently adopted in InSAR processing [17]. The orbital phase $\phi_{\text{orb}}$ can be modeled by

$$\phi_{\text{orb}}(x, r) = a_0 + a_1 x + a_2 r + a_3 x r + a_4 x^2 + a_5 r^2 + a_6 h(x, r)$$

where $a_0, a_1, \ldots$ and $a_6$ are the model parameters, and $h(x, r)$ is the topographic height at $(x, r)$. The $h(x, r)$ can be used for the mitigation of topography-dependent atmospheric artifact. If the spatial extent of the deformation signal is much
smaller than the orbital error, the orbital ramp parameters can be determined by a fitting to the interferometric phase of all coherent pixels.

Finally, the corrected interferometric phase $\hat{\phi}_{\text{InSAR}}$ can be defined as

$$\hat{\phi}_{\text{InSAR}}(x, r) = \phi_{\text{InSAR}}(x, r) - \phi_{\text{Ion}}(x, r) - \phi_{\text{Orb}}(x, r).$$

(6)

From (4) and (5), we can estimate the phase distortions caused by ionosphere noise and orbital error. We, then, remove them from InSAR phase using (6). Since the ionospheric phase may possess nonlinear phase distortions due to insufficient correction of the residual flat earth phase in azimuth and range directions that can be modeled as a second-order polynomial function similar to the orbital phase model in (5), the orbital phase correction should be applied after the MAI-based ionosphere phase correction.

The processing flow of the method is summarized in Fig. 1. Major steps include the following: 1) estimate and generate the InSAR phase azimuth derivative map from the unwrapped InSAR interferogram using (3); 2) determine the parameters of $\alpha$ and $\beta$ from the InSAR phase azimuth derivative map and the unwrapped scaled MAI interferogram using (2); 3) generate the ionospheric phase map from the azimuth integral of the scaled MAI interferogram using (4); and 4) generate a corrected InSAR interferogram from the joint correction of ionospheric and orbital artifacts by subtracting orbital error map estimated from (5) after subtracting the ionospheric phase map from the InSAR interferogram.

Note that, in the presence of long-wavelength deformation signals, the orbital error estimated from the polynomial fitting method may include long wavelength components of the deformation signal. We need to further correct the overcorrection by using in situ GPS measurements as control points, leading to the separation of two dominant long wavelength noise sources from imaged deformation signals. It needs to be mentioned that the MAI-based ionosphere phase correction method will not be needed if the azimuth displacements due to ionosphere contribution can be negligible or if the pattern of the ionospheric phase map is similar to that of the orbit error phase map. Moreover, we need to carefully handle the MAI-based ionosphere phase correction method if the azimuth displacements due to ground deformation are not negligible.

### Table I

<table>
<thead>
<tr>
<th>Master</th>
<th>Slave</th>
<th>Beam Mode</th>
<th>Incidence Angle (deg.)</th>
<th>$f_{DC}^a$ (Hz)</th>
<th>$f_{DC}^b$ (Hz)</th>
<th>$f_{DC}^c$ (Hz)</th>
<th>$f_{DO}^d$ (Hz)</th>
<th>B (m)</th>
<th>$\Delta B$ (m)</th>
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<tbody>
<tr>
<td>15/07/2007</td>
<td>20/10/2009</td>
<td>FBS$^a$</td>
<td>38.7</td>
<td>482.7</td>
<td>79.4</td>
<td>-324.0</td>
<td>792.6</td>
<td>-270.8</td>
<td>-0.028</td>
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<tr>
<td>15/10/2007</td>
<td>20/10/2009</td>
<td>FBS</td>
<td>38.7</td>
<td>474.5</td>
<td>71.1</td>
<td>-332.3</td>
<td>804.0</td>
<td>-890.5</td>
<td>-0.054</td>
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Fig. 2. (a) Original InSAR interferogram. (b) MAI interferogram. (c) Ionospheric phase map estimated from the MAI interferogram. (d) Ionosphere-corrected InSAR interferogram after MAI-based ionosphere phase correction. (e) Jointly corrected InSAR interferogram after joint correction of ionosphere and orbit error. (f) Orbit-corrected InSAR interferogram after orbital phase estimation from 2-D polynomial fit of the original InSAR interferogram. All interferograms and phase map are for the pair of 2007/07/15–2009/10/20. The area of low coherence is masked. Note that one fringe in the MAI interferogram represents $0.2\pi$. 

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III. RESULTS

We apply our method of joint correction of ionosphere noise and orbital error to two InSAR interferograms in southern California. The raw SAR data are from the Japanese ALOS PALSAR sensor. Four frames (640, 650, 660, 670) from the ascending track 214 are concatenated to generate single-look complex (SLC) SAR scenes and form the interferograms. The InSAR interferograms are multilooked by $5 \times 20$ looks in range and azimuth directions, respectively, resulting in roughly $60 \times 63$ m pixels. The interferograms are smoothed using an adaptive filter [18] with a window size of 64 to reduce phase variance.

The MAI interferograms are generated by an improved MAI approach [12]. A normalized squint of 0.5 and an effective antenna length of 8.9 m, respectively, are used for the MAI processing. For the MAI processing, the forward, average, and backward Doppler centroids and the subaperture processing bandwidth are calculated by azimuth common band filtering and summarized in Table I. The forward- and backward-looking SLC images are first produced from raw radar signal. Forward- and backward-looking interferograms are then generated, multilooked, and smoothed by the same multilooked factor and filter used for the InSAR processing. The final MAI interferograms are generated after the correction of residual flat-earth and topographic phase [12]. Both InSAR and MAI interferograms can be coregistered by simple translation since they have the same relative geometry [11]. We then base on the processing steps summarized in Section II to estimate the ionosphere noise and orbit error of InSAR interferogram using MAI-based correction (d), InSAR interferogram after the joint correction of ionosphere phase and orbital error (e) and, for comparison purpose, orbit-corrected InSAR interferogram after orbital phase estimation from 2-D polynomial fitting of the original InSAR interferogram, and (f) for the InSAR pair 2007/07/15–2009/10/20. Results for the pair 2007/10/15–2009/10/20 are shown in Fig. 3. It is clear that both pairs are dominated by severe long-wavelength ionospheric phase noise [see Figs. 2(c) and 3(c)]. For example, for the pair 2007/07/15–2009/10/20, phase variations due to the ionosphere phase artifact range from $\sim -3.9$ to $6.7$ rad, corresponding to LOS displacements of $\sim -7.3$ to $\sim 12.6$ cm. This is particularly problematic for interseismic deformation mapping since expected deformation signals due to fault slip/locking are small. The maximum variations of the MAI phase are $\sim -0.64$ to $+0.93$ rad for the pair 2007/07/15–2009/10/20, and $\sim \pm 0.9$ rad for the pair 2007/10/15–2009/10/20. These correspond to the along-track displacements of $\sim -0.9$ to $\sim 1.3$ m and $\sim \pm 1.3$ m, respectively, which are much larger than expected azimuthal displacements ($< 7$ cm) due to interseismic deformation [22]. Moreover, it is also noted that the shape of the ionospheric phase map shown in Figs. 2(c) and 3(c) is deformed to fit into that of the original InSAR interferograms shown in Figs. 2(a) and 3(a). This is because the integration constants of (4) are estimated using the correlation between ionospheric and InSAR phase. We can see that our method of joint correction of ionosphere and orbital errors can successfully estimate and correct the major components of ionospheric and orbital phase distortions [see Figs. 2(e) and 3(e)]. We also find that the 2-D polynomial fitting, which is commonly used for orbital error correction in InSAR processing, appears to remove a large portion of ionospheric and orbital phase signals...
because of long-wavelength characteristics of such noises [see Figs. 2(f) and 3(f)]. However, there are considerable amounts of ionospheric phase noises remained, particularly at the beginning and ending parts of each interferogram.

To validate our correction results, we use in situ GPS velocities from southern California Earthquake Center (SCEC) Community Motion Map-4 (CMM-4) [19] as the ground truth of interseismic deformation measurements. Fig. 4 shows the comparison between projected GPS and InSAR LOS displacements. The root-mean-square (RMS) error is used to quantify the difference between GPS and InSAR LOS displacements at the same GPS locations indicated in Fig. 6(a). Artificial correlation between InSAR and GPS LOS displacements due to ionosphere phase artifacts exists before the correction [see Fig. 4(a) and (e)]. After the MAI-based ionosphere phase correction, the RMS errors and correlation coefficients are changed from \( \sim 31.4 \) mm and 0.20 to \( \sim 10.9 \) mm and 0.15 for the pair 2007/07/15–2009/10/20, and \( \sim 27.1 \) mm and 0.60 to \( \sim 10.1 \) mm and 0.31 for the pair 2007/10/15–2009/10/20 [see Fig. 4(b) and (f)], respectively. These results suggest that the correction successfully removes the dominant ionosphere phase artifact. Note that such MAI-based ionosphere phase correction is not perfect. The ionosphere-corrected InSAR interferograms may still have phase distortions due to the orbital error and/or the undercorrection of the MAI phase distortion. These can be further corrected by the 2-D polynomial fit. Considering the risk of removing deformation signals due to the polynomial fitting, we make further correction by using GPS as ground control points. We perform a 2-D polynomial fit to the difference between corrected InSAR and GPS LOS displacements and remove the ramp error from InSAR data using the best-fit parameters. The resultant RMS errors are \( \sim 10.3 \) mm for the pair 2007/07/15–2009/10/20 and \( \sim 10.1 \) mm for the pair 2007/10/15–2009/10/20 [see Fig. 4(c) and (g)], respectively. Joint correction of the orbital error improves the RMS error but only marginally, suggesting that orbital ramp errors from both pairs are small. In comparison, the orbital and ionospheric phase corrections based on 2-D polynomial fit do not achieve the same level of RMS error reduction as the joint correction method [see Fig. 4(d) and (h)]. There is much larger scattering between InSAR and GPS LOS displacements, consistent with what we observe in Figs. 2(d) and 3(d).

After the joint correction of ionosphere noise and orbital ramp error, remaining major noise components in L-band SAR interferometry are mainly atmospheric phase delay, which are random in time and can be further suppressed through some conventional approaches such as stacking [20] or temporal filtering in InSAR time-series analysis [2], [3], [21]. We test this by stacking the derived LOS velocities from two InSAR pairs before and after the joint correction (see Fig. 5). Although the InSAR pairs have the same slave image, their stacking clearly reduces the scattering associated with individual interferograms and improves the RMS error in resultant LOS velocity. The RMS error in LOS rate is reduced from \( \sim 5.1 \) mm/year for a single pair after the joint correction to \( \sim 4.7 \) mm/year after the stacking. Considering both pairs share the same ending date, atmosphere noise is not completely random. We still achieve an RMS error reduction of \( \sim 8\% \) by using just two pairs. Again, we observe much larger scattering in the stacked LOS velocity based on interferograms that are corrected for the orbital and ionospheric phase using a 2-D polynomial fit [see Fig. 5(c)]. Fig. 6 shows the map view of stacked LOS velocity before and after the correction of ionospheric and orbital phase artifacts.
Fig. 5. Projected GPS LOS velocities versus InSAR LOS velocities derived from the stacking of (a) original InSAR interferograms; (b) jointly corrected interferograms after correcting MAI-based ionosphere phase estimation and orbital ramp error; and (c) orbit-corrected interferograms using orbital phase estimation from 2-D polynomial fitting. The RMS errors are used to quantify the difference between InSAR and GPS LOS velocities.

Fig. 6. InSAR LOS velocities obtained from the stacking of (a) original interferograms; (b) jointly corrected interferograms after correcting MAI-based ionosphere phase estimation and orbital ramp error; and (c) orbit-corrected interferograms using orbital phase estimation from 2-D polynomial fitting. Triangles in (a) indicate GPS locations from SCEC CMM-4. Only GPS sites within the InSAR image are used to compare with InSAR LOS measurements. Red lines are active fault traces from California Geological Survey fault database.

IV. DISCUSSIONS AND CONCLUSION

One of the main limitations in our joint correction of ionospheric and orbital artifacts is its requirement for good coherence for both InSAR and MAI interferograms. For southern California, due to its metropolitan setting and dry climate, the coherence is typically high even for the interferograms with temporal separation of more than 3 years [22]. Estimation of the ionospheric phase map from along-track MAI phase also requires the azimuth displacement due to ground deformation is negligible. For the ALOS ascending track used in this paper, we estimate the maximum azimuth displacement due to plate motion over a span of ~2 years is less than 7 cm. This is significantly less than the azimuth contribution (~1.3 m) caused by the ionospheric phase distortion. It is also well below the achieved accuracy of the MAI, which is about 0.8% of the azimuth resolution for ALOS PALSAR [11], equivalent to ~50 cm in our case.

Although the 2-D polynomial fit to original interferograms removes a considerable amount of long-wavelength orbital and ionospheric phase artifacts, this approach is not preferred, in particular, for interseismic deformation mapping because ionospheric artifacts cannot be simply modeled by a polynomial function. It is worthy to emphasize that the proposed joint correction provides an effective way to correct both orbital- and ionosphere-related phase distortions. The method can be used with other methods to correct major noise sources in L-band SAR interferometry. It also lends itself naturally as a stand-alone correction module to correct orbital ramp error and ionosphere phase noise in L-band InSAR time-series analysis, which we do not address in this paper. For InSAR time-series analysis, the remaining atmospheric phase delay can be further suppressed by temporal filtering.

In this paper, we present an approach of joint correction of ionospheric phase artifacts and orbital ramp errors in InSAR imagery using MAI interferogram and in situ GPS measurements. Application of this approach to the selected examples of L-band InSAR images of interseismic deformation in southern California shows it can effectively correct the ionosphere related phase distortion and orbital ramp error. Remaining tropospheric phase delay can be further reduced through the stacking. We show that this systematic treatment of major noise sources in L-band InSAR measurements are critical for accurate measurement of interseismic deformation and need to be incorporated for continental scale deformation mapping for existing and future L-band SAR missions.
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REFERENCES


