Medical Imaging with Laser Polarized Noble Gases

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January 28, 2000

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Abstract

The field of medical imaging with polarized rare gases, just five years old, has brought optical scientists together with medical researchers to perfect techniques and pursue new opportunities for biomedical research. This review, written for the likely reader of these volumes, aims to present the field from several perspectives. The historical perspective shows how applications of nuclear polarization for experiments in nuclear and particle physics led to techniques for production of large quantities of highly polarized $^4$He that are increasingly reliable and economical. The atomic/optical physics perspective details the underlying processes of optical pumping, polarization, and relaxation of the rare gases. The biomedical perspective describes work to date and the potential applications of imaging in medicine and research.

1 Introduction

Five years ago, a short article was published in the journal Nature showing Magnetic Resonance Images of $^{129}$Xe gas that had filled the airways of an excised mouse lung [Albert et al., 1994]. The images were acquired at SUNY, Stony Brook, on Long Island, NY. But the gas, prepared by laser optical pumping methods, in Princeton, New Jersey, was transported over 100 km by car in a small glass cell immersed in a cup of liquid nitrogen. (The gas was “polarized” in Princeton to provide 10,000 times greater NMR signal per atom than produced by “brute force.” This compensated for the 10,000 times lower concentration of gas.) Reading the Nature paper led many in the field of laser optical pumping to turn their attention to the new possibilities, and it led many radiologists to seek laser physicists as collaborators to help develop the potential biomedical applications. Now physicists, radiologists, neuroscientists, medical researchers, and clinicians are working together in teams around the world. The promise of entirely new ways to use NMR and MRI information from $^3$He and $^{129}$Xe images of gas in the lungs and of xenon dissolved in tissue of the lungs, heart, and brain, has attracted the attention of scientists, and physicians, as well as the pharmaceutical industry. The promise is that this marriage of laser/optical physics and medical imaging will provide new ways to study and map function in the brain, measure physiological parameters, and diagnose diseases of the lungs, heart, and brain that depend on the flow of gas and blood through the vital organs.

In figures 1 and 2, we show magnetic resonance images produced with laser polarized $^3$He and $^{129}$Xe. In figure 1, a series of consecutive images of a slice through the human lung shows the flow of gas into the air spaces after a breath is taken and exhaled [Saam et al., 1999]. This moving picture of gas flow is called a ventilation image. Ventilation images made with scintigraphy of radioactive gas (usually $^{133}$Xe) are used to assess lung function and find non-functioning portions of the lung. Combined with measures of blood flow through the lung, ventilation scans help diagnose a variety of lung diseases, such as pulmonary embolism, with moderate specificity. (The efficacy of a diagnostic technique is characterized by its sensitivity and specificity. Sensitivity is essential to discover a malady while specificity is required to determine the exact problem and the course of treatment.) In figure 2, we show images of $^{129}$Xe gas in the lung and dissolved in tissue and blood of a rat that had been breathing a polarized $^{129}$Xe – oxygen mixture. In contrast to helium, xenon crosses the blood–gas barrier in the lungs, dissolves in blood, and is carried to distal organs where it diffuses into tissue as the blood flows through capillaries from artery to vein. The NMR frequencies of $^{129}$Xe differ by about 200 ppm for gas and dissolved phases, and vary by several ppm among different types of tissue and blood.

The development of techniques of laser enhanced nuclear polarization (or hyperpolarization), has been most strongly motivated by nuclear and particle physics. Targets of polarized $^3$He are used in accelerator experiments such as those that probe the elementary particle, short range structure of the neutron [Chupp et al., 1994a]. Polarized $^3$He is also used to polarize neutrons for nuclear physics and neutron scattering research [Coulter et al., 1988]. These driving motivations and applications...
1.1 Historical perspective

The atomic nucleus of an odd-A or odd-Z isotope in general has non-zero nuclear spin and non-zero magnetic moment. These nuclear spins and moments have long been important in the development of nuclear physics through the comparison of experiment with the nuclear shell model theory (see for example, Ramsey’s book on Nuclear Moments [Ramsey, 1950]). Nuclear spin has also been an important variable for a range of approaches to studying nuclear interactions. Perhaps the best example is \(^{3}\)He. The stable \(A = 3\) isotope, \(^{3}\)He, has been extremely important in nuclear physics. Calculation of the magnetic moment has clarified the role of meson exchange corrections. Nuclear reactions induced by \(^{3}\)He and \(^{3}\)H allow study of isospin symmetry and isospin dependence in a unique way because the \(A=1\) isodoublet is much more difficult experimentally – accelerated neutron beams are not feasible. Perhaps most important is the fact that the neutron polarization in a polarized \(^{3}\)He nucleus is \(\approx 87\%\). This has allowed important short range properties of the neutron to be measured including the neutron electric charge distribution – the electric form factor \(E\) and the neutron deep \(x\).

\(^{3}\)He was accidently discovered by Alvarez at the Berkeley cyclotron in a test run preliminary to fig. 2: Magnetic Resonance Images of \(^{129}\)Xe in the lungs and dissolved in the blood and tissue of a rat. The gray–scale images are conventional proton MRI (spin–echo) images that show the animal’s anatomy. The false–color images show the concentration of \(^{129}\)Xe magnetization for each of three spectral features corresponding to xenon in the gas phase (C and F), dissolved in tissue (B and E) and dissolved in blood (A and D). Panels (A through C) are called axial images across the body, and (D through F) are coronal images through the body.

along with other historical developments are described in section 1.1. The requirements of these experiments have pushed us to understand the physics and technical limitations of optical pumping high densities. Now, we can produce liters (at STP) of \(^{4}\)He, polarized to 50% or more, and similar quantities of \(^{129}\)Xe. Optical pumping, polarization techniques, lasers, and other technical details are discussed in section 2, and the basics of NMR and MRI are described in section 3. The exciting new possible applications to medical imaging are described in sections 4 and 5 on air space imaging and dissolved phase imaging respectively. We conclude in section 6 emphasizing some of the potential applications and future promise of this new technique that provides a wonderful example of transfer of technology motivated by fundamental physics research.

The total angular momentum of the nucleus has contributions from the \(D\)-state and a small proton polarization opposite the \(^{3}\)He polarization. Even this is not enough to account for the measured magnetic moments: isovector meson exchange currents apparently contribute opposite amounts to the \(^{3}\)He and \(^{4}\)H magnetic moments. Therefore the total magnetic moment of \(^{3}\)He can be written

\[
\mu_L(^{3}\text{He}) = P^n\mu_n + P^p\mu_p + \mu_N(<L_z> + A_{MEC} <I_z>)
\]

where \(P^n = 2 <s^n_z> = 0.87\) and \(P^p = -0.027\) are respectively [Friar et al., 1990] the neutron and proton polarizations, \(<L_z> = 0.061\). The meson exchange correction is \(A_{MEC} <I_z> = -0.35\) for the isospin projection \(I_z = -1/2\). The nuclear magneton is \(\mu_N = e\hbar/2m_p\).

\(^{3}\)He is rare, and this is a problem. Primordial abundance of \(^{3}\)He produced in Big Bang nucle-
osynthesis is $^{3}\text{He}/^{4}\text{He}=0.00004$ [Arnett and Turan, 1985]. Additional $^{3}\text{He}$ has been produced in stellar burning [Trimble, 1982], in the atmosphere due to cosmic ray interactions, and underground due to natural radioactivity. Cosmic ray production of $^{3}\text{He}$ on the moon, which does not have an atmosphere, has left much greater abundances imbedded in lunar rocks [Wittenberg et al., 1986], though mining the moon may remain impractically expensive. Most of the stored $^{3}\text{He}$ reserve, less than 1000 kg, has come from the decay of tritium ($^{3}\text{H}$) produced for thermonuclear weapons.

Another feature of $^{3}\text{He}$ has motivated work to develop polarization techniques. $^{3}\text{He}$ turns out to be a potentially perfect spin filter for polarization of neutrons. The strong neutron absorption reaction $n+^{3}\text{He} \rightarrow p + ^{4}\text{He}$ is nearly 100% polarization dependent, due to an unbound $J=0$ resonance in $^{4}\text{He}$. With the neutron and $^{3}\text{He}$ spins opposite, the absorption cross section is $\sigma_{n}(v) = 5230 \frac{\text{b}}{\text{v}}$ barns ($v_{n}=2200 \text{ m/s}$ is the $\text{rms}$ velocity of thermal neutrons). Other $n+^{3}\text{He}$ interactions are negligible. Passing a neutron beam through a filter of polarized $^{3}\text{He}$ produces a beam polarized parallel to the $^{3}\text{He}$, though reduced in flux [Williams, 1980, Coulter et al., 1988, Coulter et al., 1990]. The polarization and transmission for a filter with $^{3}\text{He}$ thickness $t^{\text{He}}$ and polarization $P_{3}$ are given by

$$P_2 = \tanh(\sigma_{n}^{\text{He}}t^{\text{He}}P_{3}) = \cosh(\sigma_{n}^{\text{He}}tP_{3})\exp(\sigma_{n}^{\text{He}}tP_{3})$$

Polarized neutron beams are widely sought for condensed matter and materials science research [Fitzsimmons and Sass, 1989] and for studies of the nuclear interactions of scattered [Heckel et al., 1982], absorbed [Mitchell et al., 1999], and decaying neutrons [Abele et al., 1997]. Scattering of neutrons from materials reveals structure and momentum distributions, and the spin dependence is used to study magnetism, for example of multiple thin layers sought for magnetic recording media [Kubler, 1981]. In contrast to synchrotron x-rays, the magnetic interactions of neutrons are comparable in strength to electric interactions; for photons, magnetic interactions are suppressed by $=300$. The decay of polarized neutrons provides the opportunity to study the weak interactions [Jackson et al., 1957], and weaker interactions [Herzeg, 1998] such as those that emerge from extensions of the Standard Model of elementary particle interactions including SuperSymmetry.

The first attempts to produce useable polarized $^{3}\text{He}$ targets were not successful in spite of heroic efforts. Most notable was the effort by Daniels and Timsit [Timsit et al., 1971a, Timsit et al., 1971b]. Employing optical pumping of metastable helium atoms with lamps (described in section 2), they developed a mercury Toeppler pump (later adapted by Heil and co-workers [Becker et al., 1994]) and provided an important study of $^{3}\text{He}$ polarization relaxation in the presence of many materials [Timsit et al., 1971b]. One particularly crucial conclusion was the importance of a predominantly glass system. Timsit and Daniels presented a theory for predicting $^{3}\text{He}$ polarization relaxation rate dependence on helium permeability and glass iron content that confirmed that one should use alumino–silicate glasses such as Corning 1720 [Fitzsimmons et al., 1969], Schott Supermax [Becker et al., 1994], and Corning 7056 [Smith, 1998]. Quartz and fused silica, though relatively porous to helium, can be produced with extremely low iron content, and are useful particularly for neutron spin filters since the $^{3}\text{He}$ in most glasses strongly absorbs low energy neutrons. Timsit’s and Daniel’s efforts fell short of the goals of 0.5 liter-atm of $^{3}\text{He}$ with 25% polarization. A decade latter, the availability of lasers led to success with the first $^{3}\text{He}$ neutron spin filter [Coulter et al., 1990] and the first targets for electron scattering for study of the neutron charge form factor $G_{N}$ by quasielastic scattering of polarized electrons from the polarized $^{3}\text{He}$ [Woodward et al., 1990, Thompson et al., 1992, Chupp et al., 1992, Becker et al., 1994]. (Quasielastic scattering breaks up the nucleus by momentum transfer to a single nucleon. The spin dependence is generally dominated by the neutron.)

The next generation of polarized $^{3}\text{He}$ target was used for electron scattering at SLAC in a program that revealed the spin content of the neutron’s quarks in deep inelastic scattering [Anthony et al., 1993, Middleton et al., 1993, Abe et al., 1997]. These targets employed spin exchange with laser polarized Rb vapor, a technique that had been considered less favorable for several reasons including the extremely weak hyperfine spin exchange interaction [Walker and Happer, 1997] and problems of radiation trapping – depolarization by multiple scattering of photons in the dense alkali–metal vapor. However, it had been shown that 60-100 torr of $N_{2}$ is sufficient to suppress radiation trapping [Hrycyszyn and Krause, 1970] and that optical pumping with lasers was effective at extremely high optical density with $[\text{Rb}]\approx 10^{13} \text{ cm}^{-3}$ [Chupp and Coulter, 1985]. More detailed studies of optical pumping at high alkali–metal density [Chupp et al., 1987, Wagshul and Chupp, 1994] showed that laser intensity was the primary limitation and that $^{3}\text{He}$ pressures greater than 10 bar in volumes limited only by laser power to 200 cm$^{3}$ became possible with CW standing wave titanium:sapphire lasers [Larson and et al., 1991]. The two methods for polarizing $^{3}\text{He}$, discovered in the early 1960s, became competing techniques in the 1980s. Metastability exchange was pursued by Leduc, Schaeerrer and co-workers who teamed up with Otten and Heil at Mainz [Becker et al., 1994] and with Woodward, McKeown and Milner [Bohler et al., 1988]. This led to the neutron spin filter program at ILL, Grenoble [Surka et al., 1997, Heil et al., 1998], and quasielastic scattering measurements at Mainz [Becker et al., 1994, Becker et al., 1998], both using a two stage, titanium pump compressor to increase the $^{3}\text{He}$ pressure from 1 torr to $\approx 1$ bar. The metastability exchange technique has also been used to pump $^{3}\text{He}$ into a cooled cell in a quasielastic scattering experiment [Woodward et al., 1990] and to fill a “storage cell” that is coaxial with the circulating 30 GeV positron beam in the HERA ring at DESY, Hamburg, Germany [Adlerstaff et al., 1997]. Spin exchange has been most successful in producing high density polarized $^{3}\text{He}$ that is essential for targets used in extracted beam experiments such as the SLAC End Station A deep inelastic scattering program [Abe et al., 1997, Anthony et al., 1996] and recent efforts at TJNAF in Newport News, Virginia [Gao, 1998].

The possibility of nuclear spin gyroscopes also emerged as optical pumping techniques were developed [Colgrove, 1983]. A nuclear spin gyroscope does not require the large quantities of highly polarized $^{3}\text{He}$ demanded by applications of polarized nuclear targets and polarized neutrons. However the concept does rely on the longest possible spin–relaxation and spin–coherence times. Long spin–relaxation times are also important for high polarization, and the development of gyroscopes at industry labs...
helped advance the study of surface relaxation mechanisms. While the technical advances in polarized $^3$He have been largely motivated by work on polarized targets for nuclear and high energy physics, $^{129}$Xe polarization was advanced in the optical pumping studies led by Happer and co-workers [Zeng et al., 1985]. Early in the 1980s they began extensive investigations of spin exchange between noble gases and optically pumped alkali-metal vapors [Happer et al., 1984]. They studied many processes involved in optical pumping of alkali-metal vapors in the presence of buffer gases providing extensive data on the xenon-Rb system [Zeng et al., 1985].

$^{129}$Xe polarization of nearly 100% in small cm$^3$ volumes was produced. Experiments included studies of $I = 3/2$ $^{133}$Xe as well as a radioactive isotope ($^{131}$Xe$^m$, $^{133}$Xe and $^{133}$Xe$^m$) [Calaprice et al., 1985]. The work of Cates and Happer, with co-workers [Cates et al., 1990, Gatzeke et al., 1993], on polarized frozen $^{129}$Xe as a means for accumulating large quantities of polarized gas, may have been the initial inspiration for the development of MRI with laser polarized xenon. The first experiment at Stony Brook with gas polarized in Princeton relied on freezing the xenon for transport by car. The magnetization lifetime of frozen $^{129}$Xe is generally much longer than in the gas phase [Gatzeke et al., 1993].

Studies of spin exchange between Rb and lighter noble gases $^{21}$Ne [Grover, 1983] and $^4$He [Chupp and Coulter, 1985, Chupp et al., 1987] were motivated by nuclear physics applications, in particular the use of symmetry violations such as Parity (P) and Time Reversal (T) to study weak interactions in the presence of the dominant strong and electromagnetic interactions [Chupp et al., 1988]. Several experiments used $I = 3/2$ $^{21}$Ne and $^4$He simultaneously to search for quadrupolar interactions such as a possible dependence of nuclear binding energy on orientation with respect to an assumed absolute rest frame of the Universe [Chupp et al., 1989]. These pulsed NMR experiments were probably the first applications that specifically used laser polarized rare gases to enhance rare gas NMR signals by many orders of magnitude.

A variety of experimenters have since used laser polarized $^3$He and other noble gases to enhance NMR measurements. The low temperature work at Ecole Normal Superieur has used NMR to measure polarization and probe such phenomena as spin waves [Tastevin et al., 1985] and the properties of fermi liquids [Leduc et al., 1987], and $^3$He-$^4$He mixtures [Himbert et al., 1989, Nacher and Stolz, 1995]. Geometric phases have been measured with $^{129}$Xe [Appelt et al., 1995]. Measurement of the NMR splittings of $^{129}$Xe and $^3$He in the presence of an electric field is used to search for $T$ violation [Rosenberry, 1999]. This experiment used a Spin Exchange Pumped Zeeman Maser [Chupp et al., 1994b, Stoner et al., 1996] that exploits cavity-spin coupling and the population inversion pumped into the nuclear spins [Robinson and Myint, 1964, Richards et al., 1988].

Conventional NMR research with $^{129}$Xe (i.e. not laser enhanced) has focused on variety of problems including cross polarization, molecular dynamics, xenon molecules (e.g. XeF$_2$), diffusion in porous media, polymers, and liquid crystals. $^{131}$Xe has been used to study quadrupolar relaxation on surfaces, in macromolecules, and porous media. Xenon has been extremely important because it is normally gaseous, can be easily frozen or liquified, is relatively soluble, and is characterized by large NMR chemical shifts up to 500 ppm between the gas and dissolved phases. Alex Pines and his group recognized that many of these applications of NMR research could be enhanced with laser polarized $^{129}$Xe [Rafferty et al., 1991], and inspired the original pursuit of MRI with laser polarized noble gases [Song et al., 1999].

## 2 Nuclear Polarization Techniques

Polarization of $^4$He and $^{129}$Xe can be contemplated by brute-force, Stern-Gerlach, or by optical-pumping techniques. Brute-force polarization uses high magnetic fields and low temperatures to create an imbalance of nuclear spin state populations. At low temperatures $^4$He atoms in the liquid phase are indistinguishable obeying Fermi-Dirac statistics with the consequence that negligible polarization can be achieved at reasonable magnetic fields. (The effective spin temperature does not drop below the Fermi Temperature of $T_F = 0.18K$.) For solid $^4$He, the lattice positions, not the momentum states, distinguish atoms, and Boltzmann statistics describe the polarization. The result is that solid $^4$He can be polarized, achieving the equilibrium value

$$P_T \approx \tanh(\mu B/kT),$$

which at 10 mK and 10 T gives $P_T = 91.5\%$. Low temperature alone is not sufficient to produce solid $^3$He – high pressures are also needed. The Pomeranchuk method involves cooling the liquid in an applied magnetic field under pressure. For $T < 0.32$ K, the liquid’s entropy is less than the solid’s and the sample cools itself in a process similar to cooling by evaporation [Lomasmua, 1974]. Using this method to polarize, followed by rapid warming of the polarized $^3$He through the liquid phase, Forassatti [Frossati, 1998] has proposed producing a thousand liters of highly polarized $^3$He per day. It is not known whether $^{129}$Xe can be polarized in this way, though measured spin diffusion times seems favorable.

Stern Gerlach techniques have been used to produce beams of highly polarized $^3$He. However the tradeoffs of acceptance and polarization have limited fluxes to $\approx 10^{11}/s$ with $P_T = 0.9$ for a hexapole magnet. This is not sufficient for accumulation of useful quantities, though it is useful for applications where a trace amount of highly polarized $^3$He is required [Goldub and Lamoreaux, 1994].

Optical polarization employing either hyperfine spin exchange with an alkali-metal vapor [Bouchiat et al., 1983] for $^4$He and $^{129}$Xe or optical pumping of metastable helium atoms, for $^4$He [Colgrove et al., 1963] emerged as promising techniques with the availability of lasers. Both techniques are now used to produce liter quantities (at STP) with polarization $P_T > 50\%$ that are used for neutron polarization, polarized targets, and for medical imaging.

In all cases, relaxation of nuclear spin must be balanced by polarization rates. (Note that nuclear spin relaxation in a biological environment in vivo or in vitro is completely different from relaxation in a carefully prepared polarization system as discussed in sections 4 and 5.) Rare gas nuclear spin relaxation occurs by bulk collisions with impurities, dipole–dipole interactions in the bulk, magnetic field
gradients, and surface wall interactions. The most important impurity is paramagnetic O$_2$. Relaxation rates are proportional to the oxygen impurity level with rate constants $k$(O$_2$-He) = 0.3 s$^{-1}$/amagat [Jameson et al., 1988] and $k$(O$_2$-He) = 0.45 s$^{-1}$/amagat [Saam et al., 1996] at 14.1 kG and at room temperature with temperature dependence $T^{-1/2}$. (One amagat is the number density of a gas at STP). In order to achieve high $^3$He polarizations, O$_2$ impurity levels must be below parts per million. Relaxation due to dipole–dipole interactions have rate constants $k$(O$_{129}$Xe-$^3$He)=5 x 10$^{-6}$/s/amagat [Hunt and Carr, 1963] and $k$(O$_{129}$Xe-$^3$He)=4 x 10$^{-5}$/s/amagat [Mullin et al., 1990, Newbury et al., 1993]. Magnetic field gradient contributions to nuclear spin relaxation arise due to non-adiabatic evolution of the nuclear spin as the atoms move in the gradients between collisions. For the high densities encountered in most applications

$$\Gamma_{\Delta B} \approx D\frac{\sum B_i^2 |\nabla B_i|^2}{B^2}$$

(4)

Typically, magnetic field gradients of 0.3-1%/cm are sufficient for $^3$He and $^{129}$Xe polarization respectively. Wall interactions are moderately well understood. For $^3$He, the work of Timsit and Daniels described above shows that paramagnetic impurities and sticking time, dominated by diffusion of helium into the surface, are most important. Coating the surfaces of glass or fused silica with cesium has proved effective for attaining $^3$He relaxation times of 2 days or more [Cheron et al., 1995, Surkau et al., 1997]. For highly polarizable xenon atoms, the sticking times are much shorter, but relaxation rates can be reduced with silane wall coatings [Zeng et al., 1985, Oteiza, 1992, Sauer et al., 1999]. Sauer has shown evidence that $^{129}$Xe–proton dipolar interactions dominate relaxation in coated cells.

At 2T, $T_1 > 2$ hours has been observed for $^{129}$Xe indicating decoupling of the wall relaxation mechanisms.

### 2.1 Optical Pumping and Spin Exchange

Optical pumping [Kastler, 1956] is the means by which the internal degrees of freedom of a sample of atoms can be manipulated with light, and the angular momentum of the photons can be transferred with high efficiency to the atoms (see [Happer, 1972]). The most effective way to understand optical pumping and spin exchange is by derivation of rate equations describing these processes. For optical pumping, we begin by considering an atom with $J = 1/2$, such as an alkali-metal atom with nuclear spin $I = 0$. The polarization, $P$, is given by

$$P = \rho^{1/2} - \rho^{-1/2} \quad \text{and} \quad \rho^{1/2} + \rho^{-1/2} = 1.$$  

(5)

Both polarization and spin destruction processes must be considered. For polarization, we assume that the atoms are illuminated with right circularly polarized ($\sigma_+$) light, and we define the total the rate per atom of pumping out of the $m_j = -1/2$ state and into the $m_j = +1/2$ state as $\gamma_{opt}\rho(-1/2)$.

For atoms with resonant frequency $\nu_0$

$$\gamma_{opt}(\nu) = k \int d\nu' \Phi(\nu',\nu)|\sigma(\nu - \nu_0).$$

(6)

The laser intensity per unit frequency is $\Phi(\nu',\nu) = dI(\nu')/d\nu$, which is in general position dependent. The cross section for absorption of unpolarized light is $|\sigma(\nu)|$, and $k$ is a constant that accounts for the relative probability that an atom, after absorbing a photon, also absorbs its angular momentum. For alkali–metal atoms in the presence of sufficient buffer gas pressure to collisionally mix and randomize the spin projections in the $p$ states, $k = 1$.

The optical pumping rate equations for the two state system are

$$\frac{d\rho_{m_1/2}}{dt} = \gamma_{opt}(\nu,\nu_0) \rho_{m_1/2} + \frac{\Gamma_{SD}}{2} \rho_{m_1/2} - \frac{\Gamma_{SD}}{2} \rho_{m_{-1/2}}$$

(7)

We have included possible relaxation of electron spin polarization in the term $\Gamma_{SD}$.

For spin exchange pumped $^3$He, Rb spin relaxation is dominated by collisions with Rb atoms, $^3$He and $N_2$ and to a lesser degree by wall interactions [Wagshul and Chupp, 1994]. Walker has recently discovered a surprising magnetic field dependence to the Rb-Rb relaxation process that decouples at relatively low fields of a few hundred Gauss [Kadlecik et al., 1998]. This suggests a time scale much longer than characteristic of binary collisions between Rb atoms. Though the mechanism is not yet understood, it is clear that optical pumping at magnetic fields of a few kG can turn off the Rb-Rb collisions with the advantages of potentially higher Rb polarization or less laser power. Rb-Rb collisions are generally less important than Rb-He or Rb-$^{129}$Xe collisions. For $^3$He polarization, it is most effective to use high $^{3}$He density so that Rb-$^3$He collisions dominate the Rb spin destruction rate. For $^{129}$Xe, spin destruction is so strong that the same is effectively true, though xenon densities are much lower. Therefore the laser intensity requirements are determined by the Rb-noble gas spin destruction rate $\Gamma_{SD}$.

There are good spin destruction collisions, and there are bad ones. A good one, of course, results in a spin exchange to the noble gas nucleus. In a bad collision, the Rb atom looses its electron spin polarization to rotational angular momentum. It turns out that the ratio of spin exchange to spin rotation varies significantly among the alkali–metal atoms. Rb is worse than K, by nearly an order of magnitude, though the spin exchange rate constants are apparently approximately equal [Romalis et al., 1998]. This has become very important recently with the availability of high powered LDAs at 770 nm, the D1 wavelength for K. As long as it is practical to operate at temperatures of 250$^\circ$ C at which the density of K is sufficient for spin exchange to balance $^3$He relaxation, we can expect increased use of K as the spin exchange partner.

Radiation trapping is also a potential limitation to optical pumping in polarized targets [Holstein, 1947]. This occurs when the mean free path for the unpolarized photons is much less than the dimensions of
the pumping vessel. The incident \( \sigma_{\text{p}} \) photons can be reemitted (\text{i.e.} resonantly scattered) and depolarized. Each unpolarized photon can multiply scatter and depolarize many atoms and therefore radiation trapping can be thought of as an additional relaxation mechanism that is a function of incident laser power. Radiation trapping would limit the density of the mediating alkali-metal species in spin exchange pumped \(^3\)He targets. However molecular \( N_2 \) [Zeng et al., 1985, Chupp and Coulter, 1985] (for \(^3\)He) have been shown to effectively mitigate radiation trapping effects. At high magnetic field the Zeeman splitting of the \( S_{1/2} \) and \( P_{1/2} \) states causes the scattered photons to be off resonance and only very weakly absorbed in depolarizing transitions. The presence of \( N_2 \) or other molecular species quenches the \( P_{1/2} \) states non-radiatively reducing the branching ratio for radiative decay (\text{i.e.} resonant scattering) [Wagshul and Chupp, 1994].

Assuming that the complication of radiation trapping has been practically eliminated, the steady state solution to the rate equations predicts electron spin polarization

\[
P_S = \frac{\gamma_{\text{opt}}(I)}{\gamma_{\text{opt}}(I) + \Gamma_{SD}}
\]

and a time constant \( (\gamma_{\text{opt}}(I) + \Gamma_{SD})^{-1} \) that is typically milliseconds.

For atoms with nuclear spin, including alkali-metal atoms and metastable \(^3\)He atoms, the hyperfine coupling results in total angular momentum \( F \). Laser optical pumping must provide the angular momentum for complete atomic polarization, the time dependence becomes more complicated than the single exponentials that describe the two state system, the transients become longer, and the nuclear spin serves as a reservoir of angular momentum [Bhaskar et al., 1982, Nacher and Leduc, 1985, Wagshul and Chupp, 1994, Appelt et al., 1996]. However, the levels rapidly reach a spin temperature equilibrium mediated by electron spin exchange [Anderson and Ramsey, 1961] and it is sufficient to consider only the evolution of electron spin \( S \). For the metastability exchange, the discharge itself also leads to relaxation.

The spin exchange rate equations, including relaxation, can be written

\[
P_I = \gamma_{\text{SE}}(P_S - P_I) - \Gamma P_I
\]

where \( P_I = 2 < I_z > \) (for \( I = 1/2 \)) is the rare gas nuclear polarization and \( P_S = 2 < S_z > \) is the alkali-metal electron polarization. The steady state solution is

\[
P_I = P_S \frac{\gamma_{\text{SE}}}{\gamma_{\text{SE}} + \Gamma}.
\]

The goal is therefore to maximize alkali-metal electron spin polarization and effect long relaxation times so that \( \Gamma \ll \gamma_{\text{SE}} \).

For \(^3\)He polarized by spin exchange with Rb, \( \gamma_{\text{SE}} \) is typically many hours and relaxation times of days have been achieved, resulting in high polarizations greater than 50\%

be limited by many factors including wall relaxation, interactions with impurity gases (probably paramagnetic \( O_2 \)), and dipolar relaxation in \(^3\)He-\(^3\)He collisions.

For \(^{129}\)Xe, \( 1/\gamma_{\text{SE}} \) is typically several minutes but can be as short as 10 seconds. Relaxation times in silane coated cells seem to be 10-30 minutes at low magnetic fields, and several hours at 2T [Zeng et al., 1985, Oteiza, 1992]. Deuterated coatings have been suggested to reduce relaxation at low field [Sauer et al., 1999]. Relaxation is often dominated by wall collisions, though impurities and dipolar relaxation are also important.

In a collision between an alkali-metal atom with electron spin polarization and a rare gas atom with \( J = 1/2 \), the electron spin couples to the nuclear spin and to the rotational angular momentum of the pair [Happer et al., 1984]. The dominant contributions to the spin dependent hamiltonian are

\[
H' = \gamma N \cdot S + AK \cdot S + A_{\text{SE}} K \cdot S
\]

where \( A \) is the alkali-metal hyperfine interaction and \( A_{\text{SE}} \) is the spin exchange hyperfine interaction, both of which are in general position dependent. However the long range contributions vanish for spherically symmetric collisions, and only the Fermi-contact term acts, so that

\[
A_{\text{SE}} = \frac{8\pi}{3} 2\mu_B 2\mu_I \delta^3(R).
\]

Where \( \delta^3(r - R) = |\psi(R)|^2 \) is the probability that the alkali-metal valence electron (coordinate \( r \)) is at the position of the noble gas nucleus (coordinate \( R \)). Herman has shown that \( |\psi(R)|^2 \) is in fact enhanced due the electron exchange interactions as the electron is attracted by the positive charge of the nucleus [Herman, 1965]. An enhancement factor is defined in terms of the free alkali-metal electron wave function(\( \psi_0 \)) by \( |\psi(R)|^2 = |\psi_0(R)|^2 \cdot |\eta| \) varies from about 10 for Rb-\(^3\)He to 50 for Rb-\(^{129}\)Xe [Walker, 1989].

The hyperfine interaction \( H' \) is, of course, time dependent as an alkali-metal atom and rare gas atom move past each other. For \(^3\)He, the time scale is about \( 10^{-12} \) s because the collisions are always binary – in contrast to \(^{129}\)Xe which can form a Van der Waals molecule with an alkali-metal atom in a three body collision [Bouchiat et al., 1972]. The lifetime of this molecule can be \( 10^{-9} \) s or longer, limited in fact by the break up of the molecule in a collision with another buffer gas molecule. One consequence is that the rate constants for spin exchange are much different for \(^3\)He polarization and \(^{129}\)Xe polarization:

\[
k_{\text{SE}}(Rb-He) = 6 - 12 \times 10^{-20} \text{ cm}^3/\text{s} \quad \text{and} \quad k_{\text{SE}}(Rb-^{129}\text{Xe}) \geq 4 \times 10^{-16} \text{ cm}^3/\text{s},
\]

with this lower limit set by binary spin exchange in the absence of three body formation of Van der Waals molecules [Cates et al., 1992]. Spin rotation is a sink of angular momentum resulting from the coupling of the electron spin to the rotation of the alkali-metal–noble-gas pair, and is generally dominated by the heavier partner as discussed in [Walker and Happer, 1997].

If we neglect wall interactions, alkali-alkali collisions, and alkali-N\(_2\) collisions, the alkali-metal electron spin destruction rate reduces to the sum of spin exchange and spin rotation:

\[
\Gamma_{SE} D > k_S E[I] + k_S R[I]
\]

13

14
for a rare gas of number density \( I \). Since the incident, circularly polarized laser photons must balance this spin destruction rate, it is useful to consider the spin exchange efficiency

\[
\epsilon_{SE} = \frac{k_{SE}E}{k_{SE}E + k_{SR}R}
\]  

(14)

This quantity, in principle sets an upper limit on the “photon efficiency” (defined by Bhaskar et al., 1982) with which optical pumping can balance noble gas relaxation. In general, however, photon efficiency is much lower than \( \epsilon_{SE} \) because of other alkali–metal spin destruction mechanisms, necessarily inefficient optical transport of laser light into the cell, and the fact that lasers used in practical situations are broad band (as discussed below). The magnetic field dependence of spin exchange, spin rotation, and relaxation mechanisms are, of course, important, particularly in magnetic imaging applications at fields of 2T and greater [Hupper et al., 1984].

2.1.3 Lasers for Spin Exchange Pumping

Lasers have been the essential light source for successful polarized \(^{3}\)He and \(^{129}\)Xe experiments. Originally dye lasers were used, producing up to 1 watt near 795 nm with linewidths less than or comparable to the pressure broadened Rb absorption linewidth [Chupp et al., 1987]. (Typical standing wave dye laser linewidths are 30 GHz; the Rb D1 line is broadened by about 18 GHz per amagat of \(^{3}\)He.) In the late 1980’s, high powered arrays of laser diodes (LDAs) became available, and their suitability for spin exchange pumped \(^{3}\)He polarization was of immediate interest [Wagshul and Chupp, 1989]. Simultaneously the Titanium:sapphire laser was developed for high power applications and soon became commercially available. By about 1990, the cost per useful watt of LDAs and Ti:sapphire lasers was comparable, but a single Titainium:sapphire set up could produce 5 watts whereas the most powerful available LDA was 2 watts. Also, 795 nm was at the edge of reliable LDA production. Several experiments were undertaken each using one or more Titainium:sapphire laser. Experiment E142 at SLAC ran with up to five [Middleton et al., 1993].

By 1994, bars of LDA’s had become available with a price per watt of $500 and falling rapidly. This has been the single most important technology advance driving this field. By comparison, a Ti:sapphire laser pumped by a large frame Argon ion laser has a price per watt of $15K-$20K. Current LDA prices are $100-$200 per watt. LDA’s will dominate future experiments and make polarized \(^{3}\)He and \(^{129}\)Xe much more widely accessible.

2.1.4 Optical Pumping with Laser Diode Arrays

Laser diodes are widely recognized as work horses in atomic and optical physics. For example, near IR lasers used in cooling and trapping of K, Rb, and Cs, are generally single mode (line widths on the order of MHz) and low powered (50-100 mW with 500 mW amplifiers commonly in use). High powered LDAs are produced for a variety of commercial, industrial, and communications applications (including stripping the paint from battle ships). Currently available LDA packages utilized for Rb optical pumping consist of bars of individual LDAs. Bars with 20-30 watt nominal output consisting
of about 20 1-3 watt elements with GaAlAs and InGaAsP can be purchased for a few thousand dollars each. The injection current and temperature of the device are used to tune the arrays to 794.7 nm, the Rb D1 wavelength, and typical bandwidth is 2-4 nm. Recently, 20 watt bars at 770 nm, the K D1 wavelength have become commercially available.

Though the broadband light from a LDA is spread over 1-2 nm, much greater than the 0.1-0.2 nm typical homogeneously broadened absorption line width of Rb, the convolution of the light intensity and the absorption cross section provides a sufficiently high photon absorption rate that light 1 nm or more off resonance can effectively polarize Rb. The photon absorption rate of laser light by Rb atoms is defined in equation 6. In the case of LDAs, $\Phi(\nu)$ is spread over 2 nm or more, as shown in figure 3. The total power output per laser is about 15 watts. As the light propagates through the cell (along $z$), it is absorbed by the Rb at a rate

$$\frac{d\Phi(\nu)}{dz} = -\sigma(\nu) [\Phi(z)(1-P_z(z))$$

where

$$P_z = \frac{\gamma_{\nu}(z)}{\gamma_{\nu}(z) + \Gamma_{SD}}$$

(16)

Computer modeling based on numerical integration of these equations is generally reported by several authors to predict results for $^3$He and $^{129}$Xe polarization that are within 10% of that measured [Wagshul and Chupp, 1994, Walker and Happer, 1997, Smith, 1998, Appelt et al., 1998].

Figure 3: Profile of intensity vs. wavelength for a typical GaAlAs LDA (from Optopower Corp.), indicated by a solid line. The total power output per laser is about 15 watts. The dotted and dashed lines show the laser profile 5 cm and 10 cm into the cell, respectively, for cell parameters of: 10 amagat of $^3$He and 0.1 amagat $N_2$ at 180°C (left); 0.1 amagat of $^{129}$Xe, 0.2 amagat $N_2$, and 2.7 amagat He at 110°C (center); and 2.2 amagat of $^{129}$Xe, 0.2 amagat $N_2$, and 0.5 amagat He at 110°C (right).

The requirement for significant Rb polarization is $\gamma_{\nu} > > \Gamma_{SD}$. For $^3$He, a large portion of the initial laser spectral profile is useful. In figure 3 a, we show the spectral profile at three positions along the axis of the cell for $^3$He density of 10 amagat with 0.1 amagat $N_2$. As light burns its way into the cell, the central portion of the spectral profile is absorbed more strongly than the wings. Therefore, the front of the cell is essentially polarized by the near-resonance light. The more off-resonance light polarizes a greater portion of the cell’s length and is more important in the back of the cell. The large optical thickness of Rb typically used for $^3$He polarization ($[\text{Rb}] = 10^{14-15}/\text{cm}^3$) is the main reason polarization with LDAs can be so effective. The pressure broadening of the Rb absorption line is of secondary importance in most cases; in fact, the gains due to pressure broadening tend to saturate above 4-5 amagat of $^3$He.

The situation is quite different for $^{129}$Xe. The spin destruction rate of Rb due to $^{129}$Xe is so much greater than that due to $^3$He that much greater laser intensity or spectral density (or both) is required to satisfy $\gamma_{\nu} > > \Gamma_{SD}$. Consequently, only a much narrower part of the LDA spectrum is useful for $^{129}$Xe, even at very low xenon concentration, as illustrated in figures 1b and 1c. Broadening the absorption line with a buffer gas such as helium, which does not appreciably increase $\gamma_{\nu}$, can significantly increase the power absorbed from the LDA spectrum, though it is only practical to increase the absorption line to approximately 0.5 nm with 10 amagat of buffer gas [Driehuys et al., 1996].

The problem of balancing trade-offs of noble gas polarization, production rates, volumes, and/or magnetization involves exploring a large parameter space. For example, increasing the total density of gas produces pressure broadening of the Rb absorption line, increasing the integral $\gamma_{\nu}$, but also increasing $\Gamma_{SD}$. Greater Rb density increases $\gamma_{\nu}$ but also increases $\Gamma_{SD}$ and the absorption of the light as it propagates through the pumping cell, reducing $\gamma_{\nu}$ further into the cell. For example, one can produce 60% $^{129}$Xe polarization in 7.5 torr-liters per hour per watt of standard LDA laser power. The actual photon efficiency is less than 0.5%, compared to the 4% efficiency for Rb-$^{129}$Xe prediction [Walker and Happer, 1997]. A standard liter would require about 100 watts. For $^3$He, over 50% polarization of more than 1 liter with 30 watts of laser power has been achieved.

Significant improvement of $^{129}$Xe polarization is possible if the LDA light is spectrally narrowed. In figure 4 we show a calculation of the expected Rb and $^{129}$Xe polarizations for different combinations of xenon density, temperature i.e. Rb density, etc. for 15 watts of laser power. The total pressure is held constant at 2000 torr; for example with 500 torr xenon, we use 100 torr $N_2$, and 1400 torr helium. We show results for two cases: low xenon density, i.e. 100 torr xenon and high helium buffer gas density suggested by Driehuys et al. (1996); and high xenon density 1500 torr xenon used by Rosen et al. (1999). Narrowing LDA spectra provide significant gains in either case. The width parameter for the LDA is essentially a measure of FWHM of the spectrum. We emphasize that narrowing in this case does NOT mean that the lasers need to be single mode as in the case of cooling/trapping/BEC.

Recent progress on narrowing off the shelf LDAs in external cavities [MacAdam et al., 1992] has been reported [Nelson et al., 1999] and [Zarger et al., 1999]. For example, the Littman-Metcalf configuration has been used with 2 watt off-the-shelf LDAs. The spectral profiles for 1.0-1.5 watts output have FWHM 20-30 GHz, and the central frequency could be tuned over several nm. Simulations of the expected performance show that a single 15 watt LDA could be replaced by a 3 watt external-cavity
and 14 GHz/amagat for N$_2$ [Che’en and Takeo, 1957]. This greatly exceeds the natural (5.7 MHz) and Doppler widths. Under these conditions, broad-band laser light, from standing wave lasers or laser diode arrays, is effective for optical pumping [Wagshul and Clapp, 1989, Cummings et al., 1995]. For metastability exchange polarization of $^3$He, the densities are hundreds of times less and Doppler broadening is dominant. Effective optical absorption by all of the atoms requires careful matching of the laser frequency distribution to the Doppler distribution. Another distinction between spin exchange pumping and metastable pumping is optical thickness. We can define an absorption length for polarized resonant photons with $m_l = +1$

$$\lambda_0 = 2/(n_m \sigma_0 (-1/2)^{-1})$$

(17)

where $n_m$ is the number density of metastable atoms or the alkali-metal vapor, and $\sigma_0$ is the resonant absorption cross section for unpolarized light. For spin exchange pumping the absorption length is less than the dimension of the optical pumping vessel leading to the radiation trapping problems discussed earlier. $\lambda_0$ is generally more than 1 meter for metastability pumping, and radiation trapping does not present any limitations. Under optimum conditions, samples of $^3$He gas at a density 1.5 x 10$^{16}$/$\text{cm}^3$ can be pumped to an equilibrium polarization of over 80% with polarization rates of 10$^{18}$ atoms/sec. The dependence of the equilibrium polarization and polarization rate on gas pressure, discharge level and frequency has been studied in detail by [Lorenzon et al., 1993].

Metastability exchange polarization of $^{129}$Xe in a discharge has been studied by a few groups with little success [Schaerer, 1969, Lefevre-Seguin and Leduc, 1977]. Though electron polarization in the metastable states indicates effective optical pumping, the discharge may induce excessive nuclear spin relaxation. As an alternative, the metastable $^5$P$_{6S}$ $J=2$ state may be populated by two photon laser excitation with ($\lambda=317$ nm), or a metastable atomic beam used to separate the discharge from the optical pumping region. These methods will probably not become practical for producing large quantities of polarized $^{129}$Xe, but may be useful to study the physical processes at work.

2.2 Metastability Exchange

In the metastability exchange scheme, a sample of polarized $^3$He atoms is excited by a weak electric discharge so that a fraction of the atoms ($\sim 10^{-5}$) is in the metastable $2^3S_1$ state. This long-lived state can be optically pumped to the $2^3P_0$ and $2^3P_1,2$ states by 1.083 $\mu$m circularly polarized light. For example, the $2^3S_1$ state is split into hyperfine levels with $F = 1/2$ and 3/2. Pumping into the $F = 3/2, m_F = +3/2$ state (the C9 line) state produces high atomic and nuclear polarization of the metastable fraction. Resonant exchange of the excitation energy in metastability exchange collisions does not affect the nuclear spin, because the collision duration is short compared to the hyperfine mixing time. Thus, the ground state population attains high nuclear polarization [Colgrove et al., 1963].

In general, the same principles of optical pumping apply to metastability exchange and spin exchange. There are, however, some crucial distinctions. One distinction is the ratio of widths of the atomic absorption line and the Doppler profile. For spin exchange, the high density of $^3$He or $^{129}$Xe and N$_2$ lead to homogeneous collisional broadening of the Rb absorption line of $\approx 18$ GHz/amagat for $^3$He and 14 GHz/amagat for N$_2$ [Che’en and Takeo, 1957]. This greatly exceeds the natural (5.7 MHz) and Doppler widths. Under these conditions, broad-band laser light, from standing wave lasers or laser diode arrays, is effective for optical pumping [Wagshul and Clapp, 1989, Cummings et al., 1995]. For metastability exchange polarization of $^3$He, the densities are hundreds of times less and Doppler broadening is dominant. Effective optical absorption by all of the atoms requires careful matching of the laser frequency distribution to the Doppler distribution. Another distinction between spin exchange pumping and metastable pumping is optical thickness. We can define an absorption length for polarized resonant photons with $m_l = +1$

$$\lambda_0 = 2/(n_m \sigma_0 (-1/2)^{-1})$$

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where $n_m$ is the number density of metastable atoms or the alkali-metal vapor, and $\sigma_0$ is the resonant absorption cross section for unpolarized light. For spin exchange pumping the absorption length is less than the dimension of the optical pumping vessel leading to the radiation trapping problems discussed earlier. $\lambda_0$ is generally more than 1 meter for metastability pumping, and radiation trapping does not present any limitations. Under optimum conditions, samples of $^3$He gas at a density 1.5 x 10$^{16}$/cm$^3$ can be pumped to an equilibrium polarization of over 80% with polarization rates of 10$^{18}$ atoms/sec. The dependence of the equilibrium polarization and polarization rate on gas pressure, discharge level and frequency has been studied in detail by [Lorenzon et al., 1993].

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2.2.1 Lasers for Metastability Exchange

The success of metastability exchange based $^3$He applications has also been strongly supported by laser developments. The first lasers for 1083 nm were color center F + and NdF. Two Nd based laser materials, Nd:Yap [Schearer and Leduc, 1986, Bohler et al., 1988] and Nd:LNA [Hamel et al., 1987] are now available. Five watts of laser power at the helium transition is routinely obtained by pumping a crystal of Nd:LNAla with a CW, krypton arc-lamp in a commercial Nd:YAG cavity. The laser can be tuned to the different pumping lines by use of a solid uncoated etalon in the cavity. [Aminoff et al., 1989].

LDA pumped LNA lasers have also been used [Hamel et al., 1987]. The most recent laser development for metastability pumping of $^3$He is the diode pumped fiber laser and fiber laser amplifier [Goldberg et al., 1998, Lee et al., 1999].
2.3 Polarization and Delivery Systems

Several devices combine optical pumping and polarization with delivery of the polarized gas to a subject or a storage container. For $^3$He, the basic designs used for polarized targets are applied for both metastability exchange and spin exchange pumped systems. The metastability exchange systems have a valved port that connects to a transport container. Gentile has recently presented a relatively compact and inexpensive compressor that may see wide use [Gentile et al., 1999]. For spin exchange systems an additional valve of the appropriate material is straightforward. With $^4$He, polarization relaxation times of several days typical in glass containers, transport almost anywhere can be contemplated.

For $^{129}$Xe, the high rate of Rb electron spin depolarization in spin-rotation collisions limits the rate of $^{129}$Xe production, and a method of accumulation is essential. Cates, Happer, and coworkers have shown that frozen and liquid xenon provide very long nuclear spin relaxation times for $^{129}$Xe [Cates et al., 1990, Sauer et al., 1999], and that freezing is an ideal accumulation method [Driehuys et al., 1996]. Relaxation times are on the order of an hour at liquid N$_2$ temperatures and days at liquid He temperatures [Gatzke et al., 1993].

For human studies, it is sufficient to collect the polarized gas in a plastic bag, where it is held for several minutes before inhalation and a breath-hold. For animal studies, voluntary breathing is not possible, and delivery to the animal requires a polarized gas ventilator. There are many technical difficulties, and very few such ventilators have been constructed [Hedlund et al., 1999, Rosen et al., 1999].

Delivery of polarized gas by shipping from a geographically centralized production facility is one possible operating procedure for the future of medical imaging. In the case of $^3$He, relaxation times of several days are routine in clean, uncoated, glass containers [Middleton et al., 1993, Chupp et al., 1996], and all that is needed is a portable holding field magnet. Magnetic fields of 10-20 Gauss are sufficient to dominate the magnetic field gradients expected in normal commercial shipping. Both battery operated wire wound coils [Hasson et al., 1999a] and permanent magnet systems [Surkau et al., 1999] have been developed. If liquid He transport of polarized $^{129}$Xe becomes practical, its shipment would also be feasible.

3 Basics of MRI

Conventional magnetic resonance imaging (MRI) creates a map of the distribution of water protons in the body and has become one of the most versatile and powerful imaging methods in clinical medicine [Wehrli, 1995]. MRI uses static, RF, and gradient magnetic fields to create images. A large, static magnetic field, $B_0$, generally between 0.5 to 1.5 Tesla creates an axis of quantization, energy level separation, and energy level population difference for the spin states. A radio frequency field, $B_1(t)$, oscillating at the proton Larmor frequency causes transitions between the spin states and converts longitudinal magnetization into detectable transverse magnetization. Finally, pulsed magnetic field gradients, $\partial_B^x(t)$, $\partial_B^y(t)$, or $\partial_B^z(t)$, are used to both localize and spatially encode the nuclear spin magnetization in order to create an image. Here we present a synopsis of conventional MRI. A complete treatment can be found elsewhere [Callaghan, 1991]. In addition, we review specific aspects of MRI related to imaging laser-polarized noble gases.

3.1 Nuclear Magnetic Resonance

MRI is an application of NMR [Abragam, 1961] with the fundamental relationship given by the Larmor equation,

$$\omega_0 = \gamma B_0.$$  \hspace{1cm} (18)

The precessing spins are detected by tipping the magnetization by an angle $\alpha$ with a radio frequency pulse, $B_1(t)$ applied orthogonal to the $B_0$ field. The signal recorded as a function of time in a pick-up coil is,

$$s(t) \propto \omega_0 M \sin \alpha e^{-i\omega_0 t},$$  \hspace{1cm} (19)

where $M$ is the total magnetization of the system, and $\alpha$ is the “tip angle” of the magnetization relative to the axis defined by $B_0$.

3.2 One-dimensional imaging

Lauterbur realized that a map of the spatial distribution of the magnetization could be obtained by acquiring the NMR signal in the presence of a magnetic field gradient [Lauterbur, 1973]. The frequency of the nuclear spin is then directly proportional to the position of the spin and given by,

$$\omega(x) = \gamma (B_0 + x G_x)$$  \hspace{1cm} (20)

where $x$ is the position of the spin and $G_x$ is the gradient of $B_0$ along the $x$ axis:

$$G_x = \frac{\partial B_x}{\partial x}.$$  \hspace{1cm} (21)

The time evolution of the transverse magnetization is given by,

$$s(t) = \kappa M(x) e^{-i(\gamma (B_0 + G_x) t)}$$  \hspace{1cm} (22)

$$s(t) = \kappa M(x) e^{-i\omega_0 t} e^{-i\gamma G_x t}$$  \hspace{1cm} (23)

Where $\kappa$ is a calibration constant that depends on $\omega_0$, $\alpha$, and electronic and geometric factors. The only interesting component of $s(t)$, from an imaging point of view, is the additional frequency due to
the magnetic field gradient. Moving into a reference frame rotating at \( \omega_0 \), the time evolution of the magnetization is given by,

\[
s_p(t) = \kappa M(x) e^{-i\gamma G_x \omega t}.
\]  

(24)

The signal \( s_p(t) \) is detected by mixing signals from an oscillator at \( \omega_0 (\approx 64 \text{ MHz at } 1.5 \text{ T}) \) with \( s(t) \). One practical consequence of detection in the rotating frame is that the signals can be sampled at audio frequencies rather than RF frequencies. Again, see [Callaghan, 1991] for a complete description.

We now consider a one dimensional distribution of spins along the x-axis. The time evolution of the magnetization is given by

\[
s_p(t) = \kappa \int M(x) e^{-i\gamma G_x \omega t} dx
\]  

(25)

\[
= \kappa \int M(\omega) e^{-i\omega x} dx
\]  

(26)

This is the Fourier transform of \( M(x) \). Mansfield and Grannell showed that a one-dimensional image could therefore be created by taking the Fourier transform of the NMR signal in the presence of a magnetic field gradient [Mansfield and Grannell, 1973].

\[
M(\omega) = \frac{1}{\pi} \mathcal{F}(s_p(t))
\]  

(27)

### 3.3 MRI and k-space

For imaging, the goal is to create a plot of the intensity of the magnetization as a function of a spatial coordinate. A more appropriate representation for MRI is a coordinate system with spatial dimensions \( x \) and inverse spatial dimensions \( k_x \) where,

\[
2\pi k_x = \gamma G_x t.
\]  

(28)

Equation 26 can then be rewritten

\[
s(k_x) = \int M(x) e^{-i2\pi k_x x} dx
\]  

(29)

In this formulation, \( k_x \) and \( x \) are the conjugate Fourier variables. The Fourier transform with respect to \( k_x \) provides a one dimensional map of the magnetization. The applied gradient, and hence \( k_x \), may be time dependent:

\[
2\pi k_x(t) = \gamma \int_0^t G_x(\tau) d\tau
\]  

(30)

\[
s(k_x) = \int M(x) e^{-i2\pi k_x x} dx
\]  

(31)

Generalizing to two dimensions, we then have,

\[
s(k_x, k_y) = \int \int M(x, y) e^{-i2\pi [k_x x + k_y y]} dx dy
\]  

(32)

Much of the progress in MRI over the last decade has been made by controlling the amplitudes and durations of gradients to appropriately sample \( k \)-space. These advances have been made possible by improvements in the hardware that produce the magnetic field gradients.

It is important to realize that each point acquired in \( k \)-space is spread throughout real space. The point at \( k_x = 0 \) represents the DC component of the magnetization and is proportional to the magnitude. As \( |k_x| \) increases, we measure the Fourier coefficients of higher frequency terms. By summing together all of the Fourier components in real space, one obtains an image of the magnetization. Artifacts in MRI arise because some of the terms in \( k \)-space are not sampled correctly or are lost. For example, a beating heart introduces time dependence not due to \( G_x(t) \). The artifact does not appear at one location in real space, rather it is spread according to the sampling error in \( k \)-space. A solution to such an artifact is cardiac gating of the signal, triggered by heart monitors.

Another important concept in \( k \)-space is prephasing and rephasing of transverse magnetization. Applying a gradient adds a phase to the spins that depends on their position in the sample.

\[
\phi(x) = \gamma \int k_x(t) dt
\]  

(33)

If the direction of the gradient is reversed, the spins at each position acquire an opposite phase. When the \( \int G_x(t) dt \) of the two gradients is of equal magnitude, all transverse magnetization is in phase and a gradient echo occurs. In the language of \( k \)-space, we first move to a point where \( k_x = 0 \). Changing the sign of the gradient changes the direction we move in \( k \)-space. The gradient echo occurs when we traverse the point where \( k_x = 0 \). Most pulse sequences are designed to symmetrically sample \( k \)-space in order to maximize signal-to-noise.

### 3.4 Imaging Sequences

In most cases an MRI tomograph is a two dimensional image of a slice of the body. The slice is isolated by selective excitation of spins along the third dimension. The spatial information is encoded by either frequency dispersion or phase dispersion as discussed in the sections below.

#### 3.4.1 Selective Excitation

Slice selection is typically accomplished by simultaneous application of a magnetic field gradient and a shaped RF pulse with relatively long duration (1 - 10 ms) and correspondingly narrow bandwidth.
This creates a frequency ramp along the direction of the gradient, and the shaped RF pulse excites spins only within a relatively narrow slice. The sinc pulse, \( \text{sinc}(t) \), is the most common because its fourier transform is a rectangle. In practice, the sinc shape does provide a reasonable approximation of a rectangular pulse in space coordinates. The combination of a gradient and a frequency selective pulse only excites spins within a region defined by,

\[
\Delta z \approx \frac{2\pi}{G_z \tau}
\]

where \( G_z \) is the strength of the magnetic field gradient and \( \tau \) is the duration between the first zero crossings of the sinc pulse.

### 3.4.2 Back Projection Imaging

Back projection imaging in MRI detects the NMR signal in the presence of a magnetic field gradient, applied immediately after the slice selective RF pulse. This was the first type of imaging to be performed [Lauterbur, 1973] and is most directly related to other imaging methods such as CT or PET. For the most part, back projection imaging has been replaced by fourier imaging. However, it still maintains a niche in studies of tissues with a short transverse relaxation time, \( T_2 \). In laser polarized noble gas imaging, back projection imaging is useful because all views acquired contain the DC component of \( k \)-space, which is proportional to the total intensity of the image. Therefore, if image intensity changes from pulse to pulse due to a different amount of gas, it is possible to normalize the acquired signals for proper reconstruction. This is not possible in fourier imaging sequences such as gradient echo imaging.

The pulse sequence needed for two dimensional back projection imaging is shown if figure 5. The frequency selective RF excitation pulse only excites spins in a slice of magnetization along the z-axis in the magnet. Signal acquisition commences immediately after the RF pulse is applied, and the NMR signal is recorded in a constant magnetic field gradient. The direction of the applied gradient is varied by changing the magnitude of the x gradient and the y gradient according to

\[
G_x = G \cos(\phi_i) \quad (35)
\]

\[
G_y = G \sin(\phi_i) \quad (36)
\]

The different amplitudes in the x projection and y projection gradients are represented in figure 5 by the lines of different heights. Each radial step in \( k \)-space corresponds to a different value of \( \phi_i \). For each step, a slice selective pulse is followed by application of the gradients during which the the MRI signal is acquired. Typically \( \phi \) is varied from 0 to \( 2\pi \) in 128 steps. The sampling of \( k \)-space, shown in figure 6, is radial. Back projection images are reconstructed with a specialized algorithm and not by a two dimensional fourier transform.

**Figure 5**: Pulse sequence for Back Projection imaging in two-dimensions. The slice-selective gradient and the frequency-selective RF pulse only excite spins in a slice or slab along the z-axis. The half sinc slice-selective pulse does not require that the transverse magnetization be refocused. The two projection gradients are varied in a sinusoidal pattern.
3.4.3 Gradient Echo Imaging

All the elements of two-dimensional fourier MRI are contained in the gradient echo imaging sequence shown in figure 7. Slice selection and read-out gradients are applied as in back projection. The main difference is phase-encoding, first proposed in [Kumar et al., 1973] and later modified in [Edelestein et al., 1980]. Phase encoding now forms the basis of many MRI pulse sequences. In phase encoding, phase dispersion occurs during an interval $t_1$ before the signal is acquired during the interval $t_2$. The duration of $t_1$ or the phase-encode gradient can be varied to step through $k_y$-space, with $t_1$ fixed. Discrete samples are acquired during the interval $t_2$ to form a two dimensional dataset. The two-dimensional fourier transformation yields a correlation spectrum in $f_1$-$f_2$ space or real space.

The slice selective pulse in the back-projection imaging sequence of figure 5 is a self-refocussing pulse, allowing the magnetization to be sampled immediately following the RF pulse [Geen and Freeman, 1991]. In general one needs to apply a slice refocussing gradient of opposite magnitude after the RF pulse so that the spins are in phase at the beginning of acquisition. This is shown in figure 7. The area of the negative gradient must be one half the area of the slice selection gradient pulse. At the same time, the read-out dimension is prephased and the phase encoding gradient is applied. Prephasing in the read-out dimension $k_x$ is done to allow symmetric sampling of $k$-space by first moving in the negative $k_x$ direction before the read-out gradient moves in the positive $k_x$ direction. Phase encoding gradients are applied along the $y$-dimension. Part of the trajectory through $k$-space during the gradient-echo

Figure 6: Sampling of $k$-space by back-projection imaging. In this example, we illustrate just the first few sampled rays obtained by adjusting the gradients according to equation 36

Figure 7: Gradient echo imaging (GRAS or FLASH). Magnetization is sampled in $k_x$ and $k_y$ as shown in figure 8. A two-dimensional fourier transform of uniformly sampled $k$-space creates the image.
The phase-encode gradient varies from scan to scan and allows complete sampling of $k_y$. The readout gradient is prephased to $-k_x^{\text{max}}$ and runs to $+k_x^{\text{max}}$. The resolution of the image is determined by the value of $k_x^{\text{max}}$ and the field-of-view of the image is determined by the step size in $k$-space.

Figure 8: Sampling of $k$-space by the gradient echo pulse sequence. The phase-encode gradient varies from scan to scan and allows complete sampling of $k_y$. The readout gradient is prephased to $-k_x^{\text{max}}$ and runs to $+k_x^{\text{max}}$. The resolution of the image is determined by the value of $k_x^{\text{max}}$ and the field-of-view of the image is determined by the step size in $k$-space.

sequence is shown in figure 8. Starting in the middle of $k$-space particular values of $k_y$ and $k_x$ are determined by the phase-encode and read-out prephase gradients. The amplitude of the phase-encode gradient is changed for the next step to move to a different point in $k_y$. By continuing to raster across $k_x$ for the different values of $k_y$, a complete and even sampling of $k$-space is achieved. In typical imaging sequences, $k_x$ is acquired with 256 datapoints and $k_y$ with either 128 or 256 datapoints. Each value of $k_y$ requires repeating the sequence. This is not true for $k_x$, which is called the free dimension in MRI. The number of $k_y$ points is typically determined by the desired resolution and the transverse relaxation time, $T_2$.

### 3.4.4 Chemical Shift Imaging

Chemical shift imaging or CSI is a hybrid application of imaging and spectroscopy. CSI is used to obtain spatially resolved spectral information or images of specific spectral components. Since gradients, which would disperse frequency across spatial dimensions, cannot be applied during acquisition, phase encode gradients are applied along either one, two, or three dimensions. A two-dimensional chemical shift imaging pulse sequence is shown in figure 9. After the gradients are applied, the magnetization freely precess in the $B_0$ field so that a frequency spectrum can be measured. This pulse sequence has been used to separate the different components of xenon magnetization in the rat brain and in the rat body [Swanson et al., 1997, Swanson et al., 1999b] as described section 5. CSI requires discrete steps through each dimension of $k$-space, and is much slower than back projection and gradient echo sequences, which step through only one dimension in $k$-space. To collect a 16 by 16 image, 256 different acquisitions are required.

Figure 9: Two dimensional chemical shift imaging (CSI) sequence. After slice selection, phase encode gradients are simultaneously applied along $k_x$ and $k_y$. After the gradients are applied, the magnetization precesses freely in the $B_0$ field so that a frequency spectrum can be measured.

### 3.5 Contrast in MRI

In tissue, the proton density varies only slightly, and MRI contrast therefore depends on changes in the magnetization characterized by relaxation times. The longitudinal or spin-lattice relaxation time $T_1$ determines the time required for the spin polarization to return to equilibrium following excitation by a radio-frequency pulse. If the spin magnetization is flipped by $\pi/2$, the longitudinal magnetization recovers according to,

$$M_z(t) = M_z^0 (1 - e^{-t/T_1}).$$

(37)
Figure 10: Conventional proton MRI tomographic images of the human brain. The images were acquired using spin-echo sequences. The detected magnetization depends on $T_1$ or $T_2^*$, depending on the echo time. This provides the contrast. The white matter and grey matter in each lobe of the cerebrum is distinguished in the $T_1$ weighted image on the left. Cerebral spinal fluid and tissue are distinguished in the $T_2$ weighted image on the right.

The transverse or spin-spin relaxation time $T_2$ is the time constant for decay of the transverse ($x$ and $y$) components of magnetization.

Both $T_1$ and $T_2$ weightings require the spin-echo sequence. The spin-echo sequence is similar to the gradient echo sequence, however a $\pi$ pulse refocuses spins that dephase in the intrinsic magnetic field inhomogeneities of the sample. The $\pi$ pulse is typically applied $\approx 10$ ms and $\approx 50$ ms after the initial RF pulse for $T_1$ and $T_2$ weighting respectively. In brain imaging for example, proton concentrations in white matter and grey matter are nearly equal, in contrast to the relaxation times given in table 1. For cerebral spinal fluid (CSF) motion effectively increases $T_2$. The relaxation time differences are exploited to produce images such as those shown in figure 10.

Table 1: Typical relaxation times for protons in brain tissue [Bottomley et al., 1984].

<table>
<thead>
<tr>
<th></th>
<th>$T_1$</th>
<th>$T_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grey Matter</td>
<td>1000 ms</td>
<td>110 ms</td>
</tr>
<tr>
<td>White Matter</td>
<td>650 ms</td>
<td>70 ms</td>
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</tbody>
</table>

3.6 Low Field Imaging

NMR with nuclei polarized by laser optical pumping is less dependent on large magnetic fields than conventional NMR, and the potential of low-field imaging has emerged. The signal to noise ratio (SNR) is the important parameter, and we therefore consider both signal and noise. For conventional, NMR, the signal $S$ due to a nuclear spin $I = h/2$ (for $^1$H, $^3$H, and $^{129}$Xe) with concentration $[I]$ is proportional to the product of precession frequency ($\omega$) and magnetization:

$$S \propto \omega \mu_I [I] P$$

where $I \omega = \mu_I B$ and the brute-force polarization is $P_I \approx \mu_B B$. Thus

$$S_{brute} \propto \mu_I^2 B^2 [I].$$

In contrast, for NMR with laser polarized nuclei, $P_I$ is independent of field, and

$$S_{laser} \propto \mu_I^2 [I]$$

The most important MRI noise sources are Johnson noise due to the pick-up coil resistance, $R_c$, amplifier noise, and dissipation in the sample due to loading characterized by $R_s$. Skin depth effects generally increase the coil resistance so that $R_c \propto \sqrt{B}$. The signal to noise ratios for brute-force and laser polarization for fixed bandwidth are

$$SNR_{brute} \propto \frac{B}{\sqrt{1 + \alpha B^{-3/2}}}$$

$$SNR_{laser} \propto \frac{1}{\sqrt{1 + \alpha B^{-3/2}}}$$

where $\alpha \approx (0.2 \; T)^{-3/2}$ [Edelstein et al., 1986]. This shows that above about 0.2 T, the signal to noise ratio for laser polarized NMR and MRI increases very little, i.e. is approximately independent of $B$.

There are many advantages that may be gained from NMR and MRI at lower fields. The cost of magnets is less, open geometry permanent and conventional magnets may provide more friendly NMR scanners (important for pediatrics), high field effects such as susceptibility dependence may be less. Low field work has been most effectively pursued by [Darrase et al., 1998]. They have shown that the combination of 0.1 T magnet and a low-polarization metastability pumped $^3$He polarizer can produce lung images with resolution comparable to standard $^{133}$Xe nuclear medicine techniques as shown in figure 11. One-dimensional images of polarized $^3$He have been to study diffusion effects [Saam et al., 1996]. Very low field imaging, at 0.003 T has been demonstrated by Walsworth and collaborators [Tseng et al., 1998].

4 Imaging Polarized $^{129}$Xe and $^3$He Gas

Though either $^3$He and $^{129}$Xe may be used for gas imaging, the majority of lung ventilation imaging studies, have used $^3$He. Helium has a number of advantages over xenon for creation of high-resolution
gas images: the magnetic moment of $^{3}\text{He}$ is nearly three times larger than that of xenon, and it has generally been easier to create high magnetization with $^{3}\text{He}$. $^{3}\text{He}$ polarizations are generally of 20%–50% whereas typical $^{129}\text{Xe}$ polarizations are currently 5%. A recent study imaging both gases concluded that in general helium is approximately 10 times more sensitive than xenon for MRI studies [Moller et al., 1999a].

Helium also has fewer biological effects than xenon. Helium is biologically inert and the only consequence of helium inhalation (apart from the well known change in voice pitch) is the risk of lowering the blood oxygen content due to oxygen being removed from the inhaled gas. Xenon on the other hand, is anesthetic at concentrations greater than 35%. These effects are well known and have been addressed in CT studies where xenon is used to measure regional cerebral blood flow (rCBF) by monitoring the spatial and temporal attenuation of x-rays.

Though helium provides greater signal strength and fewer medical complications, a major concern for widespread clinical studies with helium will be the limited supply of $^{3}\text{He}$ discussed earlier. Most studies are performed with $^{3}\text{He}$ gas with an isotopic concentration of approximately 99% at a cost of approximately 100-150 USD/liter. Xenon is present in the air at a concentration of approximately 0.04%. The abundance of the spin 1/2 isotope, $^{129}\text{Xe}$, is 26.44%. Naturally abundant xenon can be purchased for approximately 10 USD/liter. $^{129}\text{Xe}$ enriched to approximately 75% can be purchased for about 300 USD/liter. This price is determined primarily by demand and could drop dramatically if specific clinical uses are identified.

4.1 MRI of polarized gas: general concerns

4.1.1 Sampling of the magnetization

In conventional MRI, longitudinal magnetization is sampled by an RF pulse and then replenished by relaxation to thermal equilibrium with time constant $T_1$. For laser polarized gases, the longitudinal magnetization in the body must be replenished by a fresh supply of polarized gas. With each sampling of the magnetization, the RF pulse destroys a portion of the longitudinal magnetization. The non-equilibrium polarization created by optical-pumping would be entirely lost if sampled by a $\pi/2$ RF pulse. Since MRI requires many excitations in order to appropriately sample $k$-space, $\pi/2$ pulses cannot be used. The gradient echo sequence shown in figure 7 with a small tip angle is the most widely used approach. As the gas is sampled, the longitudinal magnetization decays leaving magnetization after $n$ pulses is given by

$$M_z(n, \alpha) = M_0 \cos^n(\alpha)$$

where $\alpha$ is the tip angle. Thus the sampled magnetization in the initial pulses is larger than that in the later pulses if the tip angle is constant. For instance, if the tip angle is 10 degrees, the value of the magnetization at the end will be only 20 percent the initial value for 128 pulses typically used to collect an image. This will cause different fourier components of $k$-space to have intensities modified by an exponential decay. This leads to blurring of the real space image as each pixel is the convolution of the true magnetization with a lorentzian (the fourier transform of the exponential loss of magnetization to pulsing.) Variable tip angle series have been used to economically use laser pumped magnetization in two species experiments that probe fundamental principles [Chupp et al., 1989, Oteiza, 1992]. An MRI sequence with variable pulse angle that produces the proper intensity of the fourier coefficients in $k$-space has been proposed [Zhao et al., 1996]. In principle, the variable flip angle sequence has better SNR since all of the magnetization is sampled. In practice, it is difficult to program this sequence on clinical MRI systems and most studies use a constant flip angle.

4.1.2 Diffusion and $k$-space

The basic description of MRI in section 3 neglected effects due to the diffusion of spins during acquisition. For gas imaging, these effects are large and present many problems, as well as a few opportunities. The main problem stems from the fact the positions and therefore the frequencies of the spins change due to diffusion as $k$-space is sampled during the read out gradient. Since $k$-space is sampled along one dimension, we consider the mean path length for one-dimensional self-diffusion $d = \sqrt{2Dt}$ where $D$ is the diffusion constant and $t$ is the time. At one atmosphere xenon has a self-diffusion constant...
of approximately 0.06 cm$^2$/s and helium approximately 2.0 cm$^2$/s. Therefore, during a typical MRI experiment with a sampling time of about 6 ms, the resolution for $^3$He is limited to about 1.5 mm. This assumes that the spins are free to diffuse. In the lungs’ alveoli and other porous media free diffusion is restricted. This allows measurement of pore size that has recently been applied to lung imaging. A full treatment of diffusion and restricted diffusion can be found in [Callaghan, 1991].

A number of studies have investigated this phenomenon. Edge enhancement of the signal intensity near the walls of rectangular glass cells in one-dimensional images of polarized $^3$He has been observed [Saam et al., 1996]. These studies were extended to demonstrate image distortion by molecular diffusion during the read out gradient [Song et al., 1998]. In this study, the investigators varied the strength of the gradient to follow the images from the strong diffusion regime to the weak diffusion regime. In another study using thermally polarized xenon gas diffusion was used to measure the tortuosity and the surface-to-volume ratio in a system of glass beads [Mair et al., 1999]. Work from the same group also showed that the gas diffusion constant can be measured in a single experiment [Peled et al., 1999].

4.2 Airspace Imaging

Lung ventilation imaging is currently based on nuclear medicine scintigraphy of either $^{133}$Xe or aerosol sprays with Tc. Laser-polarized noble-gas imaging research with animals and human subjects has already shown that tomographic (slice selected) high resolution images can be produced. A comparison of $^{133}$Xe scintigraphy and laser-polarized $^3$He images is shown in figure 12. The first human ventilation studies with $^3$He were performed in Mainz [Ebert et al., 1996] and at Duke. The group at Mainz (see figure 13) has continued with more clinical studies of volunteers with diagnosed lung diseases [Bachert et al., 1996; Ebert et al., 1996; Kauczor et al., 1997]. Other studies have looked at helium images of from the lungs of smokers [de Lange et al., 1999] and find ventilation defects in the few cases studies. In fact even apparently healthy, active, volunteers have ventilation defects that are revealed in the high resolution laser polarized $^3$He MRIs [Mueller et al., 1997]. A study of subjects with chronic asthma suggests that ventilation defects may allow a measure of the progression and treatment of the disease [Altes et al., 1999]. Though it will be some time before the utility of high resolution lung images is clarified, it is clear that they provide new information and raise new questions: for example, what are the mechanisms of signal destruction in diseased lungs [Kauczor et al., 1998]. The lungs are not the only organ amenable to gas imaging. The sinus cavities [Rizi et al., 1998] and bowel [Hagspiel et al., 1999] can also be imaged by using laser-polarized $^3$He or $^{129}$Xe.

Animal studies provide appropriate disease models for eventual clinical studies. An advantage of using a small animal model is that the amount of polarized gas needed to create an image is significantly reduced compared to an equivalent human study. Impressive results using specialized small pick-up coils to attain high resolution images of $^3$He in animal models have been obtained by the group at the group at Duke University. They showed the first in vivo images of helium in the lungs using two- and three-dimensional gradient echo imaging [Middleton et al., 1995]. They also have demonstrated that the back projection imaging sequence can be used to reduce problems associated with changes in signal amplitude as k-space is sampled. Figure 14 shows images from a Guinea pig model. These studies also show that one can vary the tip angle to capture either the early or later phases of inhalation. More recent work has concentrated on the magnetic behavior of both $^3$He and $^{129}$Xe gas in the lungs. One study finds that the effective transverse relaxation time ($T_2^*$) for $^3$He is approximately 14 ms in the trachea but 8 ms in the intrapulmonary airspaces. For $^{129}$Xe, $T_2^*$ is 40 ms in the trachea and 18 ms in the intrapulmonary airspaces. This indicates that the $^{129}$Xe interacts more strongly with the tissue of the intrapulmonary airspaces as it crosses the blood gas barrier. The regional variation of the diffusion constant was measured in vivo in guinea pigs [Chen et al., 1998].

A study from a group in Lyon examined combining MRI of $^3$He gas with proton based methods to measure lung perfusion [Cremillieux et al., 1999]. The goal is to provide a regional assessment of lung function. Methods in nuclear medicine typically provide only low resolution images that are
Figure 13: Laser polarized $^3$He lung image. The patient is suffering from pulmonary artery obstruction due to hydatid disease. The image shows a large ventilation defect in the apical segment of the lower lobe on the right. Surprisingly, this corresponds also to an obstruction of the pulmonary arterial branch. Image Courtesy of Radiologie Klinik at Mainz University. Used with permission.

Figure 14: Ventilation images of a guinea pig lung showing the exceptional spatial resolution possible with polarized $^3$He and the specialized techniques of *in vivo* microscopy. Image Courtesy of the Center for *in vivo* Microscopy at Duke University. Used with permission.

4.3 Injection of $^3$He and $^{129}$Xe Carriers

Laser polarized gas dissolved or encapsulated in injectable carriers is also under study [Goodson, 1999]. Since xenon is highly soluble in non-polar liquids, it is possible that images of xenon can be obtained *in vivo* by injection of xenon dissolved in an appropriate carrier. Work in Alex Pines’s laboratory at the University of California, Berkeley, has shown that xenon dissolved in different carriers may have a significantly greater SNR than can be created by inhalation of xenon gas [Goodson et al., 1997]. At Duke, laser polarized $^3$He was trapped in microbubbles and introduced into the tail vein and arterial blood of a rat [Chawla et al., 1998]. This new form of angiography provided high resolution images. Also at Duke, laser polarized $^{129}$Xe was dissolved in biologically compatible lipid emulsions (Intralipid 30%) [Moller et al., 1999]. Measured relaxation times were $T_1 = 25.3 \pm 2.1$ sec, and $T_2^* = 37 \pm 5$ ms. Analysis of magnetization inflow was used to deduce the mean blood flow velocity in several organs. Several other potential carriers have been investigated including perfluorooctyl bromide (PFOB), a blood substitute [Wolber et al., 1998]

5 NMR and MRI of Dissolved $^{129}$Xe

In contrast to $^3$He, which is most useful for imaging air spaces such as the lungs and colon, $^{129}$Xe is soluble in blood with $\approx 17\%$ solubility and tissue with varying solubility [Chen et al., 1980]. Many of the biological properties of xenon have been established through research with radioactive isotopes, particularly $^{133}$Xe. Xenon freely diffuses across biological membranes including the blood gas barrier
in the lungs and capillary walls between blood and tissue. Xenon is metabolically inert, and is carried to distant organs where it accumulates in tissue. The size of the $^{129}$Xe magnetization signal in a specific region of interest can be a measure of the rate of blood flow or perfusion through the tissue. Studies using radioactive $^{133}$Xe have shown that xenon can be used in diagnosis and research to measure kidney perfusion [Cosgrove and Mowat, 1974], and cardiac perfusion [Marcus et al., 1987].

Most exciting may be the study of regional brain activation. A variety of techniques has enormously enriched our understanding of the functional organization of the nervous system. The methods of Kety and Schmidt [Kety and Schmidt, 1945] for measuring total blood flow following administration of a metabolically inert gas have been combined with radiotracer imaging techniques to measure changes in regional cerebral blood flow (rCBF) correlated with sensory stimulation, motor activity and inferred information processing in the brain. Early experiments used inhaled or injected gamma-emitting gases such as $^{133}$Xe [Lassen, 1980] or $^{85}$Kr [Lassen and Ingvar, 1961] to measure altered blood flow in the cerebral cortices. More recently positron emission tomography (PET) methods, most notably those employing $^{15}$O-$\text{H}_2\text{O}$, have been used to measure rCBF [Phelps, 1991]. However PET techniques have intrinsic resolution limited to 2-4 mm due to the range of positrons in tissue and often desire a complementary imaging technique such as MRI or CT for accurate anatomical mapping of the PET functional information. MRI methods are not subject to these intrinsic limitations and can provide functional information and anatomical registration with a single modality and apparatus. Several methods for measuring brain function with MRI have been explored [Shulman et al., 1993], and techniques based on blood oxygen level dependence of proton NMR have demonstrated high spatial resolution [Ogawa et al., 1990], though the physiological basis for the detected changes in signal is not well understood [Shulman et al., 1993].

### 5.1 Spectroscopy of $^{129}$Xe in vivo

Figure 15 shows an NMR spectrum of $^{129}$Xe from the body and head of a rat that had been breathing a mixture of $^{129}$Xe and oxygen gas [Swanson et al., 1999b]. Similar spectra have been observed in humans after a single breath-hold of laser polarized $^{129}$Xe [Brookeman, 1998]. The peaks in the rat body spectrum (figure 15 a) have been identified on the basis of work by several authors including the time dependence of the peaks [Wagshul et al., 1996, Sakai et al., 1996, Swanson et al., 1999b], the location of each resonance determined by imaging (see figure 2), and the chemical shifts revealed in in vitro experiments [Wolber et al., 1999a]. The chemical shift may also depend on the oxygenation level of the blood [Wolber et al., 1999b] and varies with tissue type. The spectrum from the head (figure 15 b) reveals at least four peaks in addition to the apparent blood peak at $\approx 210$ ppm. Though there is not yet a definitive identification of the separate tissue types, this does show that several kinds of brain tissue are highly perfused and/or have large partition coefficients for dissolved xenon. An exciting direction for future research is the identification of each chemical shift component and functional study of the differences. It may become possible to identify the kinds of tissue involved in specific neurological functions.

### 5.2 $^{129}$Xe Imaging

As $^{129}$Xe is carried throughout the body by the flow of blood, it is deposited in tissue with time dependent concentration that depends on several factors including the rate of blood flow, i.e. perfusion. Perfusion measurement has many applications ranging from rCBF measurement and research in cognitive neuroscience to assessment of pulmonary, renal, and cardiac health. One key goal of laser polarized $^{129}$Xe MRI is development of techniques of perfusion measurement, that is use of $^{129}$Xe as a magnetic tracer that uses the chemical shifts to isolate each tissue type. The development of such techniques is discussed in section 5.4.

Images of each chemical shift component of $^{129}$Xe can be created using the CSI sequence (described in section 3.4.4) and possibly frequency selective excitation. CSI produces frequency spectra for each pixel as illustrated in figure 16, where we show spectra acquired for each of four adjacent pixels. The pixel map is superimposed on proton images acquired with the spin–echo sequence described in section 3.5. In figure 2, actual images of $^{129}$Xe in gas, blood, and tissue are shown. These are magnetization maps of the signal in each of the peaks indicated in figure 15a. An Image of $^{129}$Xe dissolved in tissue in the rat head [Swanson et al., 1997] is shown in figure 17. The images of $^{129}$Xe in dissolved phases shown in figure 2 demonstrate some potential medical applications that may emerge in the coming years. Images of the lungs in the gas phase (figures
Figure 16: Illustration of the data provided by the CSI imaging sequence. For each pixel, a frequency spectrum is produced. Spectra for four pixels are shown. The background gray-scale image is a proton MRI acquired with the spin-echo sequence. The oval surrounds the heart region.

2A and 2D) show the region of ventilation. In a healthy lung, xenon crosses the blood-gas barrier, appearing also in tissue (figures 2B and 2E) and blood phase images (figures 2C and 2F). We discuss further analysis of lung function in the next section. The blood carries the $^{129}$Xe magnetization from the lungs to the left side of the heart. In the heart, the blood phase signal is dominated by pooled blood in the left heart chambers. Perfusion in the healthy heart is indicated by the appearance of $^{129}$Xe magnetization in the dissolved tissue and fat phases in the heart also shown in figures 2B and 2E. Restricted blood flow (ischemia) and unperfused regions (infarction) would be revealed by the absence of the dissolved tissue phase in that region.

5.3 Lung function

The main functions of the lung are ventilation and perfusion. Many problems in the lungs result when there is a ventilation-perfusion mismatch. For example, regions of the lung that are ventilated but not perfused characterize about 70% of pulmonary embolism cases. Tomographic measurement of ventilation and perfusion, combining gas phase imaging in the lungs and $^{129}$Xe dissolved phase imaging of the blood and tissue provide a new way to study lung function and may assist in appropriate treatment of lung disease.

The data of figure 2 can be analyzed to extract ratios of blood and gas $^{129}$Xe concentrations, shown as images in figure 18. Figure 18a shows that the gas-tissue ratio is relatively uniform except near the trachea and in the peripheral regions of the lung. The gas-blood ratio (Fig. 18b) image shows a similar mismatch in the trachea but also more variation throughout the lungs. Some of this variation may be normal.

Other possible methods of pulmonary MRI using polarized $^{129}$Xe are venous injection of dissolved gas (see section 4) followed by simultaneous imaging of the blood and gas components and study of the spatial variation in the frequency of the blood resonance, likely related to the oxygen content of the blood. The rich information content of $^{129}$Xe spectra and images provides interesting opportunities for pulmonary applications.
5.4 Time Dependence and Magnetic Tracer Techniques

The time dependence of the different chemical shift components of $^{129}$Xe is important in several applications. As we show below, laser polarized $^{129}$Xe magnetic tracer can measure blood flow and the dynamics of exchange across blood gas and blood tissue barriers. In general, the time dependence of a chemical shift magnetization component depends on the rate of delivery to the tissue in the region of interest (perfusion) and on the local magnetization relaxation time, $T_1$. This relaxation time is also, in general time dependent as oxygen concentration changes. Several authors have developed multi-compartment models of $^{129}$Xe magnetization time dependence [Peled et al., 1996, Martin et al., 1997, Welsh et al., 1998]. The goal is to measure the time dependence and use the model to extract quantities of interest, in particular $T_1$ and blood flow independently.

Nuclear medicine methods based on PET are highly developed, however MRI based methods of tissue perfusion measurement may have advantages compared to PET: 1) the chemical shift information allows blood and various tissue types to be isolated; 2) with an entirely MRI based technique, the perfusion map can be anatomically registered with conventional proton images; 3) the resolution is not inherently limited, in the way PET is limited to several millimeters by the range of high energy positrons in tissue; 4) radioactive dose restrictions that limit repeated PET studies do not impact MRI techniques.

In figure 19, we schematically illustrate how MRI of laser polarized $^{129}$Xe can be used as a magnetic tracer to measure perfusion. Once inhaled, $^{129}$Xe is carried from the lungs to heart, brain, and other distal organs. The signal produced at the frequency of the tissue resonance in a given organ (or pixel in an organ) is a measure of the total $^{129}$Xe magnetic moment in the measured volume of tissue. Tissue magnetization, $M_T$, calibrated in units of the arterial magnetization, $M_A$, depends on blood flow $F$ and the local magnetization relaxation rate $1/T_1$ in different ways. If $M_T$ is uncalibrated, data can be used to determine relative blood flow.

As the blood carries $^{129}$Xe with magnetization $M_A$ into tissue, the NMR signal size of the tissue resonance in each volume element of the tomographic image changes with time. The differential equation describing the tissue magnetization ($M_T$) in a voxel is

$$\frac{dM_T}{dt} = FM_A - \left( \frac{1}{T_1} + \frac{F}{\lambda_{BT}} \right)M_T$$

where $F$ is the rate of blood flow in units of ml/minute/ml, $\lambda_{BT}$ is the blood-tissue partition coefficient: the ratio of concentrations of xenon in blood to that in tissue. The time constant for relaxation of $^{129}$Xe magnetization to thermal equilibrium is $T_1$. This differential equation is quite similar to that for the standard nuclear medicine formulation describing wash in of a radioactive tracer (e.g. $^{18}$O-H$_2$O for PET or $^{133}$Xe for SPECT). However there is an extremely important difference: the relaxation time constant, $T_1$, is not uniform, rather it is generally different in different tissues and blood, and it depends on the blood’s oxygenation level [Wilson et al., 1999, Wolber et al., 1999a]. Measurement of dynamics of $^{129}$Xe tissue resonance in the rat brain is consistent with $T_1$ ≈ 30 s [Welsh et al., 1998]. Techniques have been proposed for separating $F$ and $T_1$ [Swanson et al., 1999a].

Absolute measurement of $F$ in units of ml/min/ml requires calibration of $M_T$ in units of $M_A$. This requires measuring the magnetization signal from known volumes of tissue and blood respectively. For quantitative measure of rCBF, it may be possible to image the blood in the carotid artery. For cardiac perfusion, imaging of the pulmonary veins and left heart chambers is possible (see figure 16). One important caveat follows from the small separation of the blood and tissue peaks, about 150 Hz at 1.5T. With the observed $T_2^*$ varying from 2 ms in blood to 20 ms in brain tissue, any NMR pulse that
tips the magnetization of $^{129}\text{Xe}$ in tissue will perturb the blood magnetization. Thus $M_A$ will come to an equilibrium value that is, in general, less than the unperturbed $M_A$. However, the perturbation can be relatively small with proper design of the pulse shape and phasing and because the rate of blood flow to the region of interest is high compared to the pulse rate $1/\tau$ [Geen and Freeman, 1991]. Another possible complication is that the blood and tissue concentrations may not equilibrate rapidly on the time scale of the imaging experiments (about 1 second) resulting in an apparent variation of $\lambda_{BT}$.

5.4.1 Dynamics of Laser Polarized $^{129}\text{Xe}$ in vivo

Features of the dynamics of Laser Polarized $^{129}\text{Xe}$ in the lungs, body and brain of rats in vivo are shown in figure 20 [Swanson et al., 1999b]. Frequency spectra collected as a function of time were used to study the dynamics of laser polarized $^{129}\text{Xe}$. Qualitative interpretation suggests that the blood component builds up more quickly and saturates with respect to the lung input function, whereas the tissue component builds up more slowly due to greater tissue capacity for xenon, and falls off more slowly due to the longer intrinsic $T_1$ in tissue and the relatively slow wash out of xenon. The amplitude of the blood resonance closely follows the amplitude of the scaled gas resonance. The blood resonance plateaus after about 13 s of xenon delivery, but the tissue/plasma peak and the fat peak continue to grow and do not level off, even when xenon delivery is stopped at about 25 s.

The amplitude of the blood resonance closely follows the amplitude of the scaled gas resonance. The blood resonance plateaus after about 13 s of xenon delivery, but the tissue/plasma peak and the fat peak continue to grow and do not level off, even when xenon delivery is stopped at about 25 s.

Figure 20: Dynamics of $^{129}\text{Xe}$ gas, blood, and tissue resonances.

6 Conclusions – Future Possibilities

The future is exceptionally bright for research in biomedicine, neuroscience, and materials science with laser polarized rare gas imaging. The scientific problems relating to polarization techniques, delivery of polarized gas with devices and in solutions are challenging, but progress continues. Ventilation images of animals and humans in the US and Europe provide unprecedented resolution and are likely to provide new information, as is often the case when we can look at something with greater sensitivity, precision, and resolution. Figure 21 provides a stunning example. The new techniques possible with $^{129}\text{Xe}$ provide resolution in chemical shift frequency and time that promise to develop into ways of measuring perfusion of specific tissues as well as organs, complementing PET. The potential for a completely quantitative measure of perfusion promises broad application. All of these possibilities have been discussed in this review.

However, research with a new imaging modality does not ensure its application as a medical diagnostic procedure. Among the potential applications of high resolution lung ventilation imaging, colonoscopy, lung function assessment, and perfusion measurement, MRI with laser polarized gases must pass the tests of

1. sensitivity to disease or injury
2. specificity for a unique diagnosis
3. Effectiveness based on cost and risk

For example, high resolution lung imaging with $^{3}$He has been shown to be clearly sensitive to small ventilation defects – regions of the lung that do not effectively fill with gas in a normal breath. But the question of what specific malady this indicates is currently open. On the other hand, lower resolution $^{3}$He or $^{129}$Xe lung images, produced with less gas and lower polarization (see figure 11) provide the same ventilation information as a $^{133}$Xe nuclear medicine scintigraphy, but without the radiation dose of nearly 1 Rad from a single study. Such lower resolution scans would therefore provide the demonstrated sensitivity and specificity of the widely used nuclear medicine techniques. However the cost of an MRI is currently many times greater a $^{133}$Xe nuclear medicine study, and the additional cost of laser polarized gas would significantly increase the cost of an MRI. Low-field imaging systems may bring the cost down. Early diagnosis procedures and repeated studies that would be limited by radiation dose may be developed by physicians with these new tools. Pediatric pulmonary medicine may be an important application of the combination of diagnosis without radiation dose and low-field, open-geometry magnets.

With the promise of these and a host of other potential applications, pre-clinical efforts are underway in the US and Europe. In the US, the efforts are organized by the commercial interest that would produce the polarized gas in regional centers and ship it, overnight, to medical facilities. In Europe, a collaboration of industry, academic, and hospital based researchers is developing the pre-clinical program. The goals of both these groups include regulatory approval for administration of polarized gas as a contrast agent and its use for medical diagnosis. Interestingly, the final step in regulatory approval, following demonstration of safety and other issues, is demonstration of efficacy: the sensitivity and specificity for diagnosis of specific maladies that physicians would be likely to use.

7 Acknowledgements

The authors are grateful to several colleagues for discussions and advice regarding this review and for scientific inspiration and guidance. They are: Bennie Agranoff, Jim Brookeman, Gordon Cates, Kevin Coulter, Tom Chenevert, Will Happer, Bob Koepe, Pierre-Jean Nacher, Eduardo Oteiza, Matt Rosen, Brian Saam, Ron Walsworth, Robert Welsh, and Jon Zerger. Images were provided by Brian Saam, Jim Brookeman, Tom Chenevert, Hans-Ulrich Kauczor, Pierre-Jean Nacher, and Al Johnson.

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