

# Tunable band-pass plasmonic waveguide filters with nanodisk resonators

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**Abstract:** A novel and simple plasmonic filter based on metal-insulator-metal plasmonic waveguides with a nanodisk resonator is proposed and investigated numerically. By the resonant theory of disk-shaped nanocavity, we find that the resonance wavelengths can be easily manipulated by adjusting the radius and refractive index of the nanocavity, which is in good agreement with the results obtained by finite-difference time-domain (FDTD) simulations. In addition, the bandwidths of resonance spectra are tunable by changing the coupling distance between the nanocavity and waveguides. This result achieved by FDTD simulations can be accurately analyzed by temporal coupled mode theory. Our filters have important potential applications in high-density plasmonic integration circuits.

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**OCIS codes:** (240.6680) Surface plasmons; (140.4780) Optical resonators; (130.7408) Wavelength filter; (130.3120) Integrated optics devices.

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## 1. Introduction

Surface plasmon polaritons (SPPs) are waves trapped on the surfaces of metals owing to the interaction between the free electrons in metal and electromagnetic field in dielectric, and attenuating exponentially in the direction perpendicular to the interface [1,2]. SPPs have the most promising applications in the highly integrated optical circuits and devices due to their overcoming of diffraction limit and light manipulation on subwavelength scales [1, 3]. Recently, the devices based on SPPs, such as the all-optical switching [4–6], Mach-Zehnder interferometers [7], splitters [8], modulators [9], mirrors [10], sensors [11], and Bragg reflectors [12,13] are simulated numerically and demonstrated experimentally. Bragg reflectors are fabricated by alternatively stacking two kinds of dielectrics in metal-insulator-metal (MIM) or insulator-metal-insulator (IMI) plasmonic waveguides [12], and can realize the filtering functions. The IMI waveguide gives rise to less loss for the longer propagation distance, but fails to confine a light into subwavelength scale and, thus, is not suitable for high optical integration [14]. The MIM waveguide has a strong confinement of light and acceptable propagation length for SPPs [12].

Quite recently, some simple plasmonic waveguide filters have been proposed, such as tooth-shaped plasmonic waveguide filters [15,16], channel drop filters with disk resonators [17], rectangular geometry resonators [2, 18], and ring resonators [17, 19]. They overcome the complexity of fabrication of Bragg reflectors and decrease the propagation length for SPPs. There exist two types of plasmonic filters in MIM waveguides, i.e., band-pass and band-stop filters. The band-stop filter prohibits light with certain frequency from propagating through the waveguide structures [15, 18]. The band-pass filter, which permits transmitting some frequency of light, is also very important in nanoscale optical devices [16, 19]. Some devices such as SPP reflectors need broad bandgaps [13]. In many cases such as wavelength division multiplexing (WDM) systems, however, narrow bandwidths are desired [16, 20].

In this paper, we propose a novel and simple plasmonic narrow-bandpass filter based on the MIM waveguide with a nanodisk resonator (i.e., disk-shaped naocavity). We focus on the tunable filtering characteristics of this filter structure. The wavelength-shift properties of resonant modes in the nanocavity calculated by the resonant theory of disk-shaped naocavity are validated by finite-difference time-domain (FDTD) method [21]. Another result obtained by FDTD simulations demonstrates that the bandwidths of resonance spectra can be manipulated by the coupling distance between the nanocavity and waveguides, which is analyzed exactly by temporal coupled mode theory.

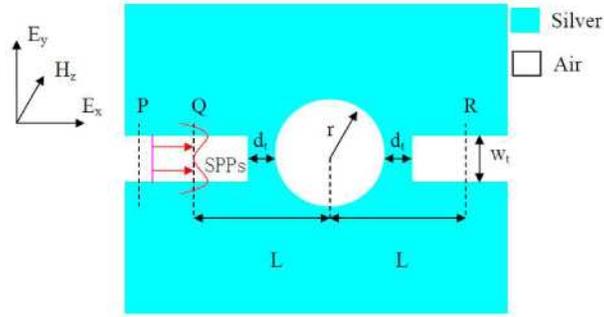


Fig. 1. Schematic diagram of the proposed plasmonic filter.  $r$ : radius of nanodisk resonator (disk-shaped nanocavity),  $w_t$ : metal slit width,  $d_c$ : coupling distance between the cavity and waveguides.

## 2. Structure and theories

Figure 1 shows the plasmonic filter structure which is composed of two slits, two semi-infinite metallic claddings, and a nanodisk resonator in the middle of the MIM structure. The insulators in the slit and cavity are set as air ( $n_d = 1$ ). The metal is assumed as silver, whose complex relative permittivity can be characterized by the well-known Drude model [15]

$$\varepsilon_m(\omega) = \varepsilon_\infty - \frac{\omega_p^2}{\omega(\omega + i\gamma)}, \quad (1)$$

where  $\varepsilon_\infty$  is the dielectric constant at the infinite frequency,  $\gamma$  and  $\omega_p$  are the electron collision frequency and bulk plasma frequency, respectively.  $\omega$  is the angular frequency of incident light. The parameters for silver can be set as  $\varepsilon_\infty = 3.7$ ,  $\omega_p = 9.1$  eV, and  $\gamma = 0.018$  eV [22]. **TM-polarized plane wave** is emitted between the detective plane  $P$  and  $Q$  and propagates to  $R$ . The distance between  $P$  and  $Q$  is 10 nm. The distance between  $Q$  and  $R$  is 800 nm, i.e.,  $L = 400$  nm. The planes  $P$ ,  $Q$ , and  $R$  detect the powers of internal field (i.e.,  $P_P$ ,  $P_Q$ , and  $P_R$ ) respectively.  $P_{in} = P_Q - P_P$  presents the incident power, and  $P_{out} = P_R$  denotes the transmission power. The transmission is defined as  $T = P_{out}/P_{in}$  [15]. The exciting stable standing wave in the disk-shaped nanocavity forms the resonant condition [23,24] which can be given by

$$k_d \frac{H_n^{(1)'}(k_m r)}{H_n^{(1)}(k_m r)} = k_m \frac{J_n'(k_d r)}{J_n(k_d r)}, \quad (2)$$

where  $k_{d,m} = k(\varepsilon_{d,m})^{1/2}$  are the wave vectors in the dielectric disk/metal, and  $r$  is the radius of the nanocavity.  $\varepsilon_d$  is the relative permittivity of the dielectric.  $\varepsilon_m$  stands for the relative permittivity of the metal, which is obtained from Eq. (1).  $k$  is the wave number and contains a relatively small negative imaginary part for a given  $n$ , where the negative imaginary part presents the loss [23].  $J_n$  and  $J_n'$  are the first kind Bessel function with the order  $n$  and its derivation,  $H_n^{(1)}$  and  $H_n^{(1)'}$  are the first kind Hankel function with the order  $n$  and its derivation, respectively. The first and second-order modes are considered in the present paper, which correspond to the first and second order of Bessel and Hankel functions. From Eq. (2) we can see that the resonance wavelength  $\lambda_0$  is dominated by  $r$  and the refractive index  $n_t$  (i.e.,  $(\varepsilon_d)^{1/2}$ ). The transmission spectra near the resonant modes in our system can be described by the temporal coupled mode theory, and the transmission  $T$  can be derived from Ref [25]. and described as

$$T(\omega) = \frac{(1/\tau_w)^2}{(\omega - \omega_0)^2 + (1/\tau_i + 1/\tau_w)^2}, \quad (3)$$

where  $w$  is the frequency of incident light, and  $w_0$  presents the resonance frequency.  $1/\tau_i$  and  $1/\tau_w$  stand for the decay rate of the field induced by the internal loss in the nanocavity and the power escape through the waveguides, respectively. At the resonance frequency  $w_0$ , the cavity mode is excited and the incident light is transmitted. Far from the resonance frequency, the incident mode is completely reflected. When  $1/\tau_i$  is far less than  $1/\tau_w$ , the on-resonance transmission (i.e., transmission peak)  $T_{max} = (1/\tau_w)^2 / (1/\tau_w + 1/\tau_i)^2$  is close to unity. From Eq. (3), we can find that the transmission spectra around the resonant modes exhibit Lorentzian profiles.

### 3. Simulation results and analysis

The parameters of the filter structure are set as  $r = 200$  nm,  $w_i = 50$  nm,  $d_i = 20$  nm, and  $L = 400$  nm. Firstly, we utilize the FDTD method to simulate the transmission characteristics. Figure 2(a) shows the transmission spectrum including the two low-order modes (Mode 1 and 2) observed in the visible and near-infrared spectral range. The transmission exhibits evident filtering property at the two modes. The transmission peaks do not reach unity due to the internal loss in the nanocavity as well as waveguide loss in the metal slits. The transmission response exhibits Lorentzian shape, which is in accordance with above theoretic analysis. Field distributions of  $|H_z|$  at the incident wavelength of 520 nm (i.e., Mode 1), the wavelength of 700 nm, and the wavelength of 816 nm (i.e., Mode 2) are depicted in Figs. 2(b)-(d), respectively. It is found that the excitations of resonant modes emerge in the nanocavity at the wavelengths of 520 nm and 816 nm, where the incident light can pass through the MIM plasmonic structure. In addition, there exists no excitation of resonant mode when the wavelength is 700 nm, where the propagation of the incident light is stopped. As shown in Fig. 2(a), the transmission at resonant mode 2 has higher coefficient than that of mode 1. This may be due to that resonant mode 2 has larger  $1/\tau_w$  than mode 1.

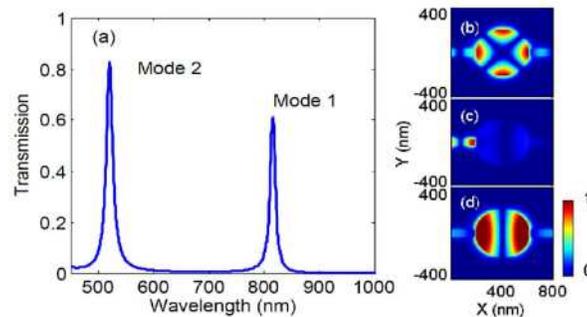


Fig. 2. (a) Transmission spectrum with the original parameters of configuration. The corresponding normalized field distributions of  $|H_z|$  with wavelengths of (b) 520 nm (Media 1), (c) 700 nm (Media 2), and (d) 816 nm (Media 3) exhibit respective transmission characteristics.

Successively, we investigate the influence of the radius of the nanocavity on the resonance wavelengths first by the FDTD method and then by the resonant mode theory. The radius is set as variable while the other parameters are fixed as above. Figure 3(a) shows the transmission response of SPPs corresponding to different radius. The resonance wavelengths have a red-shift with increasing of the radius. Figure 3(b) reveals that the wavelength-shifts of the resonant modes 1 and 2 almost have approximately linear relations with the radius of nanocavity. This result is in accordance with the solution of Eq. (2). According to the simulations and analysis above, it is seen that the band-pass filter can be easily tuned by changing the radius of nanocavity. We have known that the resonant modes are influenced by the refractive index of the material filling the nanocavity. Thus, we can manipulate the wavelengths of resonant modes by changing the value of refractive index ( $n_i$ ) in the nanocavity. The other parameters are set as above. Figure 4(a) shows the transmission spectra with different refractive index of the nanocavity. From Fig. 4(b) we find that the red-shifts of

resonance wavelengths have nearly linear relations with  $n_t$ . The results from the resonant theory of disk-shaped nanocavity are consistent with those obtained by FDTD simulations. Therefore, one can fill some dielectric material into the nanocavity to design the band-pass plasmonic filter with demanded channel.

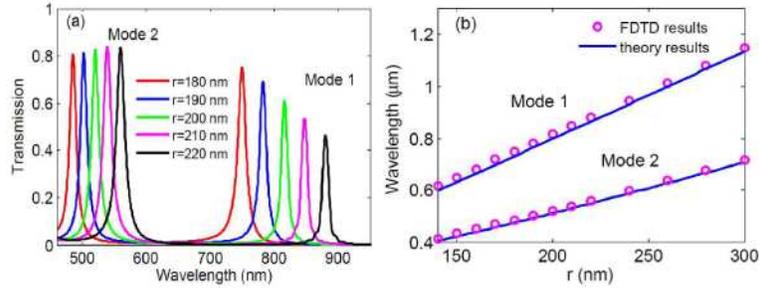


Fig. 3. (a) Transmission spectra with different radii of the nanocavity. (b) Relationship between resonance wavelengths and the radius of the cavity.

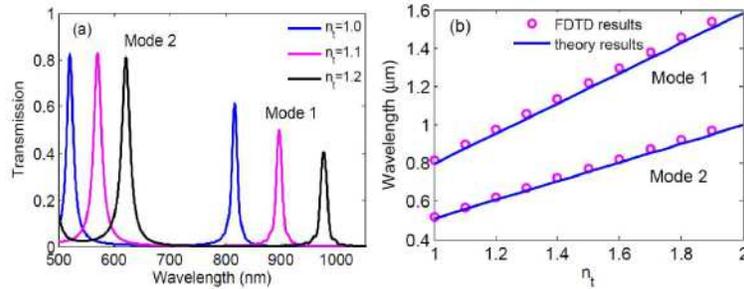


Fig. 4. (a) Transmission spectra with different refractive index. (b) Relationship between resonance wavelengths and the refractive index.

Another structure parameter  $d_t$ , which stands for the coupling distance between the nanodisk resonator and the waveguides, is an important factor influencing the intensities of transmission spectra near the resonant modes. The decay rate  $1/\tau_i$  keeps approximately unchanging when only  $d_t$  is changed. Meanwhile, the decay rate  $1/\tau_w$  will intensively decrease when  $d_t$  is increased from zero to tens of nanometers. The on-resonance transmission  $T_{max} = (1/\tau_w)^2 / (1/\tau_w + 1/\tau_i)^2$  will accordingly decrease. The results are verified by FDTD simulations, as shown in Figs. 5(a) and (b). The resonance wavelengths exhibit slight blue-shift for larger coupling distances, which is consistent with the results in Ref [19]. According to Eq. (3), full width at half maximum of the resonance spectrum  $\Delta_{FWHM} \approx 4\pi c(1/\tau_w + 1/\tau_i)/\omega_0^2$  will intensively decrease along with  $1/\tau_w$ , as shown in Fig. 5(a). Therefore, the bandwidths of the resonance spectra can be tuned by controlling the coupling distance.

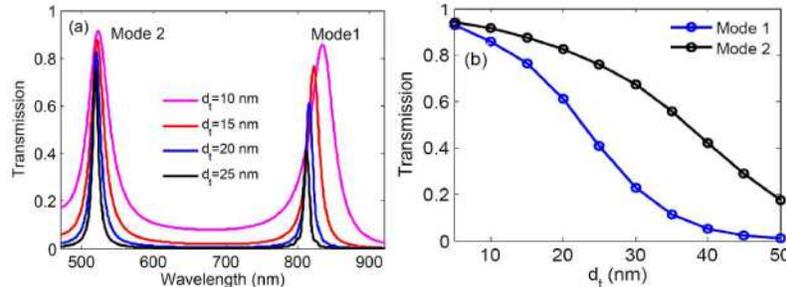


Fig. 5. (a) Transmission spectra with different  $d_t$ . (b) Relationship between the on-resonance transmissions and  $d_t$ . The other parameters are set as original values.

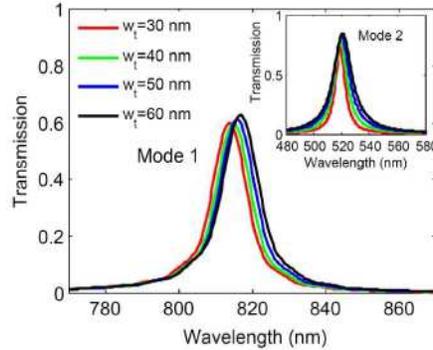


Fig. 6. Transmission spectra with different metal slit widths in the MIM waveguides.

Finally, we study the influence of the metal slit width  $w_t$  on the transmission characteristics of SPPs. Since  $w_t$  is usually set as tens of nanometers [19, 26], here the situations of  $w_t = 30, 40, 50,$  and  $60$  nm are considered for simulation. Figure 6 shows the transmission spectra with different slit widths. It is found that the transmission spectrum fluctuates quite slightly, while shows a little red-shift and height-rise which can be attributed to the waveguide loss [26].

#### 4. Conclusion

In this paper, a simple and ease of fabrication plasmonic filter based on MIM waveguides with a nanodisk resonator is proposed. The resonant modes are calculated by the resonant theory of disk-shaped nanocavity, and we find that the central wavelengths of the resonance transmission can be easily controlled by modulating the radius and refractive index of the nanocavity. The results are in good agreement with that obtained by the FDTD method. Furthermore, it is shown that the bandwidths of resonance spectra can be tuned by adjusting the coupling distance between the nanocavity and waveguides. This result achieved by FDTD simulations can be accurately analyzed by temporal coupled mode theory. This ultra-compact structure has extensive potential in nanoscale integrated optical circuits due to its simplicity for design of tunable narrow band-pass filters.

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