

## A NEW MULTIPLE HALF-DISCRETE HILBERT-TYPE INEQUALITY

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*Abstract.* By using the way of weight functions and technique of real analysis, a new multiple half-discrete Hilbert-type inequality with the best constant factor is given. As applications, the equivalent forms, operator expressions as well as some reverse inequalities are also considered.

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