Unified Constant-frequency Integration Control of Three-phase Standard Bridge Boost Rectifier

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Abstract: In this paper, a three-phase six-switch standard boost rectifier with unity-power-factor-correction is investigated. A general equation is derived that relates input phase voltage and duty ratios of switches in continuous conduction mode. Based on one of solutions and using One-Cycle Control, a Unified Constant-frequency Integration (UCI) controller for power-factor-correction (PFC) is proposed. For the standard bridge boost rectifier, unity-power-factor and low total-harmonic-distortion (THD) can be realized in all three phases with a simple circuit that is composed of one integrator with reset along with several flips-flops, comparators, and some logic and linear components. It does not require multipliers and three-phase voltage sensors, which are used in many other control approaches. In addition, it employs constant switching frequency modulation that is desirable for industrial applications. The proposed control approach is simple and reliable. Theoretical analysis is verified by simulation and experimental results.

1 Introduction.

Traditional diode rectifiers and thyristor rectifiers draw pulsed current from the ac main, causing significant current harmonics pollution. The international standards presented in IEC 1000-3-2 and EN61000-3-2 imposed harmonic restrictions to modern rectifiers, which results in a focused research effort on the topic of unity power factor rectifiers. Three-phase PFC rectifiers are preferred for high power applications due to their symmetric current drawing characteristics. Many topologies have been proposed recently [1]-[4]. Among them, the six-switch bridge boost rectifier is one of the most commonly used topologies. In the previously proposed rectifiers, hysteresis control and d-q transformation control were frequently used to control six-switch bridge boosts. Hysteresis control results in variable switching frequency that is difficult for EMI filter design. The d-q approach is based on digital implementation that leads to complicated systems. An encouraging analog solution with constant switching frequency modulation was provided in [5] for a six-switch bridge boost rectifier. However, three-phase voltage is sensed for six-step operation and multipliers are necessary to implement the three phase current references.

In this paper, a general equation that relates input phase voltage and duty ratios of switches is derived for a six-switch bridge boost rectifier based on an average model in Continuous Conduction Mode (CCM). This equation is singular and has infinite solutions. Based on the One-Cycle Control concept [6]-[9] and one solution of this general equation, a Unified Constant-frequency Integration (UCI) Controller is conceived for the standard bridge rectifier that realizes three-phase unity-power-factor and low THD. The proposed controller features the following:

- Constant switching frequency.
- No need for multipliers that are required to scale the current reference according to the load level as used in many other control approaches.
- Three-phase voltage sensor is eliminated.
- Only one integrator with reset along with some logic and linear components are required. It is simple and reliable.

2 The proposed Unified Constant-frequency Integration controller

The analysis in this section is based on following assumption:

- The switches in each arm operate complementary. For example, the duty ratios for switches $S_{an}, S_{ap}$ are $d_{an}$ and $1-d_{an}$ respectively.
- Three-phase system is symmetrical.
- Switching frequency is much higher than line frequency.

![Fig. 1. (a). Three-phase 6-switch bridge boost rectifier. (b) Average model](image-url)
$$v_{AN} = (1 - d_{an}) \cdot E$$
$$v_{BN} = (1 - d_{bn}) \cdot E$$
$$v_{CN} = (1 - d_{cn}) \cdot E$$

where $d_{an}, d_{bn}, d_{cn}$ are the duty ratios for switches $S_{an}, S_{bn}, S_{cn}$. The equivalent average model for rectifier in Fig. 1 (a) is shown in Fig. 1 (b). The average vector voltage at nodes A, B, C referring to the neutral point “O” equal the phase vector voltages minus the voltage across the inductors $L_a, L_b, L_c$, as given by

$$\dot{v}_{AO} = \dot{v}_a - jwL_a \cdot \dot{I}_a$$
$$\dot{v}_{BO} = \dot{v}_b - jwL_b \cdot \dot{I}_b$$
$$\dot{v}_{CO} = \dot{v}_c - jwL_c \cdot \dot{I}_c$$

where $L$ is the inductance of input inductors (assuming three-phase inductors are identical), $w$ is the line angular frequency, and $\dot{I}_a, \dot{I}_b, \dot{I}_c$ are the inductor current vectors. Since these inductors are operating in high frequency and the inductance $L$ is very small regarding to 60Hz utility system, the voltages across the inductors such as $jwL_a \cdot \dot{I}_a$ are very small comparing with the phase voltage and they can be neglected. Therefore, equation (2) can be approximately simplified as

$$\dot{v}_{AO} = \dot{v}_a$$
$$\dot{v}_{BO} = \dot{v}_b$$
$$\dot{v}_{CO} = \dot{v}_c$$

$$\dot{v}_a = \sqrt{2} \cdot V_i \cdot \sin(wt)$$
$$\dot{v}_b = \sqrt{2} \cdot V_i \cdot \sin(wt - 120^\circ)$$
$$\dot{v}_c = \sqrt{2} \cdot V_i \cdot \sin(wt + 120^\circ)$$

$$\dot{v}_a + \dot{v}_b + \dot{v}_c = 0$$

This leads to

$$v_{AO} + v_{BO} + v_{CO} = 0$$

The voltages at nodes A, B, C referring to neutral point are given by

$$v_{AO} = v_{AN} + v_{NO}$$
$$v_{BO} = v_{BN} + v_{NO}$$
$$v_{CO} = v_{CN} + v_{NO}$$

Combination of equation (5) and (6) yields

$$v_{NO} = -\frac{1}{3} \cdot (v_{AN} + v_{BN} + v_{CN})$$

Substituting equation (7) and (3) into (6) results in

$$v_{AO} = v_{AN} - \frac{1}{3} \cdot (v_{AN} + v_{BN} + v_{CN}) \approx v_a$$
$$v_{BO} = v_{BN} - \frac{1}{3} \cdot (v_{AN} + v_{BN} + v_{CN}) \approx v_b$$
$$v_{CO} = v_{CN} - \frac{1}{3} \cdot (v_{AN} + v_{BN} + v_{CN}) \approx v_c$$

Combination of above equation and (14) yields:

$$\begin{bmatrix}
\frac{2}{3} & -\frac{1}{3} & -\frac{1}{3} \\
-\frac{1}{3} & \frac{2}{3} & -\frac{1}{3} \\
-\frac{1}{3} & -\frac{2}{3} & \frac{1}{3}
\end{bmatrix}
\begin{bmatrix}
v_{AN} \\
v_{BN} \\
v_{CN}
\end{bmatrix}
= 
\begin{bmatrix}
v_a \\
v_b \\
v_c
\end{bmatrix}$$

Combination of equation (1) and (9) yields the relationship between duty ratio $d_{an}, d_{bn}, d_{cn}$ and voltage $v_a, v_b, v_c$, which is shown as follows:

$$\begin{bmatrix}
-\frac{2}{3} & \frac{1}{3} & \frac{1}{3} \\
\frac{1}{3} & -\frac{2}{3} & \frac{1}{3} \\
\frac{1}{3} & \frac{1}{3} & -\frac{2}{3}
\end{bmatrix}
\begin{bmatrix}
d_{an} \\
d_{bn} \\
d_{cn}
\end{bmatrix}
= 
\begin{bmatrix}
v_a \\
v_b \\
v_c
\end{bmatrix}$$

The parameter $K_1$ is limited by

$$\frac{v_a}{E} \leq K_1 \leq 1 + \frac{v_a}{E}$$

The parameter $K_2$ is limited by

$$\frac{v_a}{E} \leq K_2 \leq 1$$

The equation relates average duty ratio of switches to the line voltage. Since the matrix of equation (10) is singular, equation (10) has no unique solution. One possible solution for equation (10) is as follows:

$$d_{an} = K_1 + K_2 \cdot \frac{v_a}{E}$$
$$d_{bn} = K_1 + K_2 \cdot \frac{v_b}{E}$$
$$d_{cn} = K_1 + K_2 \cdot \frac{v_c}{E}$$

For a three-phase rectifier with unity-power-factor, the control goal is given by

$$v_a = R_e \cdot i_a$$
$$v_b = R_e \cdot i_a$$
$$v_c = R_e \cdot i_a$$

where $R_e$ is emulated resistance.
where parameter $R_s$ is the equivalent current sensing resistor.

Define $V_m = \frac{E \cdot R_s \cdot K}{R_e}$ \hspace{1cm} (17)

where $V_m$ is the output of feedback error compensator.

The equation (16) can be simplified as

$$
\begin{aligned}
R_s \cdot i_a &= V_m - V_m \cdot \frac{d_{am}}{K_1} \\
R_s \cdot i_b &= V_m - V_m \cdot \frac{d_{bm}}{K_1} \\
R_s \cdot i_c &= V_m - V_m \cdot \frac{d_{cm}}{K_1}
\end{aligned}
$$

Three-phase PFC can be achieved by controlling the switches in such a way that the duty ratios and input currents satisfy the equation (18). Replace the currents $i_a,i_b,i_c$ with peak inductor current, the control key equations for peak inductor current sensing are derived as

$$
\begin{aligned}
R_s \cdot i_{Lapk} &= V_m - V_m \cdot \frac{d_{am}}{K_1} \\
R_s \cdot i_{Lbpk} &= V_m - V_m \cdot \frac{d_{bm}}{K_1} \\
R_s \cdot i_{Lcpk} &= V_m - V_m \cdot \frac{d_{cm}}{K_1}
\end{aligned}
$$

The above equation can be implemented with an integrator with reset along with some linear and logic components as shown in Fig. 2 (a). The operation waveforms are shown in Fig. 2 (b); where $Q_{ap}, Q_{an} \cdot Q_{cn}$ are driver signal for switches $S_{ap}, S_{an} \cdots S_{cn}$ respectively. The time constant of the integrator is set to be $\tau = K_1 \cdot T_S$; where $T_S$ is the switching period. For convenience, $K_1$ is chosen to be 0.5.

In this case, the carrier $V_m - V_m \cdot \frac{t}{K_1 \cdot T_S}$ is symmetric to the $x$ axis. The overall schematic for the proposed 3-phase UCI PFC controller with peak inductor current sensing is shown in Fig. 2 (a). No voltage sensors and multipliers are required. In order to prevent short circuit, dead time for complementary switches such as $S_{am}, S_{ap}$ are considered.

![Fig. 2. (a) Schematic of proposed UCI controller for 3-phase PFC with peak inductor current sensing. (b) Operation waveforms.](image-url)
3 Limitation of the proposed control approach

With the proposed approach, the inductor current will experience larger distortion at light load. It is found that in certain region of the line cycle, the inductor current could be "partly uncontrolled". This phenomena occurs when $V_m$ is small and load is light. The open loop simulation under this condition is shown in Fig. 4, where $V_m \left(1 - \frac{t}{0.5 \cdot T_s}\right)$ is the carrier, $R_s \cdot i_{La}$, $R_s \cdot i_{Lb}$, $R_s \cdot i_{Lc}$ are the sensed inductor currents, and $Q_{an}$, $Q_{bn}$, $Q_{cn}$ are driving signals for switches $S_{an}$, $S_{bn}$, $S_{cn}$ respectively. Simulation conditions are as follows: the input inductance is 1mH; the switching frequency is 10kHz; the current sensing resistance is 0.2ohm; the output voltage is 500V, and the voltage $V_m = 4V$. Fig. 4 (a) shows the switching cycle operation waveforms and Fig. 4 (b) shows the line-cycle inductor current. In this case, the sensed signal $R_s \cdot i_{La}$ is above the envelope of carrier signal $V_m \left(1 - \frac{t}{0.5 \cdot T_s}\right)$, which indicates uncontrolled operation in a small region.

The reason for this uncontrolled operation is due to the redundancy of switching states during each switching cycle. In the beginning of each switching cycle, all the lower switches $S_{an}$, $S_{bn}$, $S_{cn}$ are turned on and the equivalent circuit is shown in Fig. 5 (a). Near end of the switching cycle when all of these three switches are turned off, all the upper leg switches $S_{ap}$, $S_{bp}$, $S_{cp}$ are turned on. The equivalent circuit is shown in Fig. 5 (b). The electrical property for these two states is identical to each other. For both cases, the inductor voltage equals phase voltage and inductor currents increase. Take phase B as an example as shown in Fig. 4 (a). When $Q_{bn}$ is off, the inductor current $i_{Lb}$ increases with a slope of $\frac{v_b(t)}{L}$ (At this time, phase $v_b$ is negative).

If the slope of inductor current is greater than the equivalent slope of ramp signal $V_m \left(1 - \frac{t}{0.5 \cdot T_s}\right)$, the current will grow beyond the envelope. To avoid this situation, a circuit limitation is required, that is
The inductor should be chosen according to equation (20)

\[ L \geq R_s \cdot \frac{V_{g \text{ max}}}{\min(V_m)} \cdot \tau \quad -(20) \]

where \( R_s \) is the current sensing resistance; \( V_{g \text{ max}} \) is the peak of the input phase voltage; \( \tau \) is the integration time constant (\( \tau = 0.5T_s \) is chosen in this paper); \( \min(V_m) \) is the minimum voltage of \( V_m \) that determines the minimum load by equation (17).

In order to verify the concept, an experimental circuit was built that employs the three-phase boost rectifier with dc diode in Fig. 3. The experimental waveforms are shown in Fig. 6. The parameters are as follows: main inductance is 300uH; the switching frequency is 50kHz. The input voltage is 90Vrms. The output voltage is 420V. The output resistance is 327ohm and output power is 540 watts. The measured input current THD is 7.5% while the input voltage has about 4% THD itself.

5 Conclusion

In this paper, a three-phase six-switch boost rectifier is investigated. The relationship between input phase voltage and switch duty ratios is given by a singular equation. Based on one of solutions and using One-Cycle Control, a UCI controller is proposed to achieve three-phase unity-power-factor. The proposed controller employs constant frequency modulation that is desirable for industrial applications. It is composed of one integrator with reset along with some linear and logic components. No multipliers and input voltage sensors are used. Nearly unity power factor was demonstrated experimentally in all three phases using this simple control circuit. The input current distortion is higher for light load operation. Design criteria are given to improve the current distortion at light load.

References