

Massive MIMO for 5G

Recent Theory

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Expectations for 5G Networks

- 5G – Next Network Generation
 - To be introduced around 2020
 - Design objectives are currently being defined

5G Performance Metrics	Expectation
Average rate (bit/s/active user)	10-100x
Average area rate (bit/s/km ²)	1000x
Active devices (per km ²)	10-100x
Energy efficiency (bit/Joule)	1000x
“Best experience follows you”	

*Source: METIS project
(www.metis2020.com)*

What is the role of Massive MIMO here?

Outline, Part 2: Recent Theory

- Spectral Efficiency
 - Designing Massive MIMO for high spectral efficiency
 - What are the fundamental limits?
- Energy Efficiency
 - How is it defined?
 - Is Massive MIMO energy efficient?
- Hardware Efficiency
 - Does Massive MIMO require high-grade hardware?
 - Can it make more efficient use of hardware (lower cost, size, and power)?
- Open Problems

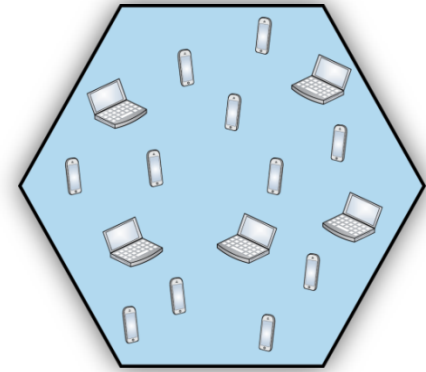
Massive MIMO and

SPECTRAL EFFICIENCY

Evolving Networks for Higher Traffic

- Increase Network Throughput [bit/s/km²]

- Consider a given area



- Simple Formula for Network Throughput:

$$\underbrace{\text{Throughput}}_{\text{bit/s/km}^2} = \underbrace{\text{Available spectrum}}_{\text{Hz}} \cdot \underbrace{\text{Cell density}}_{\text{Cell/km}^2} \cdot \underbrace{\text{Spectral efficiency}}_{\text{bit/s/Hz/Cell}}$$

- 5G goal: 1000x improvement

	More spectrum	Higher cell density	Higher spectral efficiency
Nokia (2011)	10x	10x	10x
SK Telecom (2012)	3x	56x	6x

*New regulations,
cognitive radio,
mmWave bands*

*Smaller cells,
heterogeneous
deployments*

Massive MIMO
How many ??x
can we expect?

Optimization of Spectral Efficiency

- How Large Spectral Efficiency can be Achieved?

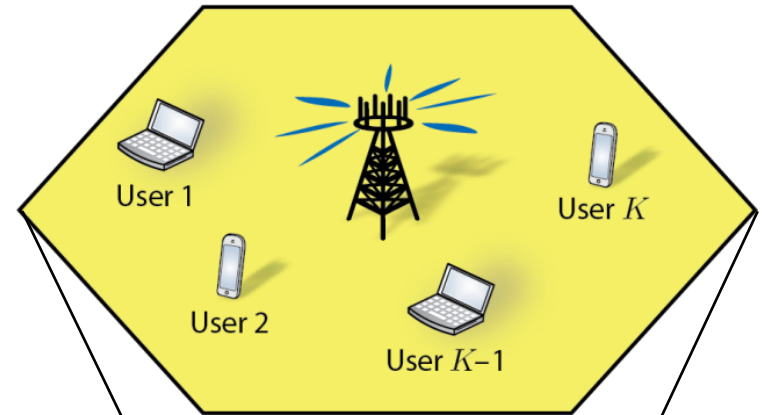
- Problem Formulation:

$$\begin{aligned} & \underset{K, \tau_p}{\text{maximize}} && \text{total spectral efficiency} && [\text{bit/s/Hz/cell}] \\ & \text{for a given } M \text{ and } \tau_c. \end{aligned}$$

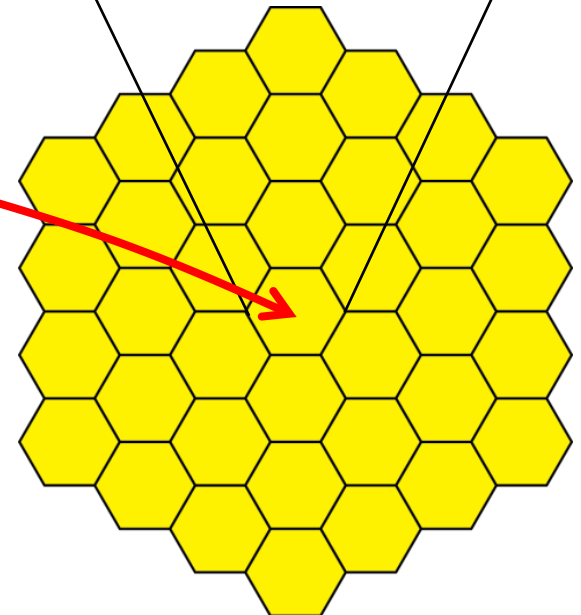
- Issue: Hard to find tractable expressions
 - Interference depends on all users' positions!
 - Expressions from before: Fixed and explicit pathloss values (β)
 - We want quantitative results – averaged over user locations
- Solution: Make every user “typical”
 - Same uplink SNR: Power control inversely proportional to pathloss
 - Inter-cell interference: Code over variations in user locations in other cells

Symmetric Multi-Cell Network

- Classic Multi-Cell Network
 - Infinite grid of hexagonal cells
 - M antennas at each BS
 - K active users in each cell
 - Same user distribution in each cell
 - Uncorrelated Rayleigh fading
 - Statistical channel inversion: $\rho_u \eta_{lk} = \frac{p}{\beta_{lk}^l}$



Every cell is “typical”



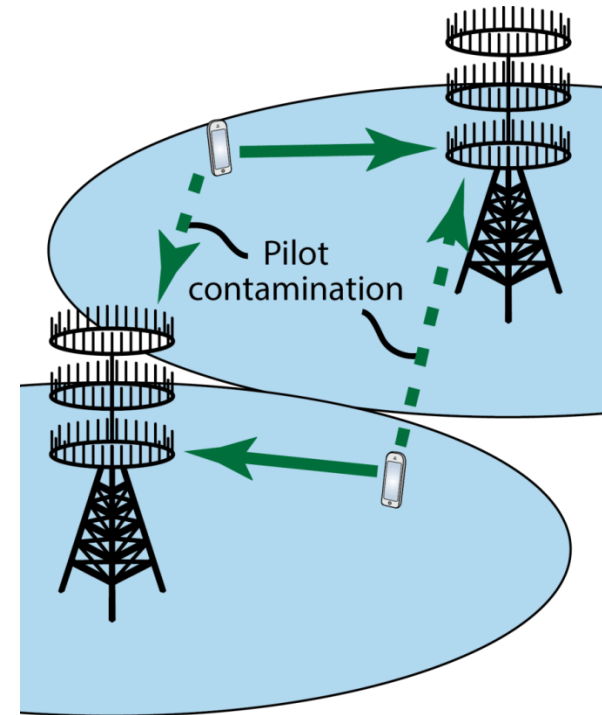
Propagation Parameters

(Average interference from cell l to BS j)

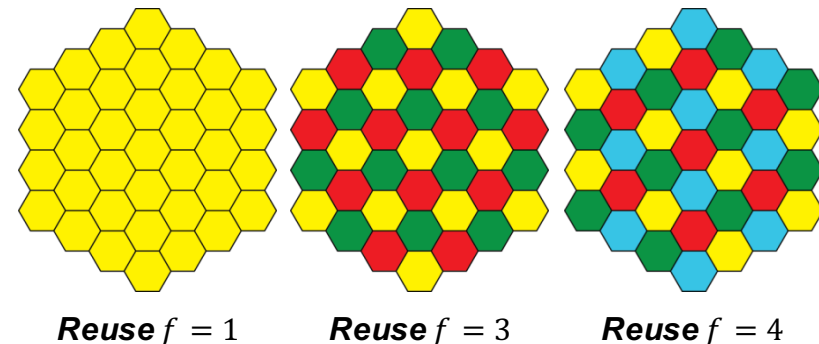
Compute $\mu_{jl}^{(1)} = \mathbb{E} \left\{ \frac{\beta_{lk}^j}{\beta_{lk}^l} \right\}$ and $\mu_{jl}^{(2)} = \mathbb{E} \left\{ \left(\frac{\beta_{lk}^j}{\beta_{lk}^l} \right)^2 \right\}$

Coordinated Pilot Allocation

- Limited Number of Pilots: $\tau_p \leq \tau_c$
 - Must use same pilot sequence in several cells
 - Base stations cannot tell some users apart:
Essence of pilot contamination
- Coordinated Pilot Allocation
 - Allocate pilots to users to reduce contamination
 - Scalability \rightarrow No signaling between BSs



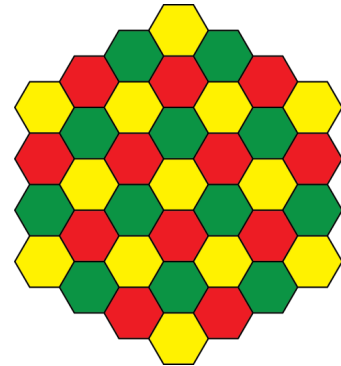
- Solution: Non-universal pilot reuse
 - Pilot reuse factor $f \geq 1$
 - Users per cell: $K = \frac{\tau_p}{f}$
 - \mathcal{P}_j = Cells with same pilots as BS j
 - Higher $f \rightarrow$ Fewer users per cell,
but fewer interferers in \mathcal{P}_j



Coordinated Precoding and Detection

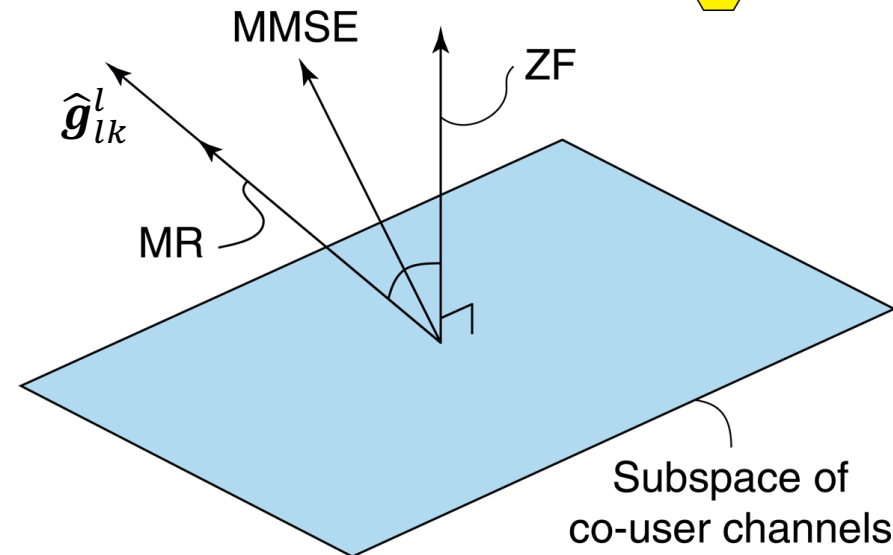
- Coordinated Multi-Point (CoMP)
 - Avoid causing strong inter-cell interference
 - Scalability \rightarrow No signaling between BSs
- Solution: Observe and react ($f \geq 1$)
 - Listen to pilot signals used only in other cells
 - Utilize to suppress inter-cell interference
 - Schemes: Multi-cell ZF and multi-cell MMSE

Reuse $f = 3$



MMSE precoding/detection:

$$\mathbf{v}_{lk} = \left(\underbrace{\sum_{j,m} \rho_u \eta_{jm} \hat{\mathbf{g}}_{jm}^l (\hat{\mathbf{g}}_{jm}^l)^H}_{\text{All estimated channels}} + \underbrace{\mathbf{E}_l + \mathbf{I}}_{\text{Estimation error covariance matrix}} \right)^{-1} \hat{\mathbf{g}}_{lk}^l$$

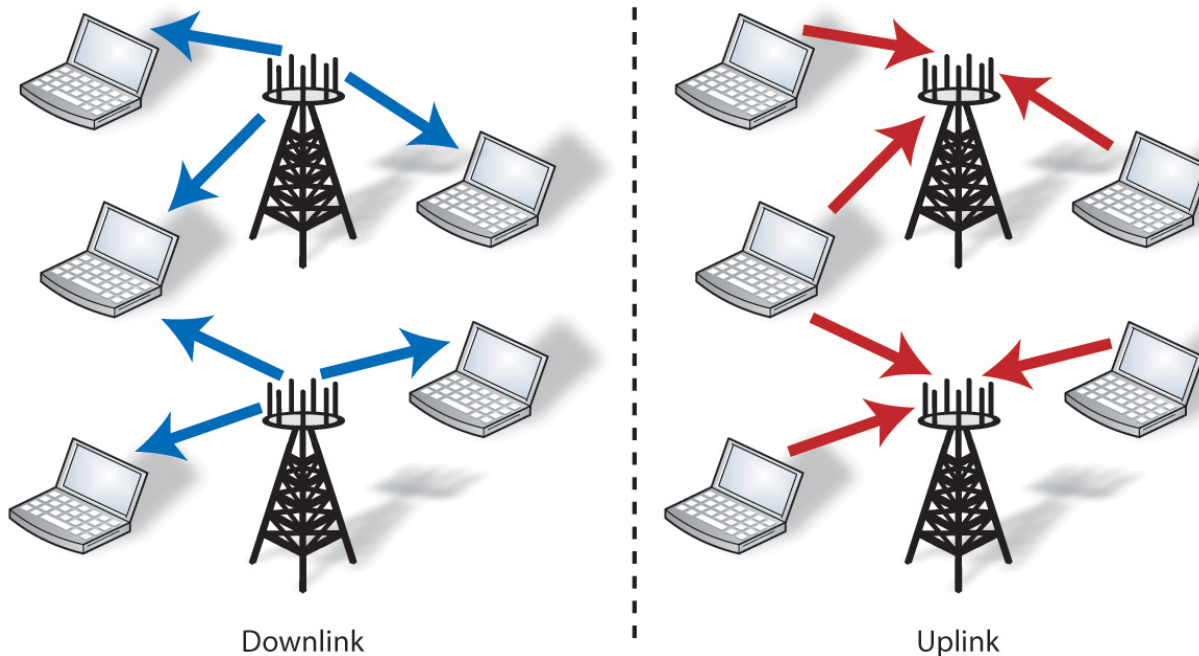


Uplink-Downlink Duality

Duality Theorem

*The uplink SEs are achievable in the downlink using same sum transmit power
Same precoding/detection vectors, but different power allocation*

Note: Equivalence between two lower bounds – uplink bound is looser!



Average Spectral Efficiency per Cell

- Lower Bound on Average Ergodic Capacity in Cell j :

$$SE_j = K \underbrace{\left(1 - \frac{\tau_p}{\tau_c}\right)}_{\text{Loss from pilots}} \log_2 \underbrace{\left(1 + \frac{1}{I_j}\right)}_{\text{SINR}}$$

- Interference term depends on processing:

$$I_j^{\text{MR}} = \underbrace{\sum_{l \in \mathcal{P}_j(f) \setminus \{j\}} \left(\mu_{jl}^{(2)} + \frac{\mu_{jl}^{(2)} - (\mu_{jl}^{(1)})^2}{M} \right)}_{\text{Pilot contamination}} + \underbrace{\left(\frac{\sum_{l \in \mathcal{L}} \mu_{jl}^{(1)} K + \frac{1}{\rho}}{M} \right)}_{\text{Interference from all cells}} \underbrace{\left(\sum_{l \in \mathcal{P}_j(f)} \mu_{jl}^{(1)} + \frac{1}{\rho \tau_p} \right)}_{1/(\text{Estimation quality})} \underbrace{\left(\sum_{l \in \mathcal{P}_j(f)} \mu_{jl}^{(1)} + \frac{1}{\rho \tau_p} \right)}_{\text{Interference suppression}}$$

$$I_j^{\text{ZF}} = \sum_{l \in \mathcal{P}_j(f) \setminus \{j\}} \left(\mu_{jl}^{(2)} + \frac{\mu_{jl}^{(2)} - (\mu_{jl}^{(1)})^2}{M - K} \right) + \left(\frac{\sum_{l \in \mathcal{L}} \mu_{jl}^{(1)} K + \frac{1}{\rho}}{M - K} \right) \left(\sum_{l \in \mathcal{P}_j(f)} \mu_{jl}^{(1)} + \frac{1}{\rho \tau_p} \right) - \sum_{l \in \mathcal{P}_j(f)} \frac{(\mu_{jl}^{(1)})^2 K}{M - K}$$

Only term that remains as $M \rightarrow \infty$: Finite limit on SE

Asymptotic Limit on Spectral Efficiency

- Lower Bound on Average Ergodic Capacity as $M \rightarrow \infty$:

$$\text{SE}_j \rightarrow K \left(1 - \frac{fK}{\tau_c}\right) \log_2 \left(1 + \frac{1}{\sum_{l \in \mathcal{P}_j(f) \setminus \{j\}} \mu_{jl}^{(2)}}\right)$$

How Many Users to Serve?

Pre-log factor $K \left(1 - \frac{fK}{\tau_c}\right)$ is maximized by $K^ = \frac{\tau_c}{2f}$ users*

$$\text{Maximal SE: } \frac{\tau_c}{4f} \log_2 \left(1 + \frac{1}{\sum_{l \in \mathcal{P}_j(f) \setminus \{j\}} \mu_{jl}^{(2)}}\right)$$

Try different f and $\mathcal{P}_j(f)$ to maximize the limit

How Long Pilot Sequences?

$$\tau_p = fK^* = \frac{\tau_c}{2} : \text{ Spend half coherence interval on pilots!}$$

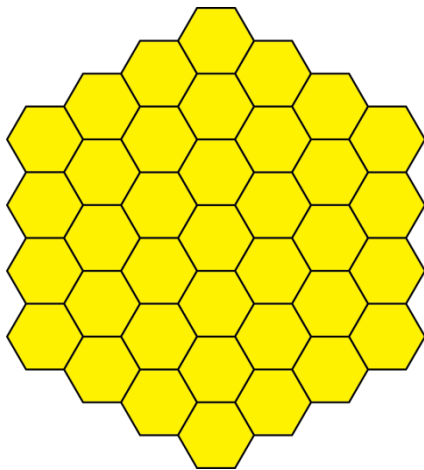
Numerical Results

- Problem Formulation:

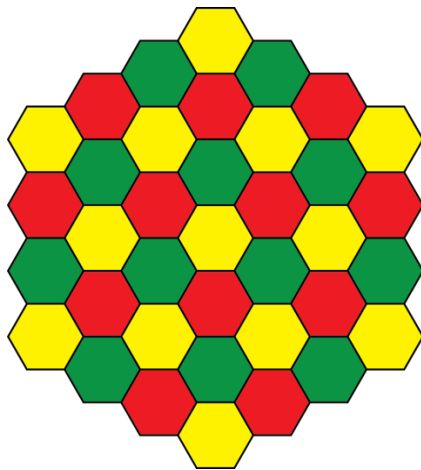
$$\underset{K, \tau_p}{\text{maximize}} \quad \text{total spectral efficiency} \quad [\text{bit/s/Hz/cell}]$$

for a given M and τ_c .

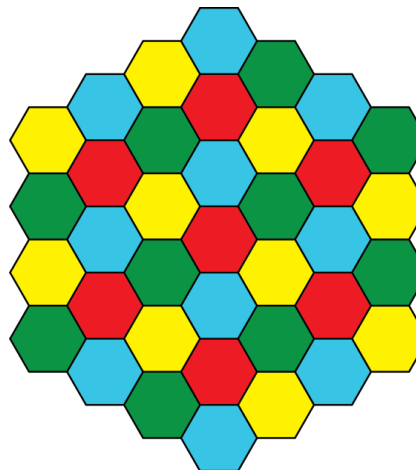
- Use average spectral efficiency expressions
- Compute average interference $\mu_{jl}^{(1)}$ and $\mu_{jl}^{(2)}$ (a few minutes)
- Compute for different K and f and pick maximum (< 1 minute)



Reuse $f = 1$



Reuse $f = 3$



Reuse $f = 4$

Assumptions

Pathloss exponent: 3.7

Coherence: $\tau_c = 400$

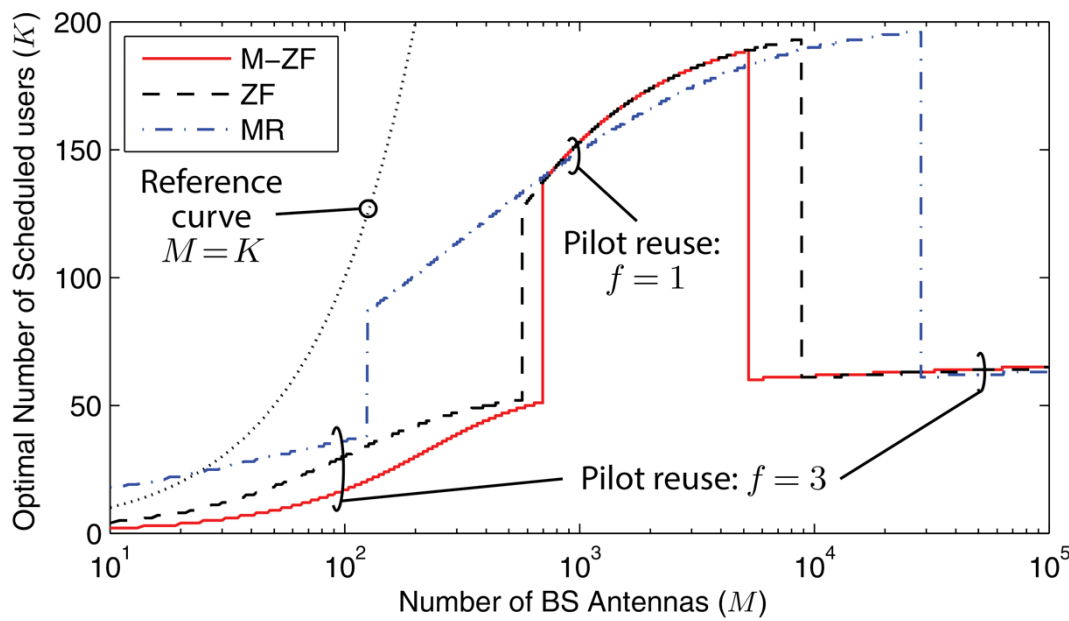
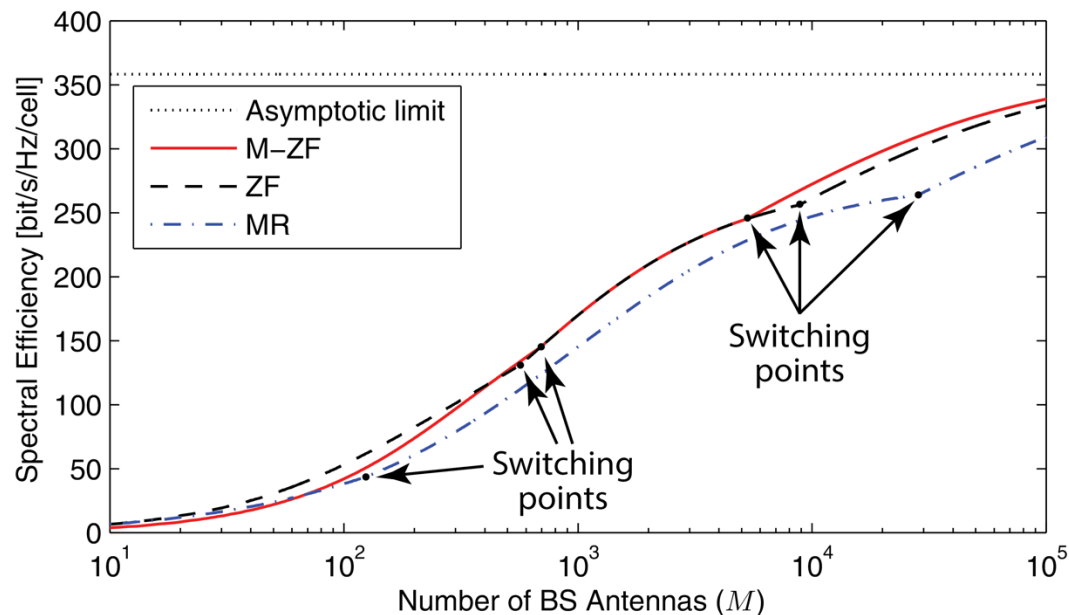
Rayleigh fading

SNR 5 dB

Asymptotic Behavior: Mean-Case Interference

Observations

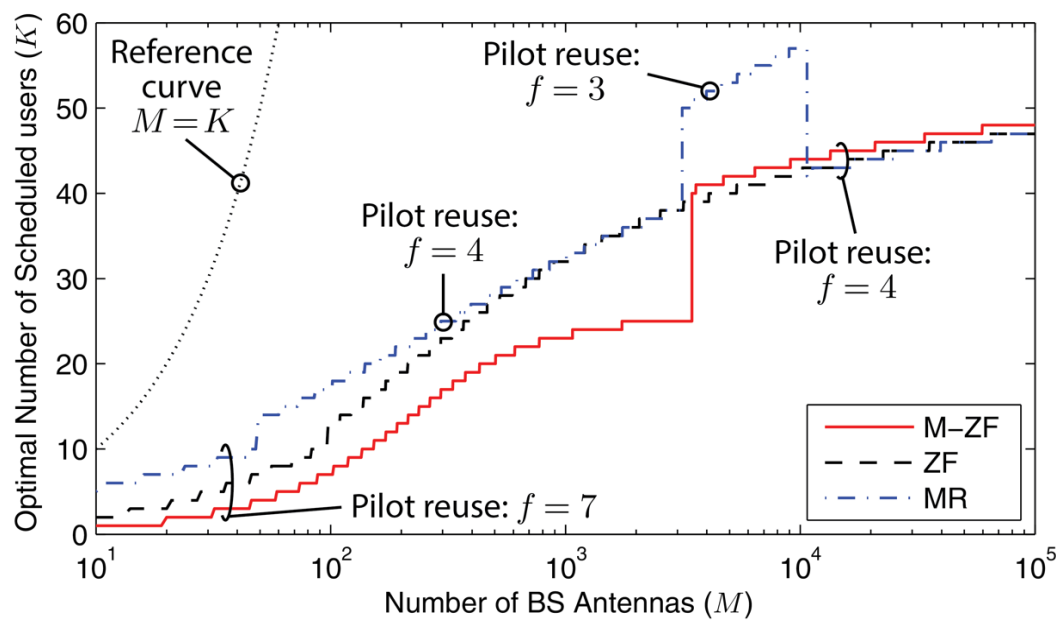
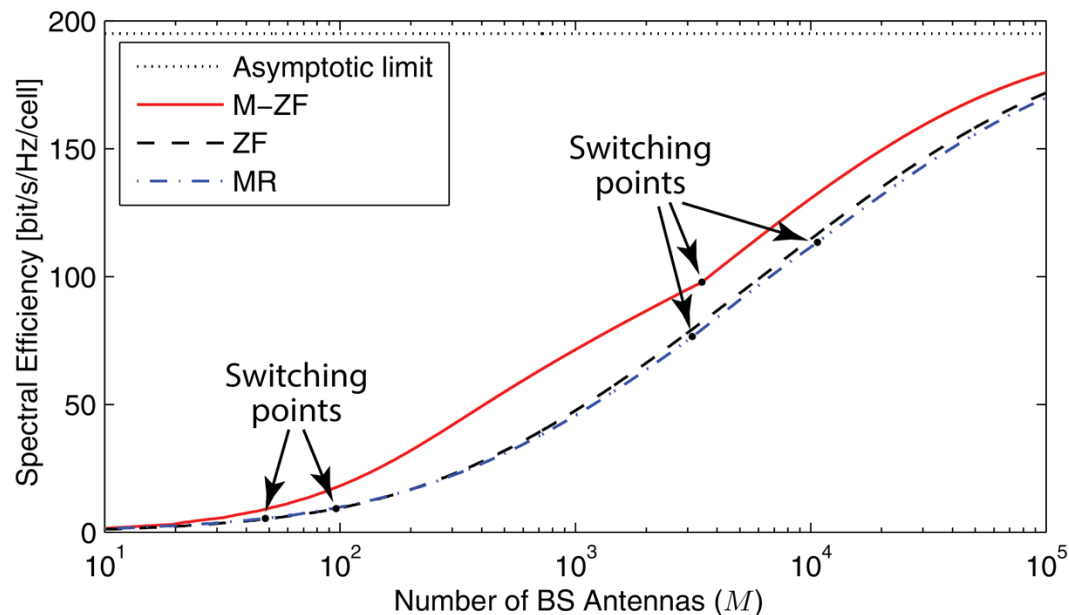
- Uniform user distributions
- Asymptotic limits not reached
- Reuse factor $f = 3$ is desired
- K is different for each scheme
- Small difference between optimized schemes
- Coordinated beamforming:
Better at very large M



Asymptotic Behavior: Worst-Case Interference

Observations

- *Interferers at worst positions*
- *Asymptotic limits not reached*
- *Reuse factor $f = 4$ is desired*
- *K is different for each scheme*
- *Coordinated beamforming:
Brings large gains for all M*



Flexible Number of Users

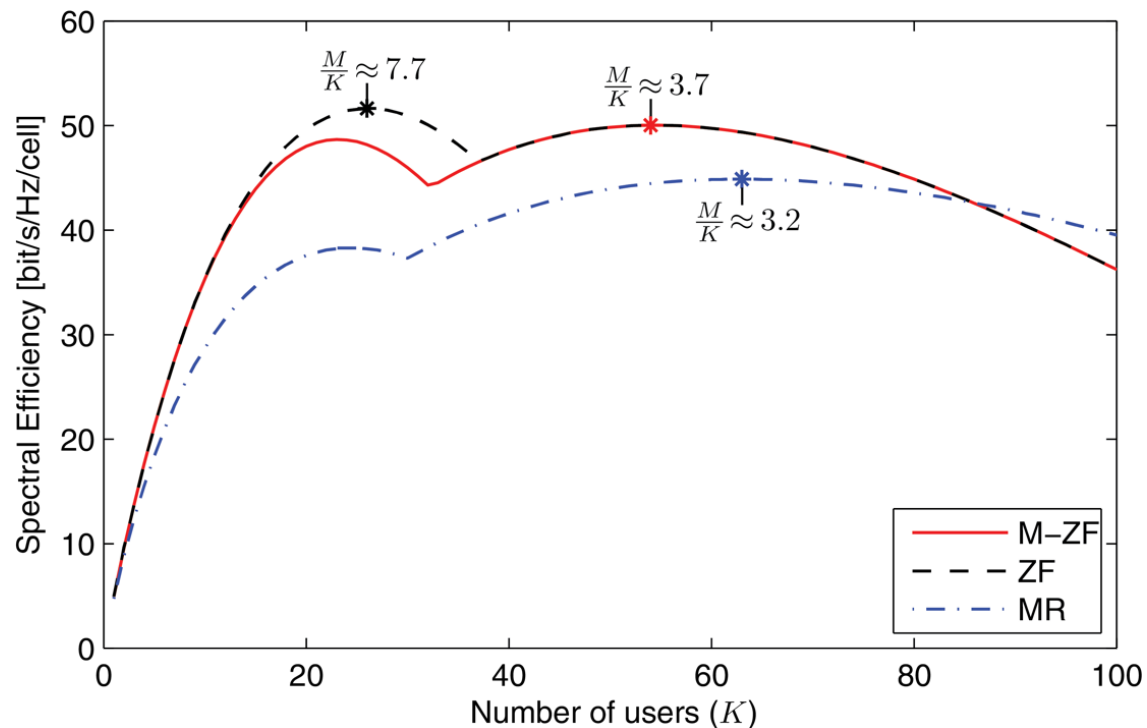
- SE w.r.t. number of users ($M = 200$ antennas)
 - Mean-case interference
 - Optimized reuse factors
 - Equal SNR (5 dB)

Observations

*Stable SE for $K > 10$:
Trivial scheduling:
Admit everyone*

*M-ZF, ZF, and MR provide
similar per-cell performance*

$M/K < 10$ is fine!



Spectral Efficiency per User

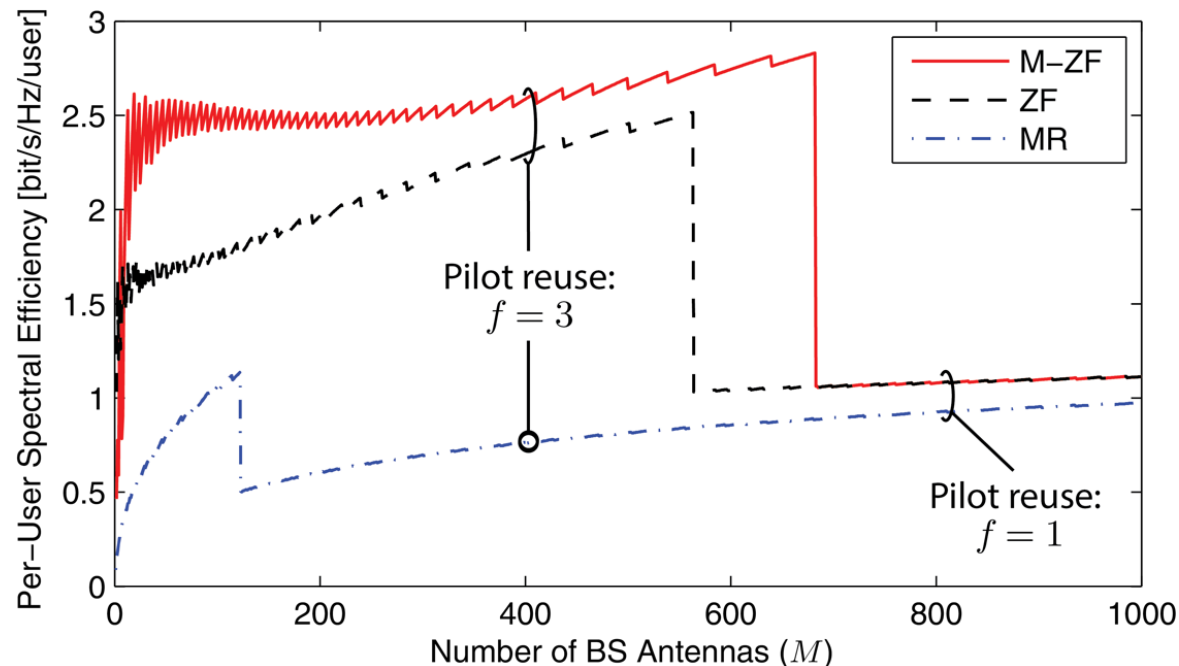
- User Performance for Optimized System
 - Mean-case interference
 - Optimized reuse factors
 - Equal SNR (5 dB)

Observations

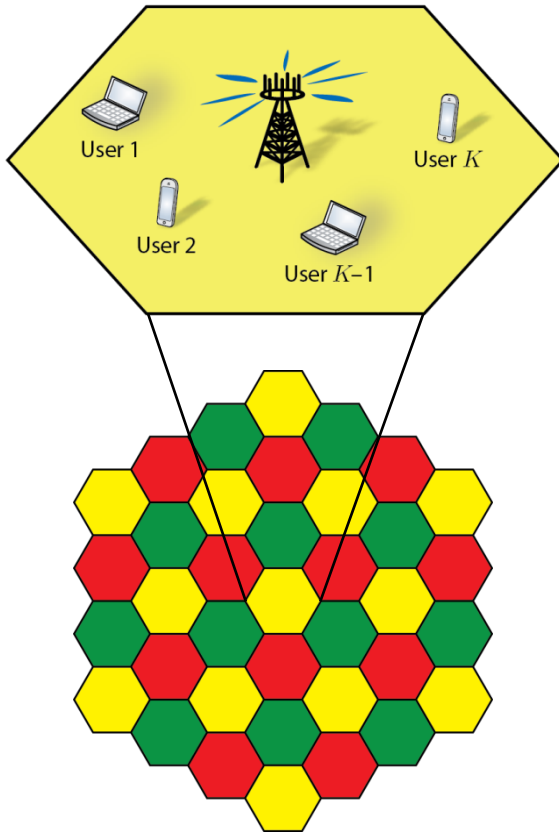
*User performance is modest:
BPSK, Q-PSK, or 16-QAM*

*Schemes for different
purposes:*

$M\text{-ZF} > \text{ZF} > \text{MR}$



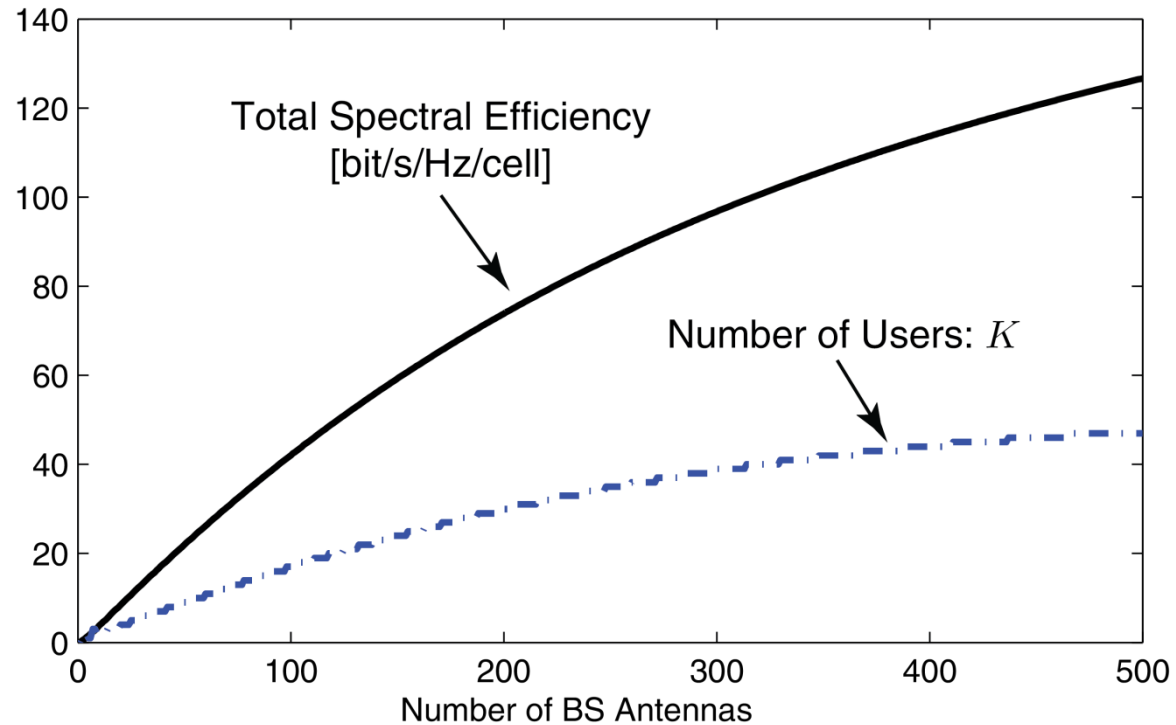
Anticipated Uplink Spectral Efficiency



Assumptions

ZF processing

Pilot reuse: $f = 3$



Observations

- Baseline: 2.25 bit/s/Hz/cell (IMT-Advanced)
- Massive MIMO, $M = 100$: x20 gain ($M/K \approx 6$)
- Massive MIMO, $M = 400$: x50 gain ($M/K \approx 9$)
- Per scheduled user: ≈ 2.5 bit/s/Hz

Control Signaling

- Coherent Precoding and Detection Require CSI
 - How to initiate the transmission without array gain?
- User Initiates Transmission
 - Easy: Find an unused pilot and send a transmission request
 - Reserve some pilot sequences for such random access
- BS Initiates Transmission
 - Harder: Must contact the user without having CSI
 - Low-rate space-time coded transmission is feasible

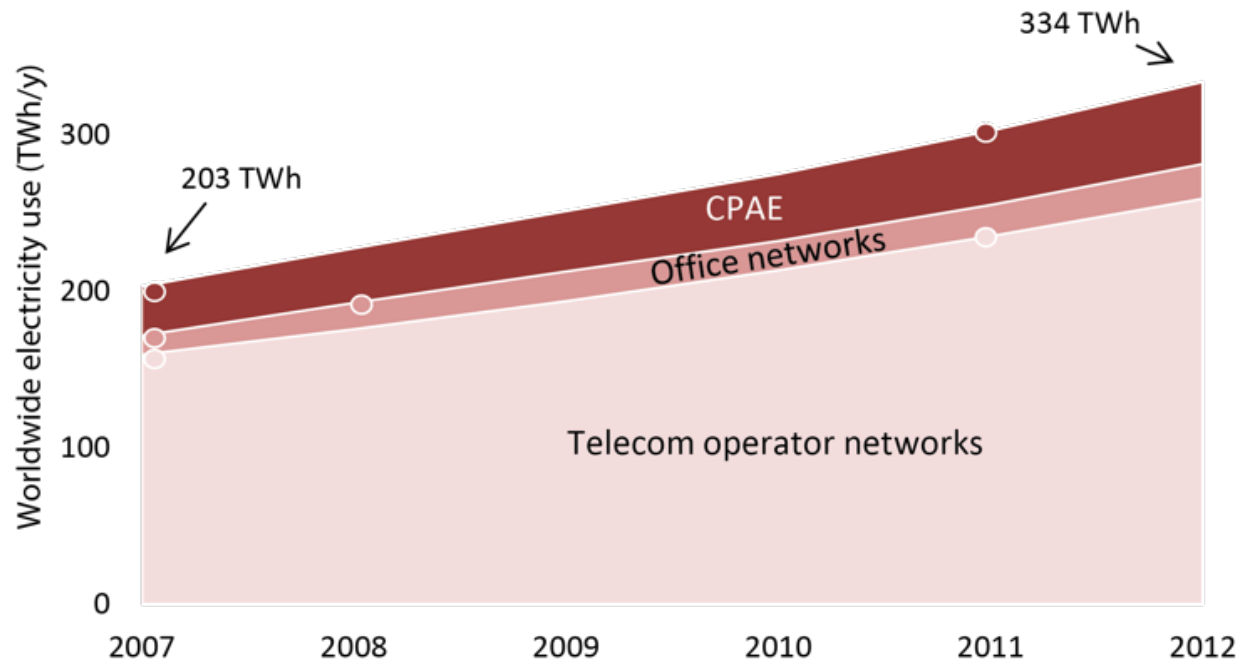
Summary

- Massive MIMO delivers High Spectral Efficiency
 - $> 20\times$ gain over IMT-Advanced is foreseen
 - Very high spectral efficiency per cell, not per user
 - Non-universal pilot reuse ($f = 3$) is often preferred
 - MR, ZF, M-ZF prefer different values on K and f
 - “An order of magnitude more antennas than users” is not needed
- Asymptotic limits
 - Coherence interval (τ_c symbols) limits multiplexing capability
 - Allocate up to $\tau_c/2$ symbols for pilots
 - We can handle very many users/cell – how many will there be?

Massive MIMO and

ENERGY EFFICIENCY

Energy Consumption

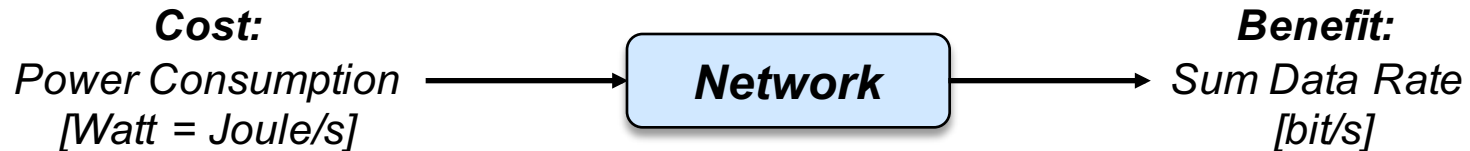


Source: Heddeghem et al.
"Trends in worldwide ICT
electricity consumption
from 2007 to 2012"

- Network Electricity Consumption
 - Dominated by network infrastructure – increases continuously
 - 1000x higher data rates: Easy to achieve using 1000x more power
 Hard to achieve without using more power
 - Calls for **much higher energy efficiency!**

What is Energy Efficiency?

- Benefit-Cost Analysis of Networks
 - Systematic approach to analyze strengths and weaknesses of networks



- Definition: Energy Efficiency (EE):

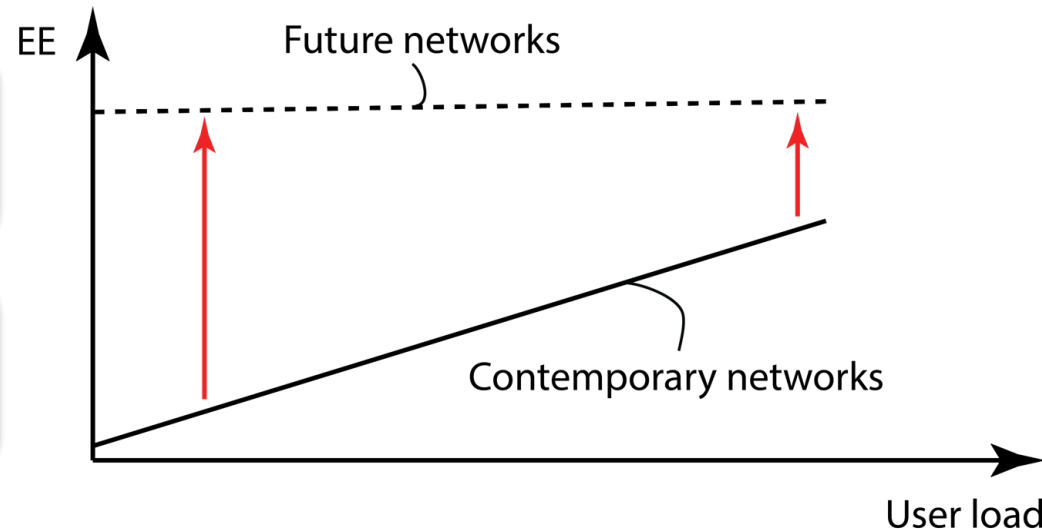
$$EE \text{ [bit/Joule]} = \frac{\text{Average Sum Rate [bit/s/cell]}}{\text{Power Consumption [Joule/s/cell]}}$$

Contemporary networks:

Very inefficient at low load

Future networks:

Must be more efficient at any load



Transmit Power Scaling Law

Power Scaling Law

If the transmit power p decreases as $1/M^\alpha$ for $\alpha \leq 1/2$:

SE will not go zero as $M \rightarrow \infty$

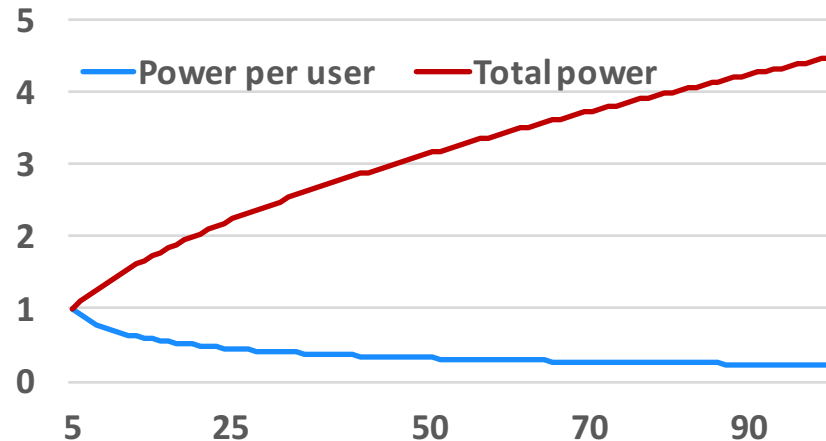
Example: Set $p = p_0/M^\alpha$ in $SE_j = K \left(1 - \frac{\tau_p}{\tau_c}\right) \log_2 \left(1 + \frac{1}{I_j}\right)$:

$$I_j^{\text{MR}} = \sum_{l \in \mathcal{P}_j(f) \setminus \{j\}} \left(\mu_{jl}^{(2)} + \frac{\mu_{jl}^{(2)} - (\mu_{jl}^{(1)})^2}{M} \right) + \left(\frac{\sum_{l \in \mathcal{L}} \mu_{jl}^{(1)} K + \frac{M^\alpha}{p_0}}{M} \right) \left(\sum_{l \in \mathcal{P}_j(f)} \mu_{jl}^{(1)} + \frac{M^\alpha}{p_0 \tau_p} \right) = \sum_{l \in \mathcal{P}_j(f) \setminus \{j\}} \mu_{jl}^{(2)} + \mathcal{O} \left(\frac{M^{2\alpha}}{M} \right)$$

Observations ($\alpha = 1/2$)

Power per antenna/user: Decreases as $\frac{1}{\sqrt{M}}$


Total power: $\frac{K}{\sqrt{M}}$ increases as \sqrt{M} for fixed $\frac{M}{K}$



Radiated Energy Efficiency

- Energy Efficiency with Power Scaling:

$$EE = \frac{\text{Average Sum Rate [bit/s/cell]}}{\text{Power Consumption [Joule/s/cell]}} = \frac{B \cdot K \left(1 - \frac{\tau_p}{\tau_c}\right) \log_2 \left(1 + \frac{1}{I_j}\right)}{\frac{K p_0}{M^\alpha} \mathbb{E} \left\{ \frac{1}{\beta_{lk}^l} \right\}}$$

- Bandwidth: B Hz
- Consequence of scaling law as $M \rightarrow \infty$:
 - Sum rate \rightarrow constant > 0
 - Transmit power $\rightarrow 0$ $EE \rightarrow \infty$

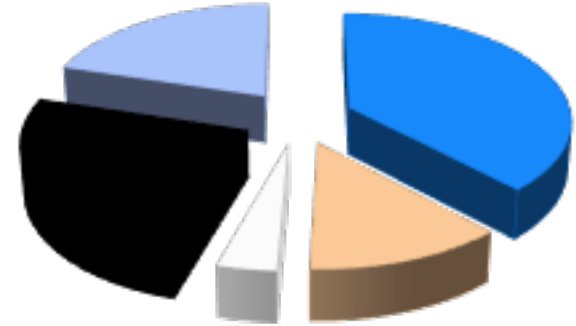
Is Massive MIMO Incredibly Energy Efficient?

Yes, in terms of bringing down the radiated transmit power

But not all consumed power is radiated!

Generic Power Consumption Model

- Many Components Consume Power
 - Radiated transmit power
 - Baseband signal processing (e.g., precoding)
 - Active circuits (e.g., converters, mixers, filters)
- Average Power Consumption Model:



$$APC = \frac{Kp}{\eta} \mathbb{E} \left\{ \frac{1}{\beta_{lk}^l} \right\} + C_{0,0} + \underbrace{C_{0,1}M + C_{1,0}K + C_{1,1}MK}_{\text{Circuit power per transceiver chain}}$$

*Power amplifier
(η is efficiency)*

*Circuit power per
transceiver chain*

*Fixed power
(control signals, backhaul,
load-independent processing)*

*Cost of digital signal processing
(e.g., channel estimation
and precoding computation)*

***Nonlinear increasing
function of M and K***

Many coefficients: $\eta, C_{i,j}$ for different i, j

Optimizing a Cellular Network for High EE

- Clean Slate Network Design
 - Select BS density:
 λ BSs per km^2
 - Select M and K per cell
 - Asymmetric user load \rightarrow asymmetric deployment

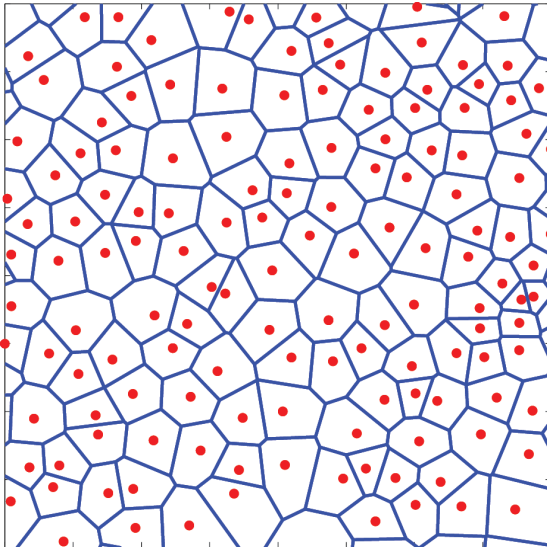
Spatial Point Processes

Tractable way to model randomness

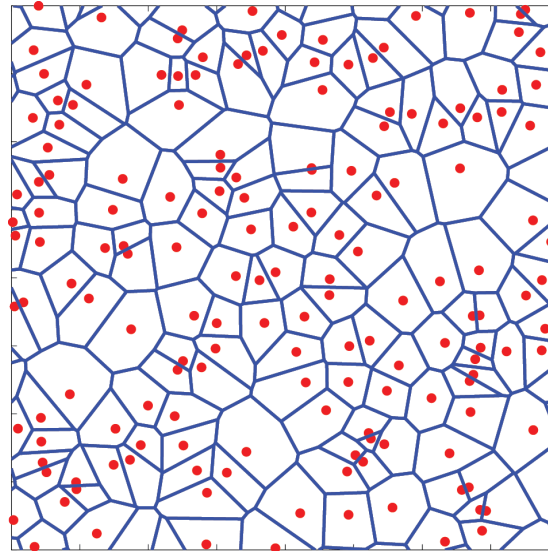
Poisson point process (PPP):

$\text{Po}(\lambda A)$ BSs in area of size $A \text{ km}^2$

*Random independent deployment:
Lower bound on practical performance*



Real BS deployment



Poisson point deployment

*Source: Andrews et al.
"A Tractable Approach
to Coverage and Rate in
Cellular Networks"*

Average Uplink Spectral Efficiency

Assumptions

BSs distributed as PPP: λ BS/km²

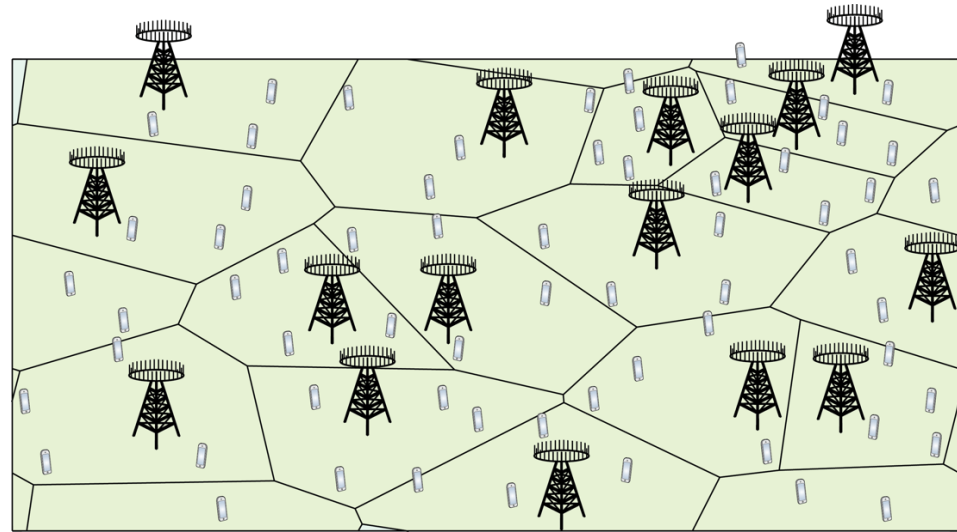
M antennas per BS, K users per cell

Random pilot allocation: $\tau_p = fK$

Statistical channel inversion: p/β_{lk}^l

Pathloss over noise:

$$\beta_{lk}^j = \omega^{-1} (\text{distance [km]})^{-\alpha}$$



Power per user: $\mathbb{E} \left\{ \frac{p}{\beta_{lk}^l} \right\} = p\omega \frac{\Gamma(\alpha/2-1)}{(\pi\lambda)^{\alpha/2}}$

Lower Bound on Average SE with MR

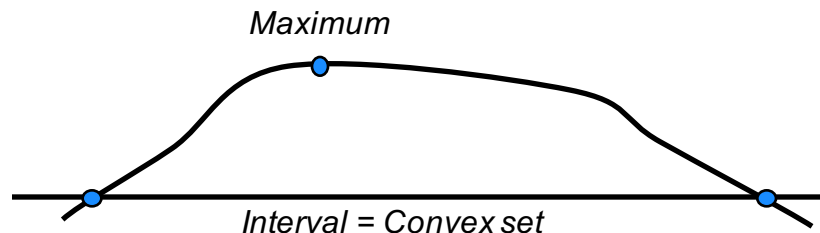
$$\underline{\text{SE}} = \left(1 - \frac{fK}{\tau_c}\right) \log_2(1 + \underline{\text{SINR}})$$

$$\underline{\text{SINR}} = \frac{M}{\left(K + \frac{1}{p}\right) \left(1 + \frac{2}{f(\alpha-2)} + \frac{1}{p}\right) + \frac{2K}{\alpha-2} \left(1 + \frac{1}{p}\right) + \frac{K}{f} \left(\frac{4}{(\alpha-2)^2} + \frac{1}{\alpha-1}\right) + \frac{M}{f(\alpha-1)}}$$

Maximizing Energy Efficiency

$$\begin{array}{ll} \underset{M, K, p, \lambda, f}{\text{maximize}} & \frac{B \cdot K \left(1 - \frac{fK}{\tau_c}\right) \log_2(1 + \underline{\text{SINR}})}{\text{APC}} \\ \text{subject to} & \underline{\text{SINR}} \geq \gamma \end{array}$$

- Average SINR constraint γ needed to not get too low SE
 - Is the solution small cells (high λ) or Massive MIMO (high M)?
 - Main Properties
 1. Can pick f to satisfy SINR constraint
 2. By setting $p = p_0 \lambda$, the EE is increasing in λ
 3. Quasi-concave function w.r.t. M and K
- Possible to solve the problem numerically*



Simulation Parameters

Parameter	Symbol	Value
Coherence interval	τ_c	400
Pathloss exponent	α	3.76
Pathloss over noise at 1 km	ω	33 dBm
Amplifier efficiency	η	0.39
Bandwidth	B	20 MHz
Static power	$C_{0,0}$	10 W
Circuit power per active user	$C_{1,0}$	0.1 W
Circuit power per BS antenna	$C_{0,1}$	1 W
Signal processing coefficient	$C_{1,1}$	3.12 mW

We publish simulation code to enable simple testing of other values!

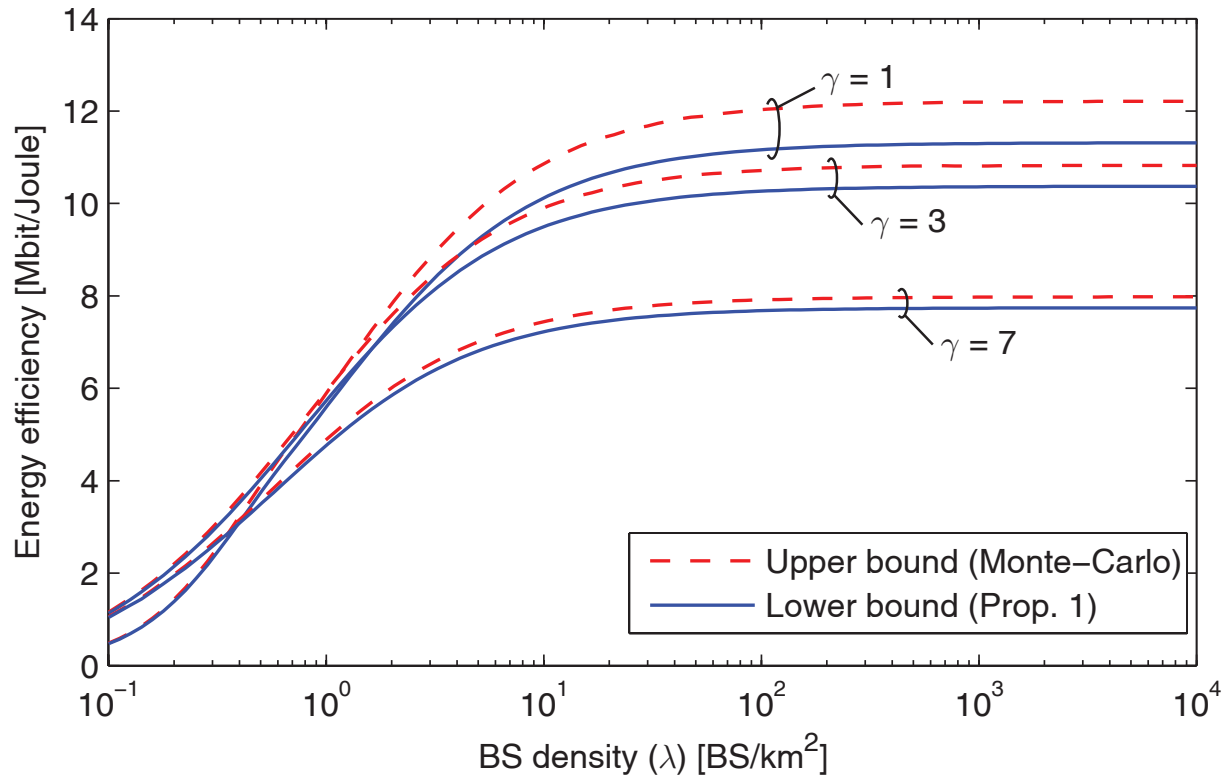
Impact of BS Density

Simulation

Different BS densities
Other variables optimized

Observations

Lower bound is tight
Higher EE with lower γ
EE increases with λ



Saturation Property

EE gain from small cells saturates at $\lambda = 10$
This is satisfied in most urban deployments (300 m between BSs)
We can safely let $\lambda \rightarrow \infty$ to simplify analysis

Optimal Number of Antennas and Users

Real-valued Optimization

Optimal $K \in \mathbb{R}$ found in closed-form for fixed M / K

Optimal $M \in \mathbb{R}$ found in closed-form for fixed K

Alternating optimization reaches global maximum

Properties: Optimal K and M

\searrow : *Decrease as $C_{0,1}$, $C_{1,0}$, and $C_{1,1}$ increase*

\nearrow : *Increase as $C_{0,0}$ increases*

Intuition: Activate more hardware if the relative cost is small

Impact of Number of Antennas and Users

Simulation

Optimized f, λ, p

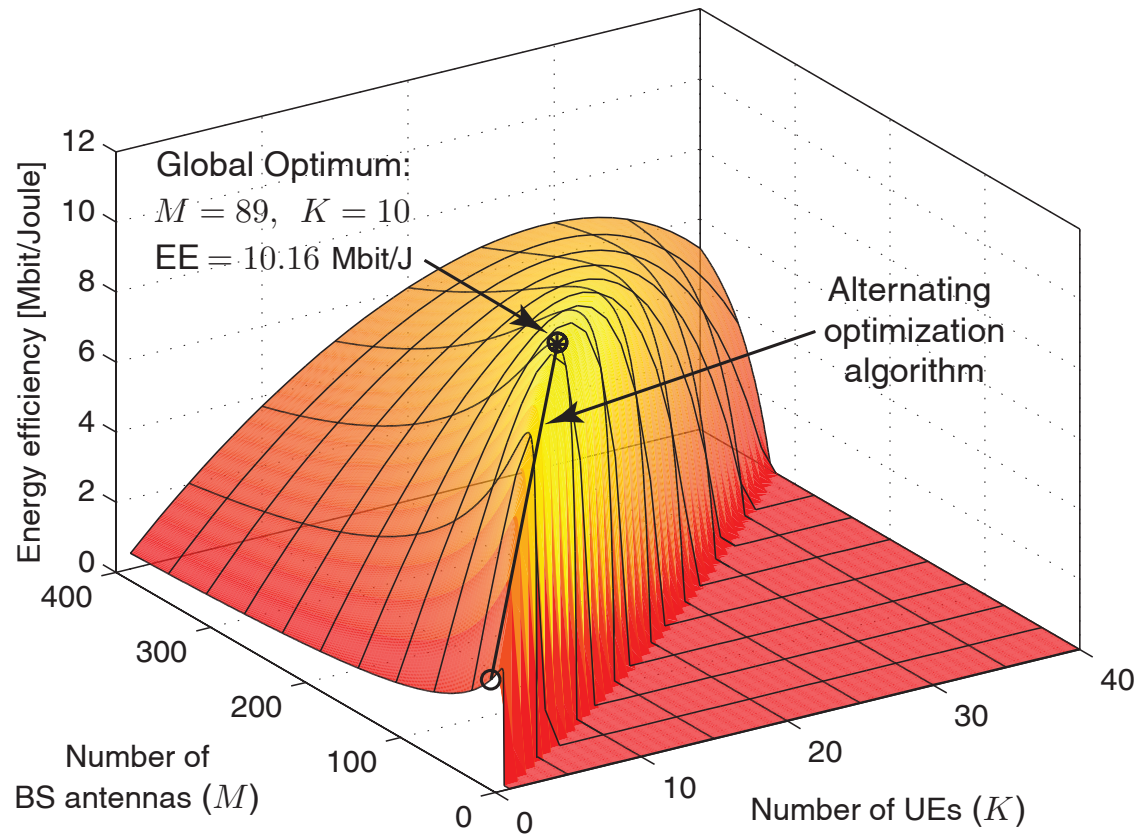
SINR constraint: $\gamma = 3$

Observations

Optimal: $M = 89, K = 10$

*Massive MIMO with
reuse factor $f \approx 7$*

Many good solutions



Why is Massive MIMO Energy Efficient?

Interference suppression: Improve SINR, not only SNR as with small cells

Sharing cost: Fixed circuit power costs are shared

Optimization with Given User Density

- User Density
 - So far: K and λ design variables
 - Density: λK users per km^2
 - Heterogeneous user distribution

Practical User Densities

Rural: 10^2 per km^2

Urban: 10^3 per km^2

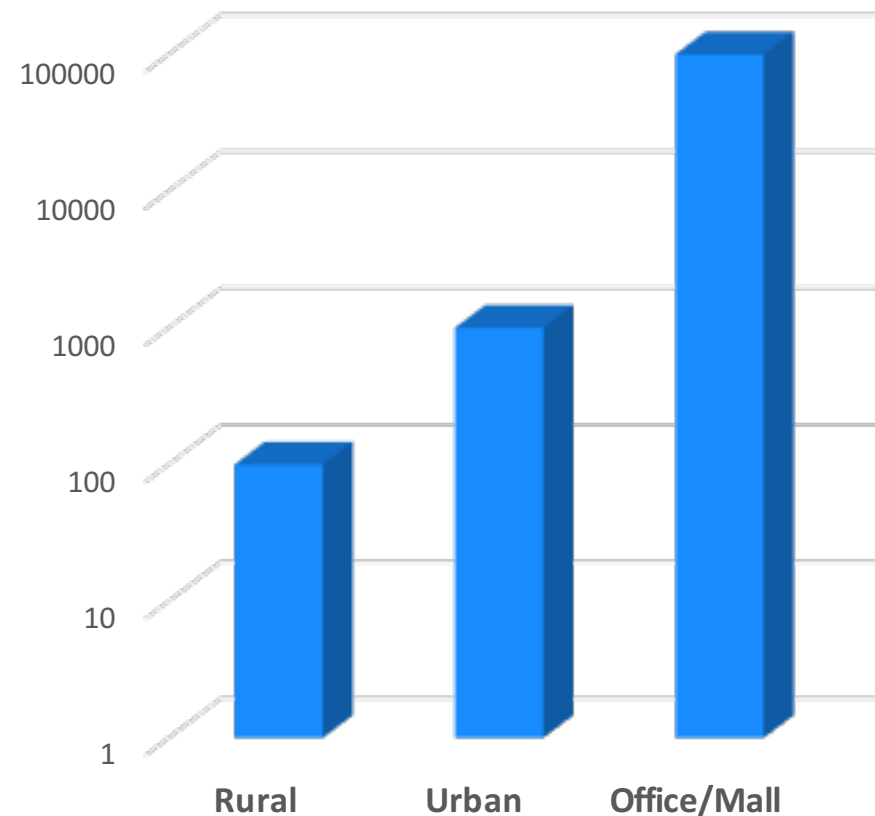
Office/Mall: 10^5 per km^2

Source: METIS, "Deliverable D1.1: Scenarios, requirements and KPIs for 5G mobile and wireless system"

Can we Optimize this Density?

Increase: No, cannot "create" users

Decrease: Yes, by scheduling



Impact of User Density

Simulation

Fixed user density μ users/km²

Rural: $\mu = 10^2$, Malls: $\mu = 10^5$

EE maximization with constraint $K\lambda = \mu$

Low User Density

Many cells with $K \approx 1$

Most important to reduce pathloss

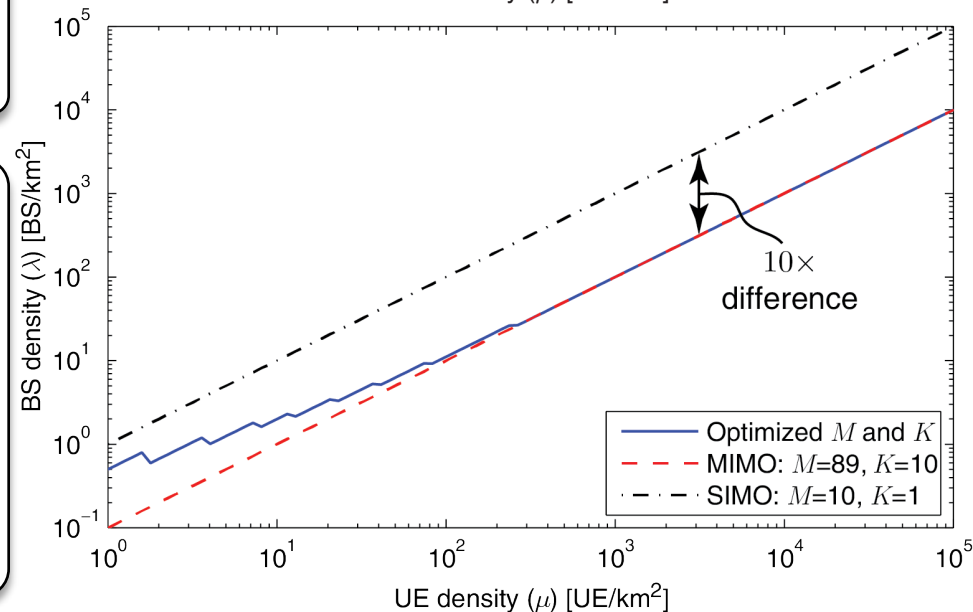
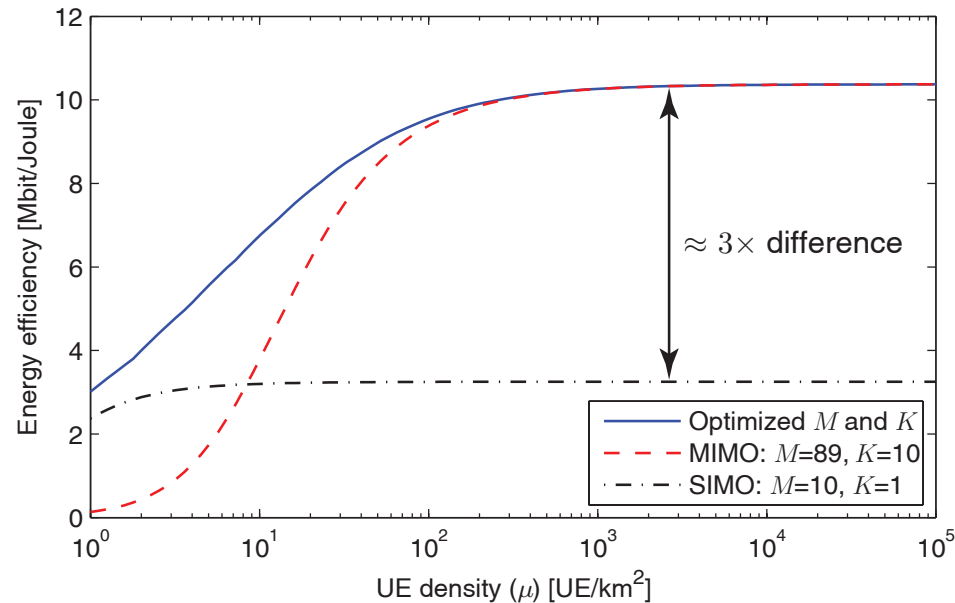
High User Density

Massive MIMO is optimal

Saturation for $\mu \geq 100$:

Covers both rural and shopping malls

Share circuit power and cost over users



Summary

- Transmit Power Scaling Law
 - Reduced as $1/\sqrt{M}$ per user, but total transmit power might increase
 - Reduced as $1/\sqrt{M}$ per BS antenna → Use handset technology?
- Designing Networks for Energy Efficiency
 - Large cells: First step is to reduce cell size
 - Smaller cells: Transmit power only a small part → Use Massive MIMO
 - Intuition: Suppress interference, share circuit power over many users
 - Non-universal pilot reuse is important in random deployments
 - Several Mbit/Joule achieved without coordination

Massive MIMO and

HARDWARE EFFICIENCY

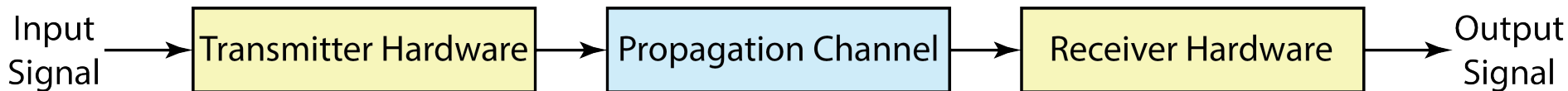
Many Antennas and Transceiver Chains

- Many Antenna Elements
 - LTE 4-MIMO: $3 \cdot 4 \cdot 20 = 240$ antennas
But only 12 transceiver chains!
 - Massive MIMO = M transceiver chains
- End-to-end Channels
 - Wireless propagation channel
 - Transceiver hardware
 - Simple model:



3 sectors, 4 arrays/sector, 20 antennas/array

Image source: gigaom.com

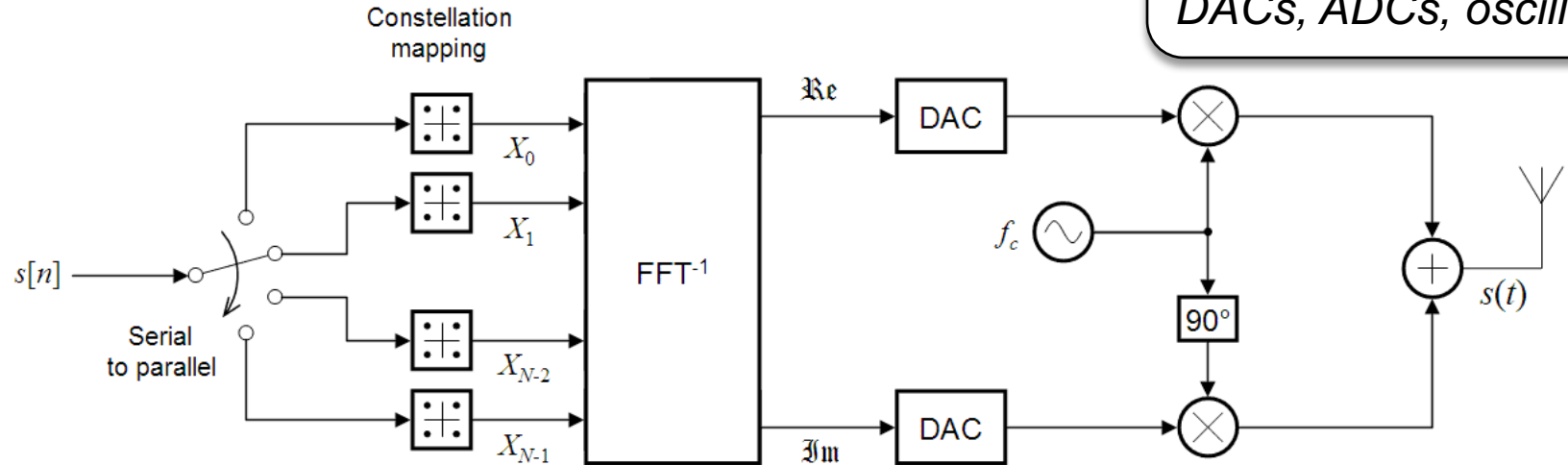


Can We Afford M High-Grade Transceiver Chains?

Can Massive MIMO utilize the hardware components more efficiently?

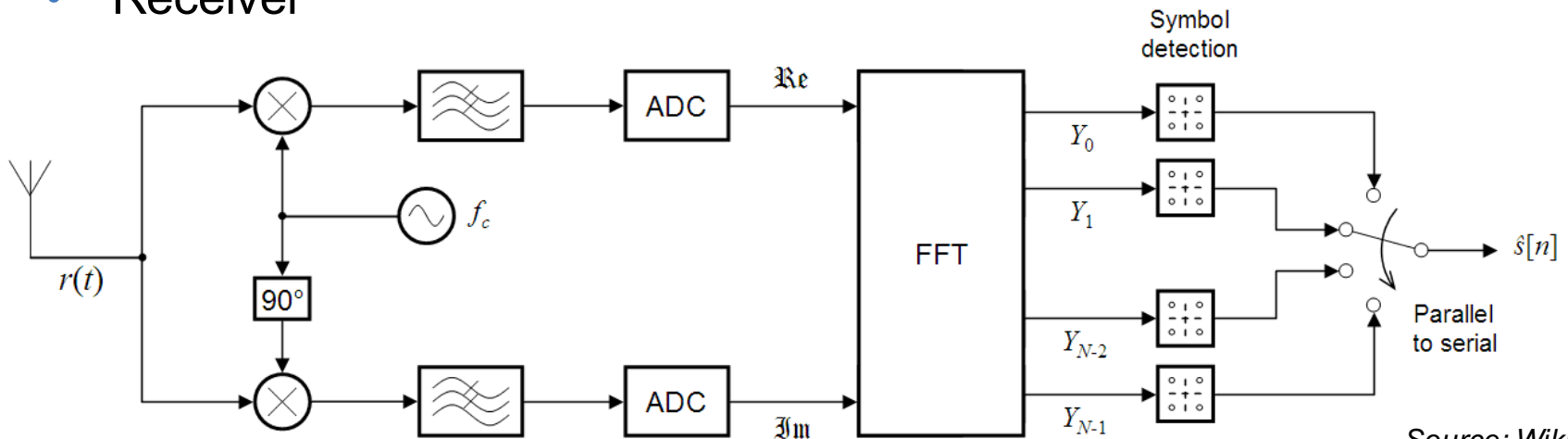
Orthogonal frequency-division multiplexing (OFDM)

- Transmitter



Main Components
*Filters, I/Q mixers,
DACs, ADCs, oscillators*

- Receiver

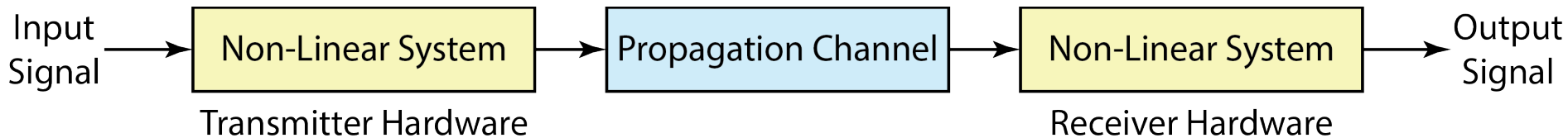


Modeling of Hardware Impairment

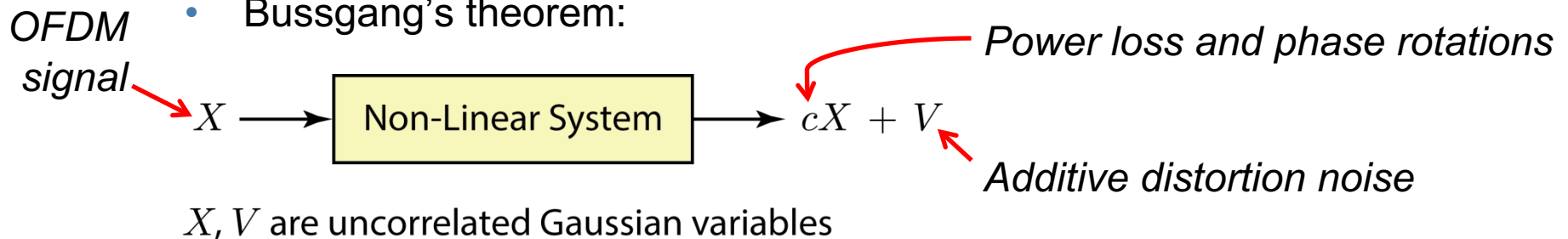
- Real Transceivers have Hardware Impairments
 - Ex: Phase noise, I/Q-imbalance, quantization noise, non-linearities, etc.
 - Each impairment can be modeled (for given hardware, waveform etc.)
 - But: Impact reduced by calibration and only combined effect matters!

More impairments = Lower price, lower power, smaller size

- High-Level Hardware Model:



- Busgang's theorem:



Classical Impact of Hardware Impairments

- Impact on Point-to-Point MIMO
 - Low SNR: Negligible impact on spectral efficiency
 - High SNR: Fundamental upper limit

Error Vector Magnitude

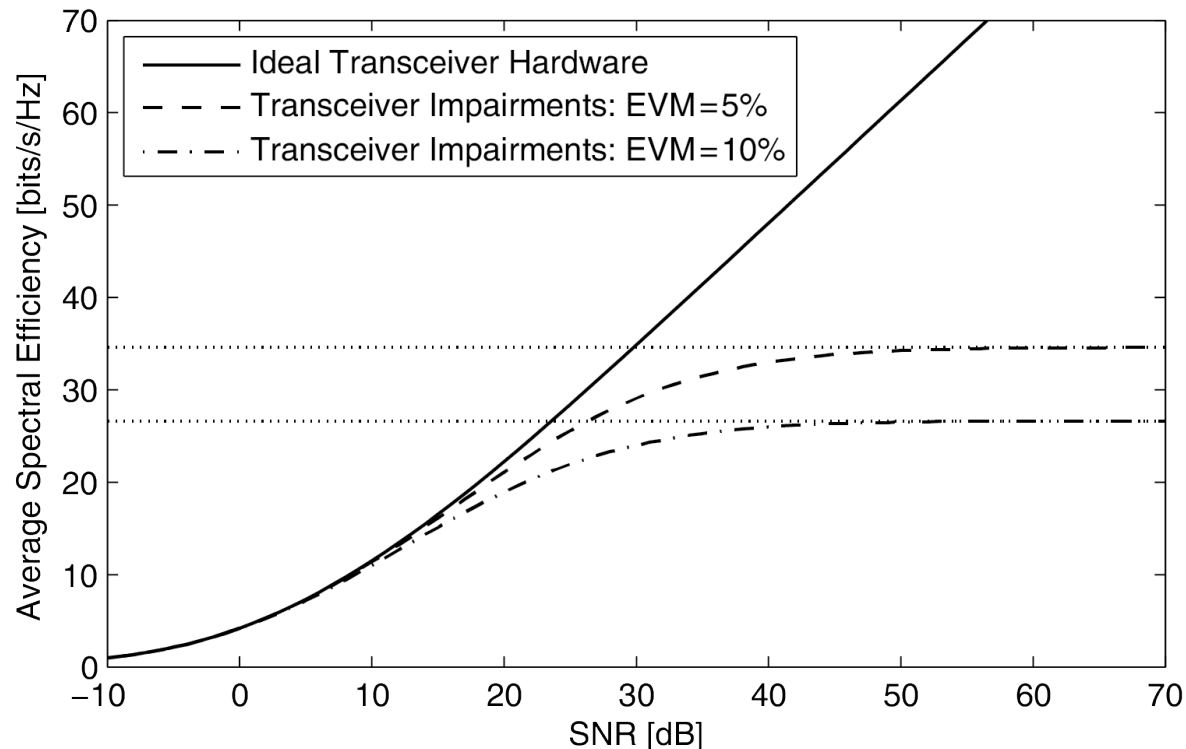
$$\text{EVM} = \frac{\text{Distortion magnitude}}{\text{Signal magnitude}}$$

Distortion scales with signal power

LTE EVM limits: 8%-17.5%

What about large M regime?

Large or small impact?



Example: 4x4 point-to-point MIMO, i.i.d. Rayleigh fading

Distortion Noise: Definition and Interpretation

- Uplink Signal (conventional):

$$\mathbf{y} = \sum_k \mathbf{g}_k x_k + \mathbf{w}$$

Distortion Noise Model

*Gaussian distributed
Independent between
users and antennas*

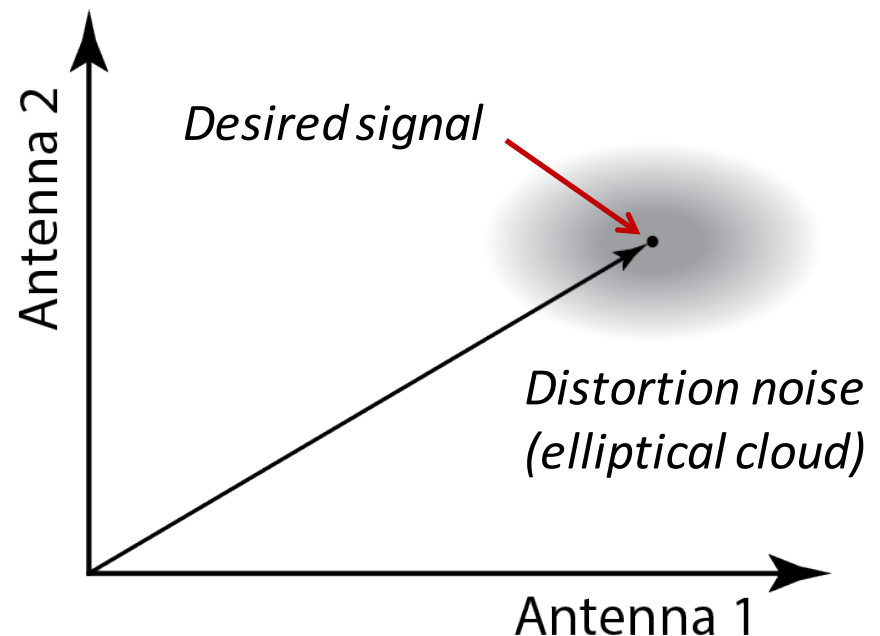
Error Vector Magnitude (at transmitter)

$$\text{EVM}^{\text{tx}} = \frac{\sqrt{\mathbb{E}\{|\xi_k^{\text{tx}}|^2\}}}{\sqrt{\mathbb{E}\{|c_k^{\text{tx}} x_k|^2\}}}$$

- Uplink Signal (with impairments):

$$\mathbf{y} = c^{\text{rx}} \sum_k \mathbf{g}_k (c_k^{\text{tx}} x_k + \xi_k^{\text{tx}}) + \xi^{\text{rx}} + \mathbf{w}$$

Gain losses
Transmitter distortion
Receiver distortion



What is the Impact of Distortion Noise?

Uplink Single-User Scenario

Rayleigh fading, SNR = 5 dB

Observations

Ideal: $SE = \mathcal{O}(\log M)$

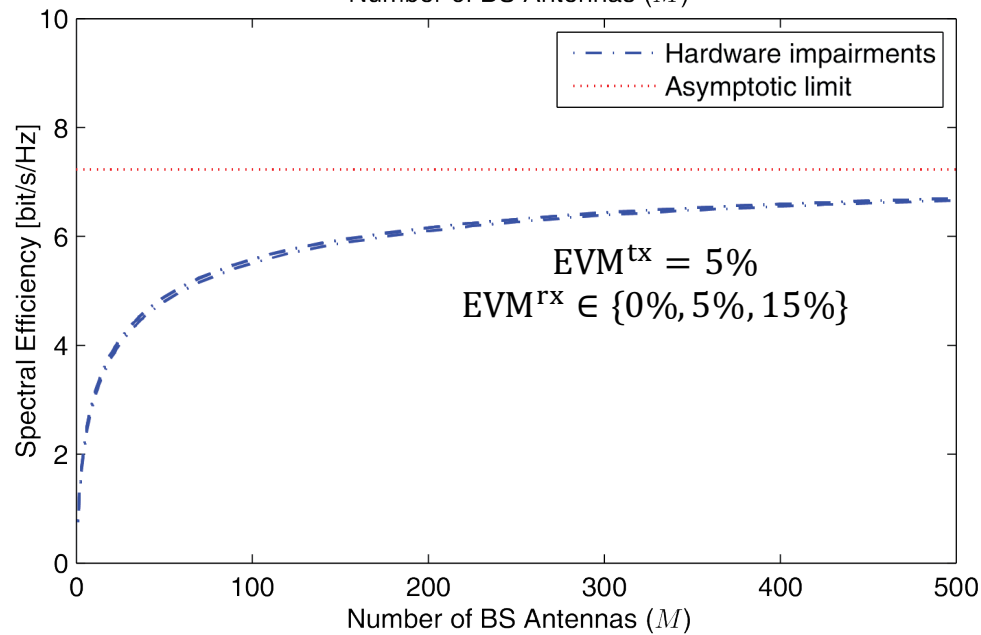
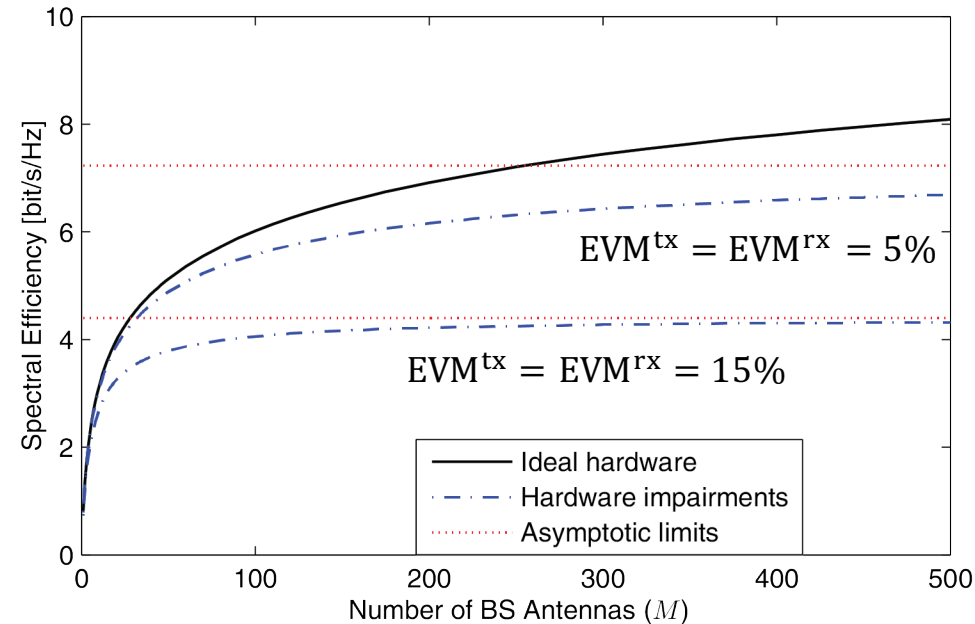
Non-ideal: Asymptotic limits

Higher EVM \rightarrow Lower limit

Observations

Impairments caused by user device determine the limit

*Distortion noise caused by BS averages out as $M \rightarrow \infty$
(cf. inter-user interference)*



Multi-Cell Scenario with Distortion Noise

Uplink Multi-Cell Scenario

Rayleigh fading, SNR = 5 dB

$K = 8$ users per cell

MR detection

Hardware Scaling Law

If BS distortion variance increases as M^κ for $\kappa \leq 1/2$:

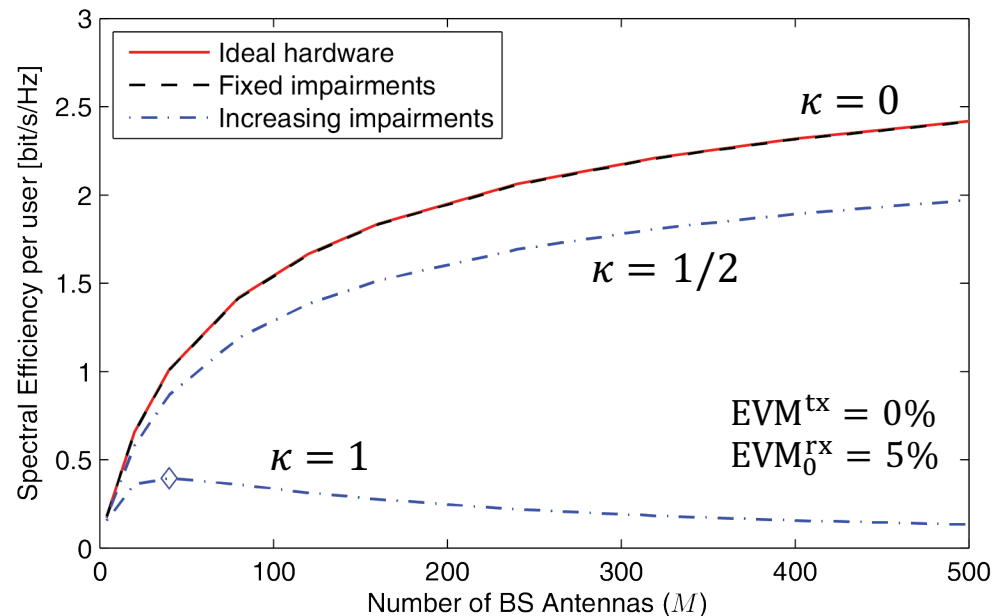
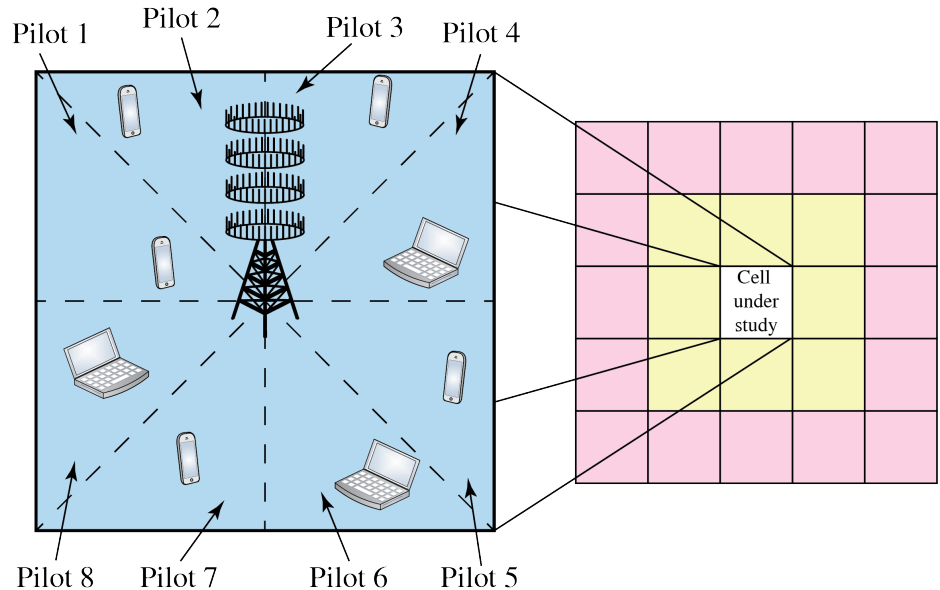
SE will not go zero as $M \rightarrow \infty$

Can be proved rigorously!

Observations

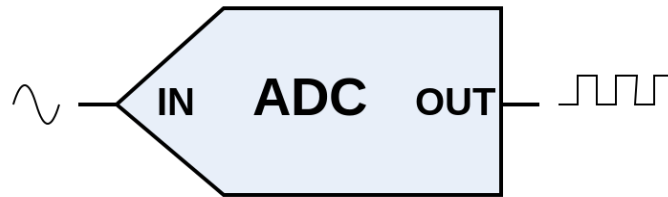
Small loss if law is followed

Otherwise large loss!



Utilizing the Hardware Scaling Law

- Massive MIMO can use Lower-Grade Hardware
 - Reduced cost, power consumption, and size
- Example: Analog-to-Digital Converter (ADC)
 - One b -bit ADC per Transceiver Chain



*Image source:
Wikipedia*

- Adds quantization noise roughly proportional to 2^{-2b} :

$$\sqrt{M} = c_0 \cdot 2^{-2b} \Rightarrow b = \frac{1}{2} \log_2(c_0) - \frac{1}{4} \log_2(M)$$

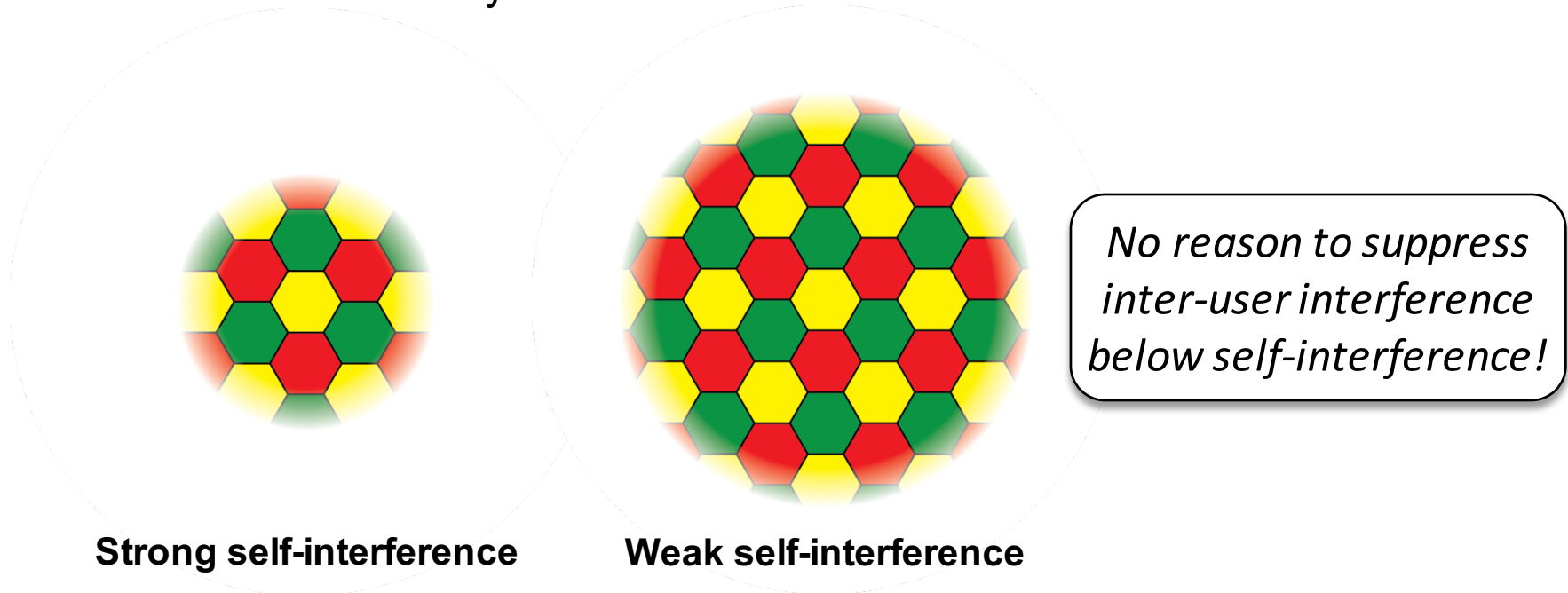
Ex: $M = 256$ requires 2 fewer bits than $M = 1$ (even 1-bit ADCs possible)

- Circuit power roughly proportional to 2^{2b} :

Ex: Power of M ADCs can scale as \sqrt{M} rather than M

Interference Visibility Range

- Only Remaining Interference as $M \rightarrow \infty$:
 - Pilot contamination (reuse of pilot resources)
 - Hardware impairments (at user devices)
- Distortion Noise as Self-interference
 - Limits the visibility of inter-user interference



Summary

- Any Transceiver is Subject to Hardware Impairments
 - Massive MIMO is resilient to such imperfections
 - Distortion variance at BS may increase as \sqrt{M}
 - High-grade BS hardware is not required!
 - User hardware quality is the fundamental limitation
- Further Remarks
 - Analysis with more detailed hardware models show same behavior
 - Phase noise is not worse than in small MIMO systems
 - Reduced transmit power and relaxed impairment constraints
→ New compact transceiver designs?

Part 4

OPEN PROBLEMS

Open Problems and Active Research Topics

1. Channel measurements and modeling
2. Circuit and transceiver design
3. Implementation-aware algorithmic design
4. Dealing with hardware impairments and reciprocity calibration
5. Exploiting $M - K$ excess degrees of freedom
6. FDD operation for “low mobility” or “highly structured channels”
7. MAC-layer design, power control, and scheduling
8. Control signaling and BS transmission without CSI
9. New deployment scenarios (e.g., distributed arrays or cell-free)
10. Mitigation of pilot contamination
11. System-level studies and coexistence with HetNets or D2D
12. Massive MIMO in millimeter wave bands

SUMMARY

Summary

- Massive MIMO has Many Extraordinary Benefits
 - **High spectral efficiency:** >20x gains over IMT-Advanced are foreseen
 - High SE per cell, but modest per user
 - Important: Non-universal pilot reuse, pilots use large part of coherence interval
 - **High energy efficiency:** Tens of Mbit/Joule are foreseen
 - Reduced transmit power per user and antenna, maybe not per cell
 - Circuit power dominates power consumption in urban scenarios
 - Important: Interference control, sharing circuit power between users
 - **High hardware efficiency:** High-grade hardware is not needed
 - Variance of distortion noise at BS can scale with number of antennas
 - Important: Quality of user device is the limiting factor

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Bringing an Extraordinary Technology to Reality

- FP7 MAMMOET project (Massive MIMO for Efficient Transmission)
 - Bridge gap between “theoretical and conceptual” Massive MIMO
 - Develop: Flexible, effective and efficient solutions

WP4 Validation and proof-of-concept

WP2 Efficient FE solutions
(IC solutions,
Comp/Calibration)

WP3 Baseband Solutions
(Algorithms,
Architectures & Design)

WP1 System approach, scenarios and requirements



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QUESTIONS?

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