

# Improved Gene Selection for Classification of Microarrays

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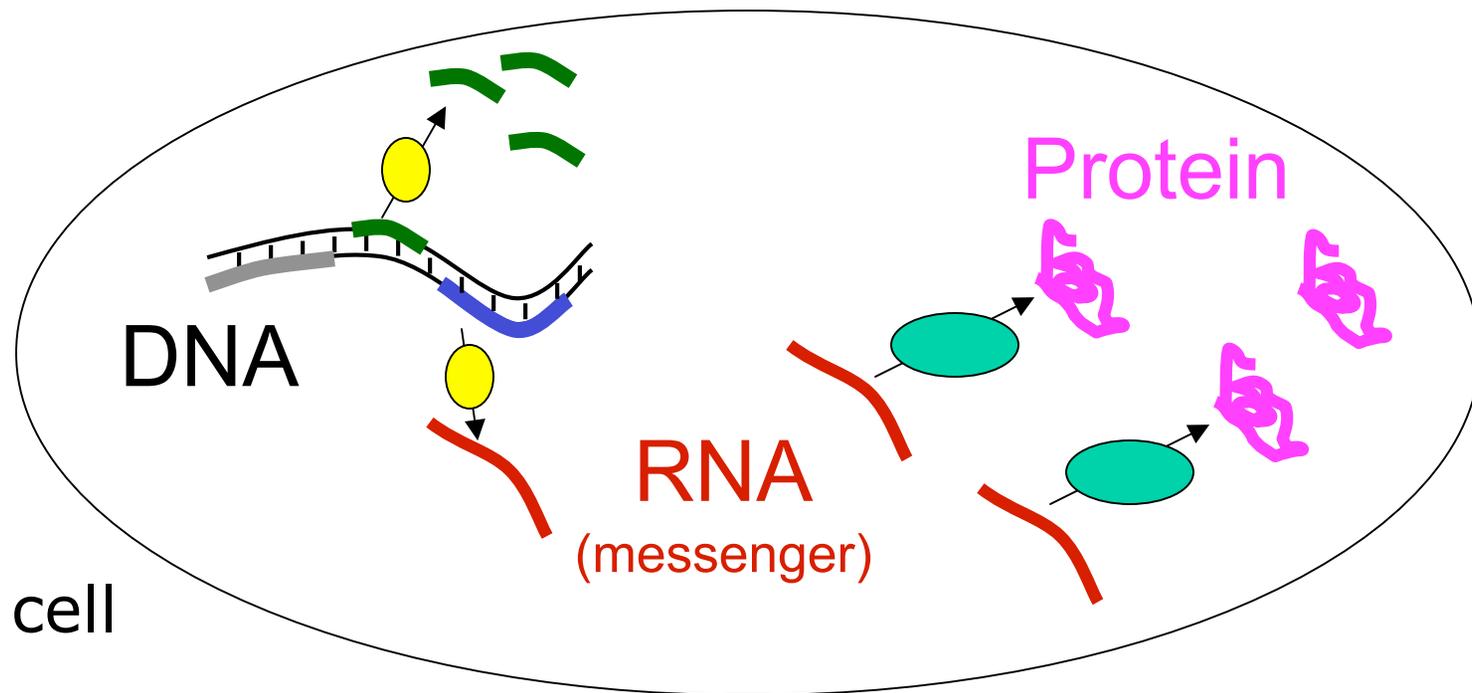
UW CSE Computational Biology Group

# Overview

- • Gene Expression Microarrays
- Classification and Feature Selection
- One Problem & Three Approaches
- Results
- Summary and Conclusions

# Gene Expression: The “Central Dogma”

DNA → RNA → Protein



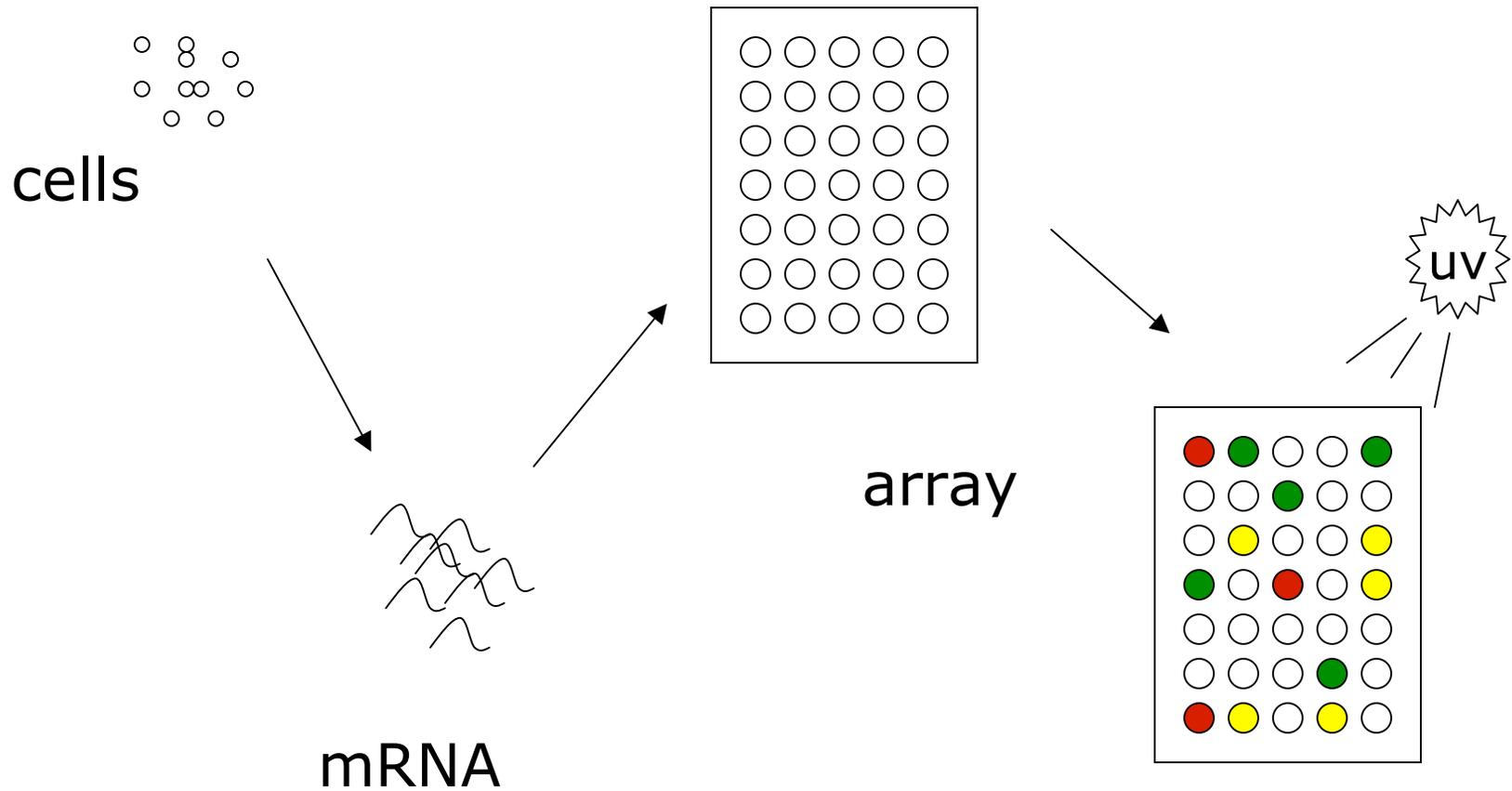
# Gene Expression

- Proteins do most of the work
- They're dynamically created/destroyed
- So are their mRNA blueprints
- Different mRNAs expressed at different times/places
- Knowing mRNA “expression levels” tells a lot about the state of the cell

# Expression Microarrays

- Thousands to hundreds of thousands of spots per square inch
- Each holds millions of copies of a DNA sequence from one gene
  
- Take mRNA from cells, put it on array
- See where it sticks – mRNA from gene x should stick to spot x

# An Expression Array Experiment

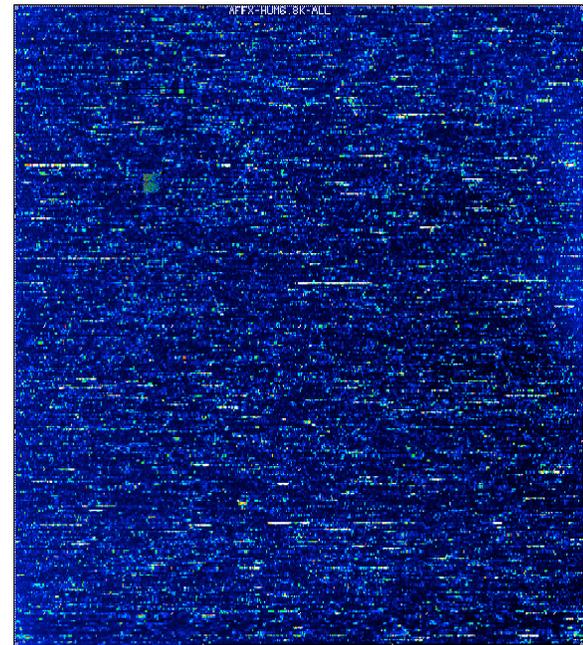


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# An Example Application

- 72 leukemia patients
  - 47 ALL
  - 25 AML
- 1 chip per patient
- 7132 human genes per chip



Golub, et al., Science 286:531-537 (1999).

# Key Issue: What's Different?

- What genes are behaving differently between ALL & AML (or other disease/normal states)?
- Potential uses:
  - Diagnosis
  - Prognosis
  - Insight into underlying biology/biologies
  - Treatment

# A Classification Problem

- Given an array from a new patient: is it ALL or AML?
- Many possible approaches:  
LDA, logistic regression, NN, SVM, ...
- Problems:
  - Noise
  - Dimensionality

# Feature Selection

- Base the classification on only a subset of the genes
  - Reduce dimensionality – for convenience
  - Drop noisy/irrelevant genes – for accuracy
- Perhaps a very small subset
  - For cost
  - For workload
  - For biological insight

# Simple Feature Selection

- Rank genes based on their individual predictive ability, e.g. by t-test or other statistic
- Keep only the top k genes
  - + simple, easy, commonly used
  - often highly correlated, so little extra info

# An Example

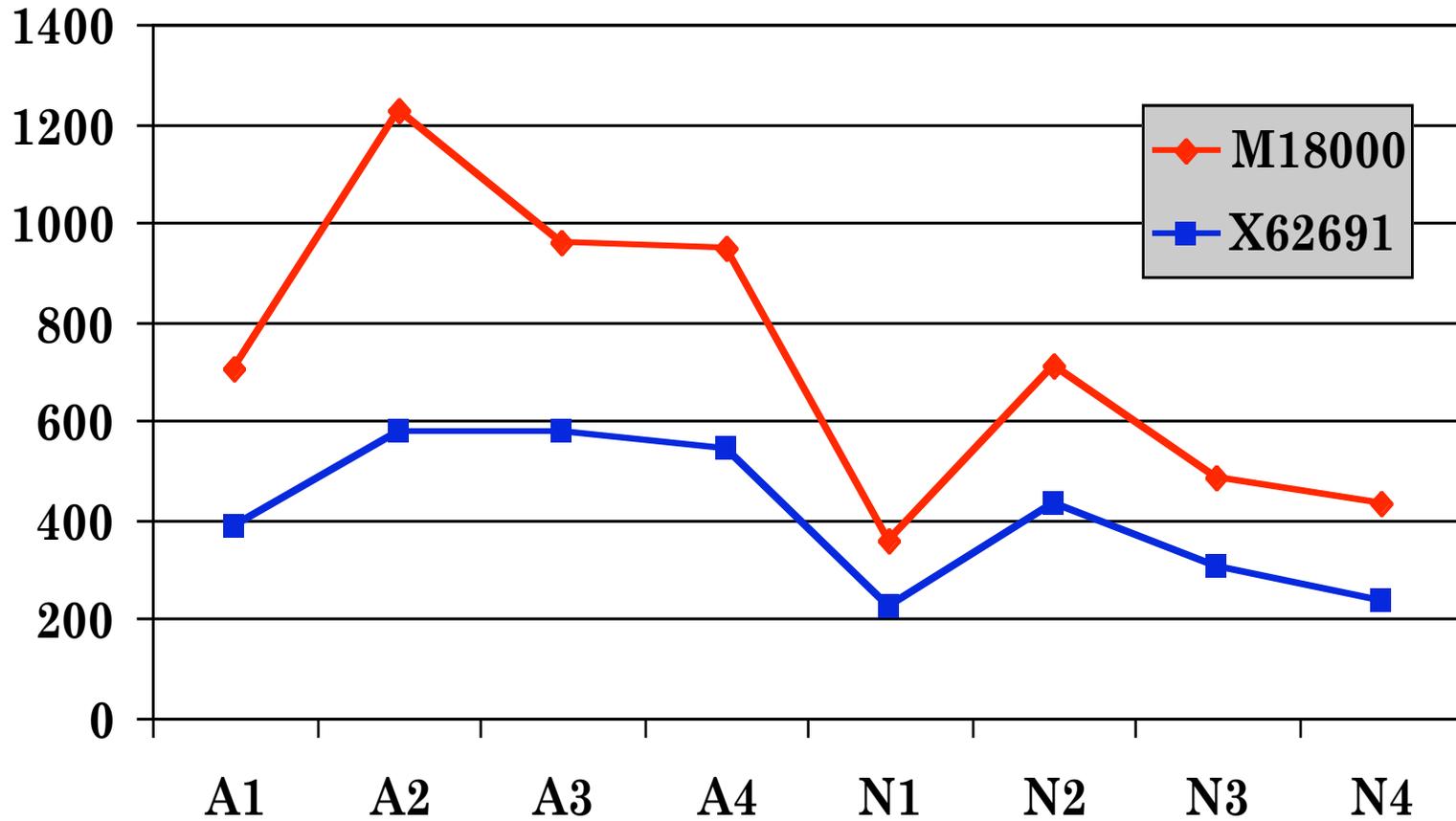
| Accession Number | Adenoma       |                |               |               | Normal□       |               |               |               | t-test p-value |
|------------------|---------------|----------------|---------------|---------------|---------------|---------------|---------------|---------------|----------------|
|                  | 1             | 2              | 3             | 4             | 1             | 2             | 3             | 4             |                |
| <b>M18000</b>    | <b>705.41</b> | <b>1227.27</b> | <b>959.35</b> | <b>951.56</b> | <b>359.83</b> | <b>711.08</b> | <b>485.33</b> | <b>431.19</b> | <b>0.014</b>   |
| <b>X62691</b>    | <b>387.91</b> | <b>577.57</b>  | <b>578.45</b> | <b>546.54</b> | <b>227.26</b> | <b>436.65</b> | <b>306.94</b> | <b>239.33</b> | <b>0.016</b>   |
| <b>M82962</b>    | <b>91.85</b>  | <b>16.27</b>   | <b>12.61</b>  | <b>61.62</b>  | <b>187.44</b> | <b>76.90</b>  | <b>181.38</b> | <b>186.53</b> | <b>0.017</b>   |
| <b>U37426</b>    | <b>0.47</b>   | <b>7.05</b>    | <b>6.30</b>   | <b>3.40</b>   | <b>-3.88</b>  | <b>1.58</b>   | <b>-2.99</b>  | <b>-2.91</b>  | <b>0.018</b>   |
| <b>HG2564</b>    | <b>2.33</b>   | <b>0.54</b>    | <b>1.58</b>   | <b>3.82</b>   | <b>-2.91</b>  | <b>-2.11</b>  | <b>1.00</b>   | <b>-2.91</b>  | <b>0.019</b>   |
| <b>Z50853</b>    | <b>35.43</b>  | <b>26.03</b>   | <b>51.49</b>  | <b>41.22</b>  | <b>27.68</b>  | <b>15.80</b>  | <b>12.46</b>  | <b>15.99</b>  | <b>0.022</b>   |
| <b>M32373</b>    | <b>-48.02</b> | <b>-28.20</b>  | <b>-64.62</b> | <b>-56.95</b> | <b>-15.05</b> | <b>-16.86</b> | <b>-7.97</b>  | <b>-34.88</b> | <b>0.022</b>   |

# An Example (cont.)

□

|        | M18000 | X62691 | M82962 | U37426 | HG2564 | Z50853 | M32373 |
|--------|--------|--------|--------|--------|--------|--------|--------|
| M18000 | 1.000  |        | □      | □      | □      | □      | □      |
| X62691 | 0.961  | 1.000  |        | □      | □      | □      | □      |
| M82962 | -0.944 | -0.971 | 1.000  |        | □      | □      | □      |
| U37426 | 0.973  | 0.975  | -0.983 | 1.000  |        | □      | □      |
| HG2564 | 0.592  | 0.653  | -0.553 | 0.529  | 1.000  |        | □      |
| Z50853 | 0.514  | 0.616  | -0.633 | 0.597  | 0.614  | 1.000  |        |
| M32373 | -0.509 | -0.590 | 0.602  | -0.580 | -0.619 | -0.874 | 1.000  |

# Example



# Problem with the simple solution

- Each gene independently scored
- Top k ranking genes might be very similar and therefore no additional information gain
- Reason: genes in similar pathways probably all have very similar score
- What happens if several pathways involved in perturbation but one has main influence
- Possible to describe this pathway with fewer genes

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# Three Approaches

- A: A greedy algorithm picks low p-values and not too high correlation
- B: Cluster genes; pick representatives from each cluster
- C: Like B, but “mask out” (omit) clusters having poor p-values

Goal of all 3: broader representation of informative genes & pathways

## A: “Correlation”

- First gene picked is the one with best p-value
- $k^{\text{th}}$  gene picked is the one with best p-value among genes having correlation less than threshold  $\rho$  to previous  $k-1$

## B: “Clustering”

- Cluster genes into  $g$  groups
- From each cluster, select one or more genes, choosing those with lowest p-values
- Take more from clusters with broad dispersion, fewer from tight clusters (which are likely to be highly correlated)

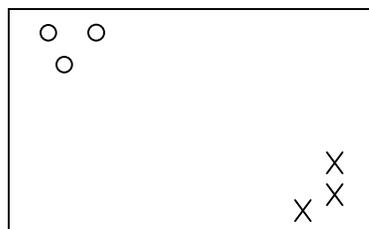
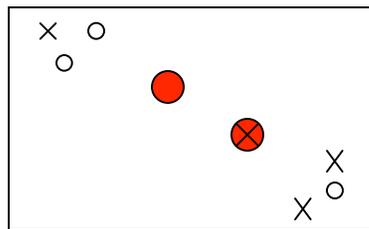
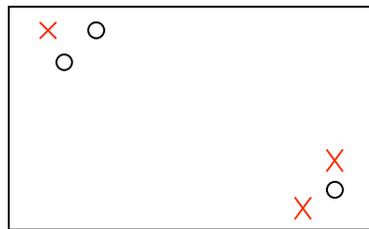
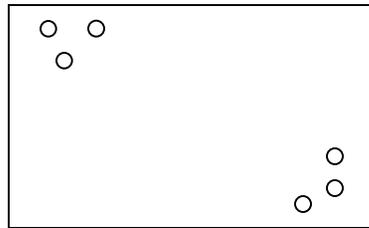
## C: “Masked out Clustering”

- Just like B, but don't take any genes from clusters whose average p-value is poor ( $> 0.2$ ).

# Clustering Algorithms

- K-means
- “Fuzzy” k-means

# Hard clustering – k-means



Randomly assign  
cluster to each point

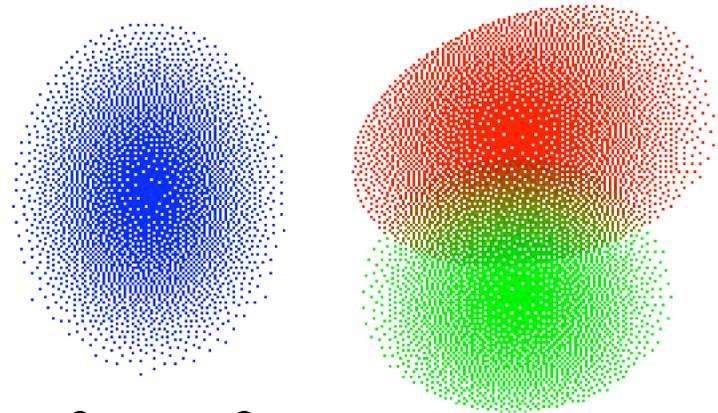
Find centroids

Reassign points  
to nearest center

Iterate until  
convergence

# Soft - Fuzzy Clustering

instead of hard assignment,  
probability for each cluster



Very similar to k-means but fuzzy softness factor  $m$  (between 1 and infinity) determines how hard the assignment has to be

# Fuzzy examples

Nottermans carcinoma dataset:

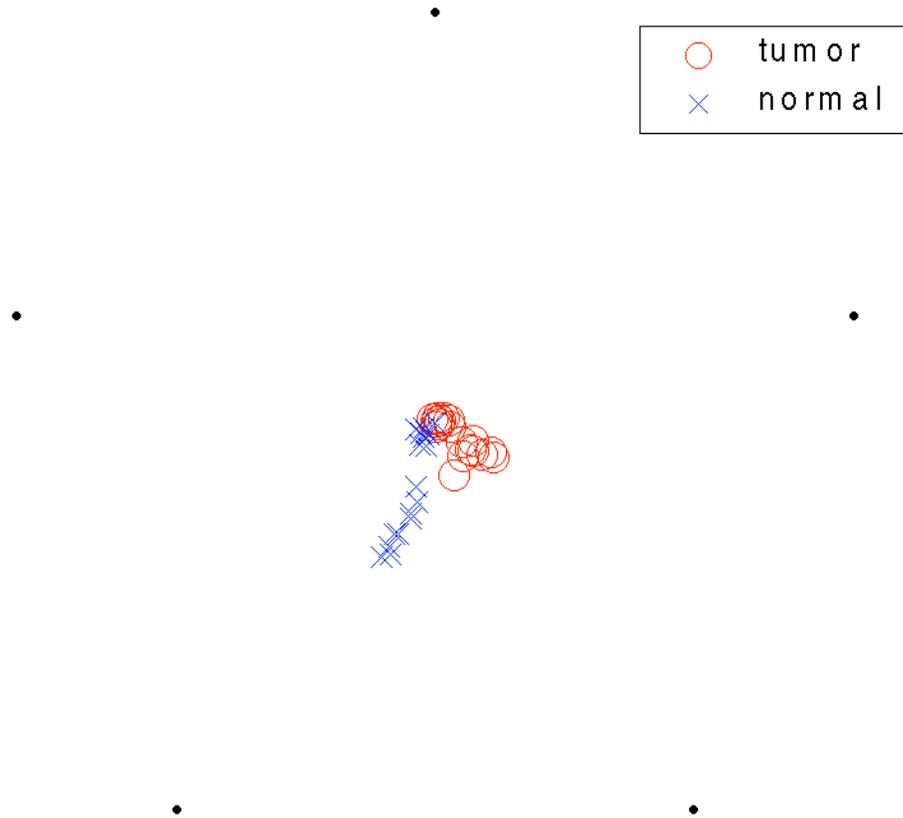
18 colon adenocarcinoma and 18 normal tissues

data from 7457 genes and ESTs

cluster all 36 tissues

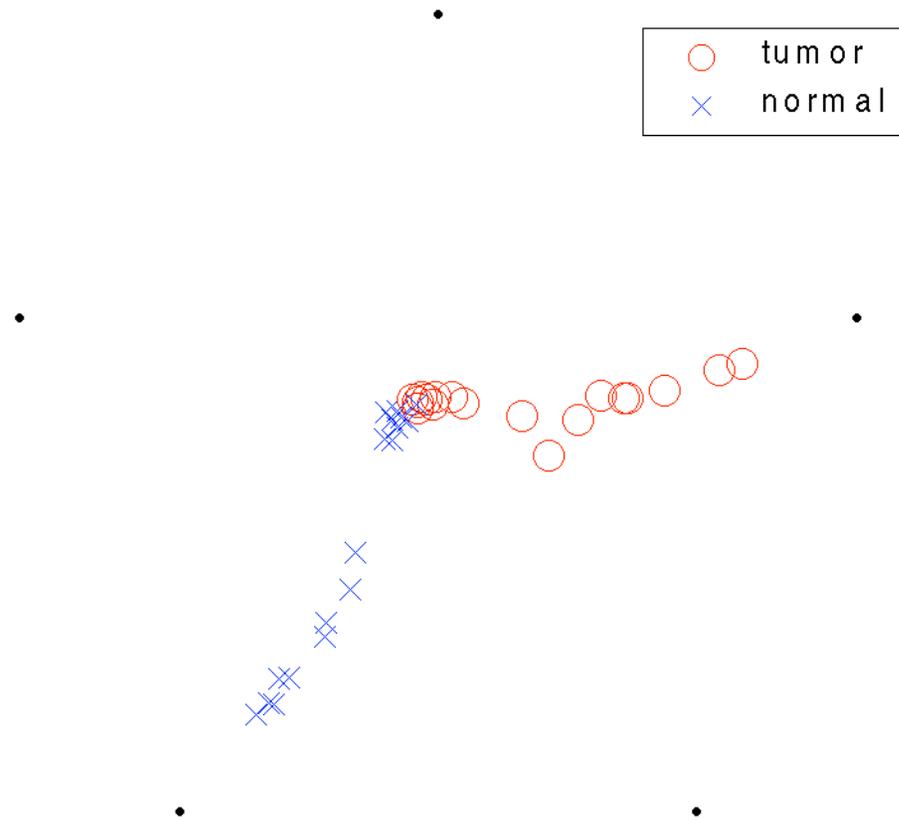
# Fuzzy softness 1.3

18 tumors, 18 normals, 5 fuzzy clusters,  $m = 1.3$



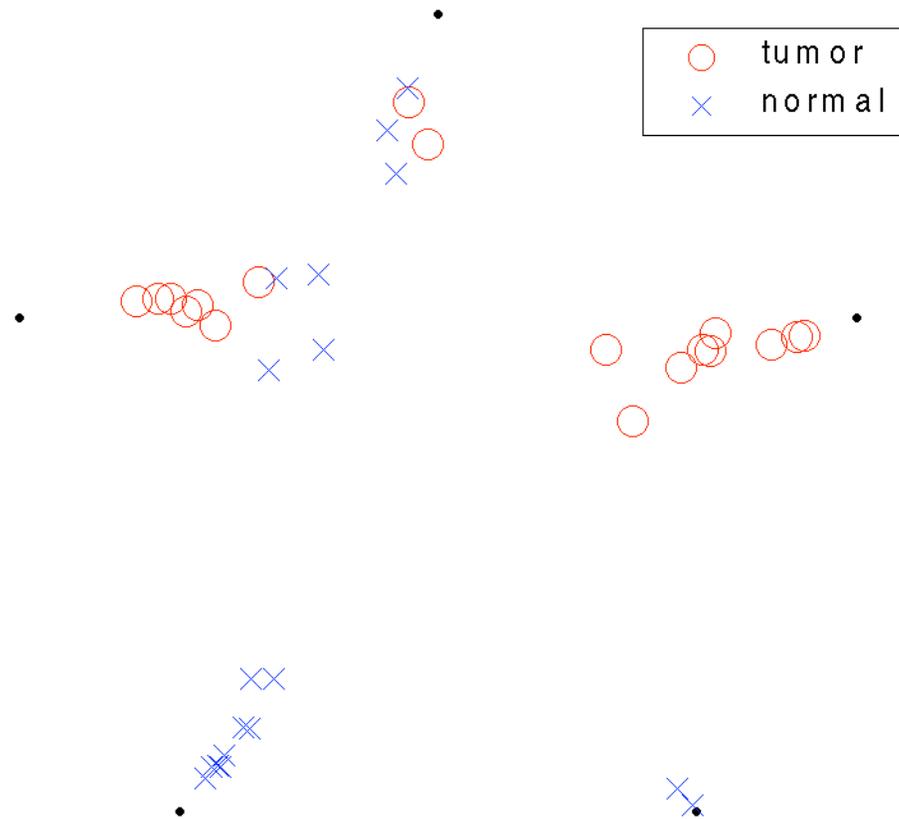
# Fuzzy softness 1.25

18 tumors, 18 normals, 5 fuzzy clusters,  $m = 1.25$



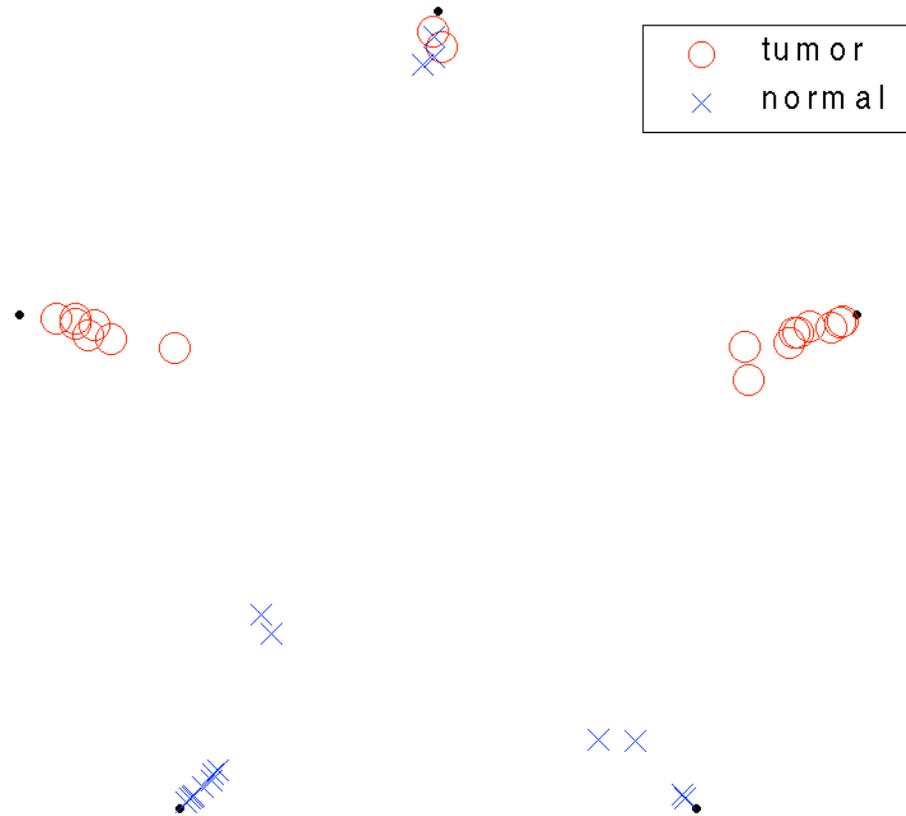
# Fuzzy softness 1.2

18 tumors, 18 normals, 5 fuzzy clusters,  $m = 1.2$



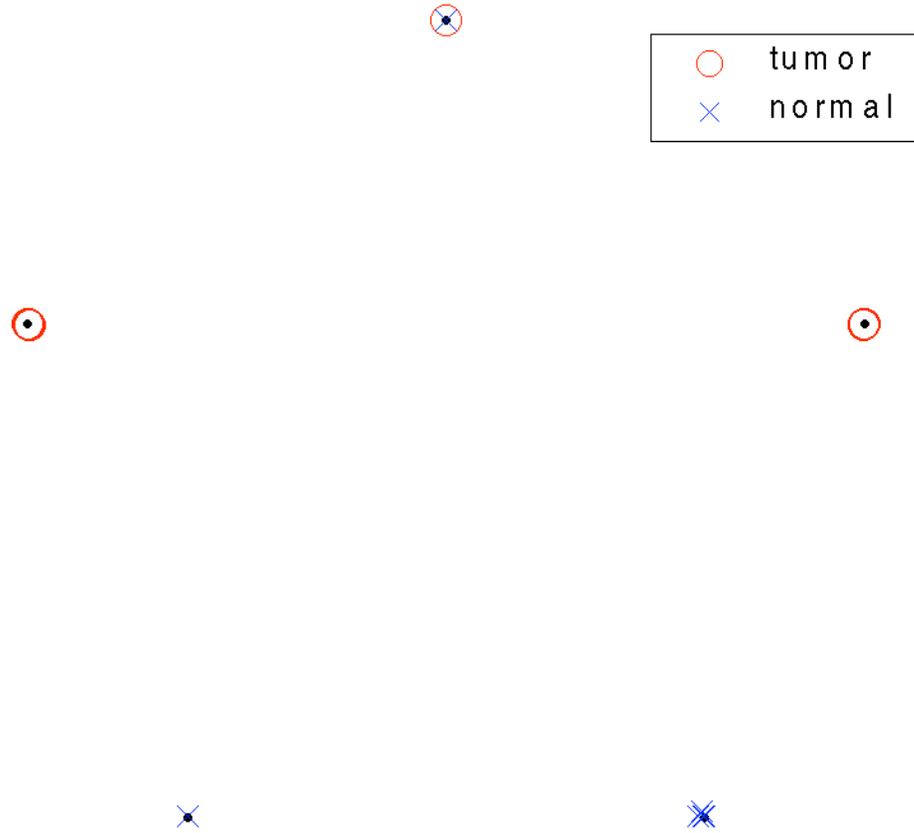
# Fuzzy softness 1.15

18 tumors, 18 normals, 5 fuzzy clusters,  $m = 1.15$



# Fuzzy softness 1.05

18 tumors, 18 normals, 5 fuzzy clusters,  $m = 1.05$



# Selecting genes from clusters

- Two way filter: exclude redundant genes, select informative genes
- Get as many pathways as possible
- Consider cluster size and quality as well as discriminative power

# How many genes per cluster?

- Constraints:
  - minimum one gene per cluster
  - maximum as many as possible
- Take genes proportionally to cluster quality and size of cluster
- Take more genes from bad clusters
- Smaller quality value indicates tighter cluster
- Quality for k-means: sum of intra cluster distance

# Which genes to pick?

- Choices:
  - Genes closest to center
  - Genes farthest away
  - Sample according to probability function
  - – Genes with best discriminative power

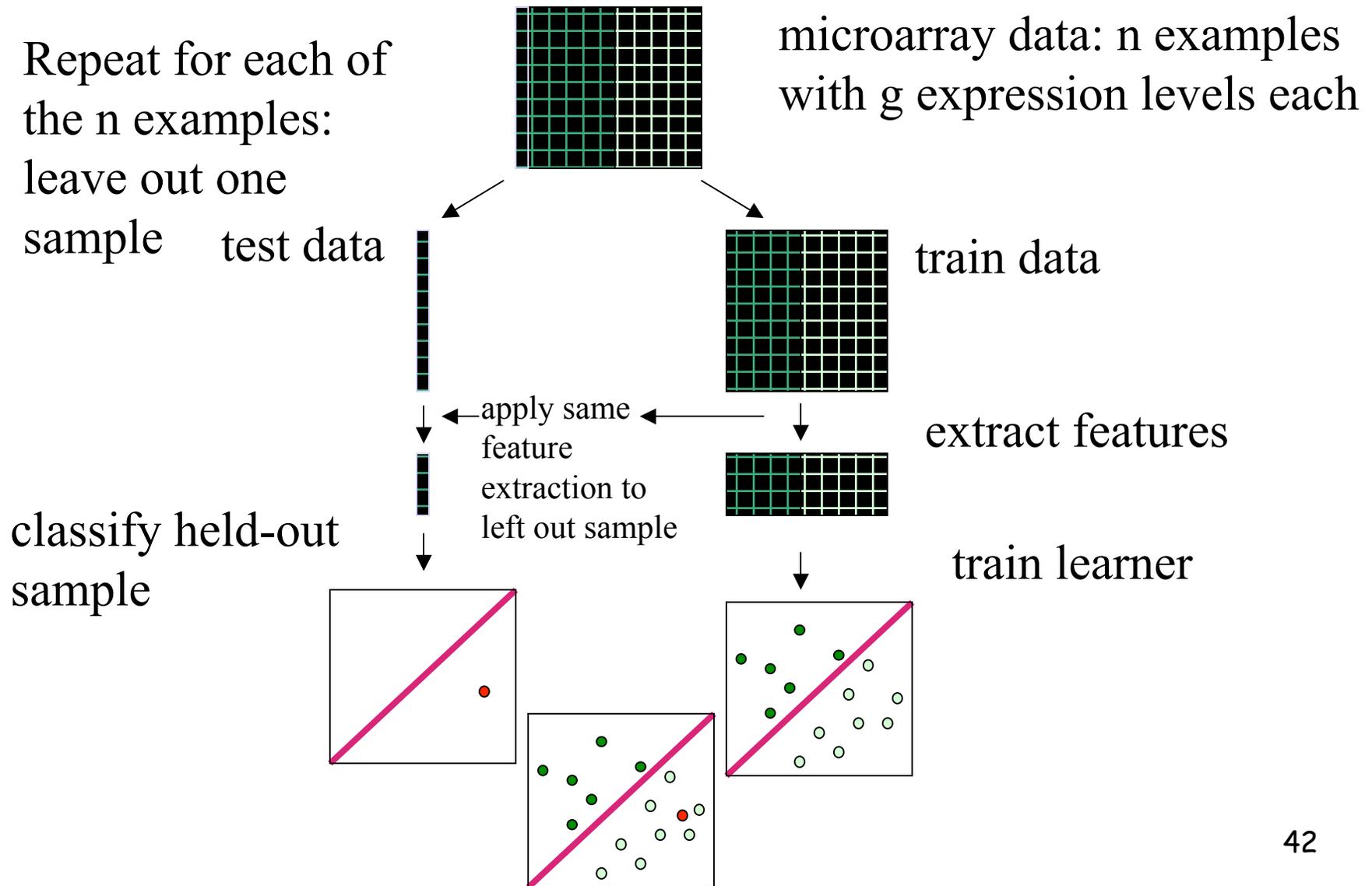
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# Experimental setup

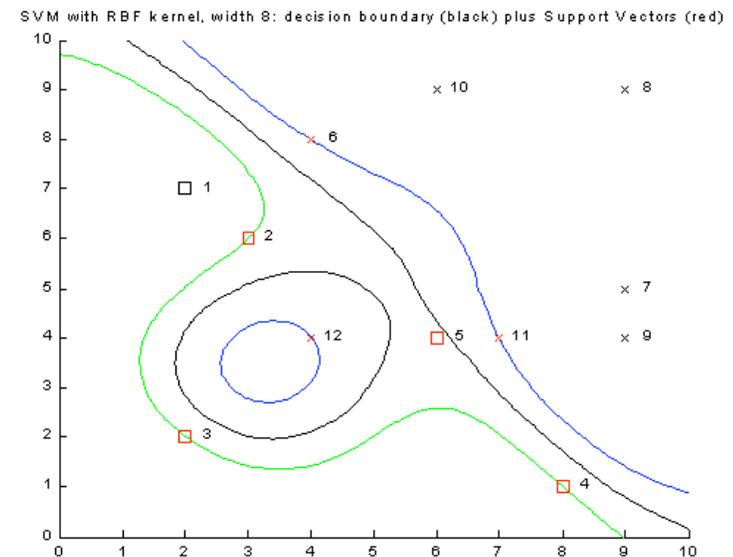
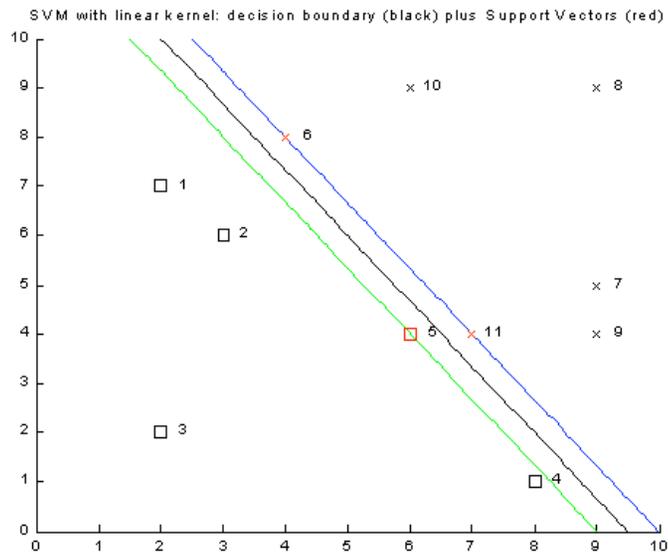
- Datasets:
  - Golub, et al.: Leukemia (47 ALL, 25 AML)
  - Alon, et al.: Colon (40 tumor and 22 normal colon adenocarcinoma tissue samples)
  - Notterman, et al.: Carcinoma and Adenoma (18 adenocarcinoma, 4 adenomas and paired normal tissue)
- Experimental setup:
  - calculate LOOCV using SVM on feature subsets
  - do this for feature size 10-100 (in steps of 10) and 1-30 clusters

# Comparison Evaluation



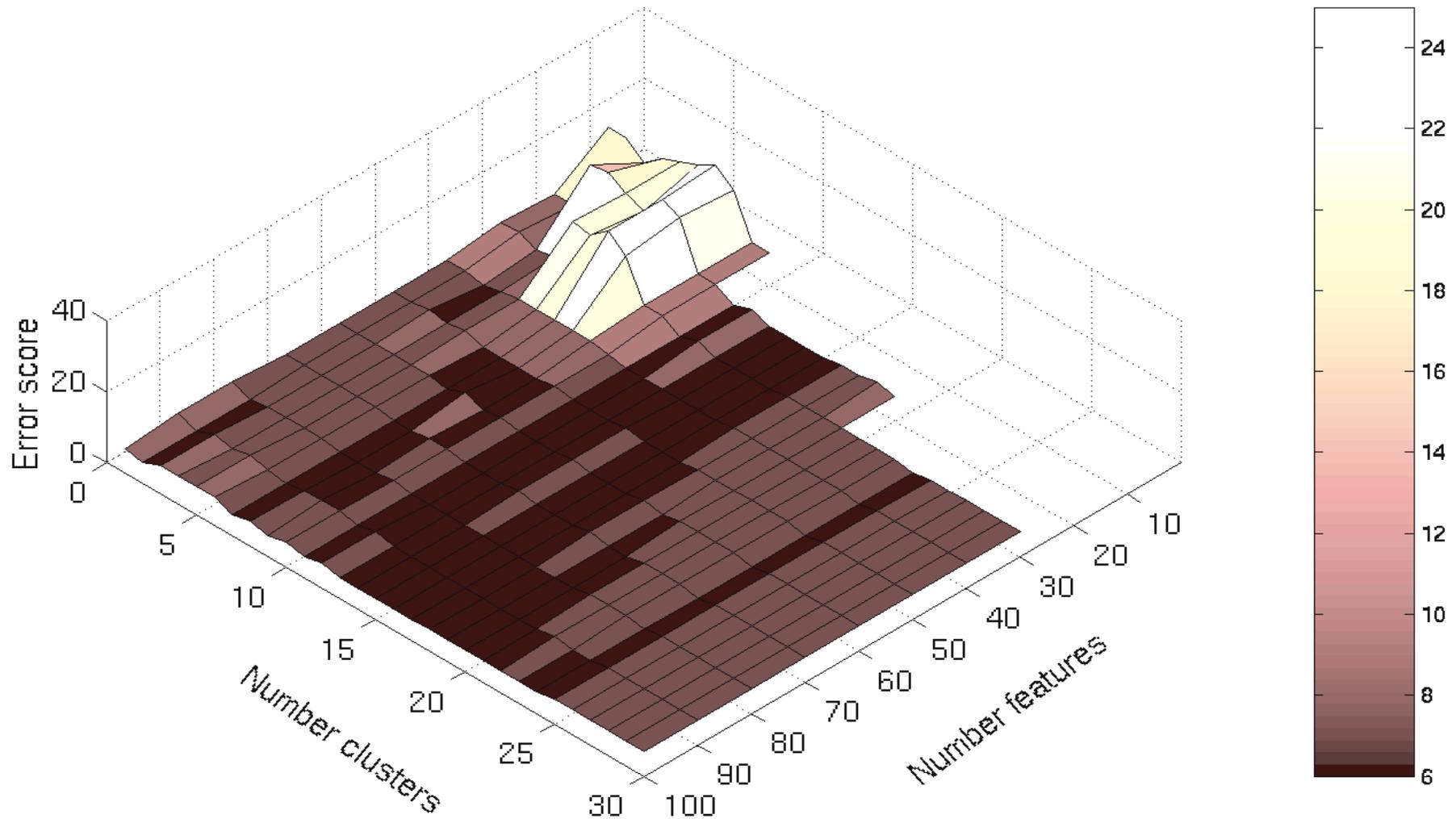
# Support Vector Machines

- Find separating hyperplane with maximal distance to closest training example



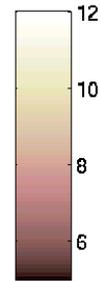
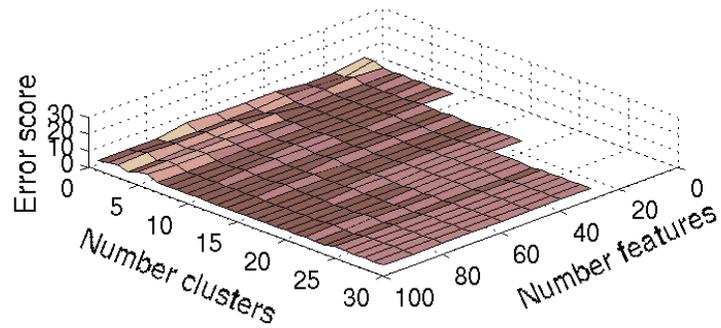
- avoids overfitting
- can handle higher order interactions and noise using kernel functions and soft margin

# Results: Alon, Fuzzy, t-test

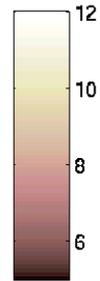
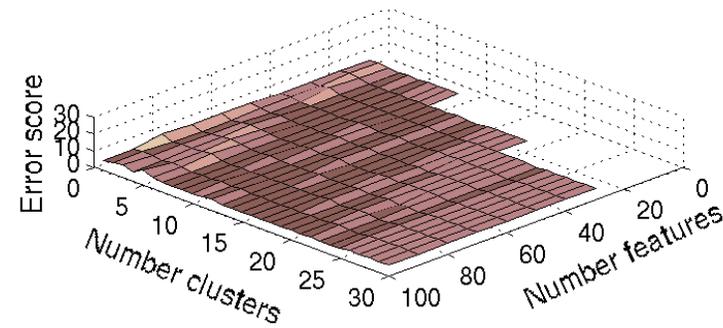


# Alon, Fuzzy, Other Stats

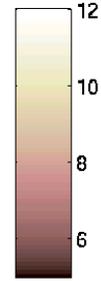
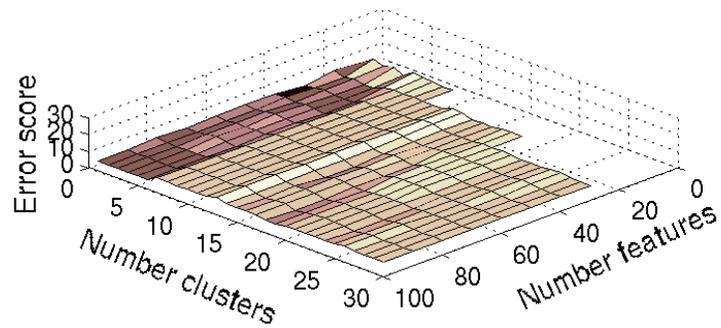
Alon Fisher



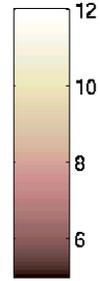
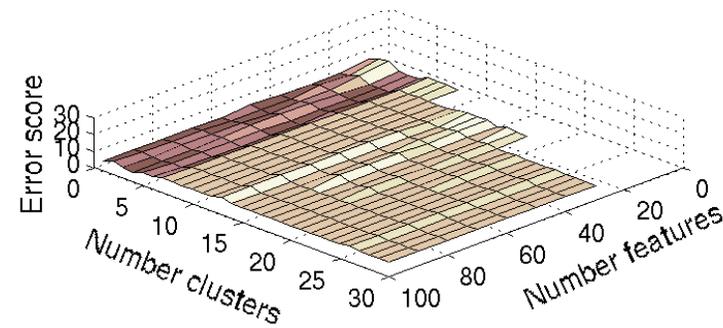
Alon Golub



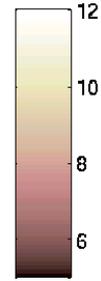
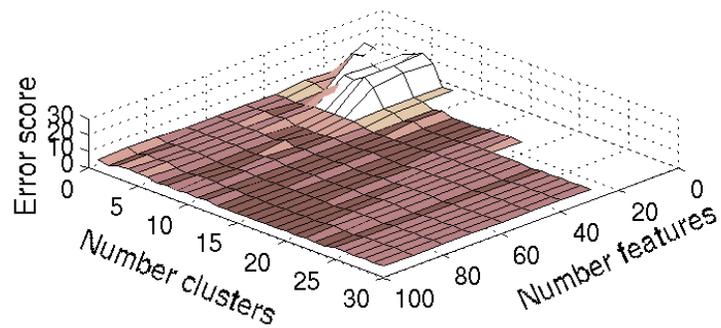
Alon Wilcoxon



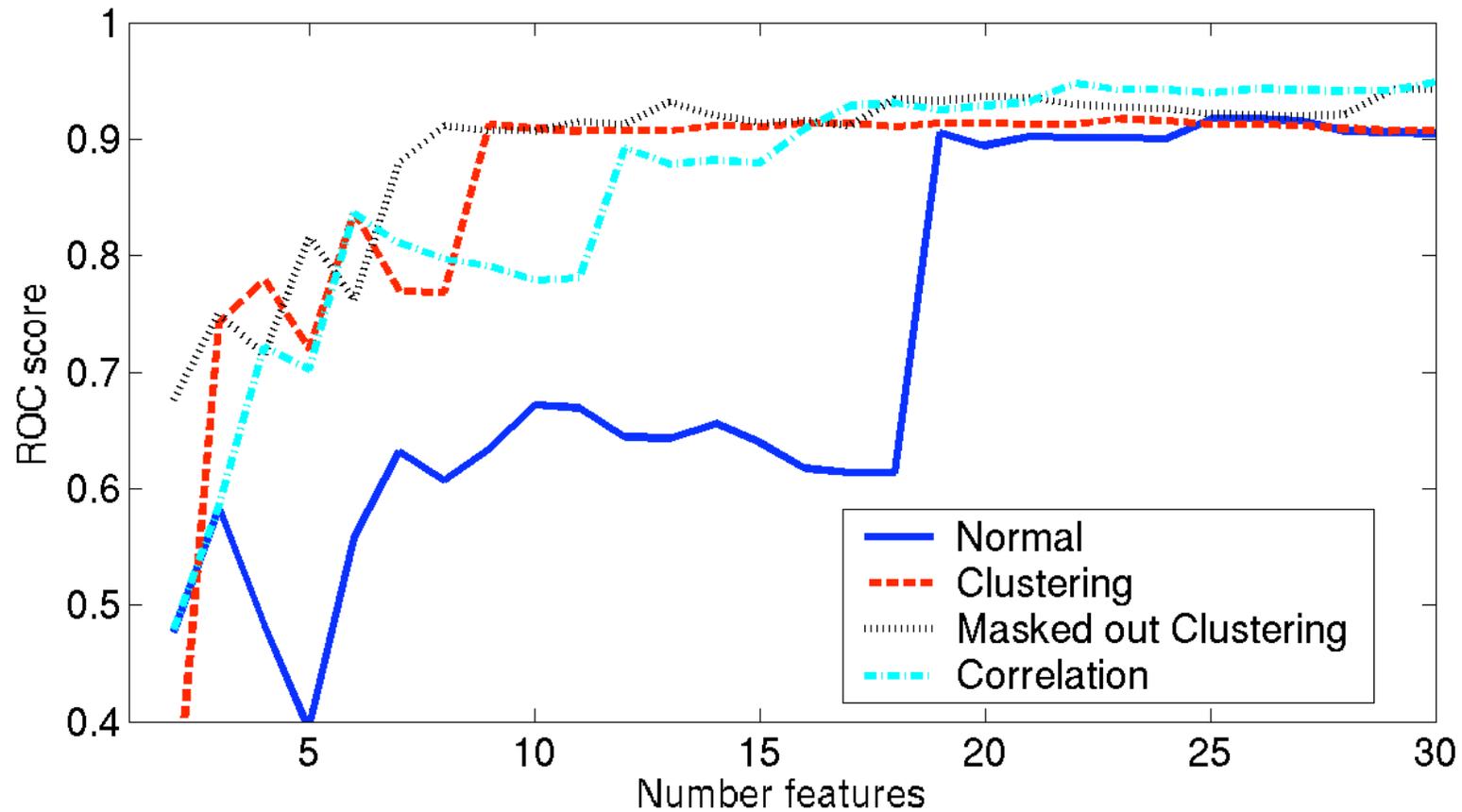
Alon TNoM



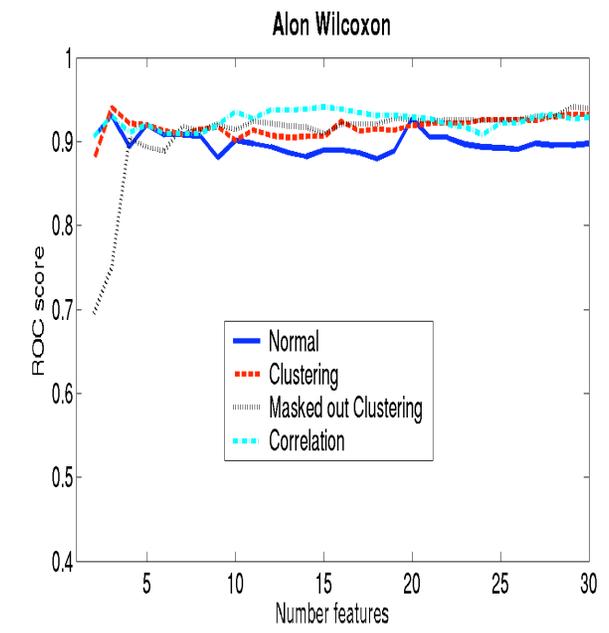
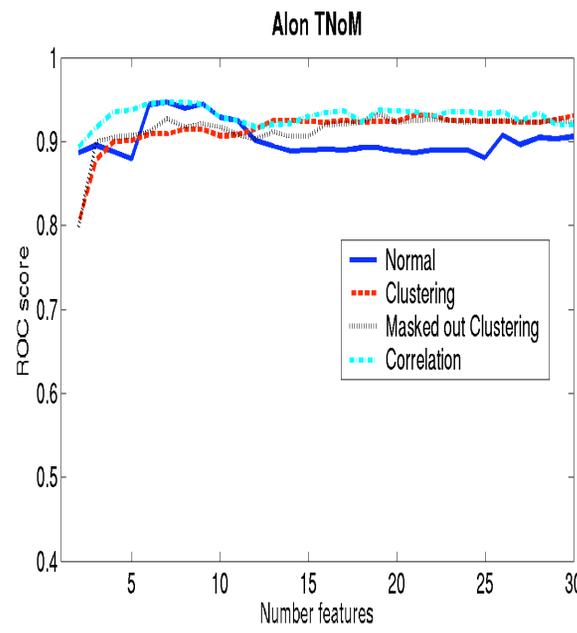
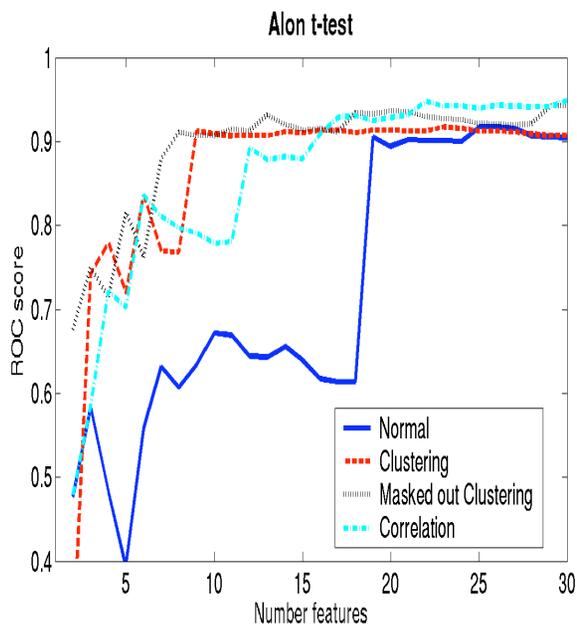
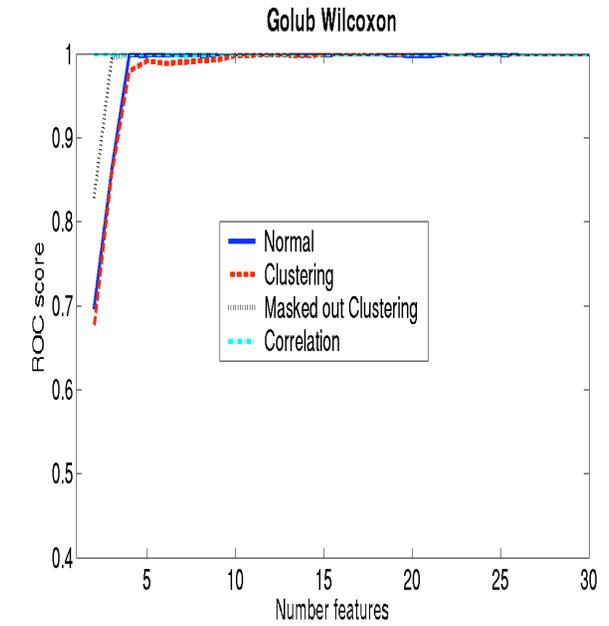
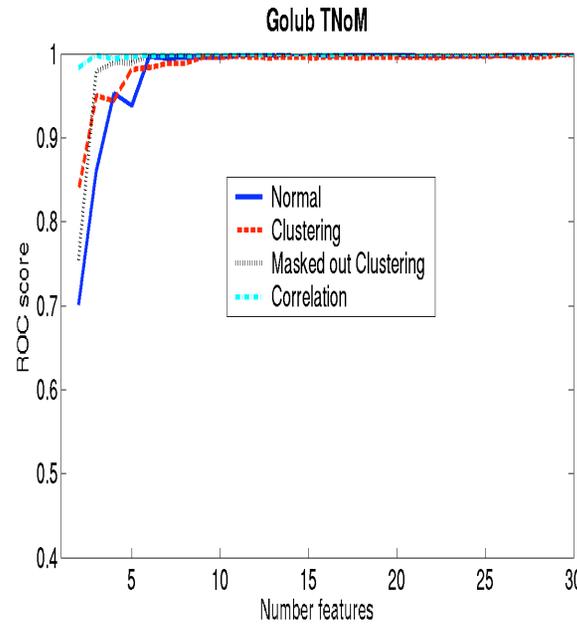
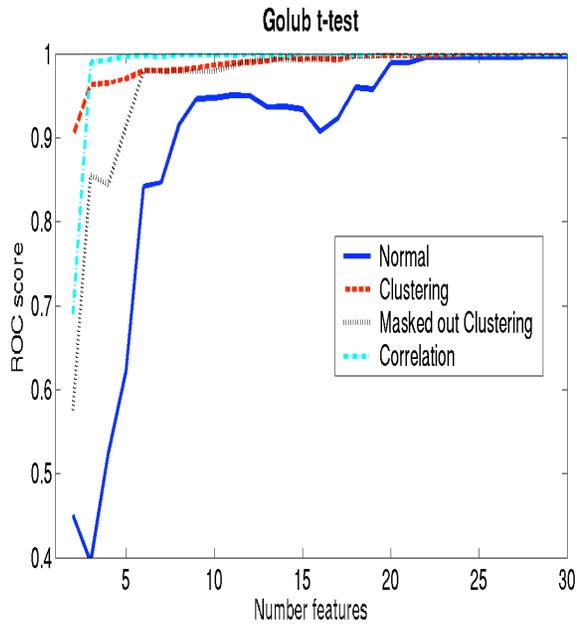
Alon t-test



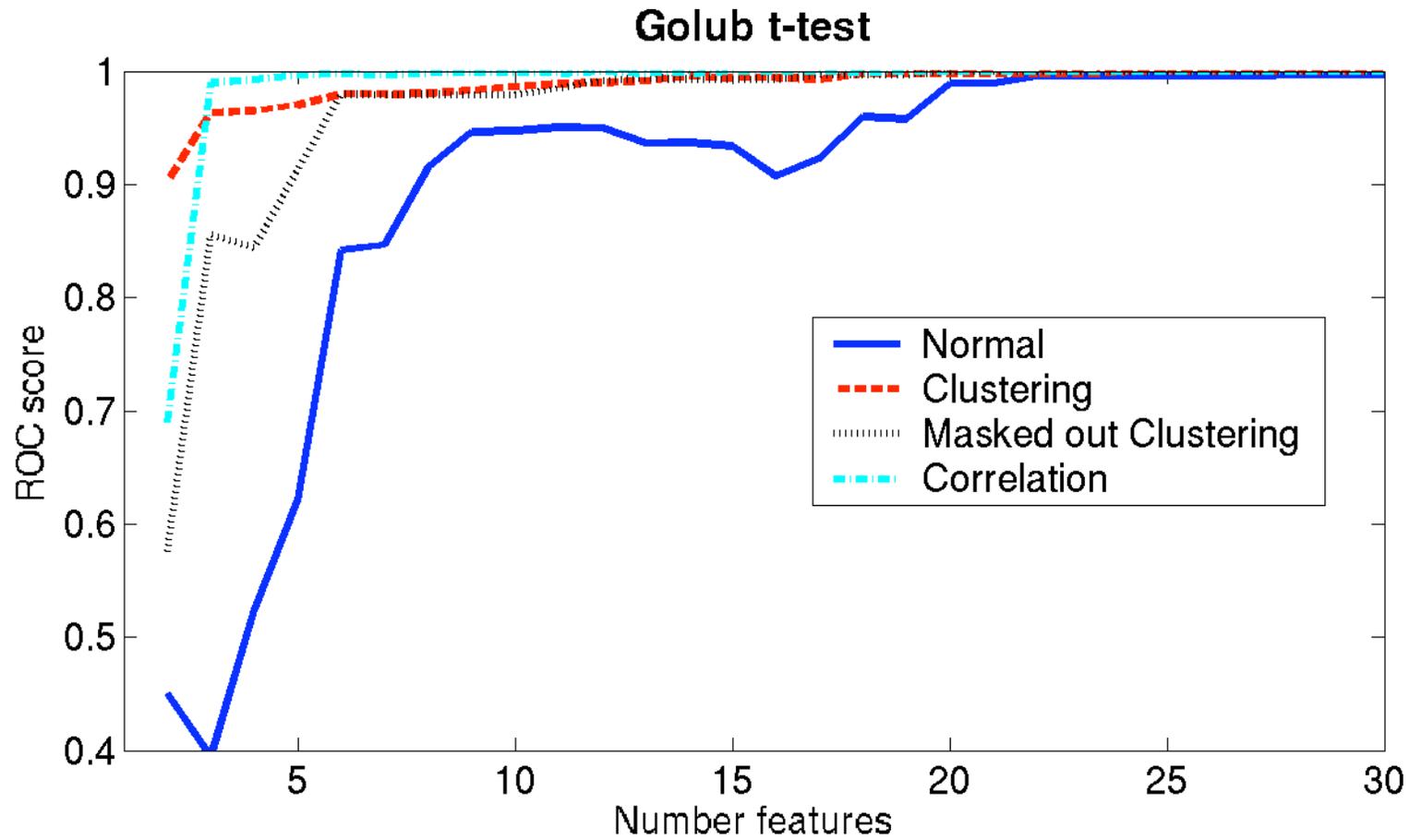
# ROC Scores: Alon, t-test



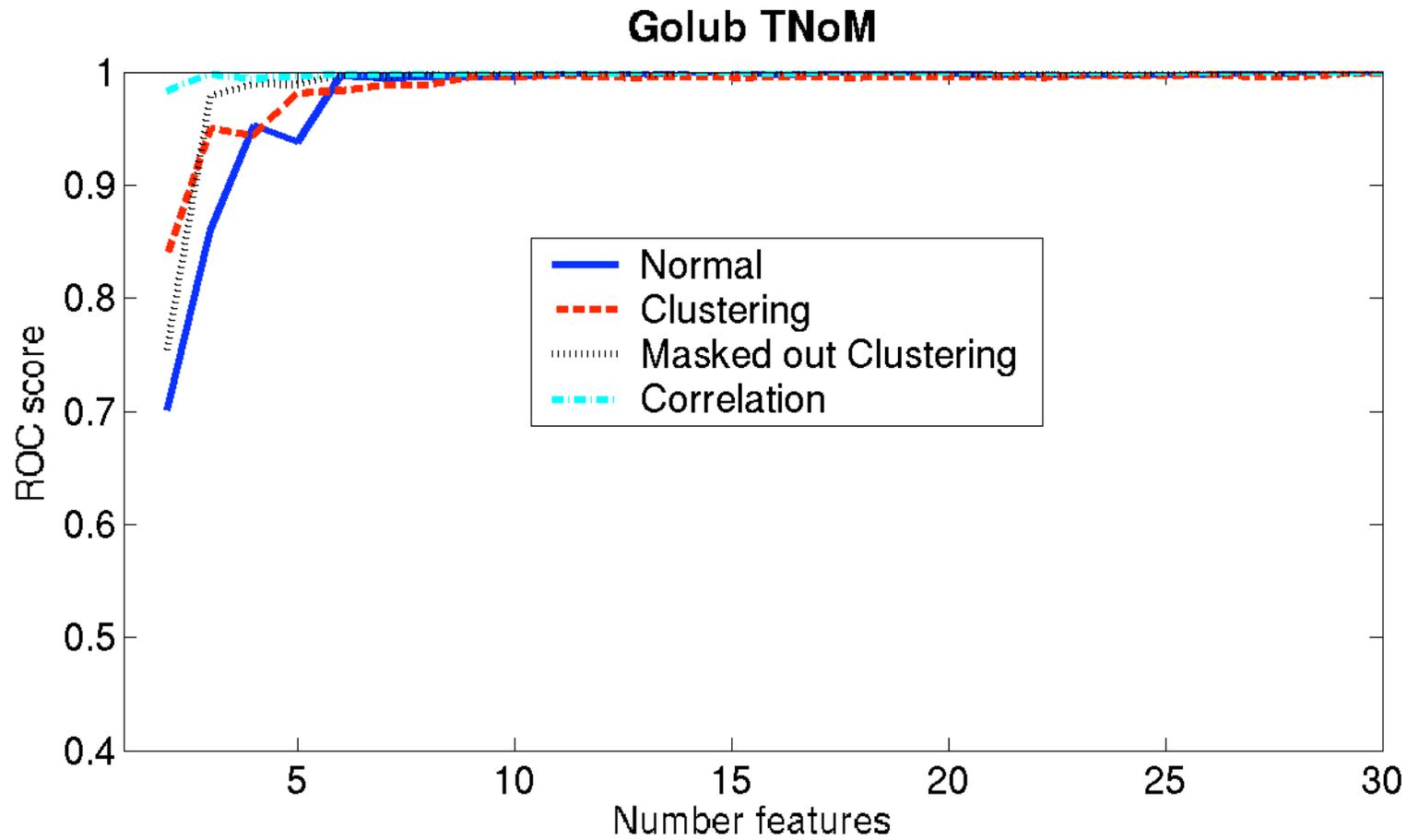
# More ROC Scores



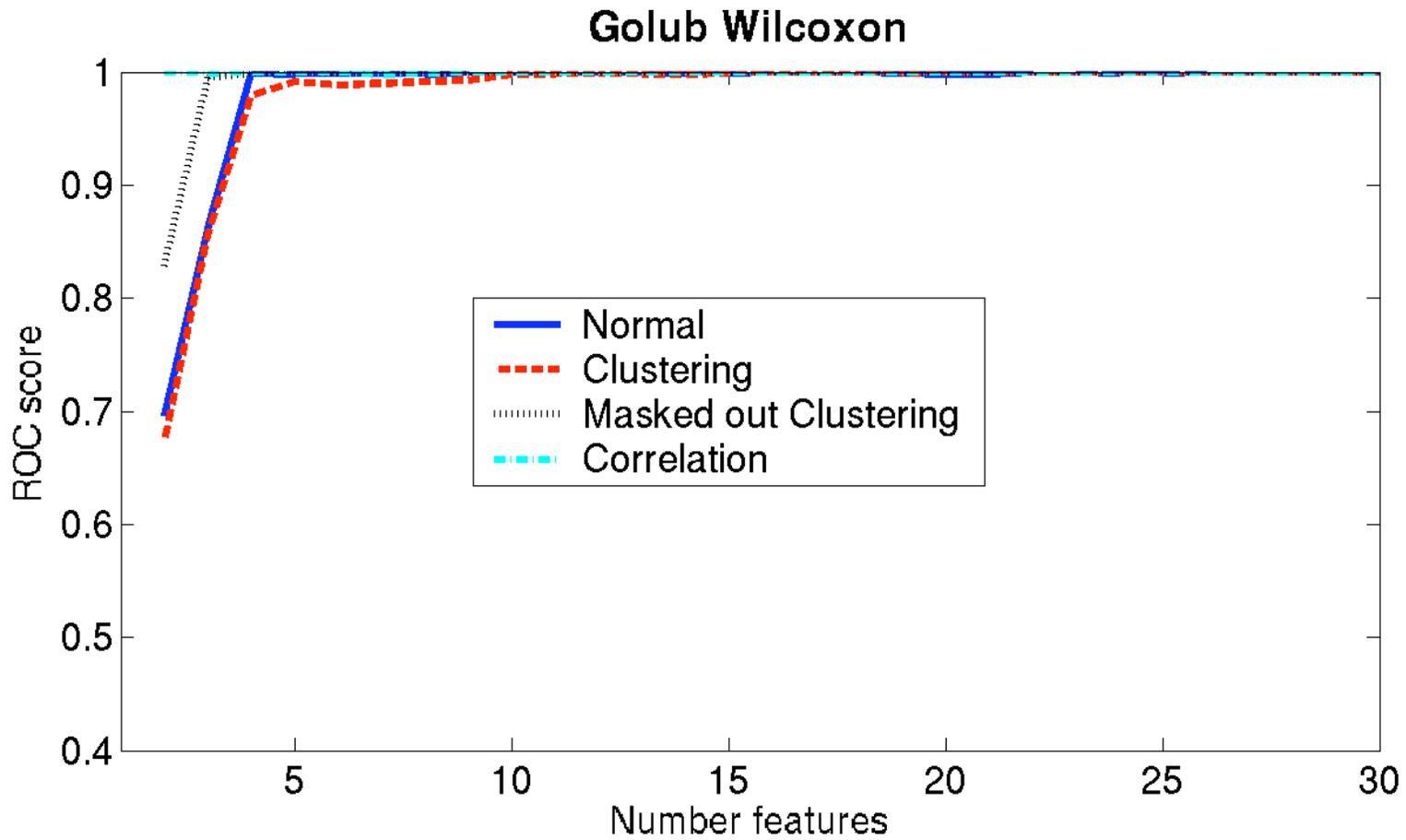
# More ROC Scores



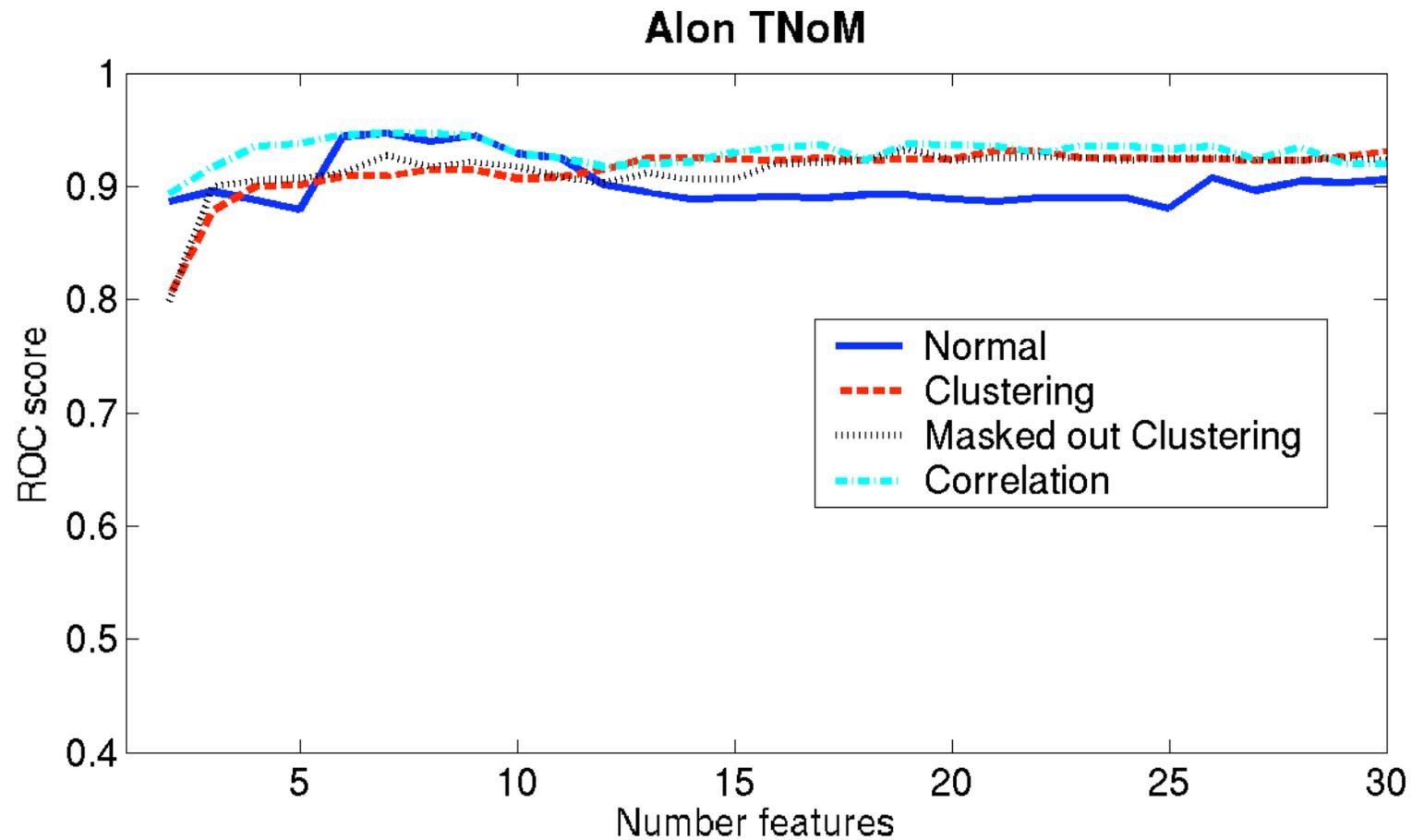
# More ROC Scores



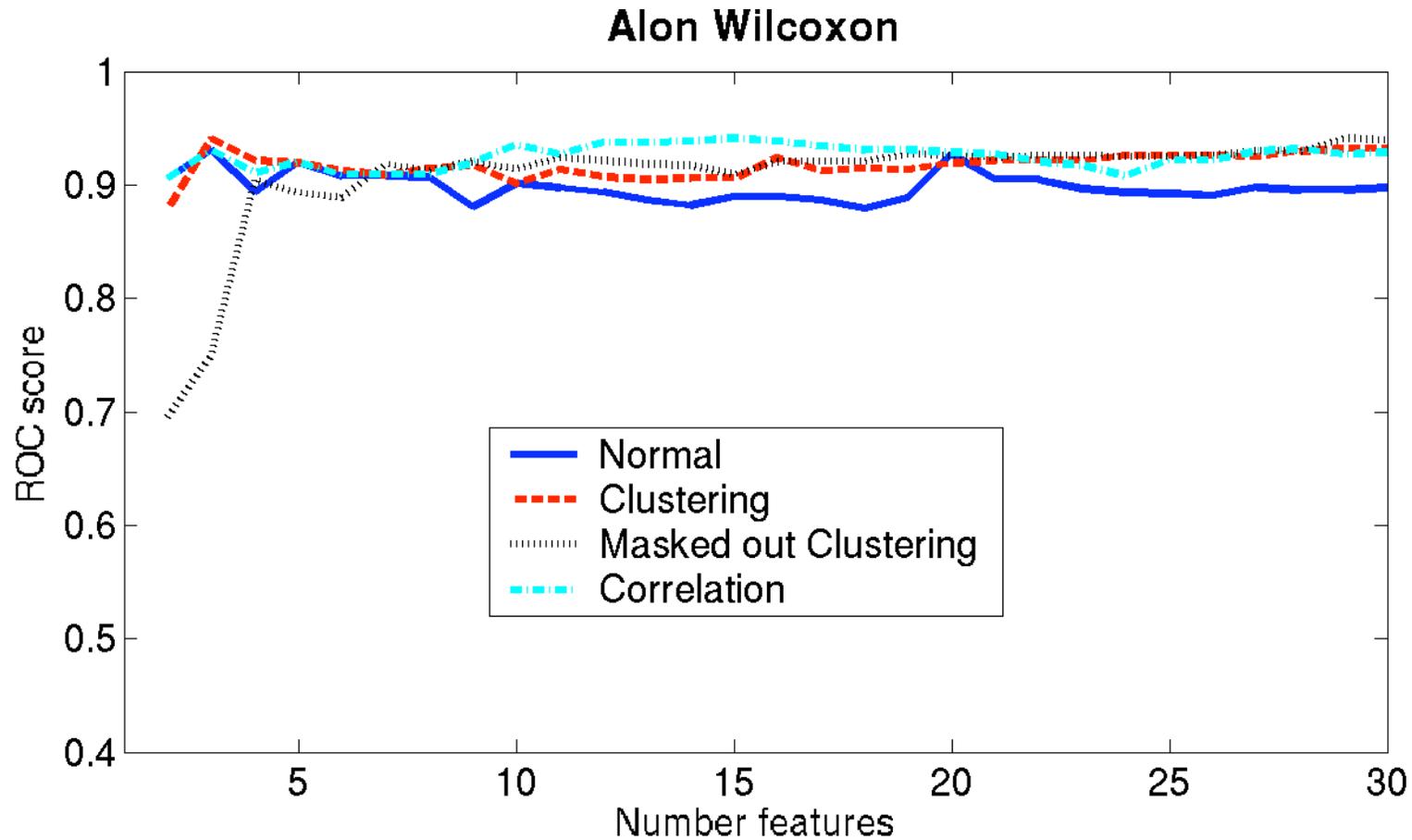
# More ROC Scores



# More ROC Scores



# More ROC Scores



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# Summary I: Problem

- Sample classification is an important application of microarrays
  - For better diagnostics, prognostics, etc.
- Finding small feature sets with high classification accuracy is important
  - For cost, for biological insight
- “Standard” method (top k genes by your favorite statistical test) is not bad
  - But very often picks highly correlated subset

# Summary II: Our Idea

- Explicitly pick subsets to emphasize diversity (reduced correlation) while retaining good individual statistics, hopefully will improve joint accuracy
- Three methods:
  - Greedy selection
  - Selection from clusters
  - Selection from clusters with masking

# Summary III: Results

- It works
- Details vary a bit depending on data set and test statistic, but all 3 methods generally better than “standard”
- Improvement most significant for small feature set sizes
- Improvement greater for parametric tests than non-parametric tests

# More Information

- Appeared in Pacific Symposium on Biocomputing, 2003
- Preprint, supplementary data
  - <http://www.cs.washington.edu/homes/ruzzo>
  - <http://www.molgen.mpg.de/~jaeger/psb>

# Acknowledgements

- My coauthors
  - Bill Noble
  - Ranier Spang
- 
- NIH
  - NSF