Image indexing and similarity retrieval based on a new Spatial Relation Model

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Abstract
Spatial relation model is important technique for image indexing and retrieval in image or multimedia databases. 2-D strings and its variants are proposed to support the representation of spatial relationship. In this paper, a new spatial knowledge representation model named “Two Dimension Begin-End boundary string” (2D Be-string) is proposed. The 2D Be-string represents an icon by its MBR (Minimum bounding rectangle) boundaries. By applying a number of “dummy objects”, the 2D Be-string can intuitively and naturally represent the pictorial spatial information without any spatial operator. In addition, an image similarity evaluation method based on the modified “Longest Common Subsequence” (LCS) algorithm is presented. By the proposed evaluation method, not only those images which all of the icons and their spatial relationships fully accord with the query image can be sifted out, but also for those images which partial of icons and/or spatial relationships are similar with the query image. It resolves the problems that the query targets and/or spatial relationships are not certain. Our representation model and evaluation also simply the retrieval progress of linear transformations, include rotation and reflection, of an image.

Keyword: image retrieval, image database, spatial knowledge, spatial reasoning, similarity retrieval, 2-D Strings, LCS algorithm, 2D Be-string

1. Introduction

In pictorial spatial application systems, it is very important to abstract the information existed in original images. For examples, how the image icons and their characteristics were recognized, how the symbolic image was encoded and constructed, how to index and retrieve these images, how to evaluate their similarity corresponding to a query image, etc. All of these are very important issues in the information retrieval and/or content-based retrieval.

There are three basic types for image indexing and retrieval: (1) by features, e.g. color, texture, shape, of the icons in images, such as the QBIC project [9.], the Virage search engine [11.]; (2) by size and location of the image icons, such like R-tree [1.], R*-tree [6.], Quadtree [4.], and Mou’s [13.]; (3) by relative position of the icons, such like the 2-D Strings [2.] and its variants [3..7..8..10..12..15..16..17.]. The third is very suitable for those applications that do not care the acute coordinates of icon objects. For example, "find all images which icon A locates at the left side and icon B locates at the right".

In this paper, we propose a new spatial knowledge representation model named “Two Dimension Begin-End boundary string” (2D Be-string). The 2D Be-string does not need to cut any image’s icons because it straightly represents an icon by its MBR (Minimum bounding rectangle) boundaries. And by applying a number of “dummy objects”, the 2D Be-string can intuitively and naturally represent the pictorial spatial information without any spatial operators. An algorithm is also introduced, which takes O(n) space complexity in the best and worst case, to build an image database using the model we proposed.

In addition, we also propose an image similarity evaluation method based on the modified “Longest Common Subsequence” (LCS) algorithm [5.]. By our evaluation method, not only those images which all of the icons and their spatial relationships fully accord with the query image can be sifted out, but also for those images which partial of icons and/or spatial relationships are similar with the query image. It resolves the problems that the query targets and/or spatial relationships are not certain. The modified LCS algorithm takes O(mn) space and time complexity, while m and n are the number of icons in a query image and a database image, respectively. It is more simply to retrieve the linear transformations of an image represented by 2D Be-string. The transformations include 90, 180, 270 degrees clockwise rotations and the reflections on x- or y-axis.

The remainder of this paper is organized as follows. Section 2 reviews the approaches of 2-D Strings and its variants. In section 3, we propose a new spatial knowledge representation model, called 2D Be-string, as well as an algorithm to construct a symbolic picture using 2D Be-string. A similarity retrieval algorithm, modified from
LCS, and the corresponding similarity evaluation progress are introduced in section 4. In section 5, we present a demonstration system, a visualized retrieval system, implemented by 2D Be-string and modified LCS algorithm. Finally, the concluding remarks and the future works are given in the last section.

2. Related works

Chang et al. [2] proposed an approach, called '2-D Strings', to represent the spatial information in a picture or image. The 2-D Strings use a symbolic projection of a picture along x- and y-axis. They define two sets of symbol, V and A. Each symbol in V presents an icon object in an image. A is a set of spatial operators contains ['=', '<', '>']. A 2D string over V and A is defined by \((u, v) = (x_1y_1x_2y_2...x_ny_n, x_1y_1x_2y_2...x_ny_n)\), where \(x_1y_1...x_n\) is a 1-D string over V, \(y_1x_2y_2...x_n\) and \(z_1y_2...z_n\) are 1-D string over A, \(x_1y_1x_2y_2...x_ny_n\) is a permutation of \(x_1y_1x_2y_2...x_n\).

The 2D C-string [7], a variant of 2-D Strings, extends the spatial relationships into two sets of spatial operators: \(R_i\) and \(R_g\), and cuts all the objects along their MBR boundaries. The set \(R_i\) defines local spatial relationships, that's the projection of two objects is partial overlap. The set \(R_g\) defines global spatial relationships, means that the projection of two objects either disjoin or adjoin or located at the same position. 2D G-string unifies the spatial relationship between two cut objects. Only those operators in set \(R_g\) are enough to specify the relationship between two cut objects.

The 2D G-string [3], a variant of 2-D Strings, extends the projection of two objects either disjoin or adjoin or located at the same position. 2D G-string unifies the spatial relationship between two cut objects. Only those operators in set \(R_g\) are enough to specify the relationship between two cut objects.

The 2D C-string [7], another variant of 2-D Strings, proposes an approach to minimize the number of cutting objects. The 2D C-string leaves the leading object as a whole. It improves the problem that there are superfluous cutting objects were generated at 2D G-string cutting progress. But there will be \(O(n^2)\) of cutting objects in the worst case.

Therefore, the 2D B-string [8] drops the cutting process, instead, represents an object by two symbols. One stands the begin boundary of that object, another one for the end. 2D B-string also reduces the spatial relationships to single operator '='. It means that two objects have the same boundary projection if '=' appears.

The basic similarity retrieval and evaluation idea in 2-D Strings [2], 2D G-string [3], 2D C-string [7] and 2D B-string [8] are the same. First, they always define three type of similarity, type-\(i\) (\(i = 0, 1, 2\)). Each is constricted by some conditions. Type-1 is stricter then type-0, type-2 is stricter then type-1. Second, they examine all spatial relationship pairs between any two objects in query image versus pairs in an image of database. Buid type-\(i\) subgraph if the pair satisfies type-\(i\) constraints. After examining, they find the maximum complete subgraph for each type-\(i\) graph. The number of objects in maximum complete subgraph is the similarity of the query image and the images of database.

The space and time complexity to examine all spatial relationship pairs requires \(O(n^2)\), where \(n\) is the number of object in an image. And finding maximum complete subgraph is an NP-complete problem [18]. It is a time consuming work. It is not suitable for large number of icon objects in an image.

3. The Spatial Representation Model using 2D Be-string

There are many approaches were proposed to represent an icon in an image. Such as MBR (Minimum Bounding Rectangle) [3,7,8,10], MBE (Minimum Bounding Ellipse), MBC (Minimum Bounding Circle) [13, etc.]

3.1 The model of 2D Be-string

The approach used in 2D Be-string is MBR too. Conceptually, it is similar with 2D B-string. They present an object by its MBR boundaries and need nothing to be cut. However, 2D Be-string adopts a quite different idea to state the spatial relationship between two boundary symbols. 2D B-string uses a spatial operator (\(=\)) to describe the projection of two boundaries is IDENTICAL. In 2D Be-string, we use a dummy object to describe the projection of two boundaries is DISTINCT!

We define a 'Dummy Object' as following:

A 'Dummy Object' is not a real object in original image. It can be specified as any size of space and be memorized as symbol '='.

Then the 2D Be-string can be defined as

\[(u, v) = (d_1x_1d_2y_2d_3...d_n, x_1y_1d_2y_2d_3...d_n)\]

Where \(d_i\) is a dummy object \(\varepsilon\) or a null string, \(i = 0, 1, ... n\), and \(x_i\) and \(y_i\) are real icon objects, they are either begin or end projected boundaries on x- and y-axis, respectively, \(i = 1, 2, ... n\). To determine \(d_i\), we need to know the maximum size of an image, say \(X_{max}\) and \(Y_{max}\) for x- and y-axis respectively. Set \(d_0\) to \(\varepsilon\) if there is a space between the begin boundary of the leftmost (bottommost) object and the left (bottom) edge of image. Similarly, set \(d_n\) to \(\varepsilon\) if there is an interval between the end boundary of the rightmost (topmost) object and the right (top) edge of image. For the rest,
set $d_i$ to $\varepsilon$ if the boundary projections of $x_i$ and $x_{i+1}$ ($y_i$ and $y_{i+1}$) are different.

The 2D Be-string, for example, is written as $(u, v) = (eA_d, eB_d, eA_e, eB_e, eB_d, eA_d, eA_e, eB_e, eB_d, eA_d, eA_e)$. The dummy object $d_i$ was set to $\varepsilon$ because there is a space before begin boundary of object $A$ on $x$-axis. The dummy object $d_i$ was set to $\varepsilon$ too because there is a space left behind object $B$ on $x$-axis. But the dummy object $d_i$ was set to null string because the end boundary of object $A$ and the begin boundary of object $C$ are projected at the same location on $x$-axis. Similar case is appeared for the end boundary of object $B$ and the begin boundary of object $C$ on $y$-axis.

Observably, the 2D Be-string has following advantages:

First, object location in original image and symbolic picture was mapped directly. There is no operator required for representing spatial relationship between objects. It is intuitively.

Second, because it does not need to cut the objects of image. It simplifies the construction of image database. And the space complexity for an image with $n$ objects in the worst and best case is $O(n)$. For the worst case, all boundary projections are distinct and there is a space left in the leftmost, bottommost, rightmost and topmost of an image, it requires $4n+1$ symbols. By constrast, the best case, all boundary projections are identical and exactly fit in an image, it requires $2n+1$ symbols only.

Third, it simplifies the similarity retrieval because there is no combining the results of spatial reasoning required.

3.2 Algorithm for constructing a symbolic picture

By default, before converting an image to a symbolic picture represented by 2D Be-string, we have abstracted all objects and their MBR coordinates from that image. Then call algorithm Convert-2D-Be-String, showed in Algorithm 1, to transform an original image to a symbolic picture. Lines 1-12 explain the meaning of variables used in input parameters and converting process. Lines 14-19 sort the input data by key coordinate and object identifier in ascending order for $x$- and $y$-axis separately. Lines 21-32 construct the 2D Be-string on $x$-axis, and lines 34-45 construct the 2D Be-string on $y$-axis.

The time complexity for algorithm Convert-2D-Be-String depends on the sorting algorithm at line 19. Time complexity on loops in line 14-18, 24-30 and 37-43 are $O(n)$, and never exceed the sorting algorithm. Ignore the sorting algorithm, the space complexity is $O(n)$ too.

Algorithm 1 to construct a symbolic picture:

```
Convert-2D-Be-String (n, C, Xh, Xe, Yh, Ye, Xmax, Ymax)
1. // n ...number of objects in an image
2. // C ...object symbols in image, C={C1, C2, ..., Cn} ...
3. // Xh ...begin boundaries on x-axis, Xh={x1, x2, ..., xn} ...
4. // Xe ...end boundaries on x-axis, Xe={x1, x2, ..., xn} ...
5. // Yh ...begin boundaries on y-axis, Yh={y1, y2, ..., yn} ...
6. // Ye ...end boundaries on y-axis, Ye={y1, y2, ..., yn} ...
7. // xhn ...maximum coordinate on x-axis
8. // yhn ...maximum coordinate on y-axis
9. // Xh ...2D Be-string on x-axis,
Xh=\{v11, v12, ..., v1n\}, where v1=dummy object \( \varepsilon \) or null string, i=0, 1, ..., n; xhn=xhn or xhn identifies the projection of begining boundary or end boundary of object ci on x-axis, i=1, 2, ..., n
10. // Yh ...2D Be-string on y-axis,
Yh=\{v21, v22, ..., v2n\}, where v2=dummy object \( \varepsilon \) or null string, i=0, 1, ..., n; yhn=yhn or yhn identifies the projection of begining boundary or end boundary of object ci on y-axis, i=1, 2, ..., n
11. // S ...a sort work for x-axis, Sx(i1, x,...,i1, x, n1; Xh) or xhn identifies the projection of begining boundary or end boundary of object ci on x-axis, i=1, 2, ..., n
12. // T ...a sort work for y-axis, Sy(i1, y,...,i1, y, n1; Yh) or yhn identifies the projection of begining boundary or end boundary of object ci on y-axis, i=1, 2, ..., n
13. // Combine MBR coordinate and object identifier as a key, sort the input data by ascending order
14. for i=1 to n
15. Si=xhn
16. Si=xhn
17. Si=xhn
18. Si=yhn
19. Sorting S and T by ascending order
20 // Construct 2D Be-string on x-axis
21 Xh=\{\}
22 if Si of xh=0 then // Insert \( \varepsilon \) at the leftmost?
23 \( Xh=\varepsilon \)
24 for i=1 to n
25 if type of x in si is xh then // convert coordinate to
26 Xh=Xh+xi
27 else // type of x in si is xh
28 Xh=Xh+xi
29 if of x of xi=0 then \( Xh=\varepsilon \)
30 Xh=Xh+xi
31 if of xi of xi=0 then // Insert \( \varepsilon \) at the rightmost?
```
While building an image database of 2D Be-string, we only require to call algorithm Convert-2D-Be-String with the MBR coordinates and object identifiers for each image, and save the results, the 2D BE-string, to database. Because the 2D Be-string is an order data, if we save the 2D Be-string with their MBR coordinates, we can easy find the location to be inserted for a new object and its MBR boundaries using binary search with key MBR coordinates and identifier of the new object. It is easy to determine whether insert a dummy object around this new object boundary or not. When we want to drop an object sequential, delete it directly and eliminate the redundant dummy object if it was found.

Image similarity retrieval and evaluation

4. Assessment of Similarity

In section 2, we discuss the symbolic image construction and the assessment of similarity using 2D B-String. In order to decide which type, Type-0, Type-1 or Type-2, of similarity it belongs to, it is necessary to record all spatial relationship for every two objects in database image. However, this assessment does not consider the situation that only partial of query objects are exist in a database image. Furthermore, the similarity assessment of Type-0, Type-1 and Type-2 is based on finding maximum complete subgraph. It is rather time-consumed to find a maximum complete subgraph from \( C_m^n \) spatial relationships of \( m \) objects in query image and \( C_n^m \) spatial relationships of \( n \) objects in database image. In this paper, we also use the number of spatial relationships, formed by every two objects and appeared in query image and database image at the same time, as the similarity assessment. But, we do not find a maximum complete subgraph; instead, we find a longest common subsequence (LCS) [5] between two 2D Be-strings. And evaluate this LCS string with respect to 2D Be-strings of query image and database image.

The intention for finding a LCS string and finding a maximum complete subgraph between two images is similar. They are used to measure a similarity. But the time complexity of LCS algorithm is \( O(mn) \), where \( m, n \) are the number of objects in query image and database image respectively. The complexity only depends on the length of 2D Be-string in query image and database image. It is not necessary to examine all the spatial relationships for every two objects. Because “The LCS string implies that, in query image and database image, all the spatial relationships of every two objects in LCS string are the same.” So, the similarity can be evaluated in a reasonable time.

4.1 Algorithms of similarity retrieval

In this paper, we propose an algorithm to find a longest common subsequence length from two 2D Be-strings. This algorithm is shown as follows and named as 2D-Be-LCS-Length. This algorithm is modified from LCS algorithm in [5]. There are two factors to revise the original LCS algorithm. The first one is, we avoid LCS from picking dummy objects continuously, because only one dummy object sufficiently represents the relative spatial relationship between two boundary symbols. The if-statement in line 21 does this evaluation. The second is, we omit the LCS paths recording matrix in original LCS algorithm by evaluating left and up paths first, line 16-19 show this, and evaluating left-up diagonal path next, as showed in line 23-24. The LCS path still can be inferred from the matrix record the LCS length.

Algorithm 2D-Be-LCS-Length takes two 2D Be-strings, \( Q \) and \( D \), as input parameters, one for query image and the other one for database image. The 2D Be-string of a query image with \( m \) objects along, each dimension has \( 2m \) boundary symbols and at most \( 2m+1 \) dummy objects. The maximum length of 2D Be-string in each dimension is \( 2m+2(m+1) \), that is, \( 4m+1 \). With the same derivation, the maximum length of 2D Be-string of a database image with \( n \) objects is \( 4n+1 \). The LCS length inferring table \( W \) needs \( (1+(4m+1)(1+(4n+1))) \) storage units; therefore, the space complexity is \( O(mn) \).

The initialization of first row and first column in LCS length inferring table \( W \), as showed in line 7-8 and 10-11 of algorithm as follows, each string symbol must be set once. They will be executed \( 4m+1 \) and \( 4n+2 \) times, respectively. The outer loop, in line 13, examines each row of \( W \) \( 4m+1 \) times. The inner loop, in lines 14-26, examines each cell of \( W \) \( (4m+1)(4n+1) \) times. Thus, the time complexity is \( O((4m+1)(4n+2)+(4m+1)(4n+1)) \), same as \( O(mn) \).
We also give a recursive procedure to print a longest common subsequence string of two 2D Be-strings. This algorithm is showed in algorithm 3. The initial invocation is Print-2D-Be-LCS (Q, W, length(Q), length(D)). From the last cell of LCS inferring table W, this procedure decreases i and/or j along the directions left and/or up in each recursive call, until either i or j reaches zero. Then all symbols of LCS string are printed out in the proper, forward order.

Algorithm 2 to find LCS length from two strings:

2D-Be-LCS-Length (Q, D)
1. m=length(Q)
2. n=length(D)
3. // Q is a 2D Be-string of query image, Q = (qi | qi ε (dummy object ε or the boundary symbols of objects in query image), i = 1, 2, ..., m).
4. // D is a 2D Be-string of database image, D = (dj | dj ε (dummy object ε or the boundary symbols of objects in query image), j = 1, 2, ..., n).
5. // LCS length is inferred in table W, W = [wi,j] is the LCS length of string q1,...,qi and d1,...,dj. If the last symbol of LCS string is dummy object then wni < 0 else wni > 0, where i = 0, 1, 2, ..., m, j = 0, 1, 2, ..., n).
6. // Initialize the first column of inferring table W by zeros.
7. for i=1 to m do
8. wi,0=0
9. // Initialize the first row of inferring table W by zeros.
10. for j=0 to n do
11. w0,j=0
12. // From row 1 column 1, infer each cell, row by row and column by column, until every cell has been evaluated.
13. for i=1 to m do
14. for j=1 to n do
15. // Set current cell value to the value of left or up cell which has maximum absolute value.
16. if |wi-1,j| ≥ |wi,j| then
17. wi,j=wi-1,j
18. else
19. wi,j=wi,j
20. // Then check whether the symbol qi, dj are the same and at least one of qi and the last symbol of LCS path from left-up diagonal is not dummy object.
21. if (qi = dj) and ((qi ≠ ε) or (wni+1,j ≥ 0)) then
22. // If all are hold, then check whether follow the path from left-up diagonal.
23. if (wni+1,j+1) > wni,j then
24. wni,j=wni+1,j+1
25. if qi = ε then
26. wni,j=wni,j
27. return W

Due to the revision of finding a longest common subsequence length from two 2D Be-strings before printing LCS string symbol, we need to compare the LCS string length of current cell with the string length of up one. It certainly implies that LCS path is induced from up direction if they are the same. The corresponding boundary symbol or dummy object doesn't belong to a symbol of LCS string. We ignore this symbol and continuously induce along up direction, as lines 5-6. On the other hand, if they are not the same, we need to compare current cell's LCS string length with left cell's length. If they are the same, the LCS is induced from left direction. With the same reason as preceding case, we also ignore this symbol and continuously induce along left direction, as lines 7-8. If the LCS is not from up nor left direction, it must be induced from left-up diagonal direction. The current cell associated boundary symbol or dummy object must be part of LCS string. After processing all cells on the left/up direction recursively, we print out this symbol, as lines 9-11.

Algorithm 3 to print LCS string of two 2D Be-strings:

Print-2D-Be-LCS (Q, W, i, j)
1. // Q is a 2D Be-string of query image, Q = (qi | qi ε (dummy object ε or the boundary symbols of objects in query image), i = 1, 2, ..., m).
2. // W is the LCS length inferring table of two 2D Be-strings, and induced from algorithm in Error! Reference source not found.,
3. if i = 0 or j = 0 then
4. return
5. if |wi,j| = |wi-1,j| then
6. Print-2D-Be-LCS(Q, W, i-1, j)
7. else if |wi,j| = |wi,j-1| then
8. Print-2D-Be-LCS(Q, W, i, j-1)
9. else
10. Print-2D-Be-LCS(Q, W, i-1, j-1)
11. print qi
12. return

5. Conclusions and Future works

A spatial representation model is proposed, called 2D Be-string spatial representation model. This model does not need to cut any icon object in an image, instead an object is represented by its MBR boundaries. It depicts the spatial relationship between two boundary symbols by apply a 'dummy object'. Thus, it can intuitively represent the spatial relationship in an image. In addition, the 2D Be-string is form by the object boundaries directly; thus, an image with n objects only needs storage units between 2n and 4n+1 in each dimension. That is, the space complexity of 2D Be-string is O(n).

We also introduce an algorithm, named Convert-2D-Be-String, to convert an image with MBR coordinate data into a symbolic image presented by 2D Be-string. The space and time complexity of this algorithm is O(n) when it does not consider the sort requirement.

We also present a similarity retrieval algorithm, named
2D-Be-LCS-Length, which is modified from LCS algorithm for the 2D Be-string representation model. All the space and time complexities of our proposed algorithm are \( O(mn) \), where \( m \) is the number of icon objects in query image and \( n \) is the number of object icons in the image database.

Moreover, we also provide an evaluation process, this process can evaluate all similarity no matter how the matched LCS string whether appears all query objects or not, or whether appears all spatial relationships or not. For the similarity retrieval of rotation and reflection, our approaches only need to reverse the string then apply the similarity retrieval and evaluation mentioned above. This process does not need any conversion of spatial operators. It is more efficient and much easier then before.

References


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