Near-Capacity Network Coding for Cooperative Multi-User Communications

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Abstract—In this contribution, we investigate Near-Capacity Multi-user Network-coding (NCMN) based systems using an Irregular Convolutional Code, a Unity-Rate Code and M-ary Phase-Shift Keying. Extrinsic Information Transfer (EXIT) charts were used for designing the proposed NCMN scheme. The design principles presented in this contribution can be extended to a vast range of NCMN based systems using arbitrary channel coding schemes.

I. INTRODUCTION

Network coding is a recently introduced paradigm conceived for efficiently disseminating data in multicast wireless networks, where the data flows arriving from multiple sources are combined to achieve compression and hence to increase the achievable throughput, as well as to reduce the delay imposed and to enhance the error-resilience of the system. The relay nodes store the incoming packets in their own buffer and then transmit the linear combinations of these packets. The coefficients used for creating the linear combination may be random numbers defined over a large finite field [2], or those gleaned from parity-check matrices of error control codes [3], [4].

Generalised Dynamic Network Codes (GDNC) were proposed in [4], [5] by interpreting the design problem as being equivalent to that of designing linear block codes defined over GF(q) for erasure correction. The authors of [4], [5] extended the original DNC concept presented in [6]–[8] by allowing each user to broadcast several (as opposed to a single in [6]–[8]) IFs of its own during the broadcast phase via orthogonal channels. Similarly, during the cooperative phases, each user transmits several nonbinary linear combinations to the base station (BS) using orthogonal channels, and these nonbinary linear combinations are considered as parity frames (PFs). In [4], [5], the authors investigated GDNCs assuming an idealised or so-called ‘perfect’ channel coding scheme, which was defined as the code that is capable of operating right at the Continuous-input Continuous-output Memoryless Channel’s (CCMC) capacity. The Frame Error Ratio (FER) performance of the GDNC scheme was determined in [4], [5] by calculating the rank of the matrix characterising GDNCs. This method, which we refer to as the Purely Rank-Based Method (PRBM), always provides an optimistic estimate of the attainable FER performance of GDNCs.

Tüchler and Hagenauer proposed the employment of Irregular Convolutional Codes (IrCCs) [9], [10] for serially concatenated schemes, which are constituted by a family of convolutional codes having different rates, in order to design a near-capacity system. They were specifically designed with the aid of Extrinsic Information Transfer (EXIT) charts conceived for analysing the convergence properties of iterative decoding aided concatenated coding schemes [11].

As a further advance, it was shown in [12] that a recursive Unity-Rate Code (URC) having an infinite impulse response is capable of efficiently spreading the available extrinsic information across the entire iterative receiver chain. This URC may be employed as an intermediate code, in order to improve the attainable decoding convergence. The URC may be viewed as a precoder invoked for creating a serially concatenated inner code component having an infinite impulse response in order to reach the (1,1) point in the EXIT chart and hence to achieve an infinitesimally low Bit Error Ratio (BER) [13], as detailed in [14]. For example, a near-capacity Irregular Convolutional Coded (IrCC)-URC-M-ary Phase-Shift Keying (IrCC-URC-MPSK) scheme may be designed for the sake of approaching the achievable channel capacity.

Based on this background, the novel contribution of this paper is that a realistic near-capacity channel coding scheme is designed for the sake of supporting network-coding aided multi-user communications. We consider the effects of both the shadow fading and of the small-scale Rayleigh fading in our channel model. The performance of the proposed system obtained by simulations is compared to that estimated by PRBM. The specific design guidelines presented in this contribution can also be extended to a diverse range of network-coding aided multi-user systems employing arbitrary channel coding schemes.

The rest of this paper is organised as follows. In Section II, outage probabilities are derived, before detailing both our system model and the detector used at the BS. In Section III, we propose design procedures for both our near-capacity IrCC-URC-MPSK and for network coding models. Our performance results are discussed in Section IV, before concluding in Section V.

II. PRELIMINARIES

A. Single Link Channel Outage Probability

We consider a single transmission link associated with the transmitted and received signals of x and y, respectively. The received signal can be represented as

\[ y = hx + n, \]

where \( h = h_x h_f \) is the complex-valued fading coefficient that comprises of two components, a slow fading coefficient (large-scale shadow fading or quasi-static fading) \( h_x \), which is constant for all symbols within a frame and a fast fading (small-scale Rayleigh fading) coefficient \( h_f \), which varies on a symbol by symbol basis, while \( n \) is the Additive White Gaussian Noise (AWGN) process having a variance of \( N_0/2 \) per dimension.

We refer to \( C \) as the maximum achievable transmission rate of reliable communication supported by this channel. Let us assume that the transmitter encodes data at a rate of \( R \) bits/s/Hz. If the channel realisation \( h \) has a capacity of \( C|_h < R \), the system is declared to be in outage, where the outage probability is given by:

\[ P_e(R) = Pr \{ C|_h < R \}, \]  

and \( C|_h \) is the capacity, i.e. the maximum achievable rate of the channel, provided that \( h \) is known. If \( x \) is i.i.d., the transmission
link obeys the CCMC model. The outage probability for the CCMC channel is given by [15]

\[ P_e^{CCMC}(R) = Pr\left\{ |h_i|^2 E[|h_j|^2] < \frac{2R - 1}{SNR} \right\}, \]  

where \( SNR \) is the signal to noise power ratio. Furthermore, the maximum achievable transmission rate of reliable communication supported by the Discrete-input Continuous-output Memoryless Channel (DCMC) was shown to be [16]

\[ C^{DCMC}(\eta) = \eta - \frac{1}{2^\eta} \sum_{l=1}^{2^\eta} \sum_{x=1}^{2^\eta} \exp(\psi_{l,x}) X_l, \]

where \( L = 2^\eta \) is the number of modulation levels, and \( \eta \) is the number of modulated bits, and \( E[A|X_l] \) is the expectation of \( A \) conditioned on the \( L \)-ary signals \( X_l \), whereas \( \psi_{l,x} \) is given by

\[ \psi_{l,x} = -|h_i(x_i - x_l)| + n_l^2 + |n_i|^2. \]

We define the receiver’s \( SNR \) as \( SNR = E[|h_i|^2| \eta R] \). At a given data rate \( R = \eta R, \) where \( R \) is the channel coding rate, we readily identify the corresponding \( SNR \) on the DCMC capacity curve described by (4). Then, similar to (3), the outage probability of the DCMC model is equivalent to the probability of the event that we have \( |h_i|^2 SNR < SNR \) as

\[ P_e^{DCMC}(R, \eta) = Pr\left\{ |h_i|^2 E[|h_j|^2] < \frac{2R - 1}{SNR} | R \right\}. \]

B. System Model

Let us initially describe a simple system having \( M = 2 \) users communicating with a BS [6]. A transmission session consists of \( (k_1 M + k_2 M) = 4 \) phases that include broadcast phases \( B_1 \) and \( B_2 \) and cooperative phases \( C_1 \) and \( C_2 \). In the transmission session, each user transmits \( k_1 = 1 \) IF during the corresponding broadcast phase and \( k_2 = 1 \) PF during the corresponding cooperative phase according to the transfer matrix \( G_{2 \times 4} \) [6]-[8]:

\[ G_{2 \times 4} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 2 \end{bmatrix}, \]

where the PF transmitted by User 1 (or User 2) during the cooperative phase \( C_1 \) (or \( C_2 \)) is given by \( PF = G_{2 \times 4}(1,3) I_1(1) + G_{2 \times 4}(2,3) I_2(2) = I_1(1) + I_2(2) \) (or \( PF = G_{2 \times 4}(1,4) I_1(1) + G_{2 \times 4}(2,4) I_2(2) = I_1(1) + 2I_2(2) \)). The variable \( I_1(t), i = [1,2] \), represents the IF transmitted by User 1 during the broadcast phase \( B_i \). For simplicity, we refer to a single transmission phase (broadcast phase or cooperative phase) as a time slot (TS), in which a user transmits a single signal (IF or PF). Note that all operations are defined over the Galois Field \( GF(q) \), but perhaps unconventionally, we represent the GF elements with the aid of the corresponding decimal numbers for the sake of convenient calculation.

To elaborate further, let us define \( G_{2 \times 4}^{co} \) as the corresponding modified transfer matrix, where the terminology modified implies that the entries of \( G_{2 \times 4} \) are modified with respect to those of the original transfer matrix \( G_{2 \times 4} \) of (7) according to the success/failure of each transmission within the actual transmission session. If all the frames transmitted within the session are successfully decoded, the transmission session can be equivalently represented by the modified transfer matrix \( G_{2 \times 4} \), where \( G_{2 \times 4}(i,i) = G_{2 \times 4}(i,1), i = [1,2] \) represents the successful decoding of the IF \( I_1(1) \) at the BS. Note that having \( G_{2 \times 4}(1,3) = G_{2 \times 4}(1,1) \) (or \( G_{2 \times 4}(2,4) = G_{2 \times 4}(2,4) \)) means that the PF transmitted by User 1 (or User 2) was successfully decoded at the BS. Similarly, having \( G_{2 \times 4}(2,3) = G_{2 \times 4}(2,3) \) (or \( G_{2 \times 4}(1,4) = G_{2 \times 4}(1,4) \)) indicates that the IF \( I_2(2) \) (or \( I_1(1) \)) was successfully decoded by User 1 (or User 2), and that the PF transmitted by User 1 (or User 2) was successfully decoded at the BS.

Let us consider the following example of the actual transmission session, where ‘\( t \)' represents the transmission direction, while ‘\( i \)’ (or ‘\( i' \)’) above the arrows means that the frame was successfully (or unsuccessfully) recovered at the destination:

\[ B_1 \]

\[ G_{2 \times 4}(1,3) = G_{2 \times 4}(1,3), \]

\[ [User 1 \quad 0 \quad BS] : G'(1,1) = 0, \]

\[ [User 1 \quad 1 \quad User 2] : G_{2 \times 4}(1,4) = G_{2 \times 4}(1,4), \]

\[ B_2 \]

\[ G_{2 \times 4}(2,4) = G_{2 \times 4}(2,4), \]

\[ [User 2 \quad 0 \quad BS] : G'(2,2) = 0, \]

\[ [User 2 \quad 1 \quad User 1] : G_{2 \times 4}(2,3) = G_{2 \times 4}(2,3), \]

\[ C_1 \]

\[ [User 1 \quad 0 \quad BS] : G_{2 \times 4}(i,3) = 0, i = 1, 2, \]

\[ C_2 \]

\[ [User 2 \quad 1 \quad BS] : G_{2 \times 4}(i,4) \text{ unchanged}, i = 1, 2. \]

This example results in

\[ G_{2 \times 4} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}, \]

where the diagonal elements “1” at the left of (7) become “0” owing to the unsuccessful [User 1 \( \downarrow \quad BS \) and [User 2 \( \downarrow \quad BS \) transmissions during the broadcast phases \( B_1 \) and \( B_2 \) respectively. The “0” elements in the third column of (9) indicate the unsuccessful [User 1 \( \downarrow \quad BS \) transmission during the cooperative phase \( C_1 \).

Let us now generalise this model. The transfer matrix \( G_{2 \times 4 \times k_1 M + k_2 M} \) (or \( G \) for shorthand) seen in Fig. 1, which comprises the identity matrix \( I_{k_1 M \times k_1 M} \) (or \( I \) for shorthand) and the parity matrix \( P_{k_1 M \times k_2 M} \) (or \( P \) for shorthand) represents a transmission session of the system, where all the frames transmitted during that session are successfully decoded. Accordingly, the binary flag \( I_{2M}^{CMC}(t) \) seen in Fig. 1 represents the success or failure of the IF decoding at the BS, namely the IF \( I_{m}(t), t = [m, M, ..., (k_1 - 1)M + m, \] transmitted by User \( m, m \in \{1, ..., M\} \). Furthermore, \( I_{2M}^{CMC}(t) \) is set during the specific broadcast phase \( t \) selected from the whole set of \( k_1 M \) broadcast phases according to [4], [5]:

\[ r_{m}(t) = \begin{cases} 1 : & \text{If } I_{m}(t) \text{ is successfully recovered} \\ 0 : & \text{Otherwise} \end{cases} \]

The \( k_2 \) PFs transmitted by each of the \( M \) users contain nonbinary linear combinations of its own IFs with the successfully decoded IFs from the set of \( k_1 (M - 1) \) ISs transmitted by the \( (M - 1) \) other users. The variable \( P_{m}(t) \) in Fig. 1 corresponds to the parity coefficient of the IF \( I_{m}(t) \) contained in the \( s^{th} \) PF transmitted by User \( m \) during the cooperative phase \( |M(s - 1) + m|, s \in \{1, ..., k_2\} \), where we have the index \( r \) determined by

\[ r = \begin{cases} M : & t \mod M = 0 \\ t \mod M : & t \mod M \neq 0 \end{cases}. \]

Let us denote the corresponding entry of \( P_{m}(t) \) in the modified matrix \( G' \) as \( P_{m}'(t) \), which is determined by

\[ P_{m}'(t) = \begin{cases} P_{m}(t) : & r = m \end{cases}. \]

Then, for the case that we have \( r \neq m \), the entry \( P_{m}'(t) \) is specified by [4], [5]

\[ P_{m}'(t) = \begin{cases} P_{m}(t) : & User \ r \neq m \\ 0 : & User \ r = m \end{cases}. \]

The column \( [M(s - 1) + m] \) of the parity matrix \( P \) shown in Fig. 1 contains the set of parity coefficients valid for the \( s^{th} \) PF transmitted
by User $m$ during the cooperative phase $[M(s - 1) + m]$. Hence, the entire column $P^*_m(s\cdot t)$, $\forall t = [1, 2, \ldots, k_1M]$ will be set to zeros, if the BS could not successfully receive the $s^{th}$ PF:

$$P^*_m(s\cdot t) = 0, \forall t = [1, 2, \ldots, k_1M] \quad \text{User } m \quad \text{through } \text{BS}. \quad (14)$$

C. Detection model

As the system proceeds through an actual transmission session, the corresponding modified transfer matrix $G\prime$ consisting of its identity matrix $I$ and its parity matrix $P\prime$ is formed, where $I$ is generated from (10), while $P\prime$ is determined in turn by (12), (13) and (14). The frames successfully received at the BS can be represented as

$$(a) \quad X\prime = Y\prime; \quad (b) \quad X\prime = Y\prime,$$

where $X = \{I_1(1), I_2(2), \ldots, I_M(k,1)\}$ is a matrix representing the IFs transmitted by the $M$ users during the transmission session of the system, while the matrices of $Y\prime$ and $Y\prime$ represent the frames successfully received at the BS during the broadcast phases and cooperative phases, respectively. In line with [4], [5], we assume that the BS is aware of how each PF was constructed, hence $G\prime$ is known at the BS. Since the matrix $I\prime$ may be different from $I$, the BS can certainly recover a set $X\prime$ of IFs, which is a subset of $X$, from $Y\prime$ according to:

$$X\prime = Y\prime.$$  

(16)

Substituting $X\prime$ given by (16) into (15b) we have

$$(X - X\prime)\cdot P\prime = Y\prime - X\prime\cdot P\prime.$$  

(17)

Then, a set $X\prime$ of IFs is retrieved from (17) by using the Gaussian elimination algorithm [17]. Ultimately, the entire set of IFs recovered at the BS is $X\prime$, $\{X\prime\}$ out of the $X$ of IFs.

Having presented the detection model above, let us now characterise the system’s optimistic performance estimated by the PRBM employed in [4], [5] by recalling the example detailed in (7) and (8). According to the prediction of the PRBM, the BS can recover $\text{Rank}(G_{2\times4}) = 1$ IF, where $G_{2\times4}$ is given in (9). However, in fact the BS cannot recover any IF, because we cannot determine two IFs, i.e. both $I_1(1)$ and $I_2(2)$, from a single equation, which is inferred from (16) and (17) as $1 \times I_1(1) + 2 \times I_2(2)$.

III. Design and Analysis

A. Near-Capacity Code Design

According to (1), (3) and (6), the average $SNR_r$ per frame can be expressed as

$$SNR_r = \frac{E[|h_s|^2]E[|h_f|^2]E[|z|^2]}{N_0} = \frac{|h_s|^2}{N_0},$$

(18)

where we have $E[|z|^2] = 1$ and $E[|h_f|^2] = 1$ for uncorrelated Rayleigh fading channels and $E[|h_s|^2] = |h_s|^2$ for quasi-static Rayleigh fading channels. Given a specific $SNR_r$, we can generate the EXIT chart [11] of the channel coding scheme for transmission over the uncorrelated Rayleigh fading channel.

As stated in Section I, a near-capacity IrCC-URC-MPSK channel coding scheme is chosen for the sake of approaching the achievable channel capacity. For the sake of brevity and readability, we present the IrCC-URC-Quadrature Phase Shift Keying (IrCC-URC-QPSK) design procedure using our generically applicable EXIT-chart aided method, which is briefly summarised as follows:

Step1: Create the EXIT curve of the inner decoder constituted by our URC-QPSK scheme for different $SNR_r$ values;

Step2: We opt for the data rate $R = \eta R_e = 1$, we fix the IrCC code rate $R_e = 0.5$ and employ the EXIT curve matching algorithm of [9] for generating the optimised weighting coefficients $\alpha_i$, $i = 1, \ldots, 17$, of the 17 different-rate component IrCC codes. More specifically, we opt for the set of codes facilitating decoding convergence to a vanishingly low $BER$ at the lowest possible $SNR_r$, while ensuring that the Monte-Carlo simulation based decoding trajectory reaches the point of $(1,1)$ at the top-right corner of the corresponding EXIT chart. This implies that a near-capacity performance can be achieved, as detailed in [14].

Having implemented the design steps mentioned above, we obtain the EXIT curves and the corresponding IrCC component-code weighting coefficients $\alpha_i$, $i = 1, \ldots, 17$, as shown in Fig. 2. Again as detailed in [14], these weighting coefficients $\alpha_i$ determine the particular fraction of the input stream to be encoded by the $i^{th}$ IrCC component code having a code rate of $\alpha_i$. The EXIT-chart results show that provided $J = 20$ iterations were affordable, the trajectory would reach the $(1,1)$ point in Fig. 2, which guarantees a vanishingly low $BER$.

Furthermore, the area property of EXIT-charts [18] states that the area under the EXIT curve of an inner decoder component is approximately equal to the attainable channel capacity, provided that the channel’s input symbols are equiprobable. Hence we exploited the area property of EXIT-charts [18] to determine the achievable DCMC capacities of the URC-QPSK and IrCC-URC-QPSK systems, which are quantified in Fig. 3. It is seen in Fig. 3 that the capacity of the URC-QPSK scheme almost coincides with the DCMC-QPSK curve. The numerical results of Fig. 4 also show the attainable channel capacity improvements corresponding to $J = 1,10,20$ and 40 iterations. There is only a negligible further improvement for having $J = 40$ in comparison to $J = 20$. It is also demonstrated in Fig. 3 that the IrCC-URC-QPSK scheme’s capacity curve is only about $(2.8 - 1.8) = 1.0$dB away from DCMC-QPSK capacity curve for $J = 20$.

Our simulation results seen in Fig. 4 verify the accuracy of our EXIT chart analysis. When employing $J = 20$ iterations between the IrCC and URC components, our IrCC-URC-QPSK channel coding scheme has a vanishingly low BER for $SNR$ in excess of 2.8dB, provided that the transmission frame length is sufficiently high. At this stage we also define the relaying-aided reduced-distance-related pathloss-reduction. Naturally, this pathloss-reduction becomes unity for each direct source-to-destination link [19]. We also observe from
parameters \((R, M, k_1, k_2, G, R_{in,fo}, D_{NCMN})\), where the system’s overall data rate \(R_{in,fo}\) is expressed as \([4], [5]\):

\[
R_{in,fo} = \frac{k_1}{k_1 + k_2}.
\]

while the diversity order \(D\) of the system is bounded \([4]–[6]\):

\[
M + k_2 \leq D_{NCMN} \leq Mk_2 + 1.
\]

By observing the \(R_{in,fo}\) expression of (19) and the \(D_{NCMN}\) formula of (20), it is plausible that we may conceive different systems having the same rate \(R_{NCMN}\), but different diversity order \(D_{NCMN}\) by independently adjusting \(k_1, k_2\), and \(M\). In other words, using (19) and (20), we are able to design a network-coding based system having the highest possible diversity order at a given overall system data rate of \(R_{NCMN}\). A higher diversity order implies that the system is capable of achieving an improved FER performance.

In order to demonstrate the design principles mentioned above, let us consider a \(G_{2 \times 4}\)-based system and a \(G_{4 \times 8}\)-based system. The matrix \(G_{2 \times 4}\) is given in (7), and \(G_{4 \times 8}\) given in \([4], [5]\):

\[
G_{4 \times 8} = \begin{bmatrix}
1 & 0 & 0 & 0 & 3 & 7 & 3 & 6 \\
0 & 1 & 0 & 0 & 5 & 7 & 7 & 4 \\
0 & 0 & 1 & 0 & 2 & 4 & 6 & 1 \\
0 & 0 & 0 & 1 & 5 & 5 & 3 & 2
\end{bmatrix}.
\]

The \(G_{2 \times 4}\)-based system is represented by \((R = 0.5, M = 2, k_1 = 1, k_2 = 1)\), \(G_{2 \times 4}, R_{in,fo} = 0.5, 3 \leq D_{(2 \times 4)NCMN} \leq 3\), and the \(G_{4 \times 8}\)-based system is characterised by \((R = 0.5, M = 2, k_1 = 2, k_2 = 2)\), \(G_{4 \times 8}, R_{in,fo} = 0.5, 4 \leq D_{(4 \times 8)NCMN} \leq 5\). The two systems are comparable, since they both have the same \(R, M\) and \(R_{in,fo}\) values. However, the more complex transfer matrix \(G_{4 \times 8}\) has a higher diversity order of \(4 \leq D_{(4 \times 8)NCMN} \leq 5\) (as opposed to \(3 \leq D_{(2 \times 4)NCMN} \leq 3\)). This also means that the \(G_{4 \times 8}\)-based system is expected to have a superior FER performance in comparison to the \(G_{2 \times 4}\)-based system.

**IV. SIMULATION RESULTS AND DISCUSSIONS**

The FER versus SNR performance of the \(G_{2 \times 4}\) and \(G_{4 \times 8}\) based systems employing the IrCC-URC-Binary Phase Shift Keying (IrCC-URC-BPSK) scheme \([14]\) and the idealised/perfect CCMC and DCMC channel coding schemes is shown in Fig. 5. We use the IrCC-URC-BPSK coding scheme having a data rate \(R = 1 \times 0.5 = 0.5\), in order to facilitate a comparison between our results and the previous results presented in \([4], [5]\). The IrCC-URC-BPSK coding scheme was also designed by the same procedure as that used for the IrCC-URC-QPSK, as detailed in Section III-A \([14]\).

It can be seen from Fig. 5 and Fig. 6 that the difference in the diversity order of the \(G_{2 \times 4}\) and \(G_{4 \times 8}\) based systems, as specified in Section III-B, is reflected by the different slope of the performance
curves. As a benefit, the $G_{4 \times 8}$-based system outperforms the $G_{2 \times 4}$-based system by about from 4.2 dB to 4.4 dB at an FER of $10^{-4}$ in the cases of using the CCMC, DCMC, IrCC-URC-BPSK and IrCC-URC-QPSK channel coding schemes.

Another important result gleaned from both Fig. 5 and Fig. 6 is that the performance of the NCMN systems using the idealised/perfect CCMC and DCMC channel coding schemes represents the best-case performance bound of all NCMN systems using realistic channel coding schemes, provided that the equivalent data rates $R$ of those schemes are the same.

Fig. 5 and Fig. 6 substantiates our analysis provided in Section II-C, where the performance estimate found with the aid of the PRBM was always superior but optimistic in comparison to that obtained by the actual simulations. More explicitly, it is shown in Fig. 5 and Fig. 6 that their deviation was found to be from 0.3 dB to 0.5 dB at an FER of $10^{-4}$.

![Fig. 5: FER versus SNR performance of the $G_{2 \times 4}$ and $G_{4 \times 8}$ based systems employing the realistic channel coding scheme IrCC-URC-BPSK and idealised/perfect CCMC and DCMC channel coding schemes.](image)

As seen in Fig. 5 and Fig. 6, the performance of the $G_{4 \times 8}$ and $G_{2 \times 4}$-based systems using our IrCC-URC-QPSK(QPSK) scheme was within 0.7 dB to 0.8 dB at an FER of $10^{-4}$ from that of the corresponding systems relying on the assumption of using an idealised/perfect DCMC channel coding scheme.

![Fig. 6: FER performance comparison between $G_{2 \times 4}$ and $G_{4 \times 8}$ based systems employing the realistic channel coding scheme IrCC-URC-QPSK and idealised/perfect CCMC and DCMC channel coding schemes.](image)

V. CONCLUSIONS

In this contribution, we investigated new Near-Capacity Multi-user Network-coding based systems using our IrCC-URC-MPSK channel coding scheme, which was designed with the aid of EXIT charts. The achievable performance was benchmarked against the corresponding systems employing the idealised/perfect channel coding schemes operating exactly at the CCMC and DCMC capacities.

REFERENCES


