Security Analysis of the Kerberos protocol using BAN logic

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Abstract—Kerberos protocol is a famous identity authentication protocol and it is widely used in the network as a standard. But there is still not a strict proof of it base on the Formal method. That is very nervous for the users. So a security analysis of the Kerberos protocol using BAN logic is proposed in this paper, and the reliability, practicability and security of Kerberos protocol are proved.

Keywords-Kerberos protocol; Formal analysis; BAN logic

I. INTRODUCTION

As one of the core technology in network security communication systems cryptographic protocols has received great attention from all over the world and achieved great development. While it is not easy to analysis the security of a cryptographic protocol, much vulnerability difficult to find are hidden in seemingly correct protocol. As we all known, the design of cryptographic protocols is a work easy to go wrong. So it is a necessary aspect for protocol design to analysis the security of protocols. To provide accurate and credible analysis of protocol security researchers has put forward many protocol security proof technologies.

Among of them, the formal analysis methods [1] have become one of the most important means and tools to analysis and design the protocol security. The formal analysis method uses rigorous theoretical models to conduct the strict mathematical and logical deduction and demonstration for cryptographic protocols to prove the security or point out secure vulnerabilities of them. The BAN logic [2] is put forward by Burrows, Abadi and Needham is one of the most famous methods of the formal analysis method. The BAN logic has the advantages of clear concept, simple and easy to understand and use and it can effectively find the secure vulnerability difficult to detect in the protocol.

Kerberos protocol [3-4] is a three-party certification network security authentication protocol that is applied to an open network environment. Kerberos protocol has become the normal network identity authentication protocol in the field. And it is a representative technology in the Internet access control technology and it has widely used in the secure access control in the Internet. But there is still not a strict proof of Kerberos protocol base on the Formal method. That is of great significance for secure using Kerberos protocol.

In this paper we use the BAN logic to model and analysis the Kerberos protocol and have proved its reliability, practicability and security finally.

This paper is organized as follows: in Section 2, the logical postulate of BAN logic is introduced; in Section 3, the Kerberos protocol is proved by using BAN logic; finally, concluding remarks are made in Section 4.

II. THE LOGICAL POSTULATE OF BAN LOGIC

Rule (1) Message meaning rule:

\[
P \text{ believes } Q \leftrightarrow K \text{, then } P \text{, sees } \{X\}K \text{ if } P \text{ believes } Q \text{ has said } X\]

Rule (2) Random number verification rule:

\[
P \text{ believes fresh}(X), P \text{ believes } Q \text{ has said } X \text{ if } P \text{ believes } X \text{ is sent currently and } Q \text{ has said } X.
\]

Rule (3) Jurisdiction rule:

\[
P \text{ believes } Q \text{ controls } X, P \text{ believes } Q \text{ has said } X, P \text{ believes } X\]

Rule (4) Fresh transmission rule:

\[
P \text{ believes fresh}(X), P \text{ believes } Q \text{ has said } X \text{ and } Q \text{ has said } X.
\]

Rule (5) Trust polymerization and trust projection rule:

\[
P \text{ believes } X, P \text{ believes } Y \text{ and } P \text{ believes } (X, Y) \text{ if } P \text{ believes } (X, Y) \text{ and } P \text{ believes } X.
\]

Rule (6) See rule:
P believes $K \rightarrow P, P$ sees $\{X\}K$ \[ (6) \]
P sees $X$

$P$ can decrypt the message he has received if $P$ has received messages encrypted by his own public key.

III. KERBEROS PROTOCOL PROOF USING BAN LOGIC

A. Kerberos protocol

The authentication process is as follows:

1. $C \rightarrow AS$: applying for the Ticket Granting Ticket (KRB_AS_REQ) and $AS \rightarrow C$ : the Ticket Granting Ticket (KRB_AS_REP)

   \begin{align*}
   & \{K_{C,TGS}, T_{C,TGS} | K_C \\
   & T_{C,TGS} = \{TGS, C, addr, N_1, lifetime, K_{C,TGS}\}K_{TGS}
   \end{align*}

   After $AS$ received the request message from the client it looks up the client’s shared key $K_C$ in its database and generate the random session key $K_{C,TGS}$ and the ticket $T_{C,TGS}$ as its response message. $K_{C,TGS}$ is encrypted by $K_C$ which is used to conduct encryption communication between the client and $TGS$. The content of $T_{C,TGS}$ includes the name of $TGS$ and client, the IP address of the client, random number, effective survival time and $K_{C,TGS}$. These data are encrypted by $TGS$’s shared key $K_{TGS}$ to ensure only $TGS$ can decrypt them. $AS$ sends its response to the client which is encrypted by the client’s key $K_C$ that can ensure only $C$ can decrypt that message. If the client can not decrypt that response message his identity is fake and the identity authentication is failure; otherwise, his identity is correct. After $C$ receives $AS$’s response he decrypts the message and he will get the $TGS$’s ticket $T_{C,TGS}$. In next step he can send $T_{C,TGS}$ to $TGS$ to prove he possesses the correct identity to visit it. At the same time the client gets $K_{C,TGS}$ that can be used to conduct encrypted communication with $TGS$ from $AS$.

2) the authorization service exchange

The authorization service exchange is also called the TGS exchange. The authorization service exchange process is consists on the message exchange (3) and (4). That is the process that client applies for the ticket $T_{C,V}$ and session key communicating with the application server $V$ from $TGS$. TGS exchange is the message exchange between client and $TGS$ and the message form is same as that in the $AS$ exchange. But there is a significant difference that the session key but not the client’s shared key is used as the encrypted and decrypted key in this process. The TGS exchange is consists
on two messages that are KRB_TGS_REQ and KRB_TGS_REP.

e) \( C \rightarrow TGS \): applying for the server ticket (KRB_TGS_REQ)

\[
V, N_2, \text{ lifetime, } T_{C,TGS}, A_{C,TGS}
\]
\[
A_{C,TGS} = \langle C, \text{ addr, timestamp} \rangle \mid \text{K}_{T_{C,TGS}}
\]

\( C \) sends the request message to \( TGS \) which wants to visit \( V \). The content is include the \( V \)’s name, \( TGS \)’s ticket \( TGT \) and authentication symbol \( A_{C,TGS} \). \( TGT \) is encrypted by using \( TGS \)’s shared key \( K_{TGS} \) so only \( TGS \) can decrypt it. \( A_{C,TGS} \) is including client’s name, client’s IP address and a timestamp. \( A_{C,TGS} \) is encrypted by using the session key between client and \( TGS \) so only \( TGS \) can decrypt it. The ticket \( TGT \) could not prove anyone’s identity and it can be re-used and its effective time is longer. While the authentication symbol is used to prove client’s identity and it can be used only one time and its effective time is very short.

After \( TGS \) received client’s request message it uses shared key \( K_{TGS} \) to decrypt \( TGT \) and knows client has got the session key \( K_{C,TGS} \) with it from \( AS \). Here the ticket \( TGT \) means that the client who uses \( K_{C,TGS} \) is \( C \). \( TGS \) uses \( K_{C,TGS} \) to decrypt the authentication symbol and compares its data with \( TGT \)’s so it can believe \( TGT \)’s sender \( C \) is just \( TGT \)’s holder.

d) \( TGS \rightarrow C \): server ticket (KRB_TGS_REP)

\[
\{K_{C,V}, T_{C,V} \} \mid \text{K}_{T_{C,TGS}}
\]
\[
T_{C,V} = \langle V, C, \text{ addr, N}_2, \text{ lifetime, } K_{C,V} \rangle \mid \text{K}_{V,TGS}
\]

After \( TGS \) verified client’s identity is correct it generates random session key \( K_{C,V} \) which is used to encrypted communicate between \( C \) and \( V \) and at the same time it generates the ticket \( T_{C,V} \) which is used to visit \( V \). The content of \( T_{C,V} \) is includes the name of the application server and client, client’s IP address, random number, effective survival time and the session key \( K_{C,V} \). \( T_{C,V} \) is encrypted by using session key \( K_{V,TGS} \) so that only \( V \) can decrypt it. The session key \( K_{C,V} \) and ticket \( T_{C,V} \) is consists on \( TGS \)’s response message which is encrypted by using \( K_{C,TGS} \) between \( C \) and \( TGS \). After \( C \) received \( TGS \)’s response message he uses \( K_{C,TGS} \) to decrypt it and gets \( T_{C,V} \) and \( K_{C,V} \).

3) the client / application server exchange

After \( AS \) exchange and \( TGS \) exchange client gets the ticket \( T_{C,V} \) and session key \( K_{C,V} \) for visiting \( V \). The both identity authentication will be achieved after they pass the client / application server exchange. The client / application server exchange is consists on two messages which are KRB_AP_REQ and KRB_AP_REP. KRB_AP_REP is only used when there is need two-way authentication and server wants to prove its identity to client.

e) \( C \rightarrow V \): applying for service (KRB_AP_REQ)

\[
V, T_{C,V}, A_{C,V}
\]
\[
A_{C,V} = \langle C, \text{ addr, N}_2 \rangle \mid K_{C,V}
\]

\( C \) sends request message to \( V \). The content is includes \( V \)’s name, ticket \( T_{C,V} \) and authentication symbol. \( T_{C,V} \) can be decrypted only by \( V \). The authentication symbol is includes client’s name, client’s IP address, random number. The authentication symbol is encrypted by using the session key between client and server so that it can be decrypted only by \( V \).

After \( V \) received client’s request message it uses \( K_{V,TGS} \) to decrypt \( T_{C,V} \) and knows \( C \) has got the session key \( K_{C,V} \). Here means \( T_{C,V} \) that the client who uses \( K_{C,V} \) is just \( C \). \( V \) uses \( K_{C,V} \) to decrypt the authentication symbol and compares its data with \( T_{C,V} \)’s so that it can believes \( T_{C,V} \)’s sender \( C \) is just \( T_{C,V} \)’s holder. So \( C \)’s identity has been authenticated.

f) \( V \rightarrow C \): server authentication (KRB_AP_REP)

After \( V \) verified \( C \)’s identity is correct it adds 1 to the random number that it has got from the authentication symbol and uses \( K_{C,V} \) to encrypt it to send to client as its response message. That response message only can be decrypted by \( C \). After \( C \) received and decrypted it he verifies the increased random number and compares with the effective of the random number to authenticate \( V \). If it is correct \( C \) will believe it is just \( V \) has added the random number so \( V \)’s identity has been authenticated.

After the whole protocol exchange process there is a shared session key between client and application server and they can use that key to conduct encrypted communication to each other.

B. Kerberos protocol proof using BAN logic

Some reasonable assumptions are constructed for the analysis condition of Kerberos protocol is as follows:

1) \( C \) believes \( C \leftarrow K_C \rightarrow AS \)

2) \( V \) believes \( V \leftarrow K_{V,TGS} \rightarrow TGS \)

3) \( V \) believes \( V \leftarrow K_{V,TGS} \rightarrow TGS \)

4) \( C \) believes \( AS \) controls \( T_{C,TGS} \)

5) \( C \) believes \( TGS \) controls \( T_{C,V} \)

6) \( C \) believes \( TGS \) controls \( K_{C,V} \)

7) \( V \) believes \( TGS \) controls \( T_{C,V} \)

8) \( C \) believes \( fresh(N_2) \)

9) \( V \) believes \( fresh(N_C) \)

10) \( C \) believes \( fresh(N_C) \)

The protocol proof using BAN logic is as follows.

1) Proof \( \) \( C \) believes \( C \leftarrow S_C \rightarrow V \)

Because \( C \) believes \( C \leftarrow S_C \rightarrow AS \), \( C \) sees \( \{T_{C,TGS}\}K_C \)

according to Rule (1) we can get: \( C \) believes \( AS \) said \( T_{C,TGS} \).

Because \( C \) believes \( fresh(N_2) \) according to Rule (2) we can get: \( C \) believes \( AS \) believes \( T_{C,TGS} \).

Because \( C \) believes \( AS \) controls \( T_{C,TGS} \) according to Rule (3) we can get: \( C \) believes \( T_{C,TGS} \).

Then according to Rule (5) we can get: \( C \) believes \( K_{C,TGS} \).

Because \( C \) sees \( \{T_{C,V}\}K_{C,TGS} \) according to Rule (1) we can get: \( C \) believes \( TGS \) said \( T_{C,V} \).

Because \( C \) believes \( fresh(T_{C,V}) \) according to Rule (2) we can get: \( C \) believes \( TGS \) believes \( T_{C,V} \).

Because \( C \) believes \( TGS \) controls \( T_{C,V} \) according to Rule (3) we can get: \( C \) believes \( T_{C,V} \).

Finally according to Rule (5) we can get:
C believes $C \xrightarrow{K_{C,F}} V$

2) **Proof** $V$ believes $C \xrightarrow{K_{C,F}} V$

Because $V$ believes $V \xrightarrow{K_{F,TGS}} TGS$, $V$ sees $\{T_{C,F}\}K_{F,TGS}$ according to **Rule (1)** we can get: $V$ believes $TGS$ said $T_{C,F}$.

Because $V$ believes $\text{fresh}(T_{C,F})$ according to **Rule (2)** we can get: $V$ believes $TGS$ believes $T_{C,F}$.

Because $V$ believes $TGS$ controls $Tc,v$ according to **Rule (3)** we can get: $V$ believes $T_{C,F}$.

Finally according to **Rule (5)** we can get:

$V$ believes $C \xrightarrow{K_{C,F}} V$

3) **Proof** $C$ believes $V$ believes $C \xrightarrow{K_{C,F}} V$

Because $C$ believes $\text{fresh}(N_c)$ so we can get:

$C$ believes $\text{fresh}(N_c+1)$.

So we can get: $C$ believes $\text{fresh}(\{N_c+1\}K_{C,F})$.

Because $C$ believes $K_{C,F}$, $C$ sees $\{N_c+1\}K_{C,F}$ according to **Rule (1)** we can get: $C$ believes $V$ said $\{N_c+1\}K_{C,F}$.

According to **Rule (2)** we can get:

$C$ believes $V$ believes $\{N_c+1\}K_{C,F}$.

Finally we can get:

$C$ believes $V$ believes $C \xrightarrow{K_{C,F}} V$  (7)

As the same we can get:

$V$ believes $C$ believes $C \xrightarrow{K_{C,F}} V$  (8)

From now, we have got the final conclusion of the authentication protocol, which is the function (7), (8), (9) and (10). We can get the conclusion that Kerberos protocol can not only achieve the key establishment process between the client and server securely but also achieve the real-time communication between the two sides. In the whole process of the protocol it combines the authentication with the ticket so that it improves the security of the system. According to our analysis process the protocol has a strict architecture. We can not find any vulnerability of the protocol and the attack outside in our logic proof so we can say Kerberos protocol is correct and reliable.

IV. CONCLUSION

Because there is still not a strict proof of the Kerberos protocol base on the Formal method which has been used in the network widely the analysis and proof of the Kerberos protocol using BAN logic is proposed in this paper. And its reliability, practicability and security have been proved finally. That is of great significance for secure using Kerberos protocol.

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REFERENCES


