



Time-of-arrival estimation for blind beamforming

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Presentation outline

- 1) Traditional beamforming / beam steering
- 2) Ad-hoc microphone arrays
- 3) Three ad-hoc array beam steering methods
 - Time-of-Arrival (TOA) based solutions
- 4) Simulation of TOA accuracy
- 5) Measurements with an array of smartphones
 - Accuracy of TOA estimation
 - Obtained beamforming quality



Traditional Beamforming

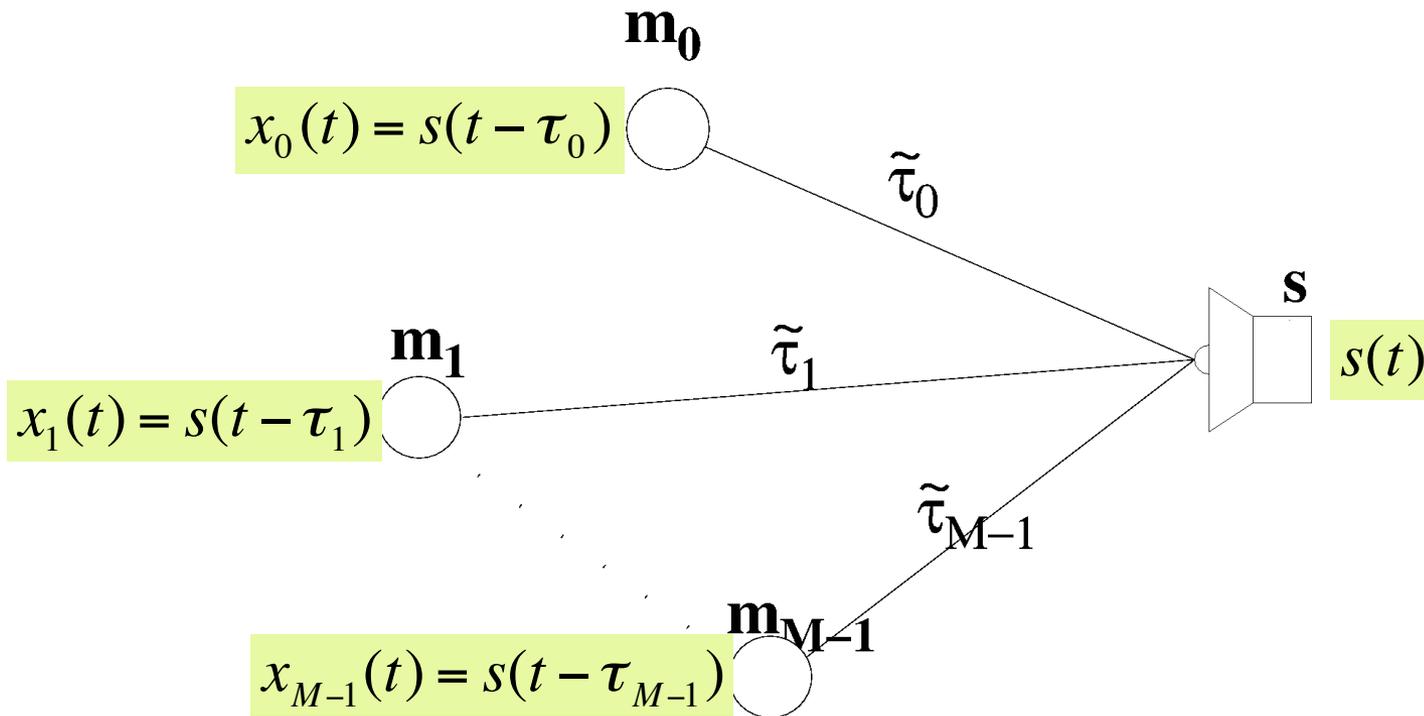
- Linear combination of microphone signals $X_i(\omega)$, where $i = 1, \dots, M$
- Requirements for steering the beam:
 - 1) Array shape is known (mic. position matrix \mathbf{M})
 - 2) Sensors are synchronous (time offset is zero/known)
 - 3) Direction/position to steer the array is known or can be scanned e.g. based on energy.
- Simple Delay-and-Sum Beamformer (**DSB**)

$$Y(\omega) = \sum_{i=0}^{M-1} \underbrace{\exp(i\omega\tau_i)}_{\text{time-shifting}} X_i(\omega)$$



Signal observation (near field)

- Sound Time-of-Flight (TOF) is $\tilde{\tau}_i = \|\mathbf{m}_i - \mathbf{s}\|c^{-1}$
- Align signals by advancing $x_i(t)$ by $\tilde{\tau}_i$



Ad-Hoc microphone array

- Independent devices equipped with a microphone
- Traditional beamforming requirements unfulfilled
 1. Array geometry is unknown (\mathbf{M} is unknown)
 2. Devices aren't synchronized (unknown time offsets Δ_i)
 3. The space cannot be easily panned to find source direction θ to steer the beam into



Time of Arrival (TOA)

- Signal time-of-arrival (TOA) for an ad-hoc array

$$\tau_i = \underbrace{c^{-1} \|\mathbf{s} - \mathbf{m}_i\|}_{\text{propagation delay}} + \underbrace{\Delta_i}_{\text{time offset}}$$

- Time-difference-of-Arrival (TDOA) for mics i, j

$$\tau_{i,j} = \tau_i - \tau_j$$

- TDOAs $\tau_{i,j}$ can be measured using e.g. correlation
- Previously considered as source spatial information

A. Brutti and F. Nesta, "Tracking of multidimensional TDOA for multiple sources with distributed microphone pairs," Computer Speech & Language, vol. 27,

- TDOA and TOA vectors are written as

$$\mathbf{y} = [\tau_{1,2}, \tau_{1,3}, \dots, \tau_{M-1,M}]^T, \mathbf{y} \in \mathbb{R}^{P \times 1}$$

$$P = M(M-1)/2$$

$$\boldsymbol{\tau} = [\tau_1, \tau_2, \tau_3, \dots, \tau_M]^T, \boldsymbol{\tau} \in \mathbb{R}^{M \times 1}$$



Time of Arrival (TOA)

- By defining an observation matrix

$$\mathbf{H} = [\mathbf{e}_1 - \mathbf{e}_2, \mathbf{e}_1 - \mathbf{e}_3, \dots, \mathbf{e}_1 - \mathbf{e}_M, \mathbf{e}_2 - \mathbf{e}_3, \dots, \mathbf{e}_2 - \mathbf{e}_M, \dots, \mathbf{e}_{M-1} - \mathbf{e}_M]^T, \mathbf{H} \in \mathbb{R}^{P \times M},$$

– E.g. for three microphones $\mathbf{H} = \begin{bmatrix} 1 & -1 & 0 \\ 1 & 0 & -1 \\ 0 & 1 & -1 \end{bmatrix}$

- The linear model between TOA and TDOA is

$$\mathbf{y} = \mathbf{H}\boldsymbol{\tau}$$

- TOA proposed as source spatial representation



Time of Arrival (TOA) – 1st

- **Baseline method (TDOA subset):**
 1. Select a reference microphone (e.g. 1st mic)
 2. Use relative delays $\tau_{i,j}$ between the reference ($i = 1$) and rest ($j = 2, \dots, M$) as TOA

$$\hat{\tau} = [0, \tau_{1,2}, \tau_{1,3}, \dots, \tau_{1,M}]^T, \hat{\tau} \in \mathbb{R}^M.$$

- Does not utilize TDOA information between all sensors



Time of Arrival (TOA) – 2nd

- Moore-Penrose inverse solution for TOA

$$\hat{\tau}_0 = (\mathbf{H}_0^T \mathbf{H}_0)^{-1} \mathbf{H}_0^T \mathbf{y}.$$

- \mathbf{H}_0 is \mathbf{H} without the first column to account for one missing degree of freedom, i.e. the TOA is relative to 1st sensor (which is set to zero).

+ Utilizes TDOA information between all sensors



Time of Arrival (TOA) – 3rd

- Kalman filtering based TOA estimation

$$\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{q}_t, \quad (\text{state eq.})$$

$$\mathbf{y}_t = \mathbf{H}_0\mathbf{x}_t + \mathbf{r}_t, \quad (\text{measurement eq.})$$

– \mathbf{x} consists of TOA and TOA velocity, $\mathbf{x} = \begin{bmatrix} \tau \\ \dot{\tau} \end{bmatrix}$

– \mathbf{A} is transition matrix, \mathbf{q} , \mathbf{r} are noise

– Predict $p(\mathbf{x}_t|\mathbf{y}_{t-1})$ and update $p(\mathbf{x}_t|\mathbf{y}_t)$ steps.

– Outlier rejection based on projected measurement likelihood $p(\mathbf{y}_t|\mathbf{x}_t, \text{target present}) = N(\mathbf{y}_t|\mathbf{H}\mathbf{x}_t, \mathbf{R})$

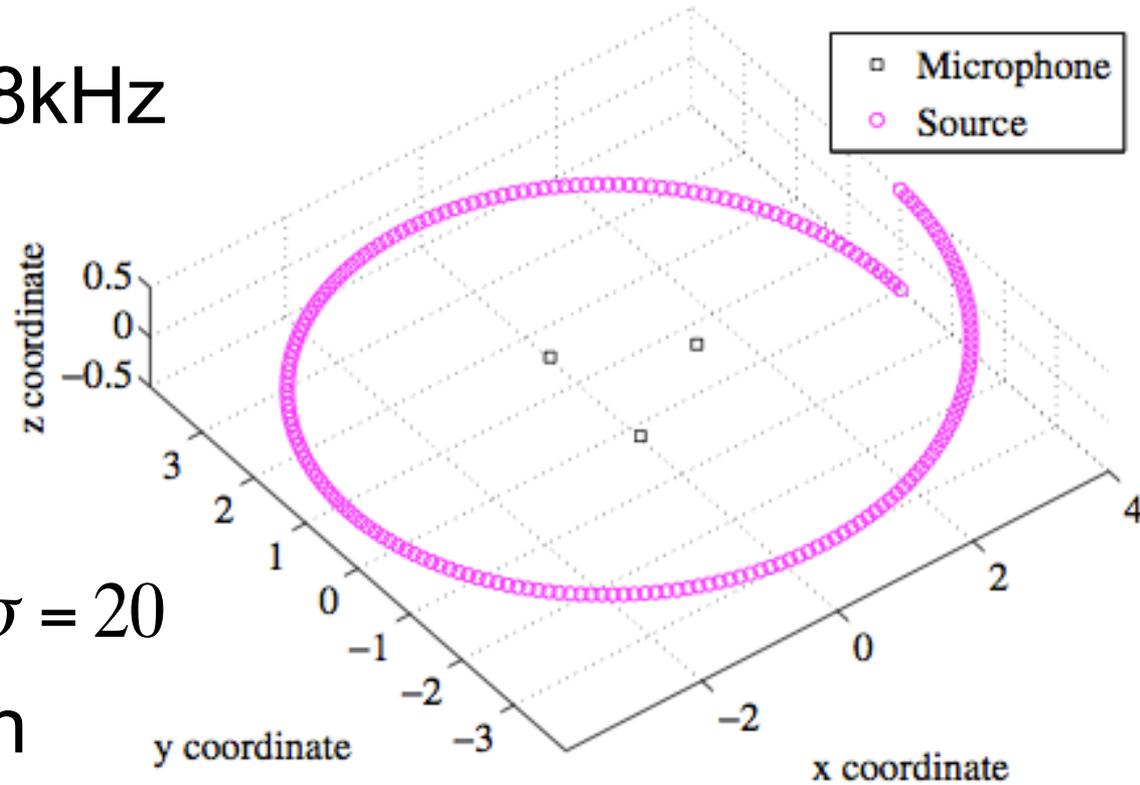
+ Utilizes TDOA information between all pairs

+ Can track speaker during noise contaminated segments.



TOA Estimation simulation

- 3 microphones 48kHz
- Source rotates around the array
- Gaussian noise added to TDOA observations τ_{ij} , $\sigma = 20$
- Gaussian noise in offset values Δ_i , $\sigma^2 = 10$

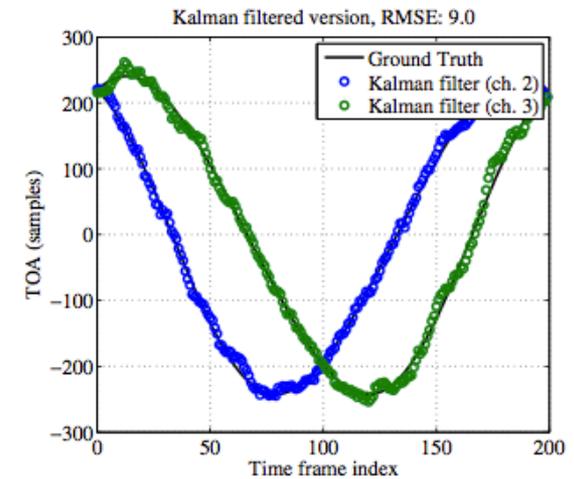
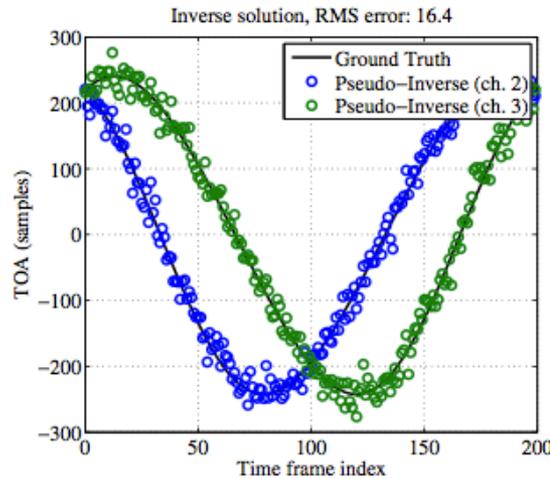
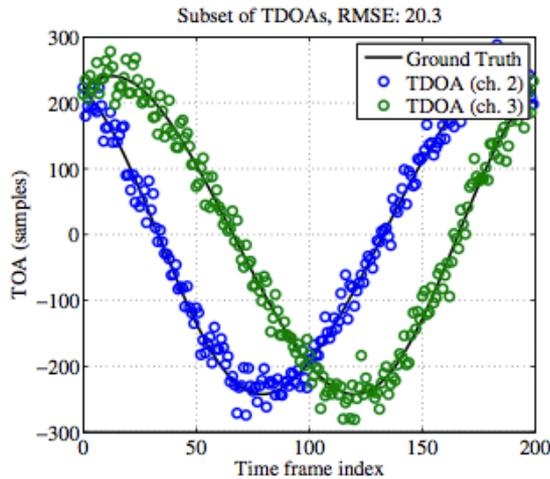


Simulation – TOA accuracy

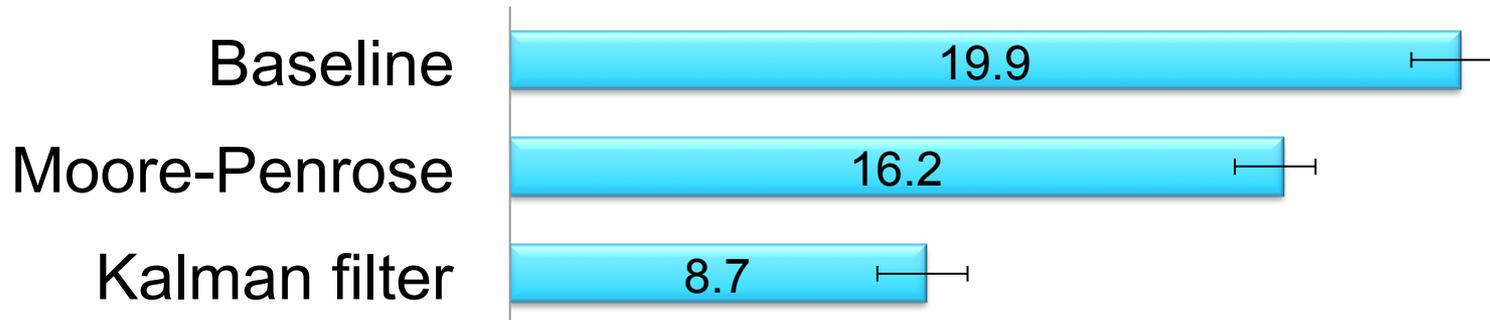
Baseline (subset of TDOAs)

Moore-Penrose Inverse

Kalman filter



TOA RMS error (samples@48k, 100 trials)

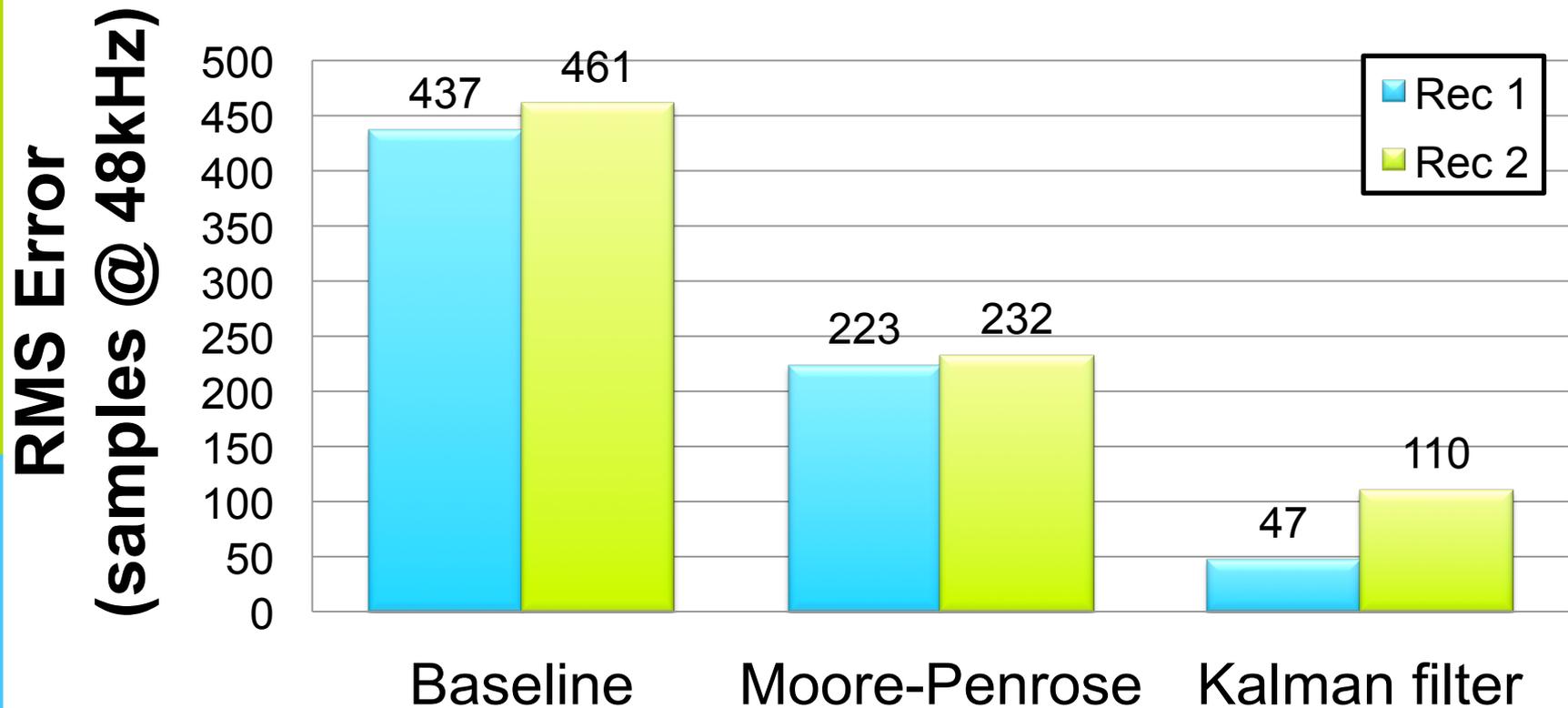


Measurements

- 10 smartphones were used to capture audio
- 9 and 12 second sentences were used
 - Speaker walked around the array
- Reverberation time $T_{60} \sim 370$ ms
- Room size: $5.1\text{m} \times 6.6\text{m}$
- TDOAs were manually annotated to obtain ground truth TOA.
- Reference signal was captured with headworn microphones.



Performance of TOA estimators in measurements



Obtained beamforming quality

- We used estimated TOAs to steer DSB
- Output $y(t)$ quality was evaluated with BSS-metric “Signal-to-Artifacts-Ratio” or SAR*)

$$\text{SAR} = 20 \log_{10} \left(\frac{\|s_{\text{target}}\|}{\|e_{\text{artifacts}}\|} \right)$$

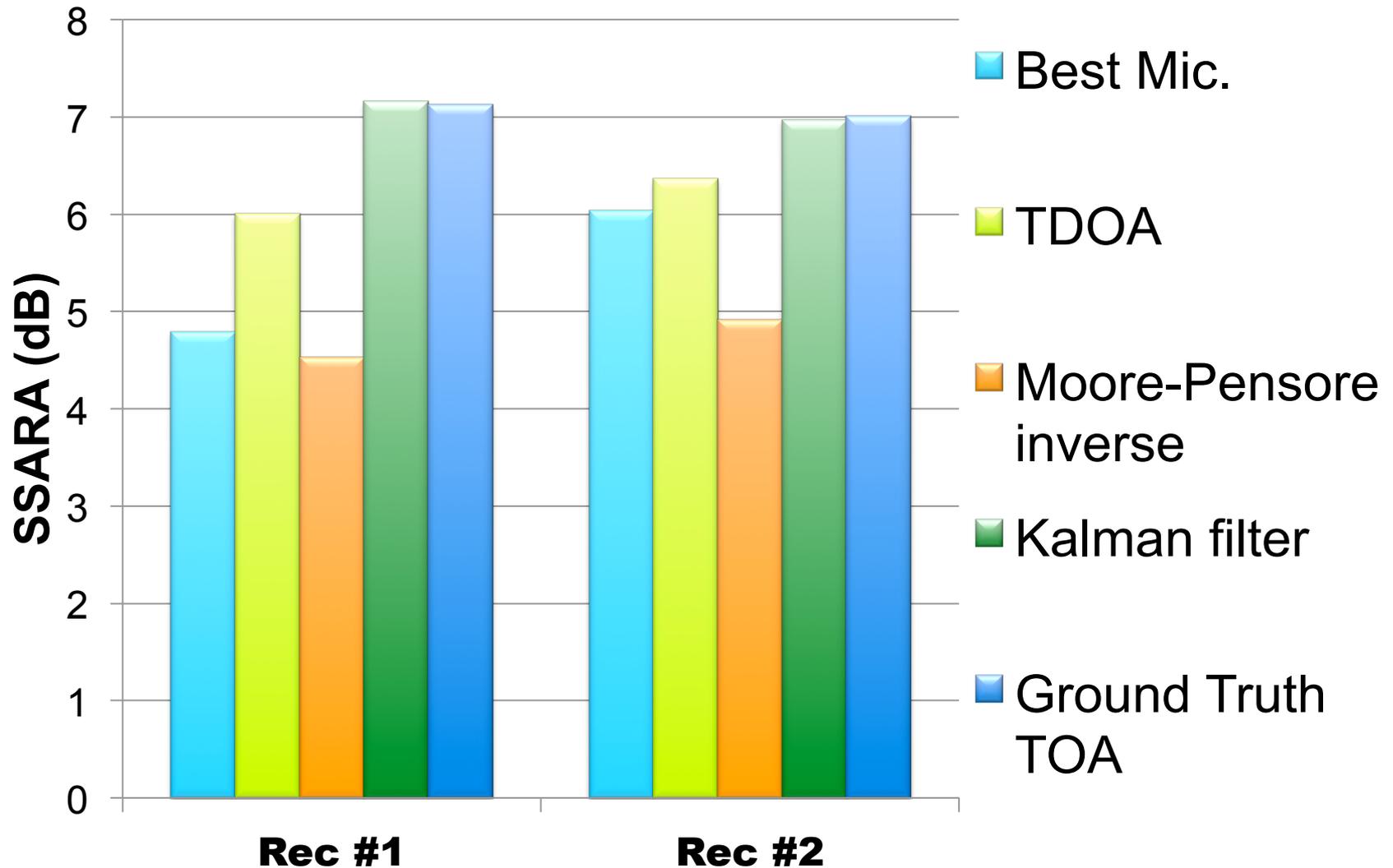
$$y(t) = s_{\text{target}}(t) + e_{\text{artifacts}}(t)$$

- Scored in segments due to speaker movement (gain variation)
- Only active segments considered (with VAD)
- Modified metric: Segmental Signal-to-Artifacts Ratio Arithmetic mean (SSARA)

*) http://bass-db.gforge.inria.fr/bss_eval/



Objective speech quality



Conclusions

- Proposed TOA as the spatial source information of an ad-hoc microphone array
 - Previous research only considered TDOA
 - Dimension of TOA is $M-1$, for TDOA $M(M-1)/2$
- Three TOA estimation solutions considered
 - TDOA subset (baseline), pseudo-inverse, and Kalman filtering → most accurate
- TOA allows beam-steering towards source
 - w/o mic. positions / synchronization: blindly
 - Kalman filter based TOA provided best objective signal quality for beamforming

