Intra-View and Inter-View Supervised Correlation Analysis for Multi-View Feature Learning

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Abstract
Multi-view feature learning is an attractive research topic with great practical success. Canonical correlation analysis (CCA) has become an important technique in multi-view learning, since it can fully utilize the inter-view correlation. In this paper, we mainly study the CCA based multi-view supervised feature learning technique where the labels of training samples are known. Several supervised CCA based multi-view methods have been presented, which focus on investigating the supervised correlation across different views. However, they take no account of the intra-view correlation between samples. Researchers have also introduced the discriminant analysis technique into multi-view feature learning, such as multi-view discriminant analysis (MvDA). But they ignore the canonical correlation within each view and between all views. In this paper, we propose a novel multi-view feature learning approach based on intra-view and inter-view supervised correlation analysis (I²SCA), which can explore the useful correlation information of samples within each view and between all views. The objective function of I²SCA is designed to simultaneously extract the discriminatingly correlated features from both inter-view and intra-view. It can obtain an analytical solution without iterative calculation. And we provide a kernelized extension of I²SCA to tackle the linearly inseparable problem in the original feature space. Four widely-used datasets are employed as test data. Experimental results demonstrate that our proposed approaches outperform several representative multi-view supervised feature learning methods.

Introduction
In real world applications, datasets are usually described with different views or representations. Multi-view feature learning refers to learning with multiple feature sets that reflect different characteristics or views of data, which is an vital research direction (Guo, 2013; Xu, Tao and Xu 2013; Wang, Nie and Huang 2013; Memisevic 2012; Wang, Li, and Ogihara 2012). Co-training and canonical correlation analysis are two representative and effective techniques in multi-view learning (Sun and Chao 2013). Co-training based methods (Kumar and Daume 2011a; Kumar and Daume 2011) are usually used for semi-supervised classification that combines both labeled and unlabeled data under multi-view setting. Canonical correlation analysis (CCA, Hardoon, Szedmak, and Shawe-Taylor 2004) has become an important technique in multi-view learning, since it can fully utilize the inter-view correlation. Multi-view CCA (MCCA, Rupnik and Shawe-Taylor 2010) is an unsupervised method. In this paper, we mainly study the CCA based multi-view supervised feature learning technique where the labels of training samples are known.

Recently, several supervised CCA based multi-view feature learning methods have been presented, such as multiple discriminant CCA (MDCCA, Gao et al. 2012), multiple principal angles (MPA, Su et al. 2012). These methods focus on investigating supervised correlation across different views. To deal with the linearly inseparable problem, researchers extend CCA to be kernel CCA (Sun et al. 2007; Leurgans, Moyeed, and Silverman 1993; Lai and Fyfe 2000; Bach and Jordan 2002). All methods mentioned above only reveal the linear or nonlinear correlation relationship between features of multiple views. However, they take no account of the intra-view correlation between samples, which is also an important part when exploiting supervised correlation among the samples. Therefore, in this paper, we need to simultaneously extract the discriminatingly correlated features from both inter-view and intra-view. The
effectiveness of the intra-view correlation samples can be further visualized in Fig. 1. As suggested in Figure 1, intra-view correlation "glues" intra-class samples better than inter-view correlation. Hence, their combination is able to further uncovered more discriminative information.

Researchers have also presented some discriminant analysis based multi-view feature learning methods, such as generalized multi-view analysis (GMA, Sharma et al. 2012), kernelized GMA (KGMA) and the multi-view fisher discriminant analysis (MFDA) (Diethe, Hardoon, and Shawe-Taylor 2008). MFDA also has a sparse version, that is, the SMFDA (Diethe, Hardoon, and Shawe-Taylor 2010). Moreover, Kan et al. (2012) presented a Multi-view discriminant analysis (MvDA) method, which can maximize the between-class variations and minimize the within-class variations of the learning common space from both intra-view and inter-view. Nevertheless, these methods ignore canonical correlation information from both intra-view and inter-view, which depicts the relationship among multiple views. Hence, we may improve the multi-view feature learning results if the discriminant correlation information among multiple views can be exploited.

For current multiview supervised feature learning methods, there is still room for further improvements. We summarize the contributions of this paper as following points:

(1) We propose a novel multi-view feature learning approach based on intra-view and inter-view supervised correlation analysis (I2SCA). It can explore the useful correlation information of samples within each view and between all views. The idea of the proposed approach is illustrated in Fig. 1.

(2) The objective function of I2SCA is designed to make the within-class correlation from both inter-view and intra-view maximized, while make the between-class correlation from both inter-view and intra-view minimized. Moreover, our approach can obtain an analytical solution without iterative calculation.

(3) We provide a kernelized extension of I2SCA, that is, KI2SCA, to tackle the linearly inseparable problem in the original feature space.

The rest of this paper is organized as follows. In Section 2, we introduce the related works. In Section 3, we describe the proposed I2SCA approach and its kernelized extension. Experimental results and analysis are provided in Section 4, and conclusion is drawn in Section 5.

Related work

CCA based Multi-view Feature Learning Methods

CCA finds linear combinations corresponding to two views, such that all transformed variables own maximum correlation. It cannot be directly applied to multi-view data, which leads to the formulation of multi-view CCA (MCCA, Rupnik and Shawe-Taylor 2010). It tends to obtain high correlations between all new variables simultaneously by optimizing the characteristics of the dispersion matrix of new variables. Multiset integrated CCA (MICCA, Yuan et al. 2010) describes an integrated correlation among multi-view variables based on generalized correlation coefficient. However, these methods are all unsupervised.

In order to utilize the supervised correlation across different views, supervised CCA methods were developed. Discriminant analysis of canonical correlations (DCC, Kim, Kittler, and Cipolla 2007) maximizes the within-class correlation and minimizes the between-class correlation for two sets of variables. Multiple discriminant CCA (MDCCA, Gao et al. 2012) was designed for multiple views, which demonstrates that CCA, MCCA and DCC are special cases of the DMCCA method. Multiple principal angles (MPA, Su et al. 2012) iteratively learns the view-specific projection transformations by following the traditional Fisher discriminant manner, and learns a global discriminative subspace on which the principal angles among multiple subspaces of same classes are minimized while those of different classes are maximized. The nonlinear extension of DCC, namely kernelized discriminative canonical correlation analysis (KDCCA,
Sun et al. 2007), was presented to deal with linearly inseparable problem.

**Discriminant Analysis based Multi-view Feature Learning Methods**

Linear discriminant analysis (LDA, Belhumeur, Hespanha, and Kriegman 1997) technique is widely used in feature learning, which employs the famous Fisher criterion to minimize the within-class scatter while maximize the between-class scatter. To obtain multi-view counterparts of LDA and other feature learning methods, a generalized multi-view analysis (GMA, Sharma et al. 2012) framework was developed, and kernelized GMA (KGMA) was also given. Multi-view Fisher Discriminant Analysis (MFDA) (Diethe, Hardoon, and Shawe-Taylor 2008) learns the classifiers by making the predicted labels of these classifiers consistent with their real label. However, MFDA can only be applied for binary class problems. To address this problem, Chen and Sun (2009) extended MFDA to a multi-class form by using a hierarchical clustering technique. By incorporating multiple views of data in a perceptive transfer learning framework, Yang and Gao (2013) presented the multi-view discriminant transfer learning method. Moreover, Kan et al. (2012) presented a Multi-view Fisher Discriminant analysis (MvDA) method, which can maximize the between-class variations and minimize the within-class variations of the learning common space from both intra-view and inter-view. MvDA is able to jointly acquire projection transforms by solving a generalized Rayleigh quotient.

**Approach Description**

Suppose that there are $N$ views. Notation usage is provided in a summary as follows:

- $X_i$: Sample set of the $i^{th}$ view;
- $n$: Number of samples from each view;
- $c_i$: Number of classes in each view;
- $n_j$: Number of samples from the $j^{th}$ class in each view;
- $N$: Number of views;
- $x_{ij}^k$: The $k^{th}$ sample from the $j^{th}$ class in $X_i$;
- $\bar{x}^i$: Mean of all samples from $X_i$;
- $\hat{x}_i$: Mean-normalized $X_i$, where $x_{ij}^k$ is normalized by using $\hat{x}_{ij}^k = x_{ij}^k - \bar{x}$;
- $S_i^b$: Between-class scatter matrix of $X_i$;
- $S_i^w$: Total scatter matrix of $X_i$;
- $C_i^w$: Between-class correlation between features of $X_i$ and $X_j$;
- $C_i^s$: Within-class correlation between features of $X_i$ and $X_j$;
- $w_i$: Projective vector of $X_i$;
- $W_i$: Projective transformation of $X_i$, where $W_i$ consists of $d$ projective vectors;
- $Z_i$: Projected features of samples set of the $i^{th}$ view $X_i$.

**Intra-view Supervised Correlation Analysis**

Let $E_s = [1, \cdots, 1]^T$, and $A = \text{diag} (E_w, E_w, \cdots, E_w)$ denote a $n \times n$ symmetric, positive semi-definite, blocked diagonal matrix, where $E_w$ is a $n_i \times n_i$ matrix with all its elements equal to 1. Assume that $C_i^w$ and $C_i^s$ denote the within-class correlation and between-class correlation of samples of the $i^{th}$ view, respectively. Their definitions are given as follows:

$$C_i^w = \frac{\left\{ \sum_{j=1}^{c_i} n_j \sum_{i=1}^{n_j} \sum_{i=1}^{n_j} w_i (x_{ij}^k - \bar{x}_i) (x_{ij}^l - \bar{x}_i) \right\} w_i}{\left\{ \sum_{j=1}^{c_i} n_j \sum_{i=1}^{n_j} \sum_{i=1}^{n_j} w_i (x_{ij}^k - \bar{x}_i)^2 \right\}^{1/2} \left\{ \sum_{j=1}^{c_i} n_j \sum_{i=1}^{n_j} \sum_{i=1}^{n_j} w_i (x_{ij}^l - \bar{x}_i)^2 \right\}^{1/2}}$$

$$C_i^s = \frac{\left\{ \sum_{j=1}^{c_i} n_j \sum_{i=1}^{n_j} \sum_{i=1}^{n_j} w_i (x_{ij}^k - \bar{x}_i) (x_{ij}^l - \bar{x}_i) \right\} w_i}{\left\{ \sum_{j=1}^{c_i} n_j \sum_{i=1}^{n_j} \sum_{i=1}^{n_j} w_i (x_{ij}^k - \bar{x}_i)^2 \right\}^{1/2} \left\{ \sum_{j=1}^{c_i} n_j \sum_{i=1}^{n_j} \sum_{i=1}^{n_j} w_i (x_{ij}^l - \bar{x}_i)^2 \right\}^{1/2}}.$$

The supervised correlation between samples of the $i^{th}$ view is thus defined as:

$$C_i^s = C_i^w - \alpha C_i^s$$

$$= \frac{n}{\sum_{j=1}^{c_i} n_j - n \alpha} \left( \sum_{j=1}^{c_i} n_j w_i \bar{x}_i \right) - \frac{n}{\sum_{j=1}^{c_i} n_j} \left( \sum_{j=1}^{c_i} n_j w_i \bar{x}_i \right).$$

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where $\alpha > 0$ is a tunable parameter that indicates the relative significance of the within-class correlation of intra-view $C_w^i$ versus the between-class correlation of intra-view $C_w^i$. For intra-view supervised correlation analysis, we design the following objective function:

$$
\max_{w_i, i=1,2,\cdots, N} \sum_{i=1}^{N} C^i.
$$

(4)

The goal of Formula (4) is to preserve the useful within-class correlation from each view and eliminate the adverse between-class correlation from each view, which is favorable for classification.

**Inter-view Supervised Correlation Analysis**

Similarly, we define the within-class correlation $C^i_w$ and between-class correlation $C^b_w$ between the samples of the $i$th and $j$th views as follows:

$$
C^i_w = \frac{1}{n^i} \sum_{j=1}^{n^i} \sum_{j'=1}^{n^i} w^i_j X_{ij}^w X_{ij'}^w,
$$

(5)

and

$$
C^b_w = \frac{1}{n^i} \sum_{j=1}^{n^i} \sum_{j'=1}^{n^i} w^i_j X_{ij}^w X_{ij'}^w - \frac{1}{n^i} \sum_{j=1}^{n^i} \sum_{j'=1}^{n^i} w^i_j X_{ij}^w \frac{1}{n^i} \sum_{j=1}^{n^i} X_{ij}^w.
$$

(6)

The supervised correlation between the samples of the $i$th and $j$th views is defined as:

$$
C^i = C^i_w - \beta C^b_w.
$$

(7)

where $\beta > 0$ is a tunable parameter that indicates the relative significance of the within-class correlation of inter-view $C^i_w$ versus the between-class correlation of inter-view $C^b_w$. Note that $C^i_j = C^j_i$.

For inter-view supervised correlation analysis, we design the following objective function:

$$
\max_{w_p, p=1,2,\cdots, N} \sum_{p=1}^{N} C^p + \beta \sum_{p=1}^{N} \sum_{q=1}^{p} C^{pq}.
$$

(9)

which is equivalent to

$$
\max_{w_p, p=1,2,\cdots, N} \xi_p \sum_{p=1}^{N} \sum_{q=1}^{p} w^p_j X_{ij}^p X_{ij'}^p + \xi_p \sum_{p=1}^{N} w^p_j X_{ij}^p X_{ij'}^p w_p
$$

s.t. $w^p_j X_{ij}^p w_p = 1, p=1,2,\cdots, N
$

(10)

where

$$
q = \frac{1}{n^i} \sum_{j=1}^{n^i} \sum_{j'=1}^{n^i} w^i_j X_{ij}^w X_{ij'}^w,
$$

(11)

and

$$
C^{pq} = \frac{1}{n^i} \sum_{j=1}^{n^i} \sum_{j'=1}^{n^i} w^i_j X_{ij}^w X_{ij'}^w.
$$

(12)

To tackle the linearly inseparable problem, I²SCA can be extended by using kernel method to work in a nonlinear space:

**Kernel I²SCA**

To effectively make full use of correlation information within each view and between different views, we combine intra-view and inter-view supervised correlation analysis, and design the following I²SCA scheme:

$$
\max_{w_p, p=1,2,\cdots, N} \sum_{p=1}^{N} C^p + \beta \sum_{p=1}^{N} \sum_{q=1}^{p} C^{pq}.
$$

(13)

Once the eigenvectors $w^k (k=1,2,\cdots,d)$ associated with the first $d$ largest eigenvalues of $F^T G F$ are obtained, we can get $w^k_1, w^k_2, \cdots, w^k_d$ from $w^k$. Let $W = [w^1, w^2, \cdots, w^d]$, where $j=1,2,\cdots, N$. Then we can obtain the projected features $Z_i$ by $Z_i = W_i^T X_i$, where $i=1,2,\cdots, N$, and fuse these features as follows:

$$
Z = [Z_1, Z_2, \cdots, Z_N]^T.
$$

(14)
feature space instead of the original input space. Kernel trick has shown its effectiveness in many methods, including some kernel CCA methods (Sun et al. 2007; Leurgans, Moyeed, and Silverman 1993; Lai and Fyfe 2000; Bach and Jordan 2002). We first perform the kernel mapping for samples and then realize the $I^2$SCA in the mapped space to obtain projection transformation. Suppose there are $N$ implicit mappings $\phi_i, i = 1, 2, ..., N$, the samples mapped to the corresponding spaces are denoted by $\phi(X) = \begin{bmatrix} \phi(x_1), ..., \phi(x_N) \end{bmatrix}$. Thus, the mapped multi-view data is $\{\phi(X_1), ..., \phi(X_N)\}$. According to the kernelized method in (Sun et al. 2007), the basis vector pair can be represented as $w_i = \phi(X_i)\alpha$, where $\alpha, \beta \in R^n$ denote the corresponding combination coefficient vectors. Note that the kernel trick has shown its effectiveness in many methods, including some kernel CCA methods (Su et al. 2007; Leurgans, Moyeed, and Silverman 1993; Lai and Fyfe 2000; Bach and Jordan 2002). We first perform the kernel trick and kernel I2SCA can be reformulated as

$$\max_{w_i, i = 1, 2, ..., N} \xi_1 \sum_{p=1}^{n} \alpha_p^{T} K_{x_i} \alpha_p + \xi_2 \sum_{i,j=1}^{N} \alpha_i^{T} K_{x_i} \alpha_j$$

$$\text{s.t.} \quad \sum_{j=1}^{N} K_{x_i} \alpha_j = 1, \quad \forall i = 1, 2, ..., N$$

(15)

where

$$\xi_1 = \frac{1}{n^2 - \sum_{i=1}^{n} n_i^2}, \quad \xi_2 = \frac{1}{\sum_{i=1}^{n} n_i^2}$$

$K_{x_i} = \phi(x_i)^T \phi(x_i) = k_i(x_i, x_i^T)$

$p = 1, ..., n, q = 1, ..., n$ . Substituting $w_i = \phi(X_i)\alpha$ into Formula (9), we employ the kernel trick and kernel I2SCA can be formulated as

$$\max_{w_i, i = 1, 2, ..., N} \xi_1 \sum_{p=1}^{n} \alpha_p^{T} K_{x_i} \alpha_p + \xi_2 \sum_{i,j=1}^{N} \alpha_i^{T} K_{x_i} \alpha_j$$

$$\text{s.t.} \quad \sum_{j=1}^{N} K_{x_i} \alpha_j = N, i = 1, 2, ..., N$$

(16)

Similar to $I^2$SCA, Formula (16) can also be written as a generalized eigenvalue problem. Its solution can be solved by reference to Section 3.3.

It is noticed that in the experiments, the tunable parameters $\alpha$ and $\beta$ are selected with 5-fold cross validation on the training set.

**Experiments**

In this section, we evaluate the proposed approaches with several related multi-view supervised feature learning methods including MDCCA (Gao et al. 2012), MPA (Su et al. 2012), MvDA (Kan et al. 2012) and KGMA (Sharma et al. 2012) on four public datasets. Note that KGMA refers to the kernel GMA, which outperforms GMA.

**Recognition Performance Evaluation**

**Experiment on Multiple Feature Dataset**

The multiple feature dataset (MFD) (Yuan et al. 2010) contains 10 classes of handwritten numerals, i.e. 10 numbers from 0 to 9. These digit characters are represented in terms of the next six feature sets, as shown in Table 1. There are 200 samples per class (for a total of 2000 samples) in each feature sets.

<table>
<thead>
<tr>
<th>Method</th>
<th>MDCCA</th>
<th>MPA</th>
<th>MvDA</th>
<th>KGMA</th>
<th>I$^2$SCA</th>
<th>KI$^2$SCA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Result</td>
<td>95.52</td>
<td>94.87</td>
<td>95.53</td>
<td>95.64</td>
<td>96.67</td>
<td>97.57</td>
</tr>
</tbody>
</table>

From Table 2, we observe that $I^2$SCA improves the average recognition rate at least by 1.03% (=96.67-95.64), and K$^2$SCA improves the average rate at least by 1.93% (=97.57-96.64) as compared with other methods. Here, to elaborate more about the improvements of our approach, we use the second digit precision. This made particular sense when data size grows big so that even a small portion of its improvement could gain significant economical concern. We also conduct the second digit precision in the following experiments.

**Experiment on Coil-20 Dataset**

The COIL-20 database (Murase and Nayar 1995) contains 7200 grayscale images of 100 objects (72 images per object) under various poses. Objects are rotated through 360 degrees and taken at the intervals of 5°. The size of each object image is 64×64 pixels.

In this experiment, 36 images per class are randomly chosen to form the training set, while the remaining images are regarded as the testing set. We extract Gabor transformation features (Grigorescu, Petkov and Kruizinga 2002), Karhunen-Loeve transformation features (Fukunaga and Koontz 1970) and Local Binary Patterns features (Ahonen, Hadid, and Pietikainen 2006) to form three sets of features. We perform the principal component analysis (PCA, Belhumeur, Hespanha, and Kriegman 1997) transformation to reduce their dimensions to 150, respectively.
Table 3. Average recognition rates (%) on Coil database

<table>
<thead>
<tr>
<th>Method</th>
<th>MDCCA</th>
<th>MPA</th>
<th>MvDA</th>
<th>KGMA</th>
<th>I²SCA</th>
<th>KI²SCA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Result</td>
<td>95.53</td>
<td>95.05</td>
<td>96.07</td>
<td>96.71</td>
<td>98.28</td>
<td>98.87</td>
</tr>
</tbody>
</table>

Table 3 shows that I²SCA improves the average recognition rate at least by 1.57% (= 98.28-96.71), and KI²SCA improves the average rate at least by 2.16% (= 98.87-96.71) as compared with other methods.

Experiments on Multi-PIE Dataset

Multi-PIE dataset (Cai et al. 2006) contains more than 750,000 images of 337 people under various views, illumination and expressions (PIE). Here, a subset about 1632 samples from 68 classes in 5 poses (C05, C07, C09, C27, C29) is selected as test data. All images from Multi-PIE are 64×64 pixels. We perform PCA transformation to reduce their dimensions to 150, respectively.

Regular Face Recognition Experiment. We randomly choose 8 samples per class as the training samples, while the remaining samples are regarded as the testing set. Thus, the total number of training samples and testing samples is 544 and 1088, respectively. Table 4 shows the average recognition rates of all compared methods across of 20 random runs for all compared methods on Multi-PIE dataset.

Table 4 shows that I²SCA and KI²SCA perform better in contrast with other related methods, which improve the average recognition rate at least by 1.09% (=97.54-96.45) and 1.78% (=98.03-96.45), respectively.

Table 5 shows that both I²SCA and KI²SCA perform better in the comparison with the other methods. I²SCA improves the average recognition rate at least by 1.18% (= 89.57-88.39) and KI²SCA improves the average recognition rate at least by 1.93% (= 90.32-88.39).

Further Experimental Analysis

Distribution of Samples

In order to analyze the separabilities of all methods, we provide the distribution of samples with two principal features extracted from 5 different views by using all related methods on Multi-PIE dataset. Here, we employ the PCA transform to obtain two principal features. Fig. 2 shows the distribution of two principal features of 20 samples (from 5 different persons and 4 samples per person) extracted from the compared methods on the Multi-PIE dataset, where the markers (*, ⋆, ○, □, and ▽) with different colors stand for 5 different persons. In Fig. 2, the red oval ring indicates the bad separability, which might lead to misclassification. Fig. 2 shows that the
proposed approaches achieve preferable separabilities in comparison with other methods.

![Sample distributions of PIE dataset of 20 samples (5 different palms and 4 samples per palm) in the feature space. Here, the markers (*, ⤵, □, and ▽) with different colors stand for 5 different classes.](image)

**Statistical Significance**

To statistically analyze the recognition results given in Table 2-4, we conduct a statistical test, i.e., McNemar’s test (Draper, Yambor, and Beveridge 2006). This test can provide statistical significance between our proposed approaches and other methods. Here, the McNemar’s test uses a significance level of 0.05, that is, if the p-value is below 0.05, the performance difference between two compared methods is considered to be statistically significant. Table 9 shows the p-values between I²SCA and other compared methods on Multiple Feature Dataset, Coil-20 Dataset and Multi-PIE dataset. And Table 10 shown the p-values between KI²SCA and other compared methods on four datasets we utilized.

<table>
<thead>
<tr>
<th>Datasets</th>
<th>MDCCA</th>
<th>MPA</th>
<th>MvDA</th>
<th>KGMA</th>
</tr>
</thead>
<tbody>
<tr>
<td>MFD</td>
<td>1.32×10^{-8}</td>
<td>2.52×10^{-10}</td>
<td>3.29×10^{-10}</td>
<td>6.12×10^{-10}</td>
</tr>
<tr>
<td>Coil-20 Dataset</td>
<td>2.46×10^{-7}</td>
<td>2.47×10^{-6}</td>
<td>5.33×10^{-16}</td>
<td>7.58×10^{-24}</td>
</tr>
<tr>
<td>Multi-PIE Dataset</td>
<td>5.17×10^{-8}</td>
<td>1.59×10^{-8}</td>
<td>4.52×10^{-9}</td>
<td>2.42×10^{-10}</td>
</tr>
<tr>
<td>LFW Dataset</td>
<td>4.59×10^{-8}</td>
<td>1.38×10^{-8}</td>
<td>4.46×10^{-9}</td>
<td>2.91×10^{-10}</td>
</tr>
</tbody>
</table>

The two above tables show that the p-values of both I²SCA and KI²SCA are much less than 0.05, which demonstrated the statistical significance of our approaches.

**Conclusion**

In this paper, we propose a novel multi-view feature learning approach called intra-view and inter-view supervised correlation analysis (I²SCA). It can fully explore the useful correlation information from both intra-view and inter-view. The objective function of I²SCA can maximize the within-class correlation from both inter-view and intra-view, and simultaneously minimize the between-class correlation from both inter-view and intra-view. We provide a kernelized extension of I²SCA, that is, kernel I²SCA (KI²SCA). The proposed approaches can obtain the analytical solutions without iterative calculation.

We employ the widely-used multiple feature dataset (MFD), COIL-20 dataset, Multi-PIE dataset and LFW dataset as the test data. As compared with several state-of-the-art multi-view supervised feature learning methods, our approaches achieve better recognition results. Besides, the demos of sample distributions in the feature space illustrate that the features learned by our approaches have better separability than that learned by other methods.

**Acknowledgements**

The work described in this paper was supported by the National Nature Science Foundation of China under Project Nos. 61231015, 61172173, 61272273 and 6123011, the Major Science and Technology Innovation Plan of Hubei Province (No. 2013AAA020), the Guangdong-Hongkong Key Domain Breakthrough Project of China (No. 2012A090200007), 333 Engineering of Jiangsu Province under Project No. BRA2011175.

**References**


Bellumuru, P. N.; Hespanha, J. P.; and Kriegman, D. 1997. Eigenfaces vs. fisherfaces: Recognition using class specific linear


