Electric-Field Dependence of the Effective Dielectric Constant in Graphene

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ABSTRACT: The dielectric constant of a material is one of the fundamental features used to characterize its electrostatic properties such as capacitance, charge screening, and energy storage capability. Graphene is a material with unique behavior due to its gapless electronic structure and linear dispersion near the Fermi level, which can lead to a tunable band gap in bilayer and trilayer graphene, a superconducting-insulating transition in hybrid systems driven by electric fields, and gate-controlled surface plasmons. All of these results suggest a strong interplay between graphene properties and external electric fields. Here we address the issue of the effective dielectric constant (ε) in N-layer graphene subjected to out-of-plane (E⊥) and in-plane (E∥) external electric fields. The value of ε has attracted interest due to contradictory reports from theoretical and experimental studies. Through extensive first-principles electronic structure calculations, including van der Waals interactions, we show that both the out-of-plane (ε⊥) and the in-plane (ε∥) dielectric constants depend on the value of applied field. For example, ε∥ and ε⊥ are nearly constant (∼3 and ∼1.8, respectively) at low fields (Eext < 0.01 V/Å) but increase at higher fields to values that are dependent on the system size. The increase of the external field perpendicular to the graphene layers beyond a critical value can drive the system to an unstable state where the graphene layers are decoupled and can be easily separated. The observed dependence of ε⊥ and ε∥ on the external field is due to charge polarization driven by the bias. Our results point to a promising way of understanding and controlling the screening properties of few-layer graphene through external electric fields.

KEYWORDS: Graphene dielectric constant, multilayer graphene screening, tunable dielectric properties, electrostatic exfoliation, dielectric response

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electron-electron interactions play a central role in a wide range of electronic phenomena in graphene-based materials,1−9 from the reshaping of the Dirac cone10−12 in suspended graphene to observations of plasmaron quasiparticles13—bound states of charge carriers with plasmons—in doped layers. One of the main ingredients that determines the Coulomb interaction strength in those systems is screening, which can be characterized by graphene’s dielectric constant (ε). In fact, the large range of values for ε found by different experiments10−18 (from 2 to 15) has become a subject of considerable debate. The presence of substrates has likely played a role in the experimental attempts to measure the intrinsic dielectric constant in graphene as, for instance, was recently shown by angle-resolved photoemission spectroscopy (ARPES) experiments.12 In practical terms the effective dielectric constant is defined by ε = (εsub + εvac)/2, with εsub and εvac the dielectric constant values for the substrate and vacuum, respectively. However, using this approach requires the detailed knowledge of the dielectric constant of the environment in which graphene is embedded, which is not always accessible. The determination of the intrinsic value of ε is therefore of great interest and importance. Here we find that ε is electric-field dependent, with values in the range 3−16. We applied a spatially periodic sawtooth-like potential perpendicular (E⊥) or parallel (E∥) to the graphene layer which simulates the external field across the supercell. In the case of E⊥, armchair nanoribbons of different width were utilized to create structures with periodic boundary conditions. The value of ε can be obtained by using εi = Eext/Eiext = 1 + 4 πχ', with i = ⊥,∥, where Eiext is the net electric field in the slab or along the ribbon surface, and χ’ is the electric susceptibility (see details in Methods). The effective electric field either between the C-layers (E⊥) or along the ribbon width (E∥) is not constant, as discussed below.

Figure 1 displays how ε⊥ and ε∥ evolve with external fields. For out-of-plane polarization, ε⊥ is almost constant ∼3.0 at low fields Eext < 0.001 V/Å, independent of the number of layers. As Eext is increased, ε⊥ takes larger values reaching ε⊥ = 13.2 at Eext = 1.0 V/Å for N = 10 layers. These values for ε⊥ agree very well with those found by many experimental groups.10−18 Notably,

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monolayer (1L),\textsuperscript{10–14} bilayer (2L),\textsuperscript{15,16} and multilayer graphene or graphite\textsuperscript{17,18} give quite different response to an external electric field: the thicker the structure (more layers) the larger the value of $\epsilon_{\parallel}$, with a linear dependence of $\epsilon_{\parallel}$ on the number of layers $N$ at a fixed value of the field. The electric susceptibility $\chi^\parallel$ extracted from the polarization $P^\parallel$ (Figure 1b) clearly shows this behavior. The in-plane dielectric constant $\epsilon_{\parallel}$ is nearly constant $\sim 1.8$ for small ribbon width ($\leq 1.8$ nm) in the whole range of external fields studied (see Figure 1c). With an increase of the width, $\epsilon_{\parallel}$ goes to higher values as a function of $E^\parallel_{\text{ext}}$ reaching $\epsilon_{\parallel} = 15.5$ at $E^\parallel_{\text{ext}} = 1.0$ V/Å for a width of 18.1 nm. This relation between $\epsilon_{\parallel}$ and the ribbon width is reflected in the linear behavior of the in-plane electric susceptibility $\chi^\parallel$ obtained from the polarization $P^\parallel$ (Figure 1d). This suggests a similar dependence of $\chi^\parallel$ on the transverse ribbon direction as that observed for $\chi^\perp$ on the number of layers $N$. The polarizations $P^\parallel$ and $P^\perp$ are related by approximately a constant factor $\sim 2$. This suggests that graphene behaves differently depending on the field polarization: it acts as a metal along the C-plane and as a semiconductor or semimetal perpendicular to it. This is in close agreement with spectroscopic ellipsometry measurements,\textsuperscript{19} performed with light polarized parallel and perpendicular to the carbon surface.

The origin of the electric-field-mediated tunable dielectric constant in graphene structures is shown schematically in Figure 2. We focus on the response of 2L graphene for out-of-plane field polarization as a simpler picture that can capture the essential features of this problem. The application of $E^\perp_{\text{ext}}$ generates an interlayer charge-transfer which partially cancels the external field, producing the value of $E^\perp_{\text{eff}}$. At low $E^\perp_{\text{ext}}$, all values of $E^\perp_{\text{eff}}$ are approximately constant (within the numerical accuracy of our model). At fields close to those used to modify the band gap of 2L graphene,\textsuperscript{1–3} 0.1 V/Å, $E^\perp_{\text{eff}}$ is already dependent on position, with a maximum at the midpoint between the layers, and smaller values close to the C-atoms (Figure 2a). The induced charge densities, $\Delta \rho^\parallel$, at different fields are shown in Figure 2b. The overall polarization charge is field-dependent and increases in magnitude with the external field intensity as discussed above. The integration of $\Delta \rho^\parallel$ along the direction perpendicular to the layers ($z$ coordinate), using the Poisson equation $\nabla^2 V(z) = -\Delta \rho^\parallel/\epsilon_0$, where $\epsilon_0$ is the vacuum permittivity, results in a response electric field $E^\parallel_{\text{eff}}$ (dashed line in Figure 2b) which screens the external electric field, that is, $E^\parallel_{\text{eff}} \approx E^\parallel_{\text{ext}} - E^\parallel_{\text{p}}$. Similar features are observed for the in-plane polarization. Figure 2c shows $E^\perp_{\text{eff}}$ as function of the position for different values of $E^\perp_{\text{ext}}$. The external field decays as it penetrates along the ribbon which indicates that an effective field $E^\perp_{\text{eff}}$ is created, with a charge accumulation at the positive potential edge and a corresponding depletion at the negative one (Figure 2d). This charge-polarization generates a response field $(E^\parallel_{\text{eff}})$ along the ribbon width that screens the external field (dashed line in Figure 2d) in a similar manner as that observed for out-of-plane polarization.

We address next the dependence of $\epsilon_{\parallel}$ and $\epsilon_{\parallel}$ on the number of graphene layers $N$ and on the ribbon width. In Figure 3 we plot $E^\parallel_{\text{eff}}$ and $E^\perp_{\text{eff}}$ as a function of the position $z$ for $N = 3, 5, 7$ (3a) and different ribbon widths: 3.8, 6.1, 18.1 nm (3b). For out-of-plane polarization, the application of $E^\parallel_{\text{ext}}$ on thicker graphene structures generates higher $E^\parallel_{\text{eff}}$ in the first few layers. For instance, in the $N = 10$ case, the maximum value of $E^\perp_{\text{eff}}$.\textsuperscript{19}
multilayer graphene is the main reason for this behavior. The nonlinear nature of the screening in the innermost regions of the structure which leads to a lower enhancement in the value of the dielectric constant with the number of layers \(N\) is directly related to the reduction of field in the innermost regions of the system. Figure 4 shows the total energy for bilayer graphene. The plate geometry is shown on the background picture. (b) Induced charge densities, \(\Delta \rho = \rho(E_{\text{ext}}) - \rho(0)\), in \(e/\text{Å}^3\), between the two C-planes. The bold and lighter shaded curves correspond to \(E_{\text{ext}}^\parallel = 0.12 \text{ V/Å}\) and \(E_{\text{ext}}^\perp = 1.22 \text{ V/Å}\), respectively. The dashed line curve corresponds to the electric field generated by the induced charge \(E_{\text{eff}}^\parallel\) at \(E_{\text{ext}} = 1.22 \text{ V/Å}\). The large black arrow shows the direction of \(E_{\text{eff}}^\perp\) relative to the bilayer structure. (c) \(E_{\text{eff}}^\parallel\) as a function of the distance along the ribbon width. The ribbon is 6.1 nm wide with armchair edges saturated by H atoms. (d) \(\Delta \rho\) along the ribbon surface for \(E_{\text{ext}}^\parallel = 0.20 \text{ V/Å}\) and \(E_{\text{ext}}^\perp = 2.24 \text{ V/Å}\), with the same legend as in b. The dashed line curve corresponds to \(E_{\text{eff}}^\parallel\) generated by the in-plane polarization charge at \(E_{\text{ext}} = 2.24 \text{ V/Å}\).

Figure 2. (a) \(E_{\text{eff}}^\parallel\) as a function of the interlayer distance at different external fields \(E_{\text{ext}}\) for bilayer graphene. There is a limit on the magnitude of \(E_{\text{eff}}^\parallel\) that can be applied to the system. Figure 4 shows the total energy for bilayer graphene as a function of the interlayer distance. The calculated equilibrium distance \(z_o\) is 3.4 Å. For \(E_{\text{ext}} = 0.0 \text{ V/Å}\), a van der Waals barrier \(E_{\text{vdW}}\) of \(28.1 \text{ meV/C}\) prevents the separation of the two layers from \(z_o\) to infinity. For \(E_{\text{ext}} > 0\) the value of \(E_{\text{vdW}}\) diminishes, indicating that the C-planes become less bound. At \(E_{\text{ext}} = 1.8 \text{ V/Å}\) the two planes of 2L graphene can be easily separated with \(E_{\text{vdW}} = 3.3 \text{ meV/C}\). The existence of a field that can be used to exfoliate graphene was previously observed by experiments to prepattern few-layer graphene onto substrates in integrated circuits. Therefore, \(E_{\text{ext}}\) should be carefully applied to just tune the electronic and screening features, without leading to exfoliation.

To summarize, we have used first-principles electronic structure calculations to demonstrate that the effective dielectric constant in multilayer or single-layer graphene is tunable by an external electric field. The effect we describe may partially explain experimentally observed results that to date had been attributed to unknown interface structure. This electric-field mediated tuning of the dielectric properties provides an additional degree of freedom in the design and modification of graphene-based materials, opening new possibilities for efficient control of electronic device properties.

Methods. The simulations reported here are based on density-functional-theory calculations using the SIESTA code. We have used the nonlocal van der Waals density functional for the exchange-correlation term. We used a double-\(\zeta\) polarized basis and norm-conserving Troullier-Martins pseudopotentials. Atomic coordinates were allowed to relax using a conjugate-gradient algorithm until all forces were smaller in magnitude than 0.01 eV/Å. Relevant lattice constants (in-plane and out-of-plane) were optimized for each system. To avoid interactions between layer images the distance between periodic images of the graphene structures along the direction perpendicular or parallel to the C-atom plane was set at 20 Å. The resolution of the real-space grid used to calculate the Hartree and exchange-correlation contribution to the total energy was chosen to be equivalent to 150 Ry plane-wave cutoff. The number of \(k\)-points was chosen according to the Monkhorst–Pack scheme and was set to the equivalent of a 44 x 44 x 1 grid in the two-atom primitive unit cell of graphene, which gives well converged values for all the calculated properties. We used a Fermi–Dirac distribution with an electronic temperature of \(k_B T = 21 \text{ meV}\).

The values of the induced electric fields along each direction were calculated taking a derivative with respect to the distance of the averaged electrostatic potential \(\langle V_{\text{el}}(r) \rangle\) by finite...
field in the calculation before the self-consistency, d is the thickness of the graphene structure, and c is the total length of the supercell in the direction of the external field. $\chi$ is calculated using $\chi = (1/4\pi)(E_{\text{eff}} = E_{\text{inp}})/(E_{\text{eff}} + E_{\text{inp}} + (1 - d/c))$. This procedure accounts for the creation of compensating dipole moment induced by the application of the external field. $\Delta\rho^{\pm}$ was calculated using a similar procedure, taking the total charge density distribution (ionic plus electronic) as the initial quantity. The polarizations $P^{\pm}$ were calculated by the integration of $\Delta\rho^{\pm}$ through $\nabla \cdot P(r) = -\Delta\rho(r)$ for each field polarization. We use the same procedure as shown in ref 29.

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**Notes**

The authors declare no competing financial interest.

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