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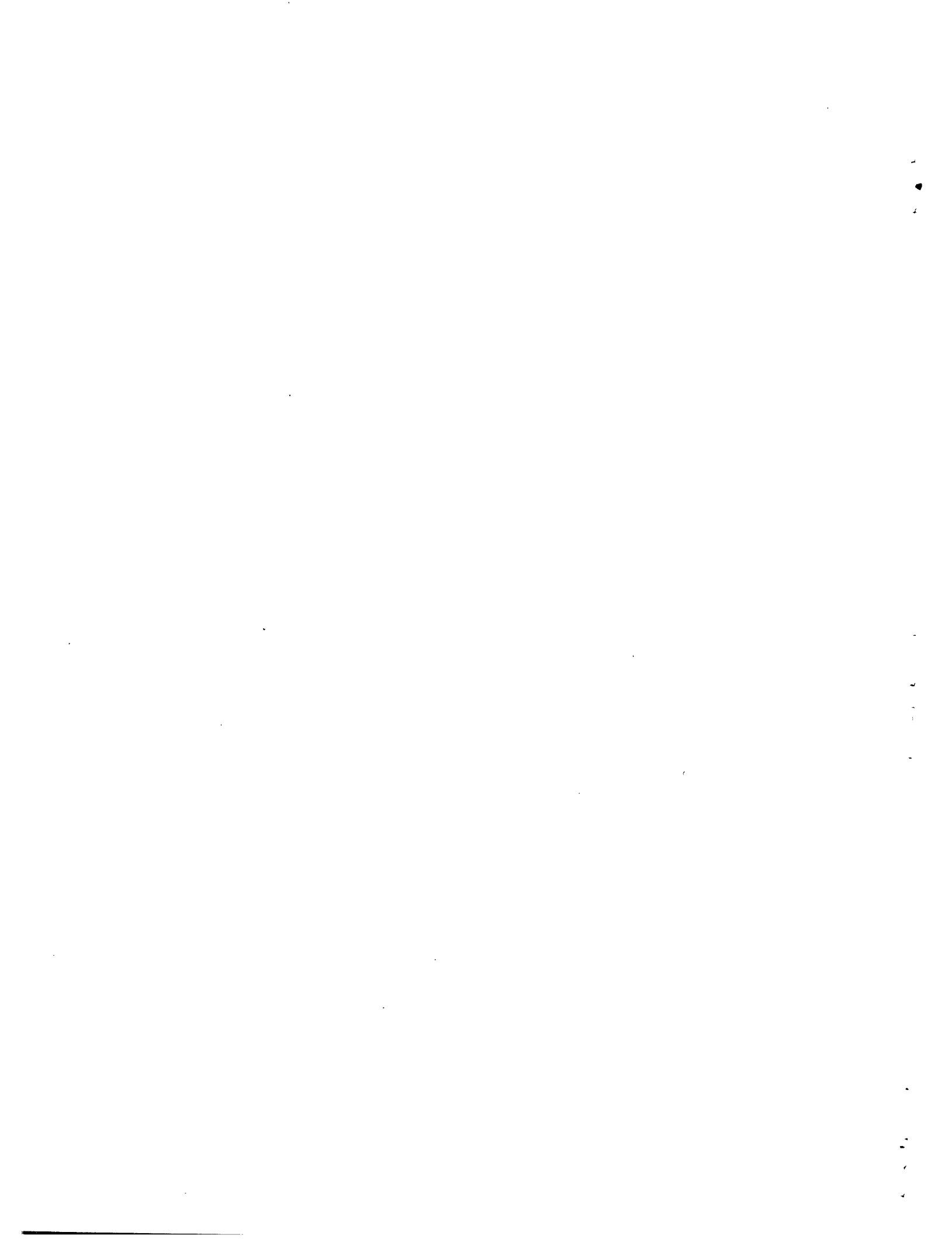
ULTRASONIC VELOCITY AND ABSORPTION IN LIQUID HELIUM

By

John R. Pellam and Charles F. Squire

Abstract

Measurements are given on the velocity and attenuation of ultrasonic energy in liquid helium at a frequency of 15 Mc/sec as a function of temperature from 1.57°K to 4.5°K. The velocity at 15 Mc/sec was found to agree with results obtained at 1.3 Mc/sec by previous investigators and hence there is no dispersion in this frequency range. The attenuation measurements exhibit three important features: a) in the upper temperature range of He I the measurements agree very well with classical theory, b) at the λ -point the attenuation coefficient rises abruptly, presumably to infinity, indicating complete absorption of the ultrasonic energy, c) just below the λ -point the attenuation has its smallest value and with lowering temperature the attenuation increases.



ULTRASONIC VELOCITY AND ABSORPTION IN LIQUID HELIUM

1. Introduction

The experiments described in this paper give the velocity and attenuation of sound in liquid helium at a frequency of 15 Mc/sec as a function of temperature from 1.57°K to 4.5°K. The object of these experiments is twofold: a) experimentally to check the theory of sound absorption for a monatomic liquid and, b) to probe into the nature of liquid helium in its low temperature phase and at the transition point. The experiments were made possible by two recent developments: the ultrasonic pulse technique which grew out of radar research¹ and the Collins Cryostat² which can produce relatively large amounts of liquid helium.

A cursory resume of the physical properties of liquid helium is appropriate to an introduction because of the dependence of sound absorption on such physical properties as viscosity, heat conductivity, and specific heat. It is well known from the pressure-temperature diagram of state³ that at normal pressures helium remains in a liquid state from its boiling point clear down to absolute zero. The liquid state is separated into two separate phases called He I for the high temperature region and He II at low temperatures. For usual conditions (i.e., the liquid under its own vapor pressure) the transition occurs at 2.19°K; and since no latent heat is involved, the transition is referred to as one of the second order. The present ultrasonic determinations as well as the several physical properties (density, compressibility, viscosity, heat conductivity, and specific heat) show abnormal behavior at the so-called " λ " point.

In some respects liquid He I displays characteristics normally attributed to gases. This occurs for example in the behavior of its viscosity measured vs. temperature⁴. Most liquids show a viscosity which tends to decrease with increasing temperature, but for liquid helium the opposite trend occurs.

Concerning the behavior of viscosity below the λ -point, no consistent picture has been formulated on the basis of classical concepts.

Above the λ -point the coefficient of thermal conductivity⁵ is of the same order of magnitude as for gases, 6×10^{-5} cal/deg.cm.sec.; however, in passing to temperatures just below the λ -point the conduction is increased by a factor of about 3×10^6 . The classical equation of heat flow is not valid in He II.

These and other physical properties of He II have led theorists to develop new concepts to describe the state of this liquid. London⁶ has suggested that He II should be interpreted in terms of a Bose-Einstein gas and that the λ -point should be considered as a condensation point in phase space for such a system. Tisza⁷ subsequently showed that the hydrodynamic and thermodynamic properties of helium can be understood on this basis. Tisza (and independently Landau⁸) regards He II as a mixture of two components; one is a normal component in the sense that it corresponds closely to He I, the other is a superfluid component possessing only zero-point energy and completely devoid of viscosity. The ratio of the density of the normal component ρ_n to the density of the entire mixture ρ is temper-

ature dependent: $\rho_n/\rho \cong (T/T_\lambda)^{5.5}$ where T is the absolute temperature below 2.19°K and T_λ is the transition temperature 2.19°K . The power to which the temperature ratio is raised originates from an experimental fit. The mechanism of heat flow is presumably a mass transport process in which the normal fluid component (carrying thermal energy) moves in the direction of the negative temperature gradient while the superfluid seeks regions of higher temperature. This represents a form of internal convection.

The specific heat shows the characteristic λ shape for a second order transition at 2.19°K . Most measurements of specific heat in helium have been made under conditions of saturated vapor pressure, and little direct data for c_v exists. The ratio of specific heat capacities $\gamma = c_p/c_v$ can be computed from data in Keesom's recent book³ by means of the thermodynamic relationship $\gamma - 1 = -\frac{T}{\rho^2 c_v} \left(-\frac{\partial p}{\partial T}\right)_\rho \left(-\frac{\partial \rho}{\partial T}\right)_p$ where ρ is the density, P the pressure, and T the temperature. Values of $(\gamma - 1)$ are included with the theoretical and experimental results of Table I.

2. Experimental Apparatus and Procedure

The special advantages and capabilities of the pulse technique originally developed for radar have made possible measurements of the type conducted in this research. By using short pulses absorption measurements may be conducted at relatively high frequencies (15 Mc/sec in this case), for which the attenuation is sufficient to make quite accurate measurements possible. As will be seen the method is direct and straightforward both for obtaining velocity and attenuation; and absorption measurements thus obtained¹⁰ are usually superior to those of older, continuous-wave methods.

The scheme is essentially to use the liquid sample as a "storage medium" for the short sound pulses and to measure the time delay and attenuation undergone by the sound in traveling a known path-length. The acoustical pulses, after being generated from electrical pulses by the transducer, travel through the liquid to a plane reflector (shown purely schematically in Fig. 1) and back again to re-excite the crystal at a later time.

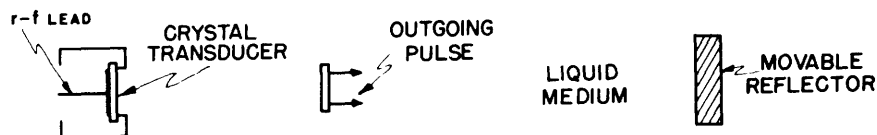


Figure 1. Transducer-Reflector System

The transducer-reflector distance is variable so that the increased delay produced by an increase in path-length is a direct measure of wave velocity. The attenuation which must be removed from the electrical circuit to balance the acoustical losses in the additional distance provides a measure of absorption.

The timing sequence is as follows (Fig. 2).

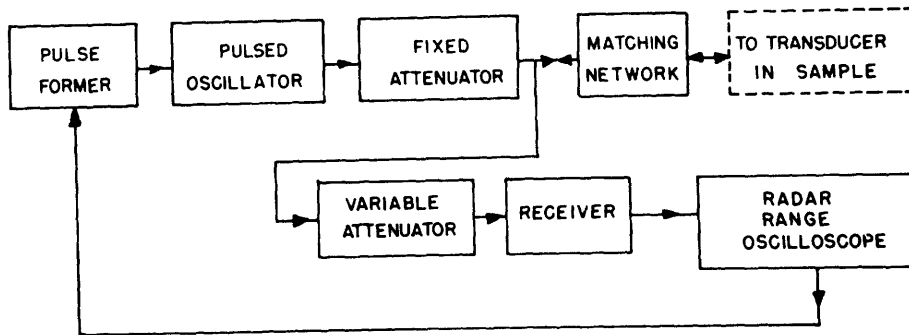


Figure 2. Block Diagram for Method of Ultrasonic Measurements

A crystal-controlled circuit in the oscilloscope starts the scope sweep and simultaneously sends a trigger to the pulse generator. The pulse formed by the generator passes through an impedance matching network to the transducer. When the resulting sound pulse returns to the transducer after its round trip within the liquid, the delayed electrical pulse is formed and returns through the matching network. Since the transmitter is off when the echo signal arrives, very little leakage loss occurs and the main portion travels through the variable attenuator to the receiver.

Both triggering and time measurements are accomplished by means of the crystal-controlled circuit in the oscilloscope (Dumont Type 256B A/R Range Scope), so that automatic synchronization occurs. In addition to setting off the pulse generator and starting the sweep, this circuit also provides marker pips spaced every 10,000 yards of radar range. For examination of the front edge of the echo signal, an expanded sweep with variable delay is used. Crystal control is necessary primarily for accurate timing of the marker pips; one pip is developed for each oscillation, and since the crystal frequency is accurate to better than 1 part in 10,000, the same holds for range marker positions.

Concerning measurement procedures, velocity is obtained directly from the slope of distance traveled plotted versus pulse delay, and absorption is obtained from the slope of compensating electrical attenuation versus distance. Since the method depends only upon observing the effects of differences in acoustical path length, knowledge of exact distance traveled by the sound is unnecessary.

Velocity readings are taken for helium at 10,000-yard (radar) range intervals by placing the returned signal pip at definite positions with respect to successive scope range markers and recording the transducer-reflector distance. By adjusting the scope properly, these markers appear as very short (dark) breaks in the sweep, and if consistent criteria are adopted, accurate range difference readings result. Since the echo signal is adjusted to a predetermined level on the scope for each range position (by means of attenuators, without disturbing the gain of the remainder of the system), absorption data are obtained directly. Figure 3 gives an example of excellent data for attenuation in liquid helium at 3.08°K; the attenuation is plotted against the transducer-reflector distance, and the slope of the straight line is a measure of absorption.

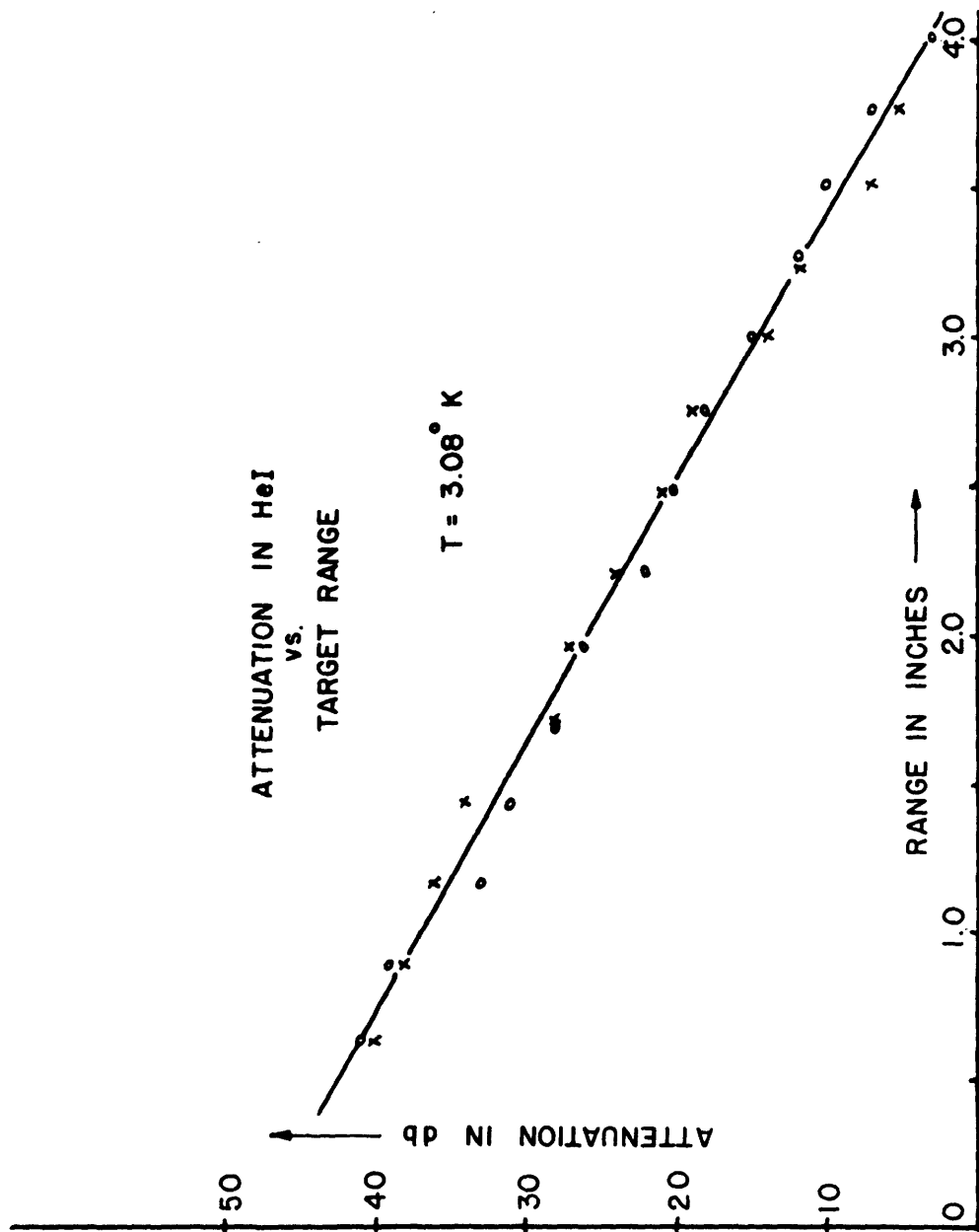


Figure 3. Sample Plot of Receiver Attenuation vs. Target Range at Constant Temperature.

Results obtained by such measurements may be regarded as physically equivalent to those obtained by continuous-wave methods. It may be shown that differences in behavior between pulsed sound and continuous sound in liquids should produce negligible effects. For example, no significant dispersion in liquids has been detected in the 15 - Mc/sec range (nor pulse distortion) so that the group velocities measured by pulsing should not differ measurably from the phase velocities ordinarily determined. Similarly, although attenuation within liquids varies as frequency squared, the bandwidth associated with the pulses is too narrow for a measurable effect to result.

The velocity of ordinary sound in liquid helium is about 2×10^4 cm/sec, corresponding to a wave-length at 15 Mc/sec of roughly 1.3×10^{-3} cm. Since the crystal radiating and receiving surface is about 1 cm. across, this corresponds to about 750 wave-lengths per diameter. Accordingly, the pulses travel out within a very narrow beam (0.1° when computed on the basis of Fraunhofer diffraction, to obtain an order of magnitude). Therefore the pulses retain nearly their exact size and shape throughout their travel, so that any geometrical attenuations due to spreading are completely overshadowed by true liquid absorption. Therefore attenuation data may be converted directly to absorption coefficients by applying a numerical factor; thus from the linearity of the curve of Fig. 3 one obtains db/inch = 11.1 and $\alpha = \frac{11.1}{44.3} = 0.25$ is the absorption coefficient, in (cm^{-1}).

In the classical theory of sound¹¹ the α is commonly referred to as the coefficient of pressure attenuation and enters into the solution of the wave equation as:

$$P = P_0 e^{-2\pi i \nu (t - x/v) - \alpha x} \quad (1)$$

where P is the pressure, ν the frequency, v the wave-velocity, and x the coordinate of distance along which the wave travels. In Fig. 3 the exponential decay is experimentally verified and it is understood that the α determined from the slope of data such as in Fig. 3 is the composite attenuation due to viscosity and heat conduction. For liquids containing polyatomic molecules an additional attenuation involving internal molecular vibrations would also be included.

In discussing the equipment for these experiments no detailed information (such as circuit diagrams) is included concerning the standard electronic elements of pulse power, transmitter, and the receiver. The ultrasonic equipment in the bath of liquid helium requires some discussion and is illustrated in Fig. 4. The entire ultrasonic equipment is placed in a Collins Cryostat² (A) where up to 5 liters of liquid helium may be produced for experiments. The ultrasonic equipment and its associated helium vapor pressure thermometer, (T), pumping tubes, (P), and vacuum jacket, (V), underwent continuous development during the course of the research program. The crystal (C) was driven by 15 - Mc/sec electrical pulses arriving through the coaxial line (L). The resulting sound waves traveled out from the crystal to the reflecting target (R). This mirror could be placed at any desired range by means of the screw (S). This precision constructed screw

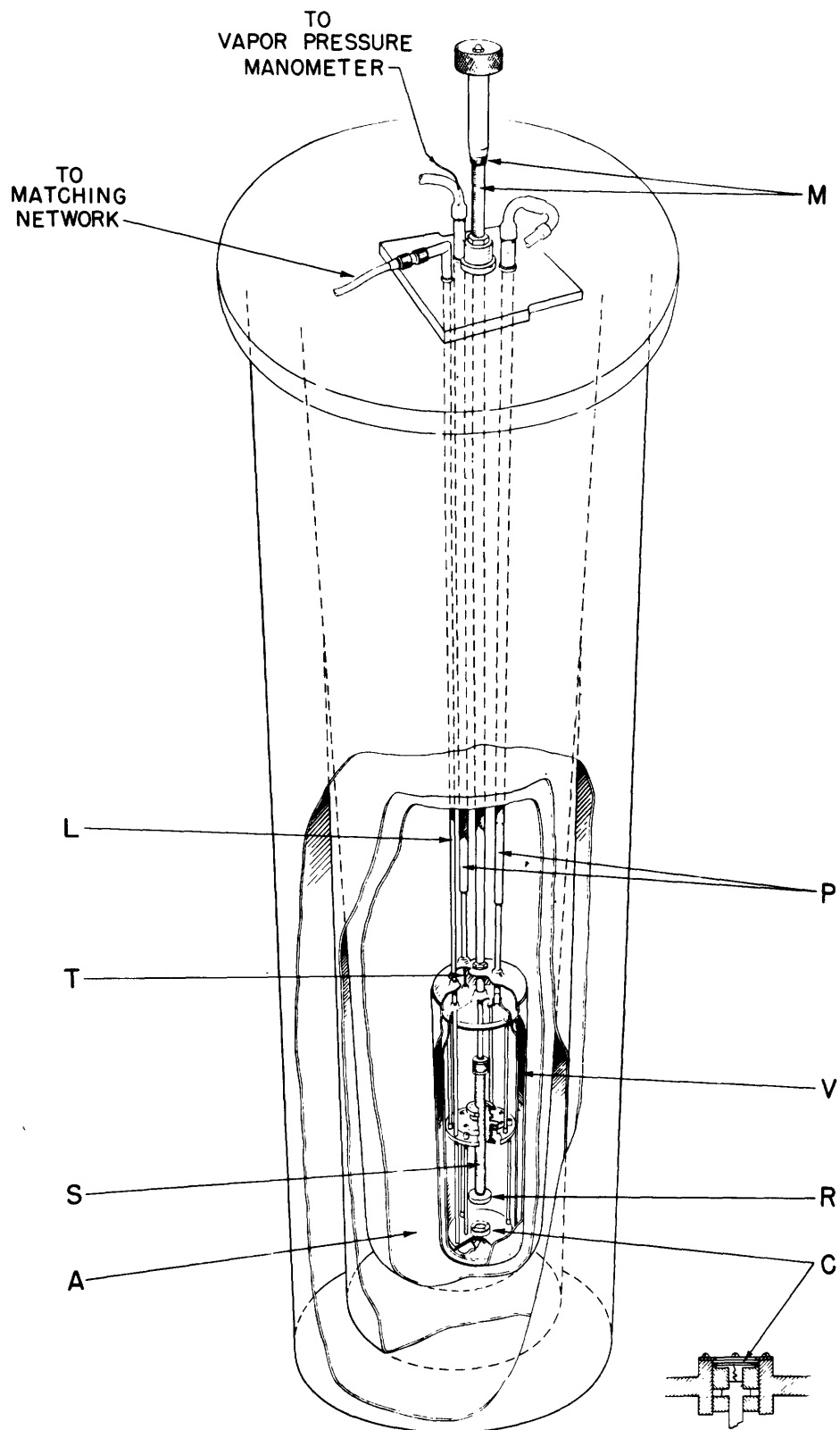


Figure 4. Composite Isometric View of Transducer-Reflector Equipment within Cryostat.

was driven by a steel rod extending from the top of the equipment and was equipped with a micrometer vernier scale (M) for precision distance readings. Liquid helium was allowed to condense in the innermost container until it covered the crystal transducer to a height of approximately 15 centimeters. The intermediate chamber (V) was then pumped out to a high vacuum so that the liquid in which the measurements are made was thermally insulated. Except at the very lowest temperatures (below 2°K) the liquid in the outer cryostat was kept at a slightly lower temperature than the liquid covering the crystal. These conditions permitted excellent temperature control and avoided rapid boiling which could have been detrimental to accurate readings.

The transducer consisted of a thin X-cut quartz crystal one cm in diameter. Such a crystal undergoes thickness vibrations when an oscillating voltage is applied across its thin dimension. The crystal was cut to the proper thickness (about 0.018 cm) for its fundamental resonance to occur at approximately 15 Mc/sec.

The upper (and radiating) surface was completely silvered and was grounded to the housing cartridge. On the other hand the silver plating on the lower surface did not extend quite to the crystal circumference, thus forming an insulated electrode to which the r-f signal could be fed from the pulser. This transducer had two separate effects on the electrical properties of the system. First of all, the geometry of the crystal provided a certain dead capacity between its electrodes, amounting to about 25 μ mf.

A more important effect of the transducer upon the system was a marked narrowing of the bandwidth, especially for the case when the crystal was in contact with liquid helium. This may be illustrated by means of the equivalent transducer circuit, Fig. 5.

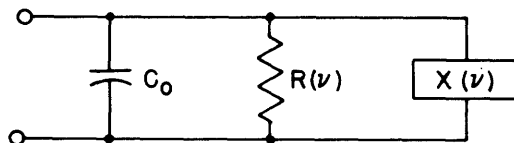


Figure 5. Equivalent Transducer Circuit.

This particular equivalent form for representing the crystal has been chosen as convenient for the present discussion. Here C_0 is the dead crystal capacity (25 μ mf) in parallel with a frequency-dependent radiation resistance $R(\nu)$ and a frequency-dependent reactance $X(\nu)$.

The bandwidth of the transducer may be determined by measuring the radiation resistance $R(\nu)$ vs. frequency and obtaining the half-power points. Sample Q-meter measurements of $R(\nu)$ given in Fig. 6 for CCl_4 and liquid helium illustrate the sensitivity of the electrical properties of the crystal to the medium into which it radiates. It is noted that, whereas for CCl_4 the bandwidth $\Delta\nu$ is about 1.7 Mc/sec, the bandwidth for liquid helium is only about 0.2 Mc/sec.

The characteristic impedance of most ordinary liquids such as CCl_4 is about one-tenth that for crystalline quartz, and this provides sufficient damping (through radiation)

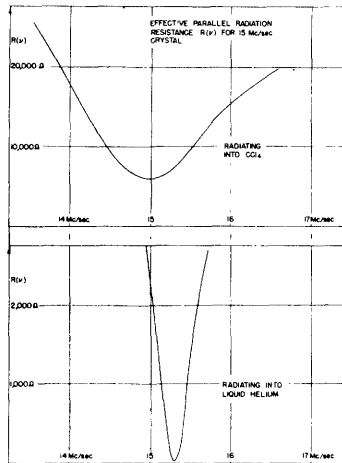


Figure 6. Radiation Resistance of Crystal vs. Frequency.

to reduce the crystal Q to the neighborhood of 10 or less. On the other hand, the characteristic acoustical impedance for liquid helium being only about one-thousandth that for quartz, the bandwidth of 0.2 Mc/sec corresponds to a Q of about 75, since

$$Q = \frac{\nu}{\Delta\nu} = \frac{15}{0.2} \approx 75 \quad (2)$$

The bandwidth $\Delta\nu = 0.2$ Mc/sec may be converted directly to the corresponding acceptable pulse-length $\Delta\tau$ by the relationship

$$\Delta\tau = (\Delta\nu)^{-1} = 5 \times 10^{-6} \text{ sec.} \quad (3)$$

It is therefore evident that pulse-lengths of at least 5 μ sec duration were required. This corresponded to about 75 complete oscillations per pulse, also numerically equal to the Q of the system. These are merely quantitative ways of expressing the fact that helium is a most difficult liquid in which to generate sound pulses.

It is necessary to match the impedance presented by the crystal system to that of the coaxial line leading from the pulser. At resonance the impedance presented by the crystal is complex, and ordinarily the impedance level is different from that of the line. Therefore a matching network was essential, and was placed directly outside the cryostat. This is illustrated in Fig. 7.

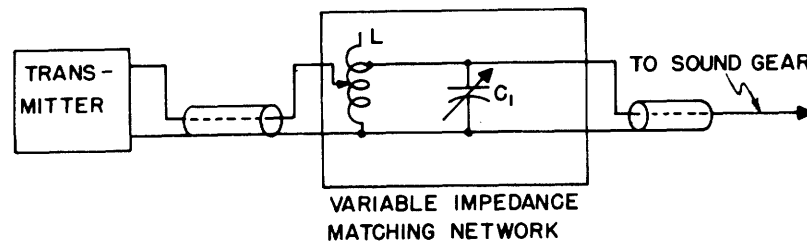


Figure 7. Impedance Matching Network

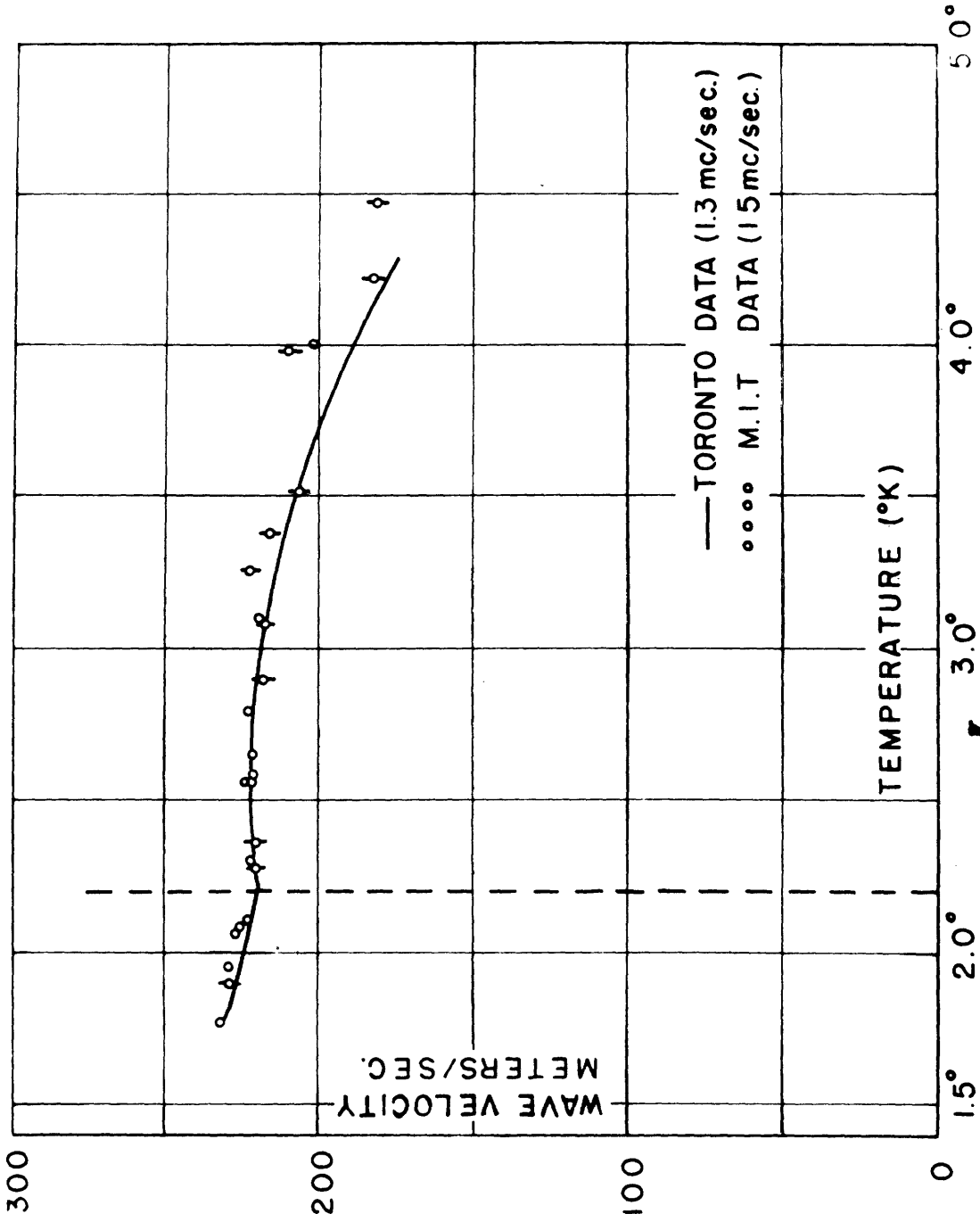


Figure 8. Ultrasonic Wave Velocity vs. Temperature in Liquid Helium

The dead capacity of the crystal (25 μ mf) plus the capacity of the internal coaxial line (100 μ mf) were tuned out by means of the coil L. The fixed tap from the coaxial line into this coil was positioned to provide somewhat more inductance than actually necessary for this purpose. The excess was available for adjustment during operation (using the echo signal as a guide) by tuning out with the variable capacity C_1 .

The input signal from the transmitter entered coil L via a variable tap T. A sliding contact was provided to make the turns ratio continuously variable, and the setting was obtained by maximizing the returned echo signal.

3. Results

3.1 Velocity. The velocity of first sound (meter/sec) is plotted versus temperature (degrees Kelvin) in Fig. 8. The circles represent individual values at 15 Mc/sec determined by the pulse method described. These are compared with results of previous investigators¹² obtained interferometrically at 1.3 Mc/sec and indicated by the solid line. The general correlation shows the absence of any dispersive effects within this frequency range. All of the above data refers to liquid helium under its own vapor pressure. The investigation by the Toronto Laboratory¹² revealed a discontinuity in velocity at the λ -point under conditions of increased pressure. The conclusion was that whatever discontinuity existed under its own vapor pressure conditions was too small for measurement by that method. Similarly the present technique was incapable of detecting such an effect.

3.2 Attenuation. The pressure attenuation coefficient α in cm^{-1} plotted as a function of temperature in degrees Kelvin in Fig. 9 and represents the essentially new information resulting from this investigation. Each point represents a separate series of electrical attenuation versus range readings at constant temperature. These db versus range data were graded according to linearity of the plots, and the most reliable results from this standpoint indicated by circles. The results of remaining runs contributing significant but less reliable values are represented by dots. The solid curves of Fig. 9 represent the composite average for the measurements. In the region above 3°K the solid curve is omitted since it merges with the theoretical curve represented by the dotted line.

It is evident from Fig. 9 that the absorption changes abruptly in the neighborhood of the λ -point, so that for this temperature region it proved impractical to conduct db versus range measurements. Accordingly, an alternative procedure was adopted of holding the transducer-reflector distance fixed and noting receiver signal strength versus temperature as the λ -point was passed. Although this technique is inadequate for detailed measurements in the low attenuation ranges, it is suitable for mapping out large-scale, rapid changes. This is represented by the triangles and dashed line of Fig. 9. Such a procedure yields only differences in α ; having obtained the shape of the curve, the absolute magnitude of α is adjusted to fit the true values of the solid line curve of Fig. 9.

Several significant features are revealed. Beginning with the highest temperatures in the He I domain, the attenuation falls steadily as temperature is decreased.

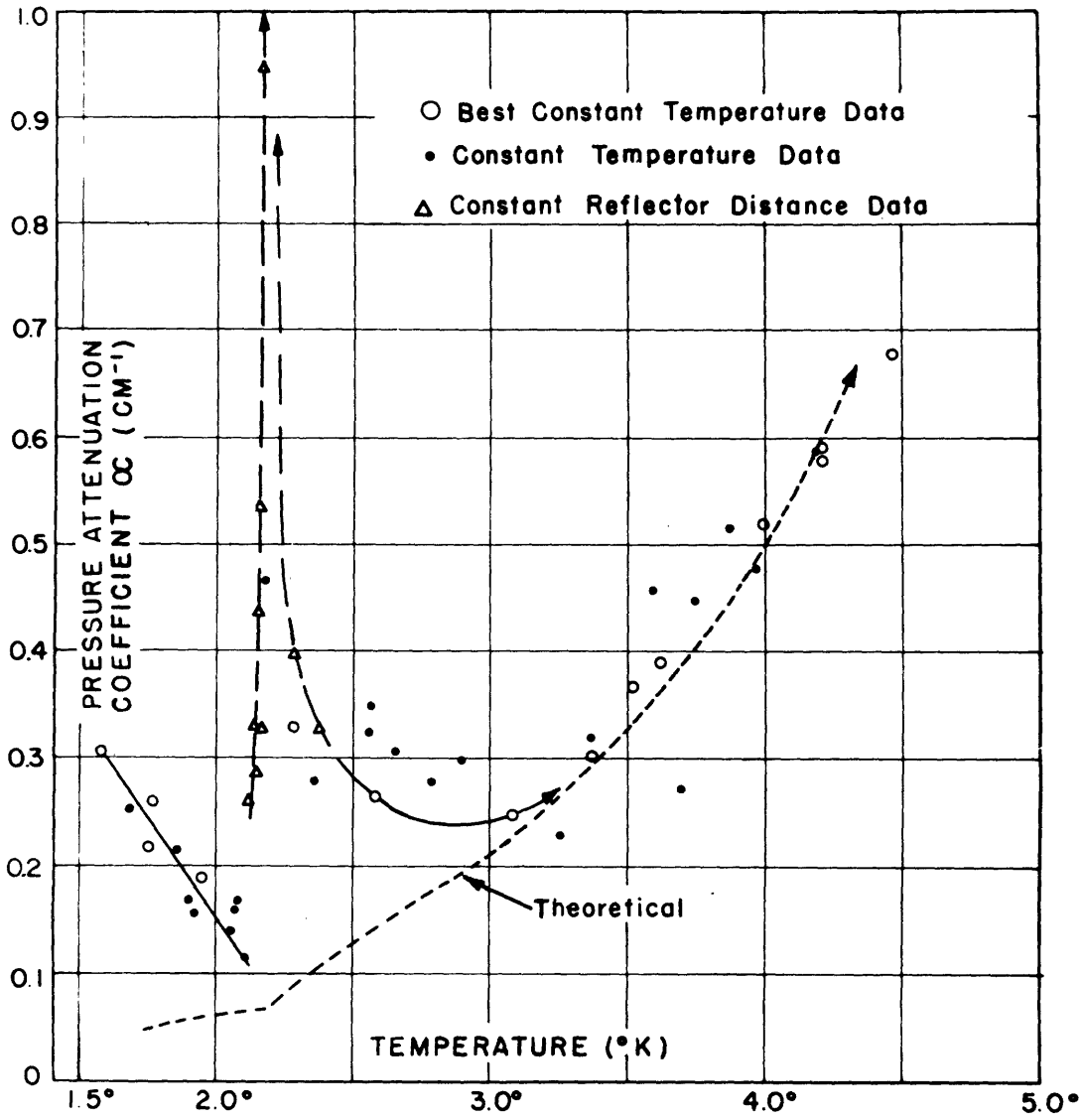


Figure 9. Ultrasonic Pressure Attenuation Coefficient α vs. Temperature.

A minimum is reached in the 2.8°K region below which the attenuation increases, finally to rise sharply in the immediate vicinity of the λ -point. It was not possible to determine whether α actually became infinite, but on the basis of signal strengths at temperatures of known attenuation it is clear that values of at least 3.5 cm^{-1} occur for α .

Lowest attenuations occur immediately below the λ -point where values of about 0.1 cm^{-1} were observed. However, at lower temperatures the attenuation again increases in a steady manner. This trend appears to continue even to the lowest temperature at which measurements were conducted (1.57°K).

Numerical values of attenuation coefficient α including one at 5.1°K are given in Table I for runs indicated by circles in Fig. 9. Numerical values for the computed α are given at corresponding temperatures where data exists for such computations.

TABLE I

<u>Temperature</u>	<u>$\gamma - 1$</u>	<u>α - viscosity</u>	<u>α - thermal</u>	<u>Total</u> <u>α - theoretical</u>	<u>Total</u> <u>α - experimental</u> (1.78 cm^{-1})
5.1 \pm 0.1°K					
4.47 \pm 0.01					0.68
4.22 "	1.35	0.244	0.382	.62	0.58
4.00 "	1.14	0.200	0.260	.46	0.52
3.62 "	0.80	0.131	0.198	.33	0.39
3.52 "	0.72	0.122	0.184	.30	0.37
3.38 "	0.58	0.114	0.164	.28	0.30
3.08 "	0.38	0.103	0.122	.22	0.25
2.58 "	0.14	0.087	0.055	.14	0.27
2.28 "	0.03	0.079	0.015	.09	0.33
λ -point (2.19)	0	0.077	0	.077	(∞)
2.11 "		0.071	0	.071	0.11
1.94 "		0.061	0	.061	0.15
1.76 "		0.050	0	.050	0.24
1.57 "		0.042	0	.042	0.30

4. Discussion

4.1 Helium I. One of the revealing features of the attenuation measurements is in the manner in which classical theory completely accounts for the absorption in He I at temperatures above about 3°K. Values computed on the basis of classical theory are represented by the dotted curve of Fig. 9 which above 3°K also represents the best experimental curve. This is significant since for ordinary liquids (with the exception of Hg) the measured values consistently exceed* the amounts expected on the basis of classical

* The discrepancy ranges to an extreme factor of 800 in case of liquid H₂S.

4.2 Helium II. The mechanism and formulas of classical absorption are not directly applicable to the case of He II since this liquid obeys a special system of complex hydrodynamics. Discussion of attenuation is rendered difficult because this complex hydrodynamics has been developed only to the first approximation. The main characteristic of He II is the possibility of a heat transfer as a first-order hydrodynamical process. The only dissipative process considered so far in the literature is the damping of an oscillating disk through viscosity. It appears that the classical formula (5) may be applied below the λ -point as long as the appropriate value of η is used. It turns out that this proper quantity is the effective viscosity η_n referred to the normal fluid only (η_s for superfluid is taken as zero). Since for first sound, which we are considering, the two fluid components vibrate in phase with essentially identical particle excursions; the fluids are effectively locked together. Therefore, in setting up a wave equation, the differential acceleration force on a thin layer involves the total density ρ , exactly as for the classical case (see footnote of Eq. (5)). However, the viscous retarding forces opposing the expansion and contraction of the layer are dependent upon the only existent viscosity present, namely η_n for the normal fluid component. Accordingly for He II this becomes

$$\alpha - \text{viscosity} = \frac{8\pi^2}{3} \frac{\eta_n}{\rho c_1^3} v^2 \quad (7)$$

which is the quantity plotted in Fig. 9 for below the λ -point. The curve falls only gradually with lowering temperature, since the viscosity coefficient η_n is given by a smooth extension* of η for He I into the He II region. The effect of heat conductivity on ultrasonic absorption is more complicated. The ordinary diffusion type of heat transfer must exist also in He II but is completely masked by the first order (reversible) heat transfer. The latter manifests itself in the so-called second sound^{7,8} which has been verified experimentally by Peshkov¹⁴ and by Lane¹⁵. The α -thermal of Eq. (6) would be of the order of magnitude in He II as it is in He I close to the λ -point and would not essentially change the total theoretical α plotted in Fig. 9. below the λ -point.

One might expect other dissipation effects which are peculiar to He II and which would give ultrasonic absorption of the relaxation type. Tisza⁷ has suggested non-adiabatic transitions between the normal and superfluid component induced by ultrasonic waves. Other relaxation mechanisms such as between the ultrasonic energy and the zero point energy may also appear. Finally the coupling between first and second sound might give rise to dissipation effects. It does not seem possible at present to compute these effects without making arbitrary assumptions.

* Viscosity measurements in He II using the oscillating disk method⁴ were originally taken to indicate a coefficient falling sharply with temperature from the λ -point. A subsequent reinterpretation of the viscosity data by Tisza leads to a normal value of η for the normal fluid and an essentially zero value of η for the superfluid.

viscosity and heat conduction losses. This is presumably attributable to the monatomic nature of helium which precludes the type of relaxation phenomena associated with the inner degrees of vibration of polyatomic molecules. Moreover, He I presents a situation in which the relative contributions to absorption between viscosity and heat conductivity vary over a large range as temperature is varied. Numerical values for these two classical contributions to absorption

$$\alpha = \alpha_{\text{viscosity}} + \alpha_{\text{thermal}} \quad (4)$$

are given in Table I and were computed according to the well known¹³ formulas

$$\alpha_{\text{viscosity}}^* = \frac{8\pi^2}{3} \frac{\eta}{\rho c_1^3} \nu^2 \quad (5)$$

$$\alpha_{\text{thermal}} = \frac{2\pi^2(\gamma-1)}{\rho c_1^3} \frac{K}{c_p} \nu^2 \quad (6)$$

In the above, ν is the ultrasonic frequency in cycles per second, c_1 the ultrasonic velocity in cm/sec, η the coefficient of viscosity in poise, ρ the liquid density in grams/cc, K the heat conductivity coefficient in cal/deg. cm. sec., c_p the specific heat at constant pressure in cal/gm. deg., and γ the ratio of specific heats. With the exception of heat conductivity K , each of these quantities is a known function of temperature. In the case of K , results are published⁵ only for 3.3°K so that this value of 6.0×10^{-5} cal/cm sec. was of necessity used throughout the temperature range of the He I calculations. It is noteworthy that the magnitude of the ultrasonic absorption places He I in the category of relatively high absorption liquids (in spite of its low viscosity). This behavior is accounted for by the occurrence in the denominator of Eq. (5) and (6) of ρ and c_1^3 , both of which are extremely low for helium.

In the general region of 3°K the experimental results of α begin to exceed considerably the classical theoretical values. Finally the sharp peak occurs at the λ -point, whereas the predicted value for that temperature is only 0.07 cm^{-1} . Clearly the inadequacy of the classical theory points to some other mechanism. Possibly a discontinuity in velocity such as suggested by the Toronto investigations might account for this effect. Another more general explanation of the complete absorption of ultrasonic energy at the λ -point is possible. The energy of transition from He II phase to He I phase is vanishingly small as the system approaches the λ -point (because the phase transition is of the second order - i.e., no latent heat at the λ -point). In just this region such transitions might be forced by the ultrasonic energy.

* The expression for $\alpha_{\text{viscosity}}$ may be derived from the wave equation:
 $\rho \ddot{\xi} - \rho c^2 \nabla^2 \xi = \frac{4}{3} \eta \nabla^2 \dot{\xi}$ where the last term involves viscosity (here ξ is the particle displacement). A similar formulation involving heat flow leads to (6).

5. Conclusions

The ultrasonic velocity and absorption of first sound in liquid helium have been measured at 15 Mc/sec as functions of temperature. The velocity of 15 Mc/sec was found to agree closely with results obtained at 1.3 Mc/sec by previous investigators. This implies the absence of dispersion in this frequency range. The attenuation measurements exhibit three important features, a) in the upper temperature range of He I the measurements agree very well with classical theory (this serves not only to reassure the overall understanding of liquid helium in the higher temperature region but also to verify the classical absorption formulas), b) at the λ -point the attenuation coefficient rises abruptly, presumably to infinity, indicating complete absorption of the sound energy, c) just below the λ -point the attenuation falls even more abruptly to a value somewhat lower than the smallest value for He I. The attenuation in He II then increases linearly with decreasing temperatures, a trend which persists to the lowest temperature reached (1.57°K).

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