We propose a mechanism by which an open quantum dot driven by two ac (radio frequency) gate voltages in the presence of a moderate in-plane magnetic field generates a spin-polarized, phase-coherent dc current. The idea combines adiabatic, nonquantized (but coherent) pumping through periodically modulated external parameters and the strong fluctuations of the electron wave function existent in chaotic cavities. We estimate that the spin polarization of the current can be observed for temperatures and Zeeman splitting energies of the order of the single-particle mean level spacing.

The advent of shape-modulated quantum dots has renewed interest in the problem of phase-coherent pumping of electrical charge by periodic modulation of external parameters [1]. The original idea of coherent charge pumping, devised for gaped, isolated systems [2], has been extended to open systems [3–5], and recently realized experimentally by Switkes et al. [6]. Subsequent theoretical work has focused on issues of symmetry, statistics, and phase coherence [7–9], including a reinterpretation of the experiment [6] as a rectification effect [10]. To date, there has been little discussion of electron spin in quantum pumps.

There is a growing interest in the mesoscopic physics of spin transport in microelectronic circuits [11]. Most coherent spin transport devices proposed or realized experimentally thus far are based on the injection of polarized electrons from metallic or semiconductor ferromagnetic contacts (for a recent review, see Ref. [12]). An alternative approach based on pumping of spin in purely one-dimensional systems using fluctuating gate voltages and magnetic fields has been recently proposed [13].

In this Letter, we propose and analyze a new method of generating spin-polarized dc currents in semiconductors based on the parametric pumping of spin without relying on spin injection. The basic idea is to apply two cyclically oscillating gate voltages to a quantum dot formed from a two-dimensional electron gas (2DEG) (similar to adiabatic charge pumping) in the presence of a uniform magnetic field applied in the plane of the 2DEG. The lifting of spin degeneracy by the magnetic field allows an arbitrary ratio of spin and charge to be pumped, including the situation in which a spin current of order $h/\omega$ per pumping cycle is produced with zero charge pumping.

The device we have in mind is an open quantum dot made from a confined 2DEG, with two point-contact leads connecting the dot to electron reservoirs. The confining potential of the dot undergoes a periodic shape deformation controlled by two ac gate voltages, $V_1(t) = A_1 \cos(\omega t + \phi_1)$ and $V_2(t) = A_2 \cos(\omega t + \phi_2)$ [6], as shown schematically in Fig. 1(a). We assume that the shape deformation is adiabatic, by which we mean $\omega \ll \gamma_{\mathrm{esc}}$, where $\gamma_{\mathrm{esc}} = N \Delta / 2 \pi \hbar$ is the escape rate from the dot, $\Delta = 2 \pi \hbar^2 / m A$ is the quantum level spacing of the closed dot with area $A$, and $N = N_l + N_r$ is the total number of channels connecting the dot to the left and right reservoirs. We further assume for the sake of simplicity that spin scattering, spin-orbit effects, and decoherence are negligible, though in practice the latter two effects may have significant consequences.

In the absence of applied magnetic fields, the pumped current produced by cyclic shape deformation of the dot
carries no net spin, i.e., the up and down spin components of the pumped current, \( I_{\uparrow} \) and \( I_{\downarrow} \), are identical. In this case, \( I_{\uparrow} \) and \( I_{\downarrow} \) fluctuate together, with zero average, as a function of external parameters, such as static dot shape and perpendicular magnetic field. Spin degeneracy can be lifted by applying a magnetic field in the plane of the 2DEG [14]. For moderate parallel fields, \( E_Z = g^* \mu_B B_\parallel > \max \{ \Delta, \hbar \gamma_{\text{esc}} k_B T \} \) (typically a few Tesla for a micron scale GaAs quantum dot at temperatures below 0.5 K) the pumped currents associated with the two spin directions \( I_{\uparrow} \) and \( I_{\downarrow} \) will become uncorrelated, and will fluctuate independently as device parameters are changed.

Let us denote the charge and spin currents passing through the dot as \( I_c \) and \( I_S \), respectively: \( I_{c;\uparrow} = I_{\uparrow} \pm I_{\downarrow} \) (we define spin current to have the same units of charge current, understanding that \( e \leftrightarrow \hbar/2 \)). Upon averaging over different realizations of the dot shape or chemical potential, \( \overline{I_{c;\uparrow}} = \overline{I_{c;\downarrow}} = 0 \). The strength of the pumping current is characterized by its variance,

\[
\overline{I_{c;\uparrow}^2} = \overline{I_{c}^2} = 2 \overline{I_{\uparrow}^2} \pm 2 \overline{I_{\downarrow}^2} = 2(\overline{I_{\uparrow}^2} \pm \overline{I_{\downarrow}^2}),
\]

where we assumed \( \overline{I_{\uparrow}^2} = \overline{I_{\downarrow}^2} \). In the absence of an in-plane field, \( \overline{I_{c;\uparrow}} = \overline{I_{c;\downarrow}} \), whereas for a strong enough applied field, we expect that incoming spin up and spin down electrons will occupy uncorrelated sets of states in the dot, leading to \( \overline{I_{\uparrow}^2} = \overline{I_{\downarrow}^2} \). As a result, \( \overline{I_{c}^2} \) decreases by a factor of 2 in the large field limit [15], while simultaneously \( \overline{I_{c;\uparrow}^2} \) goes from zero to its maximum value. The most striking situation, however, occurs when parameters are set such that \( I_{\uparrow} = -I_{\downarrow} \). Because \( I_c \) fluctuates randomly about zero as a function of external parameters, one can simply tune dot shape or perpendicular field until the condition \( I_c = 0 \) is found. This will be the state where \( I_{\uparrow} = -I_{\downarrow} \). In this case, a finite spin current exists through the quantum dot without any net charge transport. Experimentally, gate voltage control at the level of tens of microvolts is sufficient to achieve this condition to within the noise of the pumped current. This is illustrated in Fig. 2.

It is important to realize that the effect of the Zeeman field is not to polarize the electrons in the dot, but rather to create two independent electron “speckle patterns,” one for spin up and one for spin down, that are present in the dot due to quantum interference. Because the pumped current results from the motion of the electron speckle in response to shape changes of the dot, independent speckle patterns are all that is needed to produce spin pumping. It is not necessary to significantly polarize the dot whatsoever.

Let us call \( Q_{\uparrow\downarrow} \) the spin up/down charge transferred after the completion of one cycle,

\[
Q_{\uparrow\downarrow} = \int_0^{2\pi/\omega} dt \overline{I_{\uparrow\downarrow}(t)}.
\]

For a chaotic or disordered quantum dot connected to leads with many propagating channels \((N \gg 1)\), the variance of pumped charge over an ensemble of equivalent dots (e.g., differing in shape or disorder configuration) has been calculated by several authors [4,7,9]. We generalize these calculations, as presented in Ref. [9], to include a Zeeman field [16]. For our purposes, it will be sufficient to consider the theory in the limit of high temperature, when \( \hbar \omega \ll E_Z, k_B T, \hbar \gamma_{\text{esc}} \) [17]. The resulting analytical expression for \( Q_{\uparrow\downarrow} \) is further simplified if we restrict our analysis to the case of small external oscillating voltages. This allows us to use an expansion in powers of \( A_1 \) and \( A_2 \) and retain only the leading bilinear term. Following Ref. [9], we obtain

\[
\frac{Q_{\uparrow\downarrow}}{Q} = \frac{16\pi e^2 g}{NC_2 \sin^2 \phi} \int_0^\infty d\tau e^{-N\tau/\Delta} F(\tau)^2 \cos(E_Z \tau),
\]

where \( g = N_c/N_1 \), \( \phi = \phi_1 - \phi_2 \), \( F(\tau) = \tau / \sinh(2\pi \tau) \) (we take \( \hbar = k_B = 1 \) hereafter). The factors \( C_{1,2} \) are related to the quantum dot response to shape deformations and can be determined through their relation to the quantum dot energy level susceptibility [7,9].

When the Zeeman energy is set equal to zero, Eq. (3) coincides with a similar expression in Ref. [9] for \( Q^2 \) and spinless electrons. Since \( N \gg 1 \), the exponential factor dominates the integrand decay in Eq. (3) at low...
temperatures. In that case, the variance of total spin transferred per cycle, \( Q_t = Q_1 - Q_1 \), will depend strongly on \( N \).

The integral over \( \tau \) can be evaluated numerically, yielding results such as those shown in Fig. 3, where we have plotted the quantity \( r_{\text{pol}} = \frac{Q_1}{\bar{Q}_2} \) versus \( E_z \) for several values of \( T \) and \( N \), with \( \bar{Q}_c = Q_1 + Q_1 \) and \( \phi \neq 0, \pi \). Notice that at \( E_z = 0 \), \( Q_1/Q_1 = Q_1/Q_1 \), thus \( r_{\text{pol}} = 0 \). As \( E_z \) grows, the amounts of up and down spin transferred per cycle become uncorrelated. The typical amplitude of spin transfer depends strongly on temperature. The dependence on \( N \), which is pronounced at low temperatures, decreases substantially when \( T \) is of order \( \Delta \) [see Fig. 3(b)].

From Eq. (3) we can estimate the typical Zeeman energy \( E_z \) necessary to achieve \( r_{\text{pol}} = 1/2 \), i.e., that spin polarize \( \sqrt{1/2} = 70\% \) of the pumped current. When \( T < 2 \pi \gamma_{\text{esc}} \), we obtain \( E_z = 1.17 \gamma_{\text{esc}} \), while in the opposite limit, \( E_z = 1.49 \gamma T \). For a GaAs quantum dot with \( 1 \mu m^2 \) in area at \( 100 \) mK and \( 2 \) T, we find that the pumped current is typically \( 60\% \) spin polarized (\( r_{\text{pol}} = 0.36 \)) when the total number of propagating channels in the leads is four. We remark that Eq. (3) indicates that the spin pumping strength should be maximal for the smallest number of propagating channels possible, namely, two.

Spin-flip scattering limits the efficiency of the spin current pump. While several mechanisms could cause spin flipping, perhaps the most relevant one to semiconductor materials is spin-orbit coupling caused by asymmetries in the confining potential and lattice structure. In a small quantum dot at \( B_{||} = 0 \), there is a substantial reduction of the spin-orbit scattering rate as compared to the bulk two-dimensional electron gas in a GaAs heterostructure [18,19]. However, it is also known that the presence of an in-plane magnetic field (such as the one needed for the operation of the spin pump) alters significantly weak localization corrections of the conductance in laterally confined quantum dots[14,19–22], suggesting an enhancement of spin-orbit effects at \( B_{||} > 0 \). This enhancement does depend strongly on the size of the quantum dot, as observed experimentally by Folk et al. [14] and theoretically examined by Halperin et al. [19]. For example, for the dots in Ref. [14], there is a crossover to strong spin-orbit coupling for large dots (\( 8 \mu m^2 \) in area), while no substantial spin-orbit effects are detected for smaller dots (\( 1 \mu m^2 \) in area). These results suggest that for small quantum dots, in the regime of temperatures and Zeeman energies that we discussed above in our estimation for \( 1 \mu m^2 \) dots, spin-orbit scattering should not be sufficient to destroy the spin pumping mechanism we propose.

Another relevant question to be considered is whether the dc current spin polarization effect caused by pumping in the presence of an in-plane Zeeman field could be also generated by a rectification mechanism [10]. The answer is positive, since spin polarization also appears when there is a difference between the quantum dot charge conductance for up and down spin channels. That is, provided \( G_1(t) \) and \( G_1(t) \) oscillate with distinct amplitudes, for a voltage drop \( V(t) \) we would have \( \bar{I}_1(t) \neq \bar{I}_1(t) \) (here the overline denotes time average). Notice, however, that while rectification would make \( I \left( B_{\text{perp}} \right) = I \left( -B_{\text{perp}} \right) \), a quantum pumped spin current does not need to satisfy this symmetry requirement. Thus, when both mechanisms are present, the quantum pumping component can be partially separated by extracting the symmetric part of \( I \). Another distinct feature of pumping is that it causes spin transfer without voltage drop.

![Fig. 3. Relative spin polarization of the pumped current as a function of Zeeman energy for: (a) \( N = 4 \) and different temperatures: \( T/\Delta = 0 \) (upper curve), 0.1, 0.3, 0.5, 1.0, and 2.0; (b) \( T = \Delta \) and different numbers of channel.](image-url)
Recently, it was suggested [23,24] that while parametric pumping does not survive the loss of phase coherence, another mechanism of charge transfer comes into play when dephasing is strong. We believe, however, that this incoherent mechanism cannot be used to produce a spin pumping. The reasoning is as follows. Charge dephasing affects both quantum pumping and rectification mechanisms for generating dc spin-polarized currents. In both cases, dephasing washes out the intricate wave function interference patterns responsible for fluctuations in the conductance. Even if the dephasing rate \( \gamma < \frac{1}{\tau_0} \), where \( \tau_0 \) is the characteristic time scale of the system, the wave function content of spin up and spin down transport matrix elements will become essentially the same. In that case, we expect \( I \approx I_\parallel \) and therefore no net spin current.

Finally, we emphasize that, provided the quantum dot is maintained open during the pumping cycle, the Coulomb interaction does not alter the predictions of random matrix theory upon which our analytical calculations are based [25]. Nevertheless, in principle, spin pumping could be achieved in closed dots by somewhat related mechanisms [26]. In that case, Coulomb blockade should be taken into account. Electron-electron interactions are also fundamental in quantum wires [13] and may lead to effects such as spin transport quantization.

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[15] Notice that the enhancement by a factor of 2 has nothing to do with any change from orthogonal to unitary symmetry class.
[16] We assume that a weak, nonquantizing perpendicular magnetic field is also applied and time-reversal symmetry is broken at all times. We thus carry our calculations for the unitary symmetry class.
[17] By restricting our analysis to this limit, we avoid having to consider heating and nonequilibrium effects. For example, in Ref. [6], \( \omega/2\pi = 50 \text{ MHz} \approx 0.11 \mu\text{eV} \).