

Estimating relative risk for dengue disease in Peninsular Malaysia using INLA

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Abstract

Study in spatio-temporal disease mapping models give a great worth in epidemiology, in describing the pattern of disease incidence across geographical space and time. This paper studies generalized linear mixed models (GLMM) for the analysis of spatial and temporal variability of dengue disease rates. For spatio-temporal study, the models accommodate spatially correlated random effects as well as temporal effects together with the space time interaction. The space time interaction is used to capture any additional effects that are not explained by the main factors of space and time. However, as study including time dimension is quite complex for disease mapping, the temporal effects that only relate to structured and unstructured time pattern are considered in these models as initial screening in studying disease pattern and time trend. The models are fitted within a hierarchical Bayesian framework using Integrated Nested Laplace Approximation (INLA) methodology. For this study, there are three main objectives. First, to choose the best model that represent the disease phenomenon. Second, to estimate the relative risk of disease based on the model selected and lastly, to visualize the risk spatial pattern and temporal trend using graphical representation. The models are applied to monthly dengue fever data in Peninsular Malaysia reported to Ministry of Health Malaysia for year 2015 by district level.

Keywords: Spatio-temporal analysis, Disease mapping, Bayesian estimation, GLMM, INLA

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INTRODUCTION

Disease mapping is a very active research field in investigating the spatial relationship of disease burden with the geographical distribution, risk factors in the environment and human populations. Year by year, numerous methods for disease mapping have been expanded in accordance with the growing amount of routinely collected health information worldwide. Recently, the combination study of spatial and temporal effects in disease mapping is being emphasizes compared to study on spatial effects only. This is because ignoring temporal evolution by assuming static in time is not always realistic for every disease especially for infectious diseases.

In disease mapping, disease rates in a population are regularly been used to visualize on a map rather than the number of disease count. Traditionally, standardized incidence ratio (SIR) was calculated as improvement for crude rate by dividing the observed disease case count with the expected number of observations, where the expected number of observations is very sensitive to the number of population. Uneven number of population in different areas leads to large variances in rates across the map and this results to unstable patterns of disease distribution. Besides that, a small change in the number of observations, would cause abrupt changes in the expected number of observations, which is known as the small number problems. Hence, to address the drawbacks of SIR, smoothing techniques for relative risk estimation have been developed by borrowing strength or information across neighbouring spatial units (Clayton and Kaldor, 1987). Smoothing techniques help to remove the variation in disease rates, reduce the effect of measurement errors, and better smoothing leads to less bias results in further analyses (Kang et al., 2016).

More interestingly, for spatio-temporal disease mapping studies, smoothing technique is not only relating to the use of information from spatial neighbours but the context is lengthened to borrowing temporal neighbours too. Information is shared in time in a similar manner as sharing information in space. Hence, risks are smoother and more reliable because now the model is based on greater amount of information.

Bayesian models have become a familiar approach for smoothing purposes, both empirical Bayes (EB) and fully Bayes (FB). Several studies like Clayton and Kaldor (1987), Marshall (1991) and Lahiri and Maiti (2000) used EB method for smoothing in their disease mapping studies while Besag et al. (1991), MacNab et al. (2004), and Wakefield (2007) applied FB. However, with the aid of modern programming, FB is preferably being used to solve the posterior distribution especially in a complex model that requires many parameters to be estimated. Commonly, estimating parameter with FB in most studies will involve Markov Chain Monte Carlo (MCMC) algorithm computation but this method requires a huge computation time and may lead to large Monte Carlo errors especially for a big data set. Furthermore, according to Schrödle and Held (2011), specific block-sampling algorithms have to be applied in order to get reliable estimates if complex spatial and spatio-temporal models are to be fitted.

In order to circumvent these drawbacks, an alternative method using integrated nested Laplace approximation (INLA) has been proposed by Rue et al. (2009) to compute the posterior marginals of all parameters of interest. This method is believed to provide precise parameter estimates in shorter time and more practical to use. Recently, the INLA method becomes an active research development in disease mapping and has been shown to work well with generalized linear

mixed models, Bayesian quantile additive mixed models, survival analysis, and spatio-temporal models (Martins et al., 2013).

Variant models in spatio-temporal disease mapping have been described in the literature including parametric and non-parametric time trend and space-time interactions, most of them based on conditional autoregressions (CAR) models with extension to Besag, York and Mollié (BYM) models. For instance, Bernardinelli et al. (1995b) proposed a linear time trend model which an additional linear and a differential time trend. Then, Assunção et al. (2001) modified the study by applying second degree polynomial. Knorr-Held (2000) focuses on the inclusion of space-time interactions using non-parametric time models by proposing four types of interactions together with four different prior distributions for the interactions. Ugarte et al. (2009) compare the performance of six space-time disease mapping models by adopt the extension proposed by Bernardinelli et al. (1995b) and Knorr-Held (2000). In other study, Martínez-Beneito et al. (2008) link spatio-temporal study with autoregressive approach.

The combination study of spatio-temporal model is very interesting to explore as this study is not yet in abundance as spatial model study. This may be due to difficulties of linking both spatial and temporal dependence on a single model. In this study, we will focus on general time trend model as a linear time trend model may be unrealistic for some case of study. It is common to observe some changes in time trends due to the changes of the environment effects, the improvement in treatments and the advancement in research. The objectives of this study are to choose the best model that represent the disease phenomenon, to estimate the relative risk of disease based on the model selected and to visualize the spatial pattern and temporal trend using graphical representation. The models are fitted using INLA methodology and dengue data will be applied in this study.

MATERIALS AND METHODOLOGY

Case study: Dengue in Peninsular Malaysia

Dengue is the most ordinary mosquito-borne viral disease of humans, mainly transmitted by the female mosquitos *Aedes aegypti* and *Aedes albopictus*. Due to the dramatically increase of dengue cases day by day, dengue has become a major world-wide public health concern especially for regions near in tropical and sub-tropical climate. According to Mia et al. (2013), the factors that contribute to the spread of dengue in Malaysia are the changes in climate factors such as warm temperature, increased rainfall, and relative humidity that indirectly serve a conducive condition for mosquito breeding. Besides that, factors such as unstoppping urbanization, massive infrastructure development, change in population number, deforestation, poor waste sanitation, inadequate domestic water supplies, faster modes of transportation, increased migration and internationally travel are also contributing to the dramatically increase of dengue (Shafie et al., 2015; Pang and Loh, 2016). Presently, dengue outbreak can only be controlled using vector-controlled methods as licensed vaccine still in the developmental stage. In Malaysia, the vector control strategies are adulticiding, larviciding, personal protection, environmental management, community participation, legislation, and integrated control. Besides that, personal protection such as the use of mosquito coils, insecticide mats, aerosols, and bed-nets are also give benefits in controlling dengue incidence.

With a deep concern on dengue incidence in Malaysia and in line with government’s effort to control this problem, statistically research on dengue with inclusion of spatial and temporal trend are considered because it is believed that there is a relationship between geographical areas and time points on dengue risk. It is hope that this research may help the target audiences in planning more systematic vector-control prevention programmes especially for hotspots areas and also areas that has a tendency to become hotspots area.

Areal data on dengue incidence in 86 districts in Peninsular Malaysia for year 2015 recorded by monthly is used in this study. This data is obtained from Vector Borne Disease Sector, Ministry of Health Malaysia. In Malaysia, every single dengue case is recorded properly to Vector Borne Disease Sector. It is compulsory to health officer to notify any suspected or confirmed dengue case to the nearest district

health office via online notification system within 24 hours of diagnosis.

Spatio-temporal models for disease mapping

The relative risk estimation typically involves generalized linear mixed models (GLMM). Let the study region, Peninsular Malaysia be divided into n districts. Data for each area, i ($i = 1, 2, \dots, n$) with time points, t ($t = 1, 2, \dots, T$) are available for study. The number of dengue cases, O_{it} conditional to the relative risk, r_{it} is assumed to have Poisson distribution with mean, $\mu_{it} = E_{it} r_{it}$.

$$O_{it} | r_{it} \sim \text{Poisson}(\mu_{it} = E_{it} r_{it}) \tag{1}$$

where E_{it} is an expected number of cases,

$$E_{it} = N_{it} \times \left(\frac{\sum_{i=1}^n \sum_{t=1}^T O_{it}}{\sum_{i=1}^n \sum_{t=1}^T N_{it}} \right) \tag{2}$$

and N_{it} refers to number of population.

Taking logarithm to the both side of the mean, μ_{it} leads to

$$\log(\mu_{it}) = \log(E_{it}) + \log(r_{it}) \tag{3}$$

Then, different models are defined depending on the specification of $\log(r_{it})$.

General time trend models

The general time trend models describe here are similar to those proposed by Knorr-Held (2000). The log-risk is modelled as

$$\log r_{it} = \alpha + \xi_i + \phi_t + \gamma_t + \delta_{it} \tag{4}$$

where α is logarithm of the global risk, ξ_i is refer to spatial effect, ϕ_t is defined as unstructured temporal effect, γ_t is structured temporal effect, and δ_{it} is space-time interaction effect.

From Eq. (4) ξ , ϕ , and γ represent main effects and δ represents interaction effect. The prior distribution used for $\xi = (\xi_1, \xi_2, \dots, \xi_n)$ follows the Leroux et al. (2000) CAR prior, defined as $\xi \sim N(\mathbf{0}, \mathbf{Q}^{-1})$, where \mathbf{Q}^{-1} is the inverse of precision matrix.

$$\mathbf{Q}^{-1} = \sigma_s^2 (\lambda_s \mathbf{R}_s + (1 - \lambda_s) \mathbf{I}_s)^{-1} \tag{5}$$

Here, the subscript s refers to spatial elements where σ_s^2 is a spatial variance component, λ_s is a spatial smoothing parameter taking values between 0 and 1, \mathbf{I}_s is an $n \times n$ identity matrix and \mathbf{R}_s is a spatial neighbourhood matrix. The entries of matrix \mathbf{R}_s follow the following rules.

$$(R_s)_{ij} = \begin{cases} w_{ij}, & i = j \\ -1, & i \sim j \\ 0, & \text{otherwise} \end{cases} \tag{6}$$

be specified correspond to the precision parameters which are the inverse of the variance components; $t_s = 1/s_s^2$, $t_j = 1/s_j^2$, $t_g = 1/s_g^2$, and $t_d = 1/s_d^2$. The hyperpriors distributions used in this paper are similar to what has been proposed by Ugarte et al. (2014).

Besides that, to guarantee identifiability of the interaction term δ , specific sum-to-zero constraints have to be used except for Type I interaction. The vector δ follows an intrinsic Gaussian Markov random field (IGMRF). An IGMRF is improper and its structure matrix, R_δ is not of full rank. The improper density, $\pi^*(\delta)$ can be written as

$$\pi^*(\delta) = \pi(\delta | A\delta = e) \tag{12}$$

where $A\delta = e$ are linear constraints δ , A is a matrix consists of R_δ eigenvectors which span the null space, and e is a vector of zeros. The number of necessary linear constraints is always equal to the rank deficiency of R_δ .

Interestingly, in the INLA approach, the deviance information criterion (DIC) can be computed for selecting the best model. According to Spiegelhalter et al. (2002), DIC is the sum of the deviance posterior mean, \bar{D} (a measure for model fit) and the effective parameters number, p_D (a measure for model complexity). The lowest DIC values provides the best trade-off between model fit and model complexity.

$$DIC = \bar{D} + p_D. \tag{13}$$

In this study, R-programming via the R-INLA package is used for completing the methodology that has briefly described above.

RESULTS AND DISCUSSION

Table 2 DIC values for the study models.

Model	Space-time interaction	\bar{D}	p_D	DIC
1	Additive model	19172.65	97.19382	19269.84
2	Type I	5990.825	765.7633	6756.588
3	Type II	6003.618	641.8277	6645.446
4	Type III	6172.708	696.5397	6869.248
5	Type IV	6196.147	581.0601	6777.207
6	Additive model	19172.55	97.19417	19269.75
7	Type II	6003.29	641.8658	6645.156
8	Type IV	6196.199	580.9653	6777.164

Table 2 shows the result for the eight fitted models that has been described previously. This result is based on a simplified Laplace approximation. The additive models exhibit the highest values of DIC and show the worst fit although their estimated model complexity is lower. This result implies the importance of including space-time interaction in the study model. The models without unstructured temporal component seem slightly better although the difference of the DIC value between model with and without unstructured temporal component is too small. This may imply the inclusion or exclusion of the unstructured temporal component for this study model is not too important. Among the eight models proposed, Model 7 has the smallest DIC values. Hence, Model 7 is chosen as the best model in terms of model fit and complexity. This model consists of the spatial effect with

a Leroux CAR prior, a structured temporal effect with a RW1 prior and a type II interaction. Then after choosing the best model, this selective model has been fitted again using the ‘full Laplace’ approximation and the result is used for relative risk computation.

The estimated log-relative risks obtained with Model 7 can be separated into individual components: an overall global risk (\hat{a}), a risk related to the spatial location (\hat{x}), a temporal risk trend (\hat{g}) common to all areas, and an area specific temporal risk trend (\hat{d}) for each district. These are useful as the spatial and temporal effects can be varied across time and districts respectively.

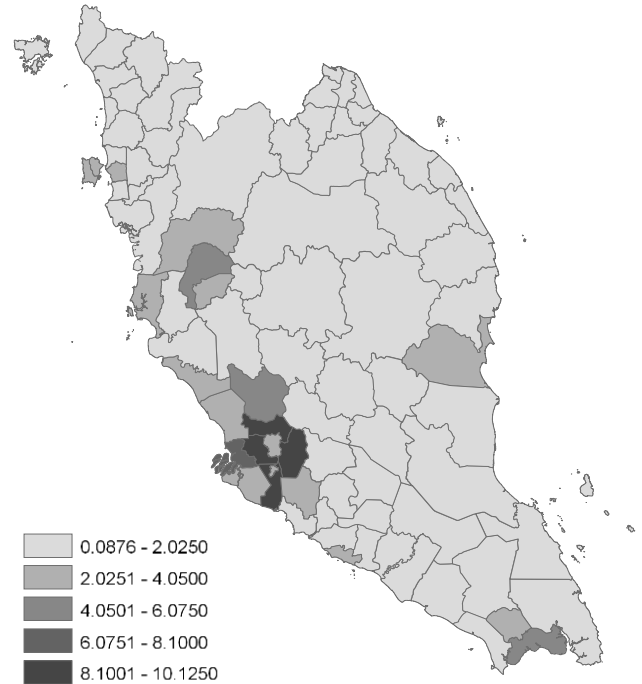


Fig. 2 The spatial pattern of dengue risk map, $\hat{z}_i = e^{\hat{x}_i}$.

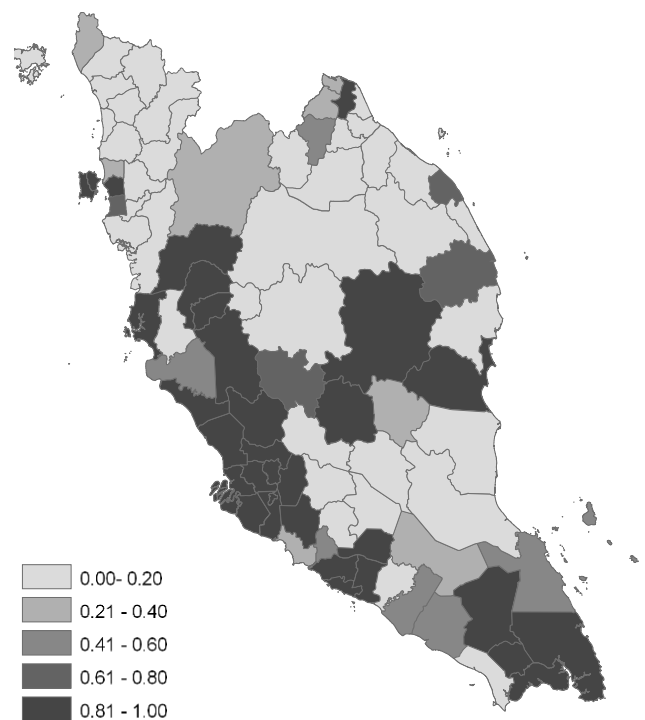


Fig. 3 The posterior probabilities map, $P(\hat{z}_i > 1 | \mathbf{O})$.

Fig. 2 presents the map of spatial dengue risk, $\hat{z}_i = e^{\hat{\zeta}_i}$ associated to each district and constant along the year. Meanwhile, Fig. 3 presents the posterior probability that the spatial risk is greater than 1, $P(\hat{z}_i > 1 | \mathbf{O})$. The degree of spatial risk is differentiated with different shades. The darker the region indicates the region's risk is higher. For simplicity, usually in the disease mapping studies, the regions with probabilities above 0.8 and 0.9 are considered as high risk regions, similar to what Richardson *et al.* (2004) has suggested. In this study, a reference threshold equal to 1 and cut-off value of 0.8 is used to detect high risk regions in all the time periods. Hence, from the both figure, Fig. 2 and Fig. 3, it is clearly seen that the districts in Selangor, Kuala Lumpur, Penang, Melaka, Southern part of Johor, and some districts in Perak and Pahang are high risk areas of dengue in year 2015.

Fig. 4 presents the line graph of the general temporal trend of dengue risk common to all districts in Peninsular Malaysia. The line graph shows a non-linear trend with a decreasing trend for the first four months and a drastic increasing pattern to the seventh month as well as a fluctuating pattern until the end of the year. This trend indicates that there might be some factors that are affecting the dengue outbreaks in Peninsular Malaysia along this period such as the climate changes or the prevention schedule.

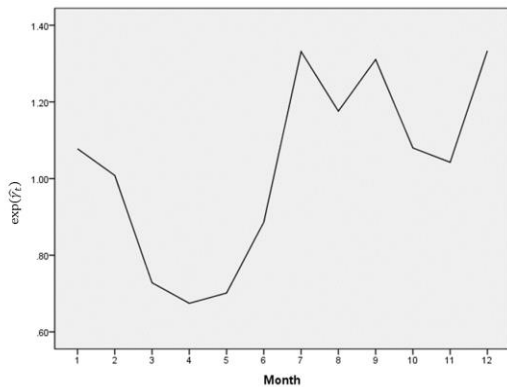


Fig. 4 The general temporal trend of dengue risk.

For the specific temporal trends, five selected districts are chosen for representing the northern, eastern, southern, western, and middle part of Peninsular Malaysia in order to see the temporal trend of different districts. These specific temporal trends (in log scale) are represented by Fig. 5 until Fig. 9. These line graphs are not converted to actual values because we are only interested to see their pattern as using the actual values will reveal the same pattern too. Kota Bharu, Kota Setar and Kuantan show slightly similar pattern which is a decreasing trend towards the middle of the year and increasing trend after that. However, Kuala Lumpur and Johor Bahru display a different trend. The temporal trend for Kuala Lumpur is quite steady along the year while for Johor Bahru, the time effect is higher in the middle of the year.

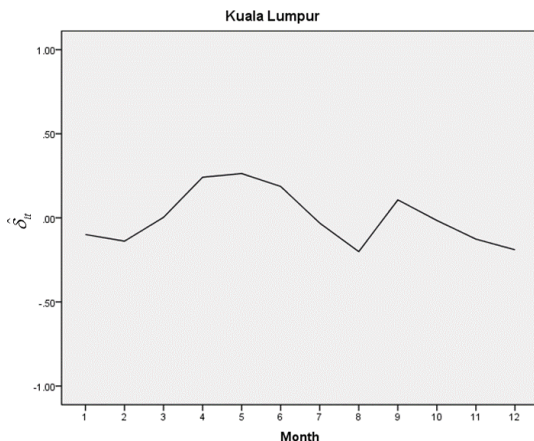


Fig. 5 Specific temporal trend for Kuala Lumpur.

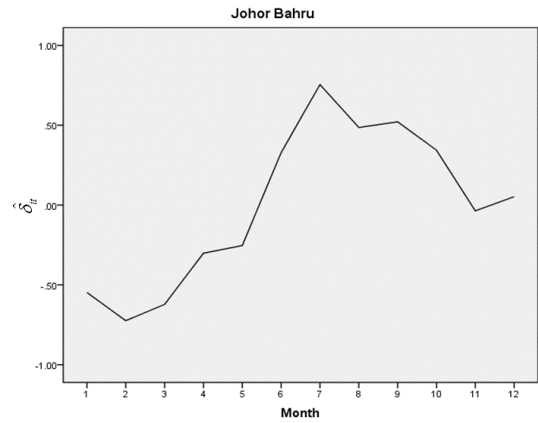


Fig. 6 Specific temporal trend for Johor Bahru.

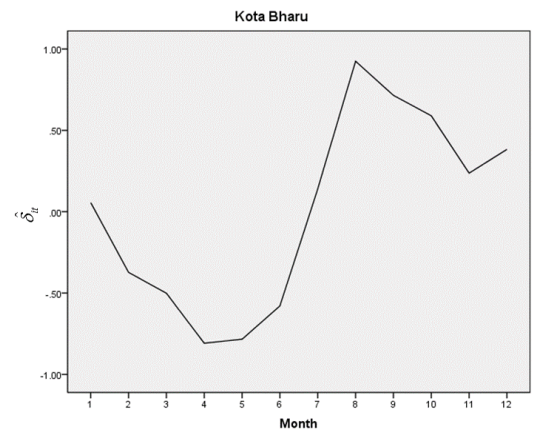


Fig. 7 Specific temporal trend for Kota Bharu.

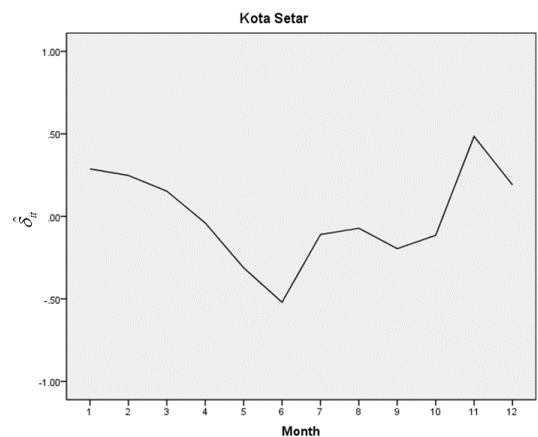


Fig. 8 Specific temporal trend for Kota Setar.

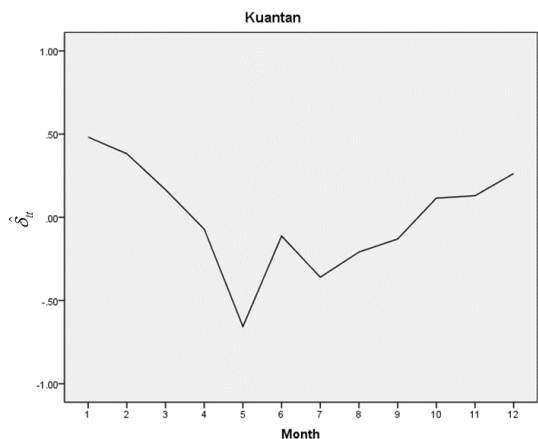


Fig. 9 Specific temporal trend for Kuantan.

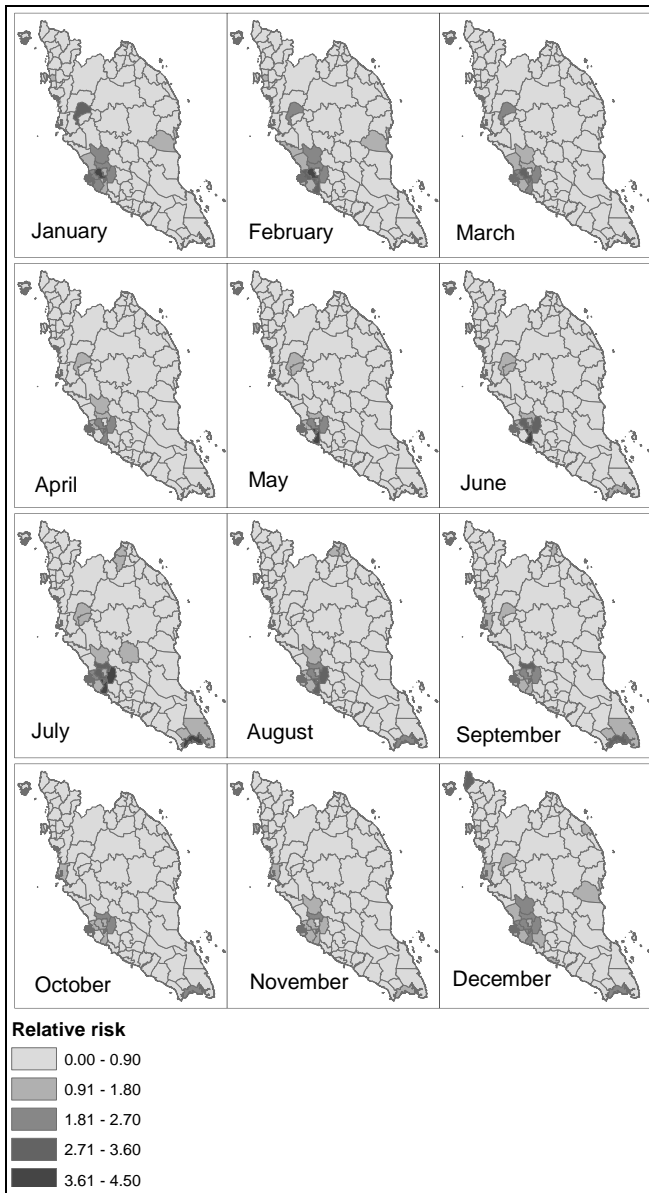


Fig. 10 Relative dengue risk distribution.

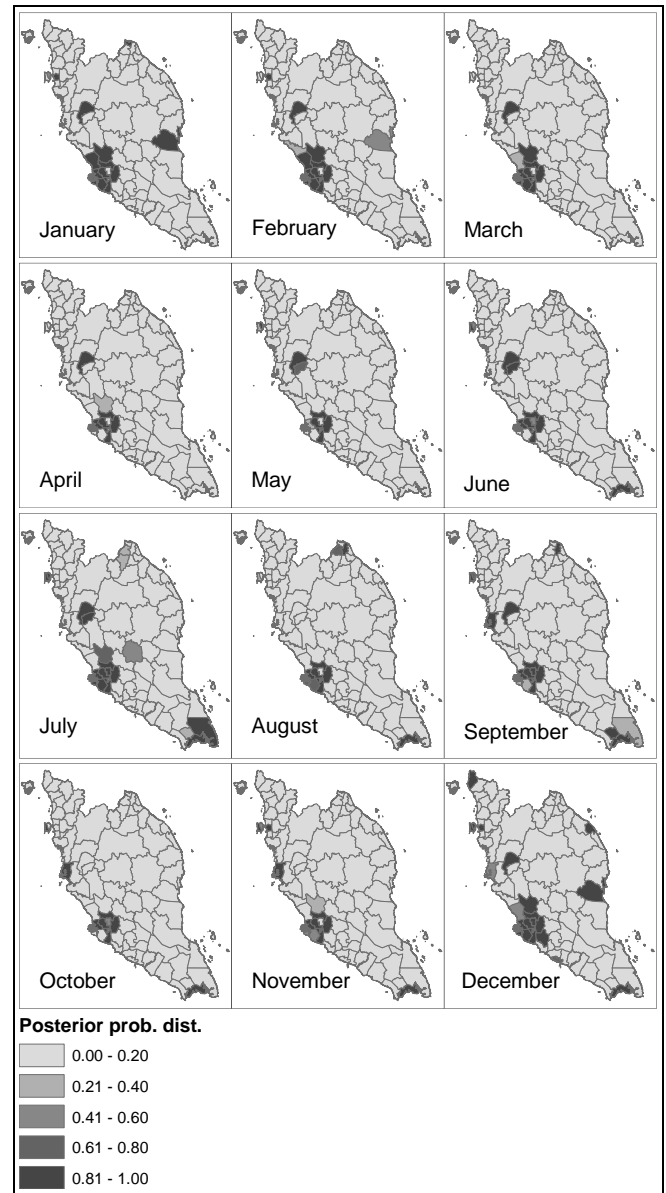


Fig. 11 Posterior probability distribution, $P(\hat{\rho}_t > 1 | \mathbf{O})$ by districts.

Fig. 10 and Fig. 11 display the maps of relative risk of dengue and the posterior probabilities that the relative risk greater than 1, $P(\hat{\rho}_t > 1 | \mathbf{O})$ for each district in Peninsular Malaysia from January to December of 2015 respectively. These figures give a clearer graphical representation in visualizing dengue disease phenomenon for all areas throughout the study period. Based on information from both figures, there are several districts that show high significant risk of dengue disease in Peninsular Malaysia for year 2015. A group of districts near to the most urbanized area in Peninsular Malaysia, Kuala Lumpur shows high significant risk throughout the year. Other than that, Kinta also shows high dengue risk for almost every month. Meanwhile, the most southern district, Johor Bahru exhibits high dengue risk during June until December with its neighbours Kota Tinggi and Kulai Jaya are also slightly affected during July and September. The rest of the areas do not give any clearer pattern of relative risk and just report high case for certain month.

CONCLUSION

Our analysis of the dengue case in Peninsular Malaysia for year 2015 shows that the gap of the relative risks of dengue between the districts under study is big. There are areas that show significant high risk throughout the year such as areas near to the capital city of

Malaysia, Kuala Lumpur which are Petaling, Sepang, Hulu Langat, Gombak, Klang and Hulu Selangor. Meanwhile, Seberang Perai Tengah, Kinta, Kuantan and Johor Bahru have a tendency to become high dengue risk area. Hence, the authorities in charge should give prioritized to these areas in planning intervention strategies to reduce the dengue cases. The rest of the districts are still under control. However, precaution must be continued and monitor from time to time. Besides that, the results obtained also shows that some areas have different temporal trends in dengue outbreak compare to other areas. Hence, we can get some ideas on the effective time for vector control activities for each district in Peninsular Malaysia. For example, areas like Kota Setar, Kota Bharu and Kuantan, the prevention control should focus more on the earlier and at the end of the year, Johor Bahru in the middle of the year while Kuala Lumpur, the prevention should be for the overall months in the year.

In general, this study provides a useful starting point for spatio-temporal dengue analysis. The result in this study can be used in clustering analysis, hotspot identification and also spatial regression. As dengue is a major infectious disease in Malaysia and believe to have strong relationship with environmental factors, adding seasonal effects in the spatio-temporal model might give more appropriate model for dengue study. Besides that, instead of using monthly data, this model can be rerun using weekly data with other suitable time series model such as autoregressive first order model (AR1).

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