



Offer, Rachel F. and Conway, Johnathan W. C. and Riis, Erling and Franke-Arnold, Sonja and Arnold, Aidan S. (2016) Cavity-enhanced frequency up-conversion in rubidium vapour. Optics Letters, 41 (10). pp. 2177-2180. ISSN 0146-9592 , <http://dx.doi.org/10.1364/OL.41.002177>

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Cavity-enhanced frequency up-conversion in rubidium vapour

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Compiled April 25, 2016

We report the first use of a ring cavity to both enhance the output power and dramatically narrow the linewidth (< 1 MHz) of blue light generated by four wave mixing in a rubidium vapour cell. We find that the high output power available in our cavity-free system leads to power broadening of the generated blue light linewidth. Our ring cavity removes this limitation, allowing high output power and narrow linewidth to be achieved concurrently. As the cavity blue light is widely tunable over the ^{85}Rb $5S_{1/2}$ $F=3 \rightarrow 6P_{3/2}$ transition, this narrow linewidth light would be suitable for near-resonant rubidium studies including, for example, second-stage laser cooling.

OCIS codes: (190.4380) Nonlinear optics, four-wave mixing; (270.1670) Coherent optical effects; (140.4780) Optical resonators.

<http://dx.doi.org/10.1364/ao.XX.XXXXXX>

Atomic vapours are a versatile tool for studying a wide range of nonlinear phenomena. In particular, quasi-resonant atomic systems allow processes such as electromagnetically induced transparency, fast and slow light, lasing without inversion and four wave mixing (FWM) to be studied at low light intensities [1]. The resonant enhancement of FWM in a rubidium vapour is such that it can be used for efficient frequency up-conversion of near-infrared light (780 nm and 776 nm) to blue light (420 nm) [2–5]. For optimal pump detuning, vapour pressure and pump polarisation, modest power diode laser pumps can be used to generate 1 mW of coherent blue light, corresponding to a conversion efficiency of 260%/W [5]. Such efficient FWM has applications ranging from quantum information [6, 7] to second-stage laser cooling [8, 9] and sensitive atomic imaging [10, 11].

Recent work on FWM in rubidium systems has shown that transverse phase structure, for example orbital angular momentum (OAM), can be transferred between the pump and generated beams [12, 13]. The ability to efficiently transfer OAM between different wavelengths may be important for future applications of structured light [14], for example higher dimensional quantum information processing. Efficient FWM is not

restricted to this particular system and various wavelengths can be generated by making use of different atomic states [15–17] or different alkali metals [18]. High conversion efficiencies have also been demonstrated in rubidium-filled hollow-core photonic crystal fibers [19].

In this letter we investigate the effect of adding a ring cavity, singly resonant with the generated blue light, to our rubidium vapour FWM system [5]. We find that a low finesse cavity more than doubles the output power and greatly reduces the linewidth of the blue light produced. In previous single pass FWM experiments, for low output powers (around 10 μW), the linewidth of the coherent blue light has been reported to be ≤ 3 MHz [2, 20]. However, in our single pass setup, up to 340 μW of coherent emission can be generated. For these high output powers the linewidth of the blue light increases to around 33 MHz. This increase in linewidth is consistent with power broadening of the 420 nm transition due to the high peak blue light intensity, as discussed later in this work. Adding a ring cavity imposes stringent spectral coherence, allowing blue light to be generated with high output power (940 μW) as well as a narrow linewidth (≤ 1 MHz). FWM in a ring cavity using a purely near-infrared FWM scheme within rubidium has also recently been investigated [21].

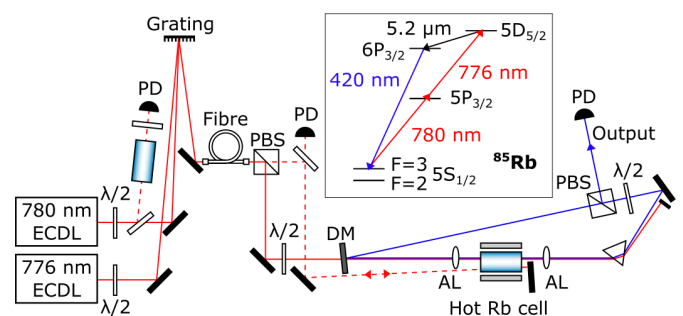


Fig. 1. Schematic of the experimental setup. Abbreviations used are: PD (photodiode), PBS (polarising beam splitter), DM (dichroic mirror) and AL (achromatic lens, $f = 200$ mm). Dashed lines represent spectroscopy probe beams used to monitor the 780 nm and 776 nm detunings.

Our experimental set-up and the relevant level scheme for 420 nm light generation in a rubidium vapour is shown in figure 1. The 780 nm and 776 nm pump beams undergo a single pass through a heated rubidium cell, exciting the two photon resonance between the $5S_{1/2}$ ground state and the $5D_{5/2}$ excited state. This develops a population inversion on the $5D_{5/2} \rightarrow 6P_{3/2}$ transition which produces a $5.2 \mu\text{m}$ field via amplified spontaneous emission (ASE) [2]. This initial ASE together with the pump lasers establishes three photon coherence on the $5S_{1/2} \rightarrow 6P_{3/2}$ transition, which in turn allows for the coherent emission of 420 nm light via FWM. The ring cavity is designed to be singly resonant with this generated blue light, adding a strong constraint on the blue light frequency. The cavity also enhances the effective length of the "laser medium", thereby increasing FWM conversion efficiency. One would expect that the cavity also has an impact on the phase matching conditions for the FWM process, which we will investigate in the future.

The 780 nm and 776 nm pump beams are provided by two free running extended-cavity diode lasers (ECDLs). To ensure they are copropagating the pump beams are overlapped on a grating and then coupled into a polarisation maintaining single mode optical fibre. The combined 780 nm and 776 nm fibre output is then horizontally polarised before entering the cavity through a dichroic mirror. Two achromatic lenses form a $2f$ imaging system ($f = 200 \text{ mm}$) that focusses the near-IR pump beam to a e^{-2} radius of $52 \mu\text{m}$ in the centre of the heated rubidium cell. The cell is 25 mm long and contains ^{87}Rb and ^{85}Rb in their natural abundancies. The cell vapour temperature was determined to within $\pm 1^\circ\text{C}$ using absorption spectroscopy of a weak ($1 \mu\text{W}$) collimated 780 nm probe beam [22].

FWM within the rubidium vapour produces horizontally polarised 420 nm light, copropagating with the pump beams. Light at $5.2 \mu\text{m}$ is also generated [17] but it is not observed in our setup as it is absorbed by the glass cell. In order for the cavity to be singly-resonant with the blue light we use a prism

to separate the 420 nm light from the near-IR pump beam. The pump beam is then blocked and the blue light is fed back to the heated cell. A half waveplate and a polarising beam splitter (PBS) are used to couple light out of the cavity. The waveplate allows the amount of output coupling to be controlled. We have studied the effect of the cavity on FWM for 65% and 5% output coupling, which correspond to a cavity finesse of 3.5 and 12.8 respectively. The parasitic loss in our cavity is around 25%, the majority of this is due to loss at the PBS and the four 4% reflections at the cell.

Firstly, we will discuss the effect of the cavity on blue output power. We do this by comparing the output power as a function of 776 nm detuning for single pass FWM and with-cavity FWM, shown by the red and blue curves in figure 2. The output power was monitored using a photodiode at the cavity output and the single pass results were recorded simply by blocking the cavity after the PBS. When recording spectra the 780 nm laser was set to the detuning for maximum single pass blue power, as detailed in figure 2. The 776 nm detuning was determined by 780 nm and 776 nm two photon spectroscopy in the heated Rb cell and is given relative to the ^{85}Rb $5P_{3/2} F=4 \rightarrow 5D_{5/2} F=5$ transition. The 780 nm detuning (relative to the ^{85}Rb $5S_{1/2} F=3 \rightarrow 5P_{3/2} F=4$ transition) was determined by saturated absorption spectroscopy in a room temperature Rb cell.

For single pass FWM, as the 776 nm laser is scanned across the ^{85}Rb $5P_{3/2} \rightarrow 5D_{5/2}$ transition, there are two detunings for which blue light is produced, near $\Delta_{776} = -1.8 \text{ GHz}$ and $\Delta_{776} = 1.2 \text{ GHz}$. These correspond to two-photon resonance with the $5S_{1/2} F=3 \rightarrow 5D_{5/2}$ and $5S_{1/2} F=2 \rightarrow 5D_{5/2}$ transitions respectively. In the cavity-enhanced results this same behaviour is observed but with the addition of large increases in blue output power when the 420 nm light, whose frequency scans with the 776 nm frequency, is resonant with the cavity.

Due to energy conservation, the frequency of the FWM fields must satisfy the condition $\omega_{780} + \omega_{776} = \omega_{5200} + \omega_{420}$, where

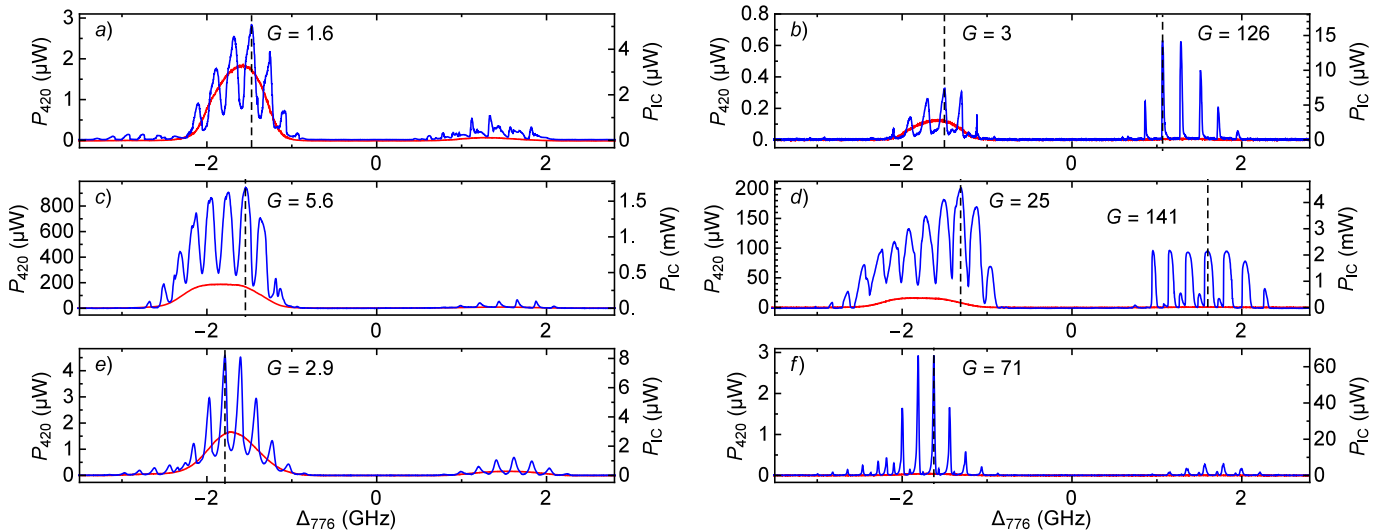


Fig. 2. Blue output power as a function of 776 nm detuning for a single pass (P_{SP} , red lines) and with the cavity (P_C , blue lines). The right hand scale shows the blue intracavity power, P_{IC} . Plots a) - f) correspond to the following conditions: a), b) 130°C , 1.6 mW 780 nm, 2.7 mW 776 nm; c), d) 130°C , 13 mW 780 nm, 23 mW 776 nm; e), f) 90°C , 13 mW 780 nm, 23 mW 776 nm. Cell temperatures of 130°C and 90°C correspond to vapour pressures of 0.12 Pa and 0.009 Pa respectively. The output coupling at the PBS was 65% for a), c) and e) and 5% in b), d) and f). Absolute frequency scales are accurate to $\pm 0.1 \text{ GHz}$. The 780 nm detuning, chosen to maximise single pass blue power, was a), b) 1.7 GHz; c), d) 1.8 GHz; e), f) 1.6 GHz. Representative values of the gain, $G = P_C / P_{SP}$, are shown, with the detuning each value was calculated at marked by a vertical dashed line.

ω_{780} , ω_{776} , ω_{5200} and ω_{420} are the frequency of the 780 nm, 776 nm, 5200 nm and 420 nm fields respectively. As a result, if the frequency of either of the pump lasers is changed then ω_{420} or ω_{5200} (or both) must change accordingly. For the case of near resonant stepwise excitation of the $5S_{1/2} \rightarrow 5D_{5/2}$ transition it has been shown that the 420 nm frequency exactly mirrors changes in pump frequency [23], suggesting that the 5.2 μm field remains resonant with the atomic transition. However, if the pump lasers are far off resonance (1 THz) with the $5P_{3/2}$ state then it has been reported that ω_{5200} can vary as well as ω_{420} [24]. In our experiment we have measured (using a scanning Fabry-Perot interferometer) the change in ω_{420} due to a change in ω_{776} to be given by $\Delta\omega_{420} = 0.92(1)\Delta\omega_{776}$. This indicates that ω_{5200} and ω_{420} have mutual tuning consistent with relative Doppler shifts, as seen in Ref. [24], likely due to the detuning of our pump lasers from the $5P_{3/2}$ intermediate state (< 2 GHz). The mean separation of the observed cavity resonances in figure 2 is 198(2) MHz. This corresponds to a change in 420 nm frequency of 182(2) MHz, which is in strong agreement with the expected free spectral range based on the length of our cavity, 181.9(3) MHz.

The result shown in figure 2 c) was obtained for the conditions we determined optimal for single pass FWM: a cell temperature of 130 °C and maximum available pump powers (13 mW 780 nm, 23 mW 776 nm). In this case 340 μW of single pass blue light is generated directly after the cell. The cavity output coupling was set to 65%. This value was chosen as it produced maximum cavity-enhanced output power. Under these conditions a peak of 940 μW of output power was produced at the cavity output; 2.8 times the power after the cell for a single pass.

To fully understand the with-cavity trace in figure 2 c) a theoretical model of the system is required. Such a model is beyond the scope of this letter, but in order to ascertain which processes would be of particular importance to such a model we have recorded spectra for a wide range of conditions: reduced cell temperature (figure 2 e) and f)), reduced pump power (figure 2 a) and b)) and decreased output coupling (right hand column of figure 2).

Firstly, we note that for high conversion efficiency, as in figure 2 c) and d), saturation effects become important, as can be seen by the flattening off of the resonances. This is particularly obvious for positive detuning in figure 2 d). Another feature of the high conversion efficiency traces is that the cavity enhances the blue output power even when it appears to be off resonant. As Δ_{776} changes, the 420 nm light will come in and out of resonance with the cavity. One would therefore expect the with-cavity output power to vary above and below the single pass output power, unlike in figure 2 c) and d). Both reducing the pump power, figure 2 a) and b), and reducing the cell temperature, figure 2 e) and f), cause the minimum cavity-enhanced power to be less than the single pass power, as expected.

By comparing the width of the resonances in each of the traces in figure 2 the predominant broadening mechanisms can be determined. Both reduced cell temperature and reduced pump power result in a narrowing of resonances. This suggests that power broadening of the 420 nm transition dominates over collision broadening. Comparing the left and right column in figure 2 it is also clear that the resonance width of the "passive" cavity (determined by the finesse) also plays a role. For 65% output coupling (left column) the passive cavity resonance width is 51 MHz, whilst for 5% output coupling (right column) it is reduced to 14 MHz. In figure 2 e) and f) this decrease is

enough to outweigh the increase in power broadening due to the increased intracavity power, and so the resonances in f) are narrower. In figure 2 c) and d) however the opposite is true, the change in power broadening is largest and consequently the resonances are broader for reduced output coupling.

However, it is clear that power broadening and the cavity finesse are not the only broadening mechanisms. For example, figure 2 a) has wider peaks than figure 2 e), for similar intracavity power, suggesting that collision broadening may have some contribution. Moreover, in figure 2 b) the cavity resonances near the $F = 2$ two-photon transition (positive detuning) are narrower and give much higher gain than those near the $F = 3$ transition (negative detuning). A theoretical model of the system will undoubtedly provide insight into this behaviour.

We have also demonstrated that the cavity significantly decreases the linewidth of the generated blue light. We obtained the linewidth by beating the FWM blue beam against a 420 nm ECDL (Newport Vantage tunable diode laser) and measured the resulting beat note using a spectrum analyser. The frequency of the 420 nm ECDL was monitored using saturated absorption spectroscopy, allowing the absolute frequency of the blue FWM light to be determined as well as the linewidth. Figure 3 shows the result of the beat note measurement for single pass and cavity-enhanced blue light generation, taken at both 90 °C and 130 °C. The 780 nm and 776 nm pump powers were 13 mW and 23 mW respectively. In the following we will first briefly discuss the beat note obtained for blue light gener-

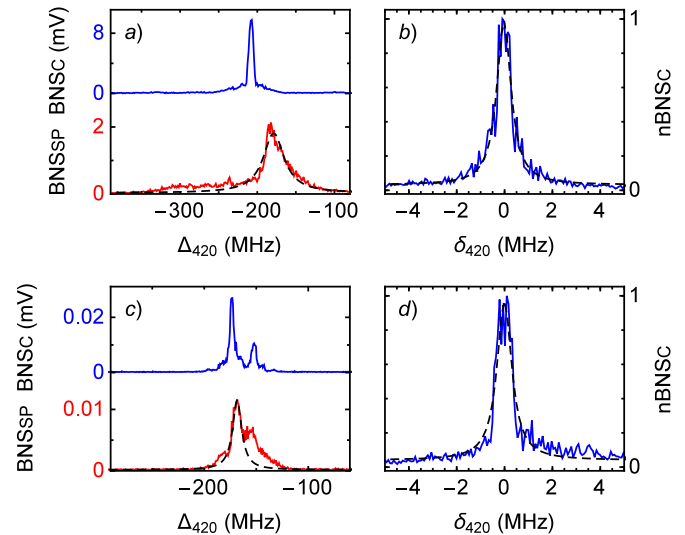


Fig. 3. Beat note between the FWM blue light and a 420 nm ECDL. The FWM cavity conditions were: 65% output coupling, 13 mW 780 nm, 23 mW 776 nm and cell temperature a), b) 130 °C and c), d) 90 °C. The 780 nm and 776 nm detunings were within 0.1 GHz of their optimal detunings for single pass FWM. Plots a) and c) compare the single pass (red, BNSp) and cavity-enhanced (blue, BNSc) beat note, Δ_{420} gives the detuning of the FWM blue light from the ^{85}Rb $5S_{1/2}$ $F=3 \rightarrow 6P_{3/2}$ $F=4$ transition, to within ± 25 MHz. In a) and c) the width of the cavity-enhanced BNS is limited by the signal analyser sweep rate; b) and d) show the normalised BNSc (nBNSc) over a smaller scan range on a relative frequency scale. Image d) shows only the larger of the two peaks in c). The dashed lines are Lorentzian fits with FWHM a) 33 MHz; b) 0.7 MHz; c) 11 MHz and d) 0.7 MHz.

ated via single pass FWM, and then go on to discuss the cavity-enhanced case.

The single pass beat note, both at 90 °C and 130 °C, is composed of more than one subpeak. Similar substructure has been observed previously in [2] where it was explained by the $6P_{3/2}$ hyperfine splitting of 10, 20 and 40 MHz between the $F'=1, 2, 3, 4$ levels. However, in our measurement the width of the subpeaks makes it difficult to determine if the substructure we observe is from the same source. Fitting to one of the subpeaks of the observed beat note signal gives the beat note linewidth to be 11 MHz (33 MHz) at 90 °C (130 °C). We attribute this difference in FWHM to power broadening of the 420 nm transition, as collision broadening of the 420 nm transition is negligible. Based on the single pass blue power and the e^{-2} radius of the blue light in the rubidium cell (46 μm), we calculate the power broadened width of the 420 nm transition to be 4 MHz (41 MHz) at 90 °C (130 °C) [25].

For a single pass, we find that maximal blue light is generated slightly red detuned from the 420 nm transition, as shown in figure 3 a) and c). These detunings are within a Doppler width of the 420 nm resonance and so are in agreement with previous work [23]. In addition, we find that the blue light can be tuned easily to frequencies either side of the transition, with a FWHM tuning range of 920(25) MHz and 770(25) MHz at 130 °C and 90 °C respectively.

Figure 3 b) and d) show the beat note for the cavity-enhanced blue light. At both 130 °C and 90 °C the linewidth is dramatically narrowed to ≤ 1 MHz FWHM. For the 130 °C cell the beat note produced is a single sharp peak of FWHM 0.7 MHz. At 90 °C the with-cavity light has a similar linewidth but there is an additional secondary peak in the beat note signal. As this beat note is for the cavity-enhanced case this secondary peak is likely due to a cavity mode, rather than due to hyperfine processes, indeed measurements of the beam profile at the cavity output indicate that it may be due to higher order transverse modes.

The beat note linewidth will have some contribution from the linewidth of the 420 nm ECDL used for the beat note measurement. To estimate this contribution the linewidth of the ECDL was measured separately by recording the frequency noise at the side of a Doppler broadened transmission feature. The autocorrelation of the laser frequency noise at 0.1 ms was found to be 0.5 MHz. The 0.1 ms time scale is relevant as it corresponds to the time taken for the spectrum analyser to scan over the FWHM of the with-cavity beat note signals. This suggests that a large proportion of the beat note FWHM may come from the ECDL linewidth, and therefore the linewidth of the cavity-enhanced FWM light will be much less than 0.7 MHz on a 0.1 ms time scale. On the same timescale, the autocorrelation of the 780 nm and 776 nm pump lasers are 0.2 MHz and 0.6 MHz respectively. This suggests that the cavity is able to narrow the linewidth of the FWM light to less than the total linewidth of the pump fields.

In conclusion, we have demonstrated the first use of a ring cavity to both enhance the power output and dramatically narrow the linewidth of blue light generated via FWM in a rubidium vapour cell. For a cell temperature of 130 °C the resulting output power is nearly 1 mW (nearly three times the output power of the cavity-free case) and the linewidth drops from a power broadened 33 MHz to less than 1 MHz. Furthermore, the blue light is generated with a frequency close to the ^{85}Rb $5S_{1/2} \rightarrow 6P_{3/2}$ transition and is tuneable over a FWHM range of almost 1 GHz. The increased output power, narrow linewidth

and large tuning range could make this FWM in a ring cavity system a valuable light source for efficient ^{85}Rb BEC production [26]. In addition, if the input laser powers were increased or the large parasitic losses present in our cavity minimised, for example by using an anti-reflection coated or Brewster cell, then even larger output powers would be possible.

FUNDING INFORMATION

We are very grateful to the Leverhulme Trust for funding this project via grant RPG-2013-386. The 420 nm laser used in this project was funded by the InnovateUK project QuDOS.

REFERENCES

1. M. Fleischhauer, A. Imamoglu, and J. P. Marangos, *Rev. Mod. Phys.* **77**, 633 (2005).
2. A. S. Zibrov, M. D. Lukin, L. Hollberg, and M. O. Scully, *Phys. Rev. A* **65**, 051801 (2002).
3. A. M. Akulshin, R. J. McLean, A. I. Sidorov, and P. Hannaford, *Opt. Express* **17**, 22861 (2009).
4. T. Meijer, J. D. White, B. Smeets, M. Jeppesen, and R. E. Scholten, *Opt. Lett.* **31**, 1002 (2006).
5. A. Vernier, S. Franke-Arnold, E. Riis, and A. S. Arnold, *Opt. Express* **18**, 17020 (2010).
6. T. P. Spiller, W. J. Munro, S. D. Barrett, and P. Kok, *Contemp. Phys.* **46**, 407 (2005).
7. R. M. Camacho, P. K. Vudyasethu, and J. C. Howell, *Nat. Photonics* **3**, 103 (2009).
8. D. C. McKay, D. Jervis, D. J. Fine, J. W. Simpson-Porco, G. J. A. Edge, and J. H. Thywissen, *Phys. Rev. A* **84**, 063420 (2011).
9. P. M. Duarte, R. A. Hart, J. M. Hitchcock, T. A. Corcovilos, T.-L. Yang, A. Reed, and R. G. Hulet, *Phys. Rev. A* **84**, 061406(R) (2011).
10. D. V. Sheludko, S. C. Bell, R. Anderson, C. S. Hofmann, E. J. D. Vredenbregt, and R. E. Scholten, *Phys. Rev. A* **77**, 033401 (2008).
11. B. Yang, Q. Liang, J. He, and J. Wang, *Opt. Express* **20**, 11944 (2012).
12. G. Walker, A. S. Arnold, and S. Franke-Arnold, *Phys. Rev. Lett.* **108**, 243601 (2012).
13. A. M. Akulshin, I. Novikova, E. E. Mikhailov, S. A. Suslov, and R. J. McLean, arXiv preprint: 1601.01368 (2016).
14. S. Franke-Arnold, L. Allen, and M. Padgett, *Laser Photon. Rev.* **2**, 299 (2008).
15. F. E. Becerra, R. T. Willis, S. L. Rolston, and L. A. Orozco, *Phys. Rev. A* **78**, 013834 (2008).
16. J. F. Sell, M. A. Gearba, B. D. DePaola, and R. J. Knize, *Opt. Lett.* **39**, 528 (2014).
17. A. Akulshin, D. Budker, and R. McLean, *Opt. Lett.* **39**, 845 (2014).
18. J. T. Schultz, S. Abend, D. Döring, J. E. Debs, P. A. Altin, J. D. White, N. P. Robins, and J. D. Close, *Opt. Lett.* **34**, 2321 (2009).
19. P. Londero, V. Venkataraman, A. R. Bhagwat, A. D. Slepikov, and A. L. Gaeta, *Phys. Rev. Lett.* **103**, 043602 (2009).
20. A. Akulshin, C. Perrella, G.-W. Truong, A. Luiten, D. Budker, and R. McLean, *Appl. Phys. B* **117**, 203 (2014).
21. E. E. Mikhailov, J. Evans, D. Budker, S. M. Rochester, and I. Novikova, *Opt. Eng.* **53**, 102709 (2014).
22. P. Siddons, C. S. Adams, C. Ge, and I. G. Hughes, *J. Phys. B: At. Mol. Opt. Phys.* **41**, 155004 (2008).
23. A. Akulshin, C. Perrella, G.-W. Truong, R. McLean, and A. Luiten, *J. Phys. B: At. Mol. Opt. Phys.* **45**, 245503 (2012).
24. E. Brekke and E. Herman, *Opt. Lett.* **40**, 5674 (2015).
25. R. W. Boyd, *Nonlinear Optics* (Academic Press, 2008).
26. S. L. Cornish, N. R. Claussen, J. L. Roberts, E. A. Cornell, and C. E. Wieman, *Phys. Rev. Lett.* **85**, 1795 (2000).

FULL REFERENCES

1. M. Fleischhauer, A. Imamoglu, and J. P. Marangos, "Electromagnetically induced transparency : Optics in coherent media," *Rev. Mod. Phys.* **77**, 633–673 (2005).
2. A. S. Zibrov, M. D. Lukin, L. Hollberg, and M. O. Scully, "Efficient frequency up-conversion in resonant coherent media," *Phys. Rev. A* **65**, 051801 (2002).
3. A. M. Akulshin, R. J. McLean, A. I. Sidorov, and P. Hannaford, "Coherent and collimated blue light generated by four-wave mixing in Rb vapour." *Opt. Express* **17**, 22861–22870 (2009).
4. T. Meijer, J. D. White, B. Smeets, M. Jeppesen, and R. E. Scholten, "Blue five-level frequency-upconversion system in rubidium." *Opt. Lett.* **31**, 1002–1004 (2006).
5. A. Vernier, S. Franke-Arnold, E. Riis, and A. S. Arnold, "Enhanced frequency up-conversion in Rb vapor." *Opt. Express* **18**, 17020–17026 (2010).
6. T. P. Spiller, W. J. Munro, S. D. Barrett, and P. Kok, "An introduction to quantum information processing : applications and realizations," *Contemp. Phys.* **46**, 407–436 (2005).
7. R. M. Camacho, P. K. Vudyasetu, and J. C. Howell, "Four-wave-mixing stopped light in hot atomic rubidium vapour," *Nat. Photonics* **3**, 103–106 (2009).
8. D. C. McKay, D. Jervis, D. J. Fine, J. W. Simpson-Porco, G. J. A. Edge, and J. H. Thywissen, "Low-temperature high-density magneto-optical trapping of potassium using the open $4S \rightarrow 5P$ transition at 405 nm," *Phys. Rev. A* **84**, 063420 (2011).
9. P. M. Duarte, R. A. Hart, J. M. Hitchcock, T. A. Corcovilos, T.-L. Yang, A. Reed, and R. G. Hulet, "All-optical production of a lithium quantum gas using narrow-line laser cooling," *Phys. Rev. A* **84**, 061406(R) (2011).
10. D. V. Sheludko, S. C. Bell, R. Anderson, C. S. Hofmann, E. J. D. Vredenbregt, and R. E. Scholten, "State-selective imaging of cold atoms," *Phys. Rev. A* **77**, 033401 (2008).
11. B. Yang, Q. Liang, J. He, and J. Wang, "Background-free fluorescence detection of cold atoms in a two-color magneto-optical trap," *Opt. Express* **20**, 11944–11952 (2012).
12. G. Walker, A. S. Arnold, and S. Franke-Arnold, "Trans-spectral orbital angular momentum transfer via four-wave mixing in Rb vapor," *Phys. Rev. Lett.* **108**, 243601 (2012).
13. A. M. Akulshin, I. Novikova, E. E. Mikhailov, S. A. Suslov, and R. J. McLean, "Arithmetic with optical topological charges in step-wise excited Rb vapour," arXiv preprint: 1601.01368 (2016).
14. S. Franke-Arnold, L. Allen, and M. Padgett, "Advances in optical angular momentum," *Laser Photon. Rev.* **2**, 299–313 (2008).
15. F. E. Becerra, R. T. Willis, S. L. Rolston, and L. A. Orozco, "Nondegenerate four-wave mixing in rubidium vapor: The diamond configuration," *Phys. Rev. A* **78**, 013834 (2008).
16. J. F. Sell, M. A. Gearba, B. D. DePaola, and R. J. Knize, "Collimated blue and infrared beams generated by two-photon excitation in Rb vapor." *Opt. Lett.* **39**, 528–531 (2014).
17. A. Akulshin, D. Budker, and R. McLean, "Directional infrared emission resulting from cascade population inversion and four-wave mixing in Rb vapor." *Opt. Lett.* **39**, 845–848 (2014).
18. J. T. Schultz, S. Abend, D. Döring, J. E. Debs, P. A. Altin, J. D. White, N. P. Robins, and J. D. Close, "Coherent 455 nm beam production in a cesium vapor." *Opt. Lett.* **34**, 2321–2323 (2009).
19. P. Londero, V. Venkataraman, A. R. Bhagwat, A. D. Slepikov, and A. L. Gaeta, "Ultralow-Power Four-Wave Mixing with Rb in a Hollow-Core Photonic Band-Gap Fiber," *Phys. Rev. Lett.* **103**, 043602 (2009).
20. A. Akulshin, C. Perrella, G.-W. Truong, A. Luiten, D. Budker, and R. McLean, "Linewidth of collimated wavelength-converted emission in Rb vapour," *Appl. Phys. B* **117**, 203–209 (2014).
21. E. E. Mikhailov, J. Evans, D. Budker, S. M. Rochester, and I. Novikova, "Four-wave mixing in a ring cavity," *Opt. Eng.* **53**, 102709 (2014).
22. P. Siddons, C. S. Adams, C. Ge, and I. G. Hughes, "Absolute absorption on rubidium D lines: comparison between theory and experiment," *J. Phys. B: At. Mol. Opt. Phys.* **41**, 155004 (2008).
23. A. Akulshin, C. Perrella, G.-W. Truong, R. McLean, and A. Luiten, "Frequency evaluation of collimated blue light generated by wave mixing in Rb vapour," *J. Phys. B: At. Mol. Opt. Phys.* **45**, 245503 (2012).
24. E. Brekke and E. Herman, "Frequency characteristics of far-detuned parametric four-wave mixing in Rb," *Opt. Lett.* **40**, 5674–5677 (2015).
25. R. W. Boyd, *Nonlinear Optics* (Academic Press, 2008).
26. S. L. Cornish, N. R. Claussen, J. L. Roberts, E. A. Cornell, and C. E. Wieman, "Stable 85 Rb Bose-Einstein Condensates with Widely Tunable Interactions," *Phys. Rev. Lett.* **85**, 1795–1798 (2000).