

Research Article

Quality-Aware Incentive Mechanism for Mobile Crowd Sensing

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Mobile crowd sensing (MCS) is a novel sensing paradigm which can sense human-centered daily activities and the surrounding environment. The impact of mobility and selfishness of participants on the data reliability cannot be ignored in most mobile crowd sensing systems. To address this issue, we present a universal system model based on the reverse auction framework and formulate the problem as the *Multiple Quality Multiple User Selection* (MQMUS) problem. The *quality-aware incentive mechanism* (QAIM) is proposed to meet the quality requirement of data reliability. We demonstrate that the proposed incentive mechanism achieves the properties of computational efficiency, individual rationality, and truthfulness. And meanwhile, we evaluate the performance and validate the theoretical properties of our incentive mechanism through extensive simulation experiments.

1. Introduction

A new paradigm of sensing with smartphones has emerged which is usually called people-centric mobile sensing or mobile crowd sensing [1]. Compared with the traditional sensor networks, MCS is an effective way for large-scale data sensing, processing, and gathering without deploying a large number of sensor nodes. MCS has enabled numerous large-scale applications such as urban environment monitoring [2–4], traffic flow surveillance [5–7], healthcare [8], behavior and relationship discovery [9, 10], indoor localization [11], 3G/Wi-Fi discovering [12–14], activity monitoring [15, 16], and bus arrival time prediction [17].

The effect of the aforementioned mobile crowd sensing applications relies heavily on the quantities of participants. However, the ordinary individuals are not willing to share their sensing capabilities unless there are sufficient incentives. Research on incentive mechanism has been widely concerned by investigators, and considerable designed schemes about the incentive mechanism design have been put forward which can be classified into nonmonetary incentives [18–20] and monetary incentives [21–29].

The key of any crowd sensing system is not only the quantities of participants but also the sensing quality offered by participants. However, most of the existing solutions usually assume that each sensing task (e.g., air quality in a certain region) in a sensing cycle could be performed by a single participant. It is intuitive that the quality of sensing project would be higher if each sensing task was performed by multiple participants. One of the main reasons is that the sensed data cannot always be trusted because participants maybe intentionally (e.g., malicious participants) or unintentionally (e.g., making mistakes) offer the data contrary to the truth. Another reason may come from the recruitment system model itself. A typical MCS consists of two roles: the recruiter who publicizes the sensing tasks and the participants who constitute potential sensing capability selected by the recruiter from many candidates. The interaction between the recruiter and the candidates is modeled as a reverse auction in many existing solutions which can be illustrated by Figure 1. The recruiter always selects participants according to the sensing plans of the candidates. However, changes always go beyond plans. The participants may not be able to complete the task according to their schedule for unexpected incidents

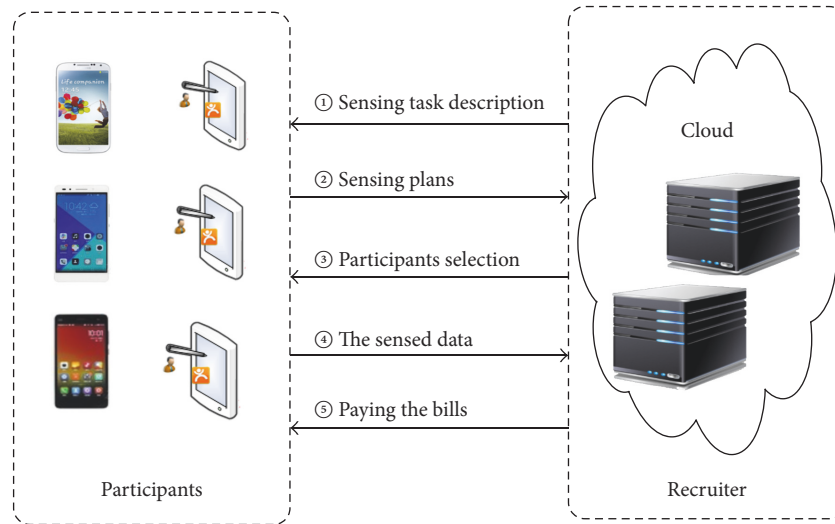


FIGURE 1: A typical mobile crowd sensing system as a reverse auction framework.

(e.g., a selected participant cannot go to the specific locations claimed in his sensing plan). These participants may offer some forged data or do nothing. As a result, the tasks could not be completed in time.

In this paper, we address the issue of quality-aware monetary incentive mechanism design. We design a truthful incentive mechanism satisfying the properties of computational efficiency, individual rationality, and truthfulness with low approximation ratio.

The remainder of this paper is organized as follows. In Section 2, we review the related work. In Section 3, we describe the system model and formulate the MQMUS problem. Thereafter, in Section 4 we propose the incentive mechanism, named QAIM, which consists of two phases, winner selection and payment determination, and analyze the properties of QAIM. Section 5 presents the experimental results. Finally, we draw the conclusion and discuss some possible future directions in Section 6.

2. Related Work

There are lots of incentive mechanisms which can be classified into nonmonetary incentives [18–29] and monetary incentives [30–45]. Paying for sensed data in crowd sensing tasks is the most intuitive incentive. Monetary incentive mechanisms are mainly based on two kinds of schemes: Stackelberg game and auction.

Stackelberg game is a game where one leader player has the dominant influence over the other players [46]. Duan et al. [30] make use of the Stackelberg game to design a threshold revenue model for service providers. The system and the users interact through a two-stage process similar to that of Stackelberg game. The system announces the total reward and the threshold number of required participants. Each participant decides whether to accept the task or not. Yang et al. [31] also model the proposed platform-centric incentive mechanism as a Stackelberg game, prove

that this Stackelberg game has a unique equilibrium, and design an efficient mechanism for computing it. The above two Stackelberg game solutions have theoretical guarantees. However, the premise of this kind of method is that the costs of all users or their probability distributions are assumed to be known, which limits the applicability of Stackelberg game-based mechanisms because participants may keep their costs private in the real world.

An auction-based mechanism is originally the process of buying and selling goods by negotiating the monetary prices [47]. A kind of auction, called reverse auction, is adopted to model the negotiation process in crowd sensing, which is shown in Figure 1. Lee and Hoh [32] firstly design a reverse auction-based dynamic price incentive mechanism with virtual participation credit with the objective of minimizing and stabilizing the platform cost while maintaining the participation level. Yang et al. [31] consider two system models for smartphone crowd sensing system: the platform-centric model with the solution based on the Stackelberg game and user-centric model with the solution based on the reverse auction. Feng et al. [33] formulate the winning bids determination problem and present a truthful auction for location-aware collaborative sensing. Zhang et al. [34] focus on the user-centric model and study three methods which involve cooperation and competition among the services. Xu et al. [35, 36] investigate truthful incentive mechanisms for time window dependent tasks with the strong requirement of data integrity and propose two incentive mechanisms for the single time window case and the multiple window case, respectively. Subramanian et al. [37] consider offline and online incentive mechanisms using the same bidding framework with MSensing Auction proposed in [31]. Zhao et al. [38] investigate the incentive mechanisms in the online setting based on an offline budget feasible mechanism [39], which provides a starting point for the online mechanism. Jin et al. [40] pay attention to the quality of the mobile crowd sensing systems and incorporate a metric named QoI

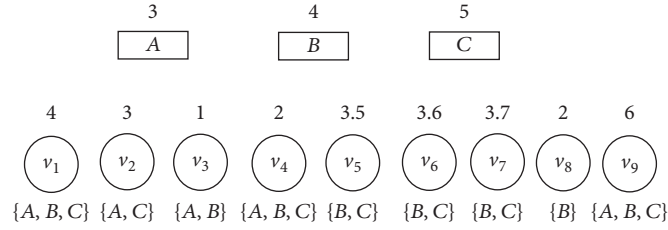


FIGURE 2: A motivating example with diversity requirements.

(Quality of Information) into the incentive mechanisms. SRC and MRC mechanisms with the criterion of the combinatorial QoI and price are proposed. However, the authors fail to consider the truthfulness of the MRC mechanism. The aforementioned solutions assume that each measurement of sensing task can be represented by a single sensor reading.

Several solutions are proposed to ensure the quality of crowd sensing data. Tanas and Herrera-Joancomartí [48] achieve the first work, which focuses on how to validate sensing data, but the premise of their work is that there are multiple users to submit multiple sensing readings on each task. Kazemi et al. [49] assume each worker has a reputation score, and assign enough number of workers to each spatial task such that workers' aggregate reputation can satisfy the confidence of the task. However, they focus on self-incentivized spatial crowdsourcing, in which people perform the tasks voluntarily without any reward. Zhang et al. [41] propose a task management framework to match workers to the merged query and sensing tasks efficiently. In their model, each task can be assigned to multiple workers, and each worker can be assigned to at most one task, although each worker may have the preference for multiple tasks. Xu et al. [42] design the incentive mechanism, which considers the issue of stimulating the biased requesters in the competing crowdsourcing market. Xiong et al. [43] consider the k -depth coverage as an MCS data collection constraint, but every subtask is assigned to the same value of k . Wang et al. [44] present a detailed quality-aware mobile crowdsourced sensing framework, composed of three MCS components: send, crowdsourcer, and crowdsourcing platform. The crowdsourcer is a new role who assesses the posted contributions' quality. He et al. [45] propose a recruitment strategy in vehicle-based crowdsourcing through taking full advantage of predictable mobility patterns of vehicles, which bring a new insight to improve the quality of crowd sensing system. However, the behaviors of human are affected by many factors. It is far more difficult to predict the mobility patterns of human beings than those of vehicles.

In this paper, we try to enhance the quality-aware incentive mechanism from two main dimensions: the reputation of participants and the design of task.

3. Problem Statement

Different from most crowd sensing systems, the objective of this paper is designing the truthful incentive mechanism

with maximum social efficiency and high sensing quality. To achieve this objective, the recruiter needs to select participants who can match the diverse requirements of the crowd sensing application with minimum social cost. Before demonstrating the rigorous problem definition, we would like to present a motivating example to make the problem better understood.

3.1. A Participant Recruitment Example in Air Quality Monitoring. We take the urban air quality monitoring MCS task as an example. As shown in Figure 2, the MCS recruiter wants to collect the state of the air in three regions (denoted as $G = \{A, B, C\}$). Nine candidates ($\{v_1, v_2, \dots, v_9\}$) are interested in performing the task and reporting their sensing plans, which include what they can do with the corresponding bid price. The industrial structures vary greatly in different regions. The regions with more plants, which can discharge waste gas, need more participants to monitor. For example, the recruiter wants 5 participants to monitor region C and only 3 to monitor region A because there are more chemical plants in region C. We use squares to represent the regions, and the number above each square denotes its requirement. To the perspective of the candidates, people may not just stay in a certain region in one sensing cycle and can fulfill multiple sensing tasks in different regions. We use disks to represent the candidates, and the number above each disk denotes its corresponding bid price, and the set of regions below each disk denotes the regions that he can monitor.

In this example, the mobile crowd sensing system has some requirements: (1) Every subtask should be assigned to enough participants so that their aggregate sensing results can ensure the sensing quality. (2) Every subtask has different sensing requirement. The different number of participants should be recruited to satisfy different sensing requirements with minimum costs. (3) Every participant has different ability in terms of the task completion and should be assigned to the different number of subtasks based on his particular ability.

3.2. System Model and Problem Formulation. We present the rigorous definition and formulation of the MQMUS problem. In this problem, the recruiter can divide the task into multiple subtasks with different quality factors and the participants can be assigned to multiple subtasks in one sensing cycle.

Suppose that a crowd sensing task G can be divided into e disjoint subtasks according to the sensing geographic areas,

and each subtask g_k has its sensing quality factor $h(g_k)$ (to simplify, we use the number of participants to represent $h(g_k)$ as shown in the above motivating example). The recruiter publicizes the sensing task $G = \{g_1, g_2, \dots, g_k, \dots, g_e\}$ and the quality factor $h(G) = \{h(g_1), h(g_2), \dots, h(g_k), \dots, h(g_e)\}$ as a quality constraint for participants selecting.

Considering n candidates, $U = \{v_1, v_2, \dots, v_i, \dots, v_n\}$ are interested in performing the sensing task. Each candidate $v_i \in U$ submits a sensing plan $B_{v_i} = (\psi_{v_i}, b_{v_i})$ to the recruiter, in which $\psi_{v_i} = \{g_1^{v_i}, g_2^{v_i}, \dots, g_k^{v_i}\}$ is the set of subtasks that candidate v_i can perform (the superscript v_i of $g_k^{v_i}$ is only used to represent that v_i can fulfill the subtask g_k) and b_{v_i} is bid price that candidate v_i wants to charge for performing ψ_{v_i} .

We assume that the candidate v_i has a reputation score r_{v_i} , which states the probability that the candidate performs a task correctly. The recruiter is responsible for maintaining and updating the reputation score of every candidate. The value of r_{v_i} is set to 1 initially and updated by

$$r_{v_i} = r_{v_i} + \sum_{g_m \in \psi_{v_i}} \frac{(h(g_m) - 1) \eta}{\max_{g_k \in G} \{h(g_k)\}}. \quad (1)$$

We utilize a voting mechanism to set the value of η . This intuition is based on the idea of the wisdom of crowds [50] that the majority of the participants are trusted. The recruiter aggregates the different sensing results to get the reliable result at the end of the sensing cycle. The setting way of η is inspired by [44]. η is set to “-1” in two cases: (1) the candidate cannot perform the subtask as the claimed sensing plan; (2) the sensing result of the same subtask is contrary to more than half of participants’ results; otherwise, η is “0.” If $r_{v_i} < 0$, v_i will not be selected until the recruiter resets r_{v_i} to 1 after a period of time (e.g., 10 sensing cycles).

Assume that the number of candidates is sufficient to fulfill the sensing task G with its quality constraints $h(G)$. This assumption is reasonable for mobile crowd sensing systems as made in [31, 33, 35]. The selected participant s_j is placed into the list $S = \{s_1, s_2, \dots, s_{j-1}\}$ according to the order. s_j is the ID of the candidate and its subscript j denotes that s_j is the j th selected participant. The recruiter has to calculate the payment p_{s_j} for each participant as the incentive. The utility of participant can be calculated by (2), in which c_{s_j} is the real cost of the participant s_j and only known by itself. b_{s_j} is not less than c_{s_j} due to the selfishness and rationality of participants (if the reputation score of s_j is set to a value less than 0 in this sensing cycle, the utility of s_j will be 0 in the next sensing cycle because he will not be selected).

$$u_{s_j} = p_{s_j} - c_{s_j}. \quad (2)$$

The utility of the recruiter is calculated by (3). $V(h(G))$ is the value to the recruiter when it has collected enough data to satisfy the quality constraints $h(G)$ of the sensing task G .

$$u_0 = V(h(G)) - \sum_{s_j \in S} p_{s_j}. \quad (3)$$

The social efficiency of the sensing task G (with the quality constraints $h(G)$) is calculated by (4). Although the

real cost c_{s_j} is only known by participant s_j , we will prove that claiming a different cost b_{s_j} cannot help to increase the utility of participant s_j in our designed mechanisms. So we use b_{s_j} when we attempt to maximize social efficiency in the mechanisms designed below. The objective of maximizing the social efficiency is equivalent to the objective of minimizing the social cost.

$$u_{h(G)} = V(h(G)) - \sum_{s_j \in S} b_{s_j}. \quad (4)$$

Given the list of selected participants $S = \{s_1, s_2, \dots, s_i, \dots, s_m\}$, G_{s_i} is the set of the remaining subtasks excluding those subtasks of participants $\{s_1, s_2, \dots, s_i\}$ according to their sensing plans. The goal of achieving high quality crowd sensing with minimum social cost can be formulated as (5) and constrained by (6).

$$\min \left(\sum_{s_j \in S} b_{s_j} \right) \quad (5)$$

$$\text{s.t. } |\psi_{s_1} \cap G| + |\psi_{s_2} \cap G_{s_1}| + \dots + |\psi_{s_m} \cap G_{s_{m-1}}| \geq \sum_{g_k \in G} h(g_k). \quad (6)$$

We design a truthful incentive mechanism, QAIM, to select appropriate participants to satisfy the objective of this paper, and to eliminate the fear of market manipulation (the participants cannot improve their utility by submitting a bid price different from its real cost).

QAIM consists of two phases: winner selection algorithm QAIM(S) and payment determination algorithm QAIM(P). For a given $h(G)$ and a set of bids $B = \{B_{v_1}, B_{v_2}, \dots, B_{v_i}, \dots, B_{v_n}\}$, the algorithm QAIM(S) selects a subset of participants $S \subseteq U$ and the algorithm QAIM(P) returns the vector (p_1, p_2, \dots, p_m) for those selected participants.

We cannot find the optimal solution in polynomial time for the MQMUS problem presented in (5) and (6) because this problem is NP-hard. The proof is in Appendix.

Our objective is to design the incentive mechanisms satisfying the following four desirable properties to solve MQMUS problem:

- (i) *Computational Efficiency.* A mechanism is computationally efficient if both the winner selection function and payment decision function can be computed in polynomial time.
- (ii) *Individual Rationality.* Each participant will have a nonnegative utility upon performing the sensing task.
- (iii) *Truthfulness.* A mechanism is truthful if no participant can improve its utility by submitting a bid price different from its real cost, no matter what others submit. In other words, reporting the real cost is a dominant strategy for all participants.
- (iv) *Social Optimization.* The objective function is maximizing the social efficiency. We attempt to find optimal solution or approximation algorithm with low approximation ratio when there is no optimal solution computed in polynomial time.

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Input:  $h(G)$ , set of bids  $B$ 
(1)  $\lambda = 1$ ;  $G_\lambda = G$ ;  $S = \Phi$ ; for  $l \in U$  if  $(r_l < 0)$   $U = U - \{l\}$ ;
(2) while  $(G_\lambda \neq \Phi)$  {
(3)   for each  $l \in (U - S)$  if  $(\omega_l(G_\lambda) \neq 0)$   $T_l(\lambda) = \frac{b_l}{\omega_l(G_\lambda)}$  else  $T_l(\lambda) = \text{MAX}$ ;
(4)   for each  $l \in (U - S)$  Sort  $T_l(\lambda)$  in non-decreasing order;
(5)    $q = 1$ ;  $y = 1$ ;  $\min h_\lambda = \min_{g_k \in G_\lambda} \{h(g_k)\}$ ;
(6)   while  $(y \leq \min h_\lambda)$  {
(7)      $i = \arg(T_q(\lambda))$ ;  $S = S \cup \{i\}$ ;  $y = y + 1$ ;  $q = q + 1$ ;
(8)     for each  $(g_k^i \in \psi_i)$  {
(9)       if  $(g_k^i \in G_\lambda)$  {
(10)         $h(g_k) = h(g_k) - 1$ ;
(11)        if  $h(g_k) = 0$   $G_{\lambda+1} = G_\lambda - \{g_k\}$ ; } } }
(12)    $\lambda = \lambda + 1$ ; }
(13) return  $S$ 

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ALGORITHM 1: QAIM(S).

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input:  $h(G)$ , set of bids  $B$ , list of selected participants  $S$ 
(1) for all  $u \in U$  do  $\{p_u = 0\}$ ; for  $l \in U$  if  $(r_l < 0)$   $U = U - \{l\}$ ;
(2) for all  $s_i \in S$  do {
(3)    $U' = U - \{s_i\}$ ;  $\chi = \Phi$ ;  $v = 1$ ;  $G_v = G$ ;
(4)   while  $(G_v \neq \Phi)$  {
(5)     for  $l \in (U' - \chi)$  {if  $(\omega'_l(G_v) \neq 0)$   $\Gamma_l(v) = \frac{b_l}{\omega'_l(G_v)}$  else  $\Gamma_l(v) = \text{MAX}$ ; }
(6)     for  $l \in (U' - \chi)$  {Sort  $\Gamma_l(v)$  in non-decreasing order; }
(7)      $q = 1$ ;  $y = 1$ ;  $\min h = \min_{g_k \in G_v} \{h(g_k)\}$ ;
(8)     while  $(y \leq \min h)$  {
(9)        $r = \arg(\Gamma_q(v))$ ;  $p_{s_i} = \max\{p_{s_i}, \frac{\omega'_{s_i}(G_v)}{\omega'_r(G_v)} b_r\}$ ;
(10)       $\chi = \chi \cup \{r\}$ ;  $y = y + 1$ ;  $q = q + 1$ ;
(11)      for  $(g_k^r \in \psi_r)$  {
(12)        if  $(g_k^r \in G_v)$  {
(13)           $h(g_k) = h(g_k) - 1$ ;
(14)          if  $h(g_k) = 0$   $\{G_{v+1} = G_v - \{g_k\}\}$ ; } } }
(15)      $v = v + 1$ ; } }
(16) return  $P$ 

```

ALGORITHM 2: QAIM(P).

4. Mechanism Design and Analysis

4.1. Mechanism Design. We attempt to find an approximation algorithm following a greedy approach which can be solved in polynomial time because the MQMUS problem is NP-hard problem. The winner selection algorithm QAIM(S) is illustrated in Algorithm 1 and the payment algorithm QAIM(P) is illustrated in Algorithm 2.

In Algorithm 1, l is the ID of candidates, λ is the number of selection round, and G_λ is the set of remaining subtasks excluding those in the sensing plans of the selected participants before the previous $\lambda - 1$ rounds. The *effective sensing units* of l in the λ th round are denoted by $\omega_l(G_\lambda)$ which can be calculated by (7), the *effective average sensing*

weight of candidate l in the λ th round is denoted by $T_l(\lambda)$ which is calculated in Line (3) of Algorithm 1.

$$\omega_l(G_\lambda) = |G_\lambda \cap \psi_l|. \quad (7)$$

The main idea of greedy approach is to select candidate with least effective average sensing weight, so $T_l(\lambda)$ of all remaining candidates are sorted in nondecreasing order in Line (4) of Algorithm 1, and $\arg(T_q(\lambda))$ is the ID of the q th selected participant in the λ th selection round.

The trick of QAIM(S) lies in the use of $\min h_\lambda$ which denotes the number of participants that can be selected in the

λ th round. The nondecreasing sorting of $T_l(\lambda)$ implies that (8) is true.

$$\begin{aligned} \frac{b_{\arg(T_1(\lambda))}}{\omega_{\arg(T_1(\lambda))}(G_\lambda)} &\leq \frac{b_{\arg(T_2(\lambda))}}{\omega_{\arg(T_2(\lambda))}(G_\lambda)} \leq \dots \\ &\leq \frac{b_{\arg(T_{\min h_\lambda}(\lambda))}}{\omega_{\arg(T_{\min h_\lambda}(\lambda))}(G_\lambda)}. \end{aligned} \quad (8)$$

Equation (9) is true; otherwise the first selected participant in the $(\lambda + 1)$ th round will be selected in the λ th round.

$$\frac{b_{\arg(T_{\min h_\lambda}(\lambda))}}{\omega_{\arg(T_{\min h_\lambda}(\lambda))}(G_\lambda)} \leq \frac{b_{\arg(T_1(\lambda+1))}}{\omega_{\arg(T_1(\lambda+1))}(G_\lambda)}. \quad (9)$$

The calculation method of $G_{\lambda+1}$ in Line (10) of Algorithm 1 implies that $|G_{\lambda+1}|$ cannot be bigger than $|G_\lambda|$, so (10) is true which implies the participant is selected in the nondecreasing order of the *effective average sensing weight*:

$$\begin{aligned} \frac{b_{\arg(T_{\min h_\lambda}(\lambda))}}{\omega_{\arg(T_{\min h_\lambda}(\lambda))}(G_\lambda)} &\leq \frac{b_{\arg(T_1(\lambda+1))}}{\omega_{\arg(T_1(\lambda+1))}(G_\lambda)} \\ &\leq \frac{b_{\arg(T_1(\lambda+1))}}{\omega_{\arg(T_1(\lambda+1))}(G_{\lambda+1})}. \end{aligned} \quad (10)$$

Let $s_p, s_{p+1}, \dots, s_{p+\min h_\lambda-1}$ denote the IDs of the selected participants in the λ th selection round; the set of remaining subtasks would possibly be changed only at the end of the λ th selection round, so (11) is true.

$$\begin{aligned} G_{s_p} &= G_{s_{p+1}} = \dots = G_{s_{p+\min h_\lambda-2}} = G_\lambda, \\ G_{s_{p+\min h_\lambda-1}} &= G_{\lambda+1}. \end{aligned} \quad (11)$$

Equation (12) is true by derivation from (10) and (11).

$$\begin{aligned} \frac{b_{s_1}}{\omega_{s_1}(G)} &\leq \frac{b_{s_2}}{\omega_{s_2}(G_{s_1})} \leq \dots \leq \frac{b_{s_i}}{\omega_{s_i}(G_{s_{(i-1)}})} \leq \dots \\ &\leq \frac{b_{s_m}}{\omega_{s_m}(G_{s_{(m-1)}})}. \end{aligned} \quad (12)$$

In Algorithm 2, u is the ID of candidates with the same role as l in QAIM(S), v is the number of payment determination round, and G_v is the set of remaining subtasks excluding those in the sensing plans of the selected participants before the previous $v - 1$ rounds. The *effective sensing units* of l in the v th round are denoted by $\omega'_l(G_v)$ with the same calculation method used in (7). The *effective average sensing weight* of candidate l in the v th round is denoted by $\Gamma_l(v)$ which is calculated in Line (5) of Algorithm 2.

To compute the payment for each s_i in the winner list S , we consider the set of candidates $U - \{s_i\}$ and reselect appropriate participants into the list χ^{s_i} with the same method used in QAIM(S) (the superscript s_i of χ^{s_i} is used to identify that s_i is not considered as a candidate). Let $\chi^{s_i} =$

$\{x_1^{s_i}, x_2^{s_i}, \dots, x_k^{s_i}, \dots, x_a^{s_i}\}$ and $x_k^{s_i}$ denote the k th selected participant, $G_{x_k^{s_i}}$ is the set of remaining subtasks excluding those effective subtasks of participants $\{x_1^{s_i}, x_2^{s_i}, \dots, x_k^{s_i}\}$ according to their sensing plans, and (13) is true for the same reason of (12).

$$\begin{aligned} \frac{b_{x_1^{s_i}}}{\omega'_{x_1^{s_i}}(G)} &\leq \frac{b_{x_2^{s_i}}}{\omega'_{x_2^{s_i}}(G_{x_1^{s_i}})} \leq \dots \leq \frac{b_{x_k^{s_i}}}{\omega'_{x_k^{s_i}}(G_{x_{k-1}^{s_i}})} \leq \dots \\ &\leq \frac{b_{x_a^{s_i}}}{\omega'_{x_a^{s_i}}(G_{x_{a-1}^{s_i}})}. \end{aligned} \quad (13)$$

4.2. A Walk-Through Example. To better understand the algorithm, we use the example in Figure 2 to illustrate how the QAIM works.

With regard to the aforementioned example, the crowd sensing task $G = \{A, B, C\}$ is divided into 3 subtasks: $h(A)$ is set to 3, $h(B)$ is set to 4, and $h(C)$ is set to 5. There are 9 candidates $U = \{v_1, v_2, \dots, v_9\}$ who want to participate in the task and report their sensing plan: the bid price of v_i is shown above it, and the subtask that v_i can fulfill is given below it in Figure 2. Take v_3 , for example, $\psi_{v_3} = \{A, B\}$, which can also be represented as $\psi_{v_3} = \{A^{v_3}, B^{v_3}\}$, and $b_{v_3} = 1$. The *effective sensing units* of v_3 in the first round are denoted by $\omega_{v_3}(G_1)$ which is calculated by (7) (i.e., $|\{A, B, C\} \cap \{A, B\}| = 2$), and the *effective average sensing weight* of v_3 in the first round is denoted by $T_{v_3}(1)$ which is calculated in Line (3) of Algorithm 1 (i.e., $b_{v_3}/\omega_{v_3}(G_1) = 1/2$).

We first assume that all participants are trustworthy and can fulfill the sensing units as they had claimed in their sensing plan.

In the first selection round, $G_\lambda = \{A, B, C\}$, $h(A) = 3$, $h(B) = 4$, $h(C) = 5$, $\min h_\lambda = 3$. $T_l(\lambda)$ of each candidate in the first round is listed in Table 1. According to QAIM(S), v_3 is the first winner and then v_4 , and v_1 is the third one in the first round. The selected list $S = \{v_3, v_4, v_1\}$, $G_{v_3} = \{A, B, C\}$, $G_{v_4} = \{A, B, C\}$, and $G_{v_1} = \{B, C\}$.

In the second selection round, $G_\lambda = \{B, C\}$, $h(A) = 0$, $h(B) = 1$, $h(C) = 3$, and $\min h_\lambda = 1$. $T_l(\lambda)$ of each candidate in the second round is listed in Table 2. According to QAIM(S), v_5 is the first and only winner. The selected list $S = \{v_3, v_4, v_1, v_5\}$ and $G_{v_5} = \{C\}$.

In the third selection round, $G_\lambda = \{C\}$, $h(A) = 0$, $h(B) = 0$, $h(C) = 2$, and $\min h_\lambda = 2$. $T_l(\lambda)$ of each candidate in the third round is listed in Table 3. According to QAIM(S), v_2 is the first winner and v_6 is the second one. The selected list $S = \{v_3, v_4, v_1, v_5, v_2, v_6\}$, $G_{v_2} = \{C\}$, and $G_{v_6} = \emptyset$.

In the fourth selection round, $G_\lambda = \emptyset$, which implies the selected participants ($v_3, v_4, v_1, v_5, v_2, v_6$) can satisfy the sensing requirements.

If v_3 is a malicious participant, he lies in the results of all sensing units; the reputation of v_3 is 0 calculated by (1) which means he will not be selected in the next sensing recruitment cycle.

Owing to the limitation of the space and the similarity of the algorithm process, we only give the payment example

TABLE 1: $T_i(\lambda)$ in the first selection round.

| | $T_{v_1}(\lambda)$ | $T_{v_2}(\lambda)$ | $T_{v_3}(\lambda)$ | $T_{v_4}(\lambda)$ | $T_{v_5}(\lambda)$ | $T_{v_6}(\lambda)$ | $T_{v_7}(\lambda)$ | $T_{v_8}(\lambda)$ | $T_{v_9}(\lambda)$ |
|---------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| $\lambda = 1$ | 4/3 | 3/2 | 1/2 | 2/3 | 3.5/2 | 3.6/2 | 3.7/2 | 2/1 | 6/3 |

TABLE 2: $T_i(\lambda)$ in the second selection round.

| | $T_{v_2}(\lambda)$ | $T_{v_5}(\lambda)$ | $T_{v_6}(\lambda)$ | $T_{v_7}(\lambda)$ | $T_{v_8}(\lambda)$ | $T_{v_9}(\lambda)$ |
|---------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| $\lambda = 2$ | 3/1 | 3.5/2 | 3.6/2 | 3.7/2 | 2/1 | 6/2 |

TABLE 3: $T_i(\lambda)$ in the third selection round.

| | $T_{v_2}(\lambda)$ | $T_{v_6}(\lambda)$ | $T_{v_7}(\lambda)$ | $T_{v_8}(\lambda)$ | $T_{v_9}(\lambda)$ |
|---------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| $\lambda = 3$ | 3/1 | 3.6/1 | 3.7/1 | MAX | 6/1 |

TABLE 4: $\Gamma_i(v)$ in the first payment determination round considering v_3 .

| | $\Gamma_{v_1}(v)$ | $\Gamma_{v_2}(v)$ | $\Gamma_{v_4}(v)$ | $\Gamma_{v_5}(v)$ | $\Gamma_{v_6}(v)$ | $\Gamma_{v_7}(v)$ | $\Gamma_{v_8}(v)$ | $\Gamma_{v_9}(v)$ |
|---------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| $v = 1$ | 4/3 | 3/2 | 2/3 | 3.5/2 | 3.6/2 | 3.7/2 | 2/1 | 6/3 |

TABLE 5: $\Gamma_i(v)$ in the second payment determination round considering v_3 .

| | $\Gamma_{v_5}(v)$ | $\Gamma_{v_6}(v)$ | $\Gamma_{v_7}(v)$ | $\Gamma_{v_8}(v)$ | $\Gamma_{v_9}(v)$ |
|---------|-------------------|-------------------|-------------------|-------------------|-------------------|
| $v = 2$ | 3.5/2 | 3.6/2 | 3.7/2 | 2/1 | 6/2 |

TABLE 6: $\Gamma_i(v)$ in the third payment determination round considering v_3 .

| | $\Gamma_{v_6}(v)$ | $\Gamma_{v_7}(v)$ | $\Gamma_{v_8}(v)$ | $\Gamma_{v_9}(v)$ |
|---------|-------------------|-------------------|-------------------|-------------------|
| $v = 3$ | 3.6/1 | 3.7/1 | MAX | 6/1 |

of the first selected winner v_3 which is similar to the payment determination of other participants. p_{v_3} is initialized to 0.

In the first payment determination round, $G_v = \{A, B, C\}$, $h(A) = 3$, $h(B) = 4$, $h(C) = 5$, and $\min h_v = 3$. $\Gamma_i(v)$ of each candidate in the first round is listed in Table 4. According to QAIM(P), v_4 is the first winner; then $p_{v_3} = \max\{p_{v_3}, (\omega'_{v_3}(G_v)/\omega'_{v_4}(G_v))b_{v_4}\} = \max\{0, (2/3) * 2\} = 4/3$. v_1 is the second winner; then $p_{v_3} = \max\{p_{v_3}, (\omega'_{v_3}(G_v)/\omega'_{v_1}(G_v))b_{v_1}\} = \max\{4/3, (2/3) * 4\} = 8/3$. v_2 is the third winner; then $p_{v_3} = \max\{p_{v_3}, (\omega'_{v_3}(G_v)/\omega'_{v_2}(G_v))b_{v_2}\} = \max\{8/3, (2/2) * 3\} = 3$.

In the second payment determination round, $G_v = \{B, C\}$, $h(A) = 0$, $h(B) = 1$, $h(C) = 2$, and $\min h_v = 1$. $\Gamma_i(v)$ of each candidate in the second round is listed in Table 5. According to QAIM(P), v_5 is the first and only winner; then $p_{v_3} = \max\{p_{v_3}, (\omega'_{v_3}(G_v)/\omega'_{v_5}(G_v))b_{v_5}\} = \max\{3, (1/2) * 3.5\} = 3$.

In the third payment determination round, $G_v = \{C\}$, $h(A) = 0$, $h(B) = 0$, $h(C) = 1$, and $\min h_v = 1$. $\Gamma_i(v)$ of each candidate in the second round is listed in Table 6. According to QAIM(P), v_6 is the first and only winner; then $p_{v_3} = \max\{p_{v_3}, (\omega'_{v_3}(G_v)/\omega'_{v_6}(G_v))b_{v_6}\} = \max\{3, (0/1) * 3.5\} = 3$.

In the fourth payment round, $G_v = \emptyset$, so the payment to v_3 is 3.

4.3. Properties of QAIM. In this section, we analyze the properties of QAIM theoretically to show that QAIM is computationally efficient, individually rational, and truthful. The approximation is also discussed in the end. We use n to denote the number of candidates, e to denote the number of subtasks, $\Omega(G)$ to denote all the sensing units, and $\Omega(G'_{s_i})$ to denote the effective sensing units of the selected participants $S = \{s_1, s_2, \dots, s_i\}$, and for ease of analysis they can be calculated by

$$\Omega(G) = \sum_{k=1}^e h(g_k), \quad (14)$$

$$\Omega(G'_{s_i}) = |\psi_{s_1} \cap G| + |\psi_{s_2} \cap G_{s_1}| + \dots + |\psi_{s_i} \cap G_{s_{i-1}}|. \quad (15)$$

(1) *QAIM Is Computationally Efficient.* We analyze QAIM(S) and QAIM(P), respectively, where QAIM takes $O(n^3 * e)$ in the worst case.

The nested for-loop (Lines (8)–(11)) of QAIM(S) will be executed $\lambda * |\psi_{s_i}| * \min h_\lambda$ times. The maximal value of λ is $\Omega(G)$ which is less than n obviously in the worst case when the *effective sensing unit* of every candidate has only one subtask. $|\psi_{s_i}|$ is less than e and $\min h_\lambda$ is far less than n obviously, so QAIM(S) takes $O(n^2 * e)$ in the worst case.

QAIM(P) takes $O(n^3 * e)$ in the worst case because there are similar processes in both QAIM(S) (Lines (2)–(11)) and QAIM(P) (Lines (4)–(14)), which will be executed $|S|$ times less than n .

(2) *QAIM Is Individually Rational.* When considering the set of candidates $U - \{s_i\}$, let $x_k^{s_i}$ be the replacement of participant s_i which appears in the k th place in the selected list $\chi^{s_i} =$

$\{x_1^{s_i}, x_2^{s_i}, \dots, x_k^{s_i}, \dots, x_d^{s_i}\}$. Equation (16) is true according to the main idea of winner selection.

$$s_1 = x_1^{s_i}, s_2 = x_2^{s_i}, \dots, s_{i-1} = x_{i-1}^{s_i}, \quad (16)$$

$$\left(\text{That is } G_{s_{i-1}} = G_{x_{i-1}^{s_i}} \right).$$

$x_k^{s_i}$ will not be selected in the k th place if s_i is considered, so (17) is true.

$$\frac{b_{s_i}}{\omega_{s_i}(G_{s_{i-1}})} \leq \frac{b_{x_i^{s_i}}}{\omega_{x_i^{s_i}}(G_{s_{i-1}})}, \quad (17)$$

$$\left(\text{That is } \frac{b_{s_i}}{G_{s_{i-1}} \cap \psi_{s_i}} \leq \frac{b_{x_i^{s_i}}}{G_{s_{i-1}} \cap \psi_{x_i^{s_i}}} \right).$$

Equation (18) is true based on the derivation from (16) and (17).

$$\frac{b_{s_i}}{G_{x_{i-1}^{s_i}} \cap \psi_{s_i}} = \frac{b_{s_i}}{G_{s_{i-1}} \cap \psi_{s_i}} \leq \frac{b_{x_i^{s_i}}}{G_{s_{i-1}} \cap \psi_{x_i^{s_i}}}$$

$$= \frac{b_{x_i^{s_i}}}{G_{x_{i-1}^{s_i}} \cap \psi_{x_i^{s_i}}}, \quad (18)$$

$$\left(\text{That is } b_{s_i} \leq \frac{G_{x_{i-1}^{s_i}} \cap \psi_{s_i}}{G_{x_{i-1}^{s_i}} \cap \psi_{x_i^{s_i}}} b_{x_i^{s_i}} \right).$$

Equation (19) is true according to the main idea of payment calculation in Line (9) of QAIM(P).

$$p_{s_i} = \max_{x_r^{s_i} \in \chi^{s_i}} \left\{ \frac{\omega'_{s_i}(G_{x_{r-1}^{s_i}})}{\omega'_{x_r^{s_i}}(G_{x_{r-1}^{s_i}})} b_{x_r^{s_i}} \right\}. \quad (19)$$

From the analysis of (18) and (19), we know $b_{s_i} \leq p_{s_i}$.

(3) *QAIM Is Truthful*. According to Myerson's Theorem [51], an auction is truthful if and only if the selection rule is monotone and each winner is paid the critical value p_i ; if a participant wins the auction by bidding b_i , he also wins by bidding $b'_i < b_i$ but loses by bidding $b'_i > p_i$.

The monotonicity of the selection rule is obvious: if s_i bids a smaller b'_{s_i} that means $b'_{s_i}/\omega_{s_i}(G_{s_{i-1}}) \leq b_{s_i}/\omega_{s_i}(G_{s_{i-1}})$, s_i will also be selected according to (12).

Suppose $p_{s_i} = \max_{x_r^{s_i} \in \chi^{s_i}} \{(\omega'_{s_i}(G_{x_{r-1}^{s_i}})/\omega'_{x_r^{s_i}}(G_{x_{r-1}^{s_i}}))b_{x_r^{s_i}}\} = (\omega'_{s_i}(G_{x_{f-1}^{s_i}})/\omega'_{x_f^{s_i}}(G_{x_{f-1}^{s_i}}))b_{x_f^{s_i}}$; (20) is true if b_{s_i} is greater than p_{s_i} .

$$b_{s_i} \geq \frac{\omega'_{s_i}(G_{x_{f-1}^{s_i}})}{\omega'_{x_f^{s_i}}(G_{x_{f-1}^{s_i}})} b_{x_f^{s_i}}, \quad (20)$$

$$\left(\text{That is } \frac{b_{s_i}}{\omega'_{s_i}(G_{x_{f-1}^{s_i}})} \geq \frac{b_{x_f^{s_i}}}{\omega'_{x_f^{s_i}}(G_{x_{f-1}^{s_i}})} \right).$$

Equation (20) shows the fact that s_i will not be selected before the previous f participants $(x_1^{s_i}, x_2^{s_i}, \dots, x_f^{s_i})$ are selected. But if the previous f participants are selected, there is no reason to select s_i because the previous selected participants can satisfy different sensing requirements.

(4) *The Approximation Factor to Optimal Solution Is $\ln(\Omega(G)) + 1$* . Let OPT denote the minimal social cost computed by optimal solution, $\Omega(G'_{s_i})$ denote the effective sensing units of the selected participants $S = \{s_1, s_2, \dots, s_i\}$ calculated by (15), and $\text{cost}(s_{i+1})$ denote the social cost of the $(i+1)$ th selected participant s_{i+1} .

Because the participant is selected in the nondecreasing order of the *effective average sensing weight* according to QAIM(S) and the average cost of the rest uncovered sensing units is not greater than $\text{OPT}/(\Omega(G) - \Omega(G'_{s_i}))$, (21) is true.

$$\text{cost}(s_{i+1}) \leq \frac{\text{OPT}}{\Omega(G) - \Omega(G'_{s_i})}. \quad (21)$$

Hence the total cost of QAIM can be calculated by

$$\sum_{r=1}^m \text{cost}(s_r) \leq \sum_{r=1}^m \frac{\text{OPT}}{\Omega(G) - \Omega(G'_{s_{r-1}})}$$

$$\leq \frac{\text{OPT}}{\Omega(G)} + \frac{\text{OPT}}{\Omega(G) - 1} + \frac{\text{OPT}}{\Omega(G) - 2} + \dots$$

$$+ \frac{\text{OPT}}{\Omega(G) - (\Omega(G) - 2)}$$

$$+ \frac{\text{OPT}}{\Omega(G) - (\Omega(G) - 1)}$$

$$\leq (\ln(\Omega(G)) + 1) \text{OPT}. \quad (22)$$

5. Performance Evaluation

5.1. Before the Simulation Setup. Because there is no real data set which is consistent with the proposed system model, we have to mine the ways of human mobility from Gowalla [52] and Brightkite [53], which come from the location-based social networking website where users share their locations by checking-in. The details of the data sets are listed in Table 7.

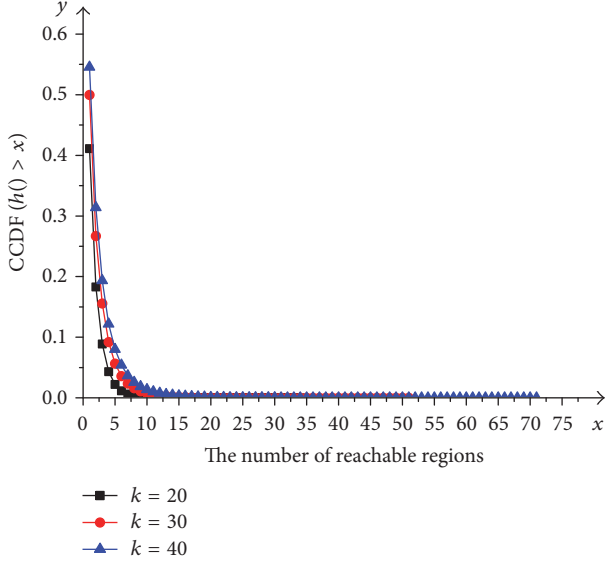
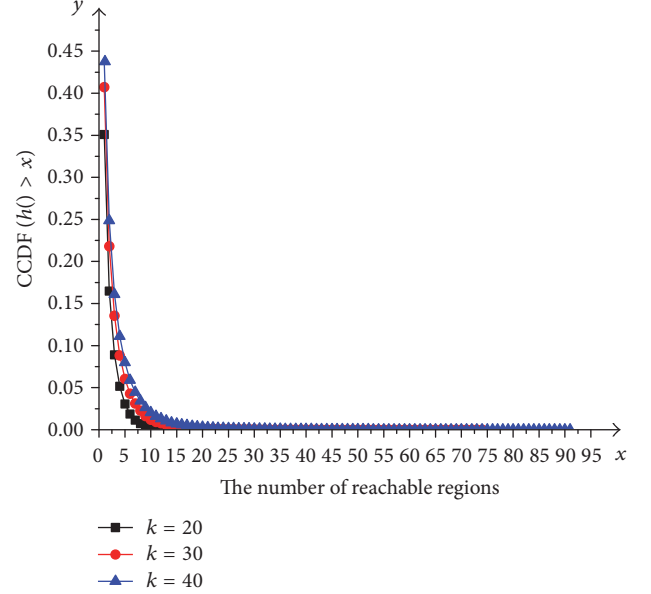
We consider the variation law of user's mobile preferences because the sensing task is dependent on location in most crowd sensing systems. Observing a user's visiting history can help discover the user's abilities to fulfill the subtasks in different locations.

We divide the region Q into $k * k$ square blocks and let $q(x, y) \in Q$ denote the block in which $x, y \in \{1, 2, \dots, k\}$ represents horizontal and vertical locations, respectively. Let $f_i(t, q(x, y))$ denote the number of checking-ins of user i during the time period $t \in [t_1, t_2]$ in block $q(x, y)$. If $f_i(t, q(x, y))$ is greater than zero, $q(x, y)$ is called the reachable region of user i during the time period t .

The reachable regions of user i can be viewed as the subtasks in different locations that the user can fulfill. Let $h(i, t)$ denote the number of reachable regions which can be

TABLE 7: Facts about studied traces.

| Trace source | Brightkite | Gowalla |
|-------------------------|----------------|----------------|
| Time/duration of trace | 2008/4–2010/10 | 2009/2–2010/10 |
| The number of users | 58228 | 196591 |
| The number of check-ins | 4491143 | 6442890 |

FIGURE 3: The complementary cumulative distribution of $h(i, t)$ in Gowalla.FIGURE 4: The complementary cumulative distribution of $h(i, t)$ in Brightkite.

viewed as the number of subtasks that the user can fulfill, which is calculated by

$$h(i, t) = \sum_{x=1}^k \sum_{y=1}^k \eta_i(t, q(x, y)), \quad (23)$$

$$\eta_i(t, q(x, y)) = \begin{cases} 0, & f_i(t, q(x, y)) = 0, \\ 1, & f_i(t, q(x, y)) > 0. \end{cases}$$

With different partition granularity in different data set, more than 95% of the users' number of reachable regions is smaller than 1.25% of the number of region blocks; the complementary cumulative distribution of $h(i, t)$ follows the same power-law distribution formulated by (24), which can be seen in Figures 3 and 4, respectively.

$$p(X > x) = \left(\frac{x}{x_{\min}} \right)^{-k}. \quad (24)$$

The phenomenon of power-law distribution is consistent with our life experience: the activity scope of most people has a limited range in several specific regions in their daily life. The above-mentioned result tells us how to set the number of subtasks that the user can fulfill.

5.2. Performance Evaluation. In order to evaluate QAIM, we first introduce two baseline algorithms with the similar ideas of using redundancy.

- (i) $\max(K)$ is derived from the K -depth coverage objective solution proposed in [43]. No matter how different the sensing quality factor of each subtask is, K is set to the maximal value of these quality factors.
- (ii) Greedy(1) is derived from the idea proposed in [41]. No matter how many subtasks one participant can do, he is only assigned with one subtask at a time. So, the participant is selected in the nondecreasing order of the bid price.

The performance metrics include the social cost, the number of winners, the running time, and the truthfulness, and the importance of reputation score is also checked up.

Simulation parameters are shown in Table 8. Each measurement is averaged over 100 instances.

(1) *Impact of $|U|$.* Figures 5–7 show the performance of QAIM(S) with different candidates when the number of sensing subtasks is set to 100. As shown in Figures 5 and 6, the social cost and the number of winners of QAIM(S) are both less than those of Greedy(1) or $\max(K)$. The variation does not follow the rule of decreasing with increment of the

TABLE 8: Simulation settings.

| Simulation parameters | Settings |
|---|--|
| $h(g_k)$ | Uniformly distributed over $[3, 7]$ |
| b_{v_i} | Uniformly distributed over $[5, 7]$ |
| $\psi_{v_i} = \{g_1^{v_i}, g_2^{v_i}, \dots, g_k^{v_i}\}$ | $g_k^{v_i}$ is random in G but $ \psi_{v_i} $ is between 3 and 10 which abides to Pareto distribution with $x_{\min} = 1$ and $k = 1.75$. |

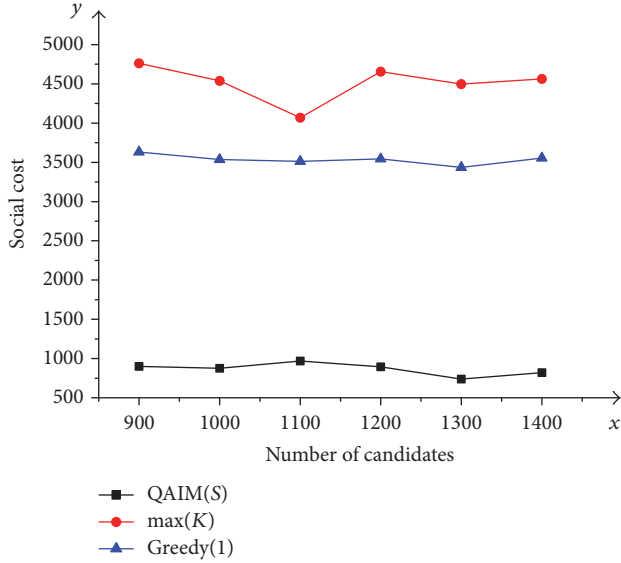


FIGURE 5: The social cost with different candidates.

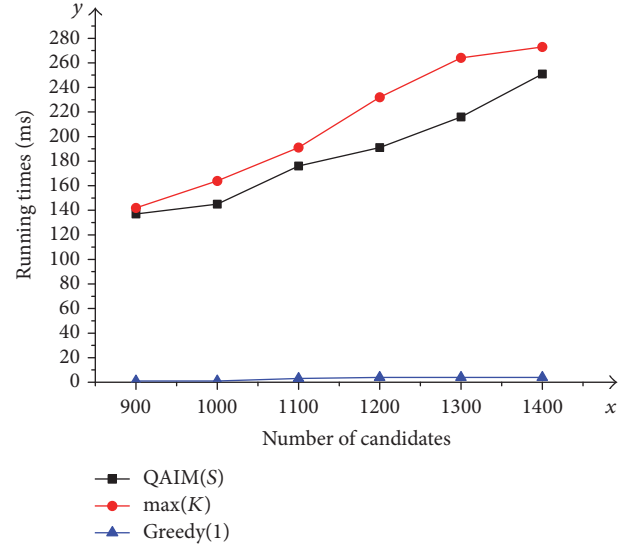


FIGURE 7: The running time with different candidates.

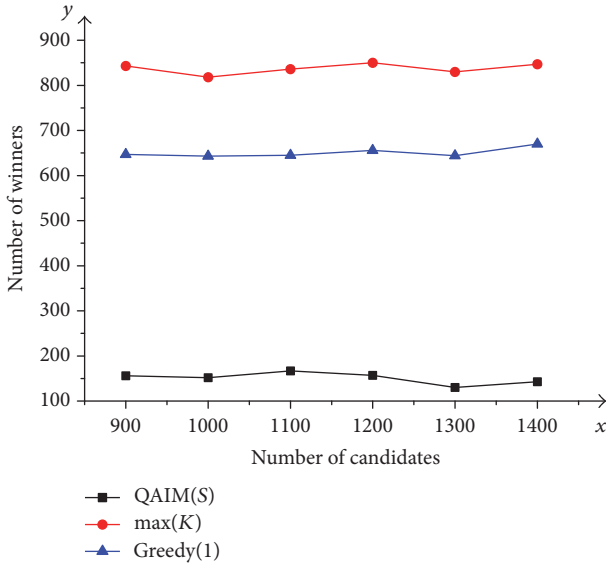


FIGURE 6: The number of winners with different candidates.

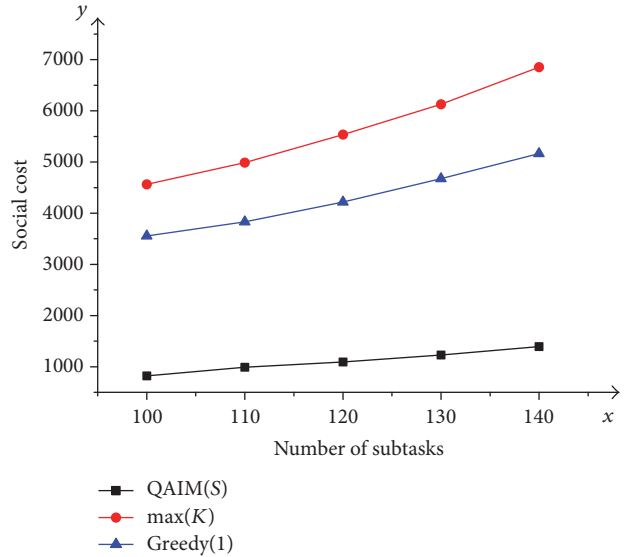


FIGURE 8: The social cost with different number of sensing subtasks.

number of candidates but is within a certain range. The reason is $h(g_k)$ and b_{v_i} which are generated randomly. QAIM(S) has superiority in achieving high quality crowd sensing with minimum social cost. The running time of QAIM(S) is larger than Greedy(1) but less than max(K) as shown in Figure 7. The variation trend of the running time is consistent with

the property of theoretical analysis which increases with the increasing number of candidates.

(2) *Impact of $|G|$* . Figures 8–10 show the performance with a fixed number of 1400 candidates when the number of sensing subtasks varies from 100 to 140 with increment of 10. As shown in Figures 8 and 9, both the social cost and the number

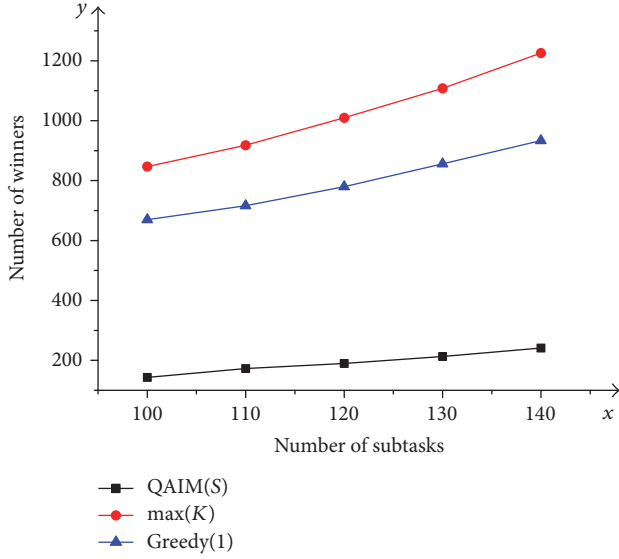


FIGURE 9: The number of winners with different number of sensing subtasks.

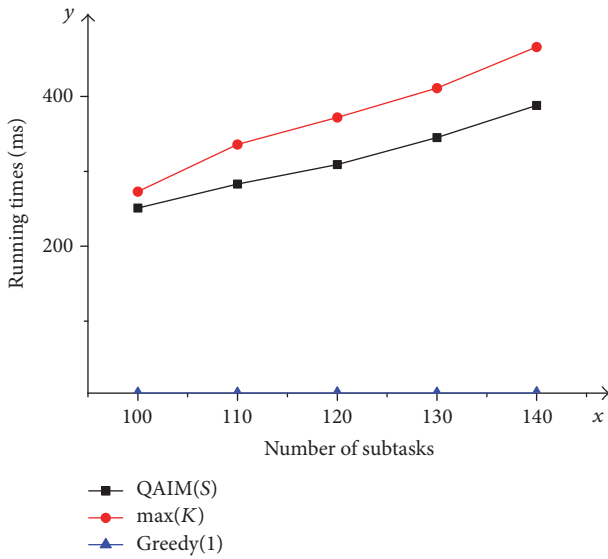


FIGURE 10: The running time with different number of sensing subtasks.

of winners of QAIM(S) increase with the increment of $|G|$ and are less than other algorithms. The running time of QAIM(S) is larger than Greedy(1) but less than max(K) and increases with $|G|$ as shown in Figure 10, which is consistent with the property of theoretical analysis.

(3) *Truthfulness.* We verified the truthfulness of QAIM with different candidates when the number of subtasks is set to 100. We randomly selected the 78th participant and changed the bid price b_{78} of the 78th participant. When $b_{78} > p_{78}$, the 78th participant would not be selected. The running time of QAIM(P) is recorded in Figure 11 which shows the time cost of the truthfulness. The running time of QAIM(P) is bounded by 80 and increases with the increment of the number of

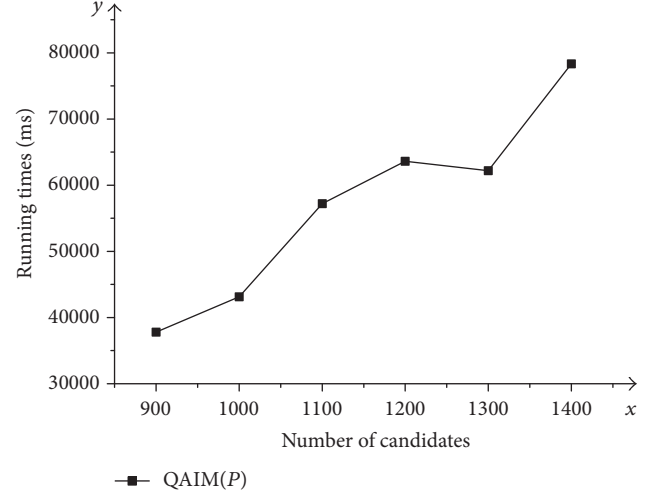


FIGURE 11: The running time of QAIM(P) with different candidates.

candidates except when the number of candidates is 1300, which is a reasonable phenomenon since the running time of QAIM(P) is related to not only the number of candidates but also the number of winners.

(4) *The Effect of Reputation Value.* Finally, we verified the importance of the calculation of reputation value. We first set the 78th participant as the malicious user and offer the contrary sensing result to correct ones of all subtasks intentionally; we find that it would not be selected after the second test. Then we reset the reputation score to 1 and let the 78th participant be selected but the 78th participant does not fulfill one of the subtasks; we find that it would be selected after the second test and would not be selected after the third test.

6. Conclusion

In this paper, we address the fundamental research issue: how can we achieve high quality crowd sensing with the minimum social cost? To answer this question, we study different conditions of recruiter and candidates in crowd sensing system. Based on the findings, we formulate the sensing quality assurance problem as an optimization problem (MQMUS) and prove it to be NP-hard. We design a polynomial-time greedy approximation algorithm QAIM which consists of two phases: QAIM(S) selects appropriate participants to satisfy the objective of this research which approximates the optimal solution with the times of $\ln(\Omega(G)) + 1$ and QAIM(P) eliminates the fear of market manipulation. Through rigorous theoretical analysis, we demonstrate the proposed mechanisms with the properties of high computation efficiency, individual rationality, and truthfulness and then evaluate our algorithm using synthetic data with the features of real data sets. Evaluations show that our algorithms outperform existing approaches. In the future work, we will explore the quality-aware incentive mechanisms in more complex scenarios, for example, how to prevent cocheating using the

history of mobility traces and the completed tasks list of participants.

Appendix

The MQMUS Problem Is NP-Hard

Demonstration. In order to prove that the MQMUS problem is NP-hard, we first prove that the MQMUS₁ problem is NP-hard. We define MQMUS₁ as a special case of MQMUS in which every $h(g_k)$ is equal to one. Thereafter, we conclude that the MQMUS problem is NP-hard.

The problem of MQMUS₁ can be illustrated below which is a set cover problem with weight b_i .

Given a set of elements $G = \{g_1, g_2, \dots, g_k, \dots, g_e\}$ and a set of $B = \{B_1, B_2, \dots, B_k, \dots, B_n\}$ in which ψ_i is the subset of G and b_i is the cost of ψ_i , the problem of MQMUS₁ is to find a collection $S = \{B_{s_1}, B_{s_2}, \dots, B_{s_k}\}$ from B such that the union of ψ_{s_i} equals G with the least costs. We cannot find an efficient optimal solution for the special case of MQMUS₁ in polynomial time, so MQMUS₁ is NP-hard.

MQMUS₁ is a special instance of MQMUS while $h(g_k)$ varies with different sensing quality requirement. Therefore, MQMUS is also NP-hard.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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References

- [1] R. K. Ganti, F. Ye, and H. Lei, "Mobile crowdsensing: current state and future challenges," *IEEE Communications Magazine*, vol. 49, no. 11, pp. 32–39, 2011.
- [2] V. Sivaraman, J. Carrapetta, K. Hu, and B. G. Luxan, "Haze-Watch: a participatory sensor system for monitoring air pollution in Sydney," in *Proceedings of the IEEE 38th Conference on Local Computer Networks Workshops (LCN '13)*, pp. 56–64, IEEE Computer Society, Sydney, Australia, October 2013.
- [3] R. K. Rana, C. T. Chou, S. S. Kanhere, N. Bulusu, and W. Hu, "Ear-phone: an end-to-end participatory urban noise mapping system," in *Proceedings of the 9th ACM/IEEE International Conference on Information Processing in Sensor Networks (IPSN '10)*, pp. 105–116, Stockholm, Sweden, April 2010.
- [4] N. Maisonneuve, M. Stevens, M. E. Niessen, and L. Steels, "NoiseTube: Measuring and mapping noise pollution with mobile phones," in *Information Technologies in Environmental Engineering*, Environmental Science and Engineering, pp. 215–228, Springer Berlin Heidelberg, Heidelberg, Germany, 2009.
- [5] P. Mohan, V. Padmanabhan N, and R. Ramjee, "Nericell: rich monitoring of road and traffic conditions using mobile smartphones," Tech. Rep. 323-336, Microsoft Technical Report, Raleigh, NC, USA, 2008.
- [6] E. Koukoudidis, L.-S. Peh, and M. R. Martonosi, "SignalGuru: leveraging mobile phones for collaborative traffic signal schedule advisory," in *Proceedings of the 9th International Conference on Mobile Systems, Applications, and Services*, pp. 127–140, ACM, Bethesda, Md, USA, July 2011.
- [7] A. Thiagarajan, L. Ravindranath, K. LaCurts et al., "VTrack: accurate, energy-aware road traffic delay estimation using mobile phones," in *Proceedings of the 7th ACM Conference on Embedded Networked Sensor Systems (SenSys '09)*, pp. 85–98, November 2009.
- [8] S. Reddy, A. Parker, J. Hyman, J. Burke, D. Estrin, and M. Hansen, "Image browsing, processing, and clustering for participatory sensing: Lessons from a DietSense prototype," in *Proceedings of the 4th Workshop on Embedded Networked Sensors, EmNets 2007*, pp. 13–17, IRL, June 2007.
- [9] E. Miluzzo, N. D. Lane, K. Fodor et al., "Sensing meets mobile social networks: the design, implementation and evaluation of the cenceme application," in *Proceedings of the 6th ACM Conference on Embedded Networked Sensor Systems (SenSys '08)*, pp. 337–350, ACM, New York, NY, USA, November 2008.
- [10] W. Dong, B. Lepri, and S. Pentland, "Tracking co-evolution of behavior and relationships with mobile phones," *Tsinghua Science and Technology*, vol. 17, no. 2, pp. 136–151, 2012.
- [11] Z. Yang, C. Wu, and Y. Liu, "Locating in fingerprint space: wireless indoor localization with little human intervention," in *Proceedings of the 18th Annual International Conference on Mobile Computing and Networking (Mobicom '12)*, pp. 269–280, ACM, Istanbul, Turkey, August 2012.
- [12] C. Costa, C. Laoudias, D. Zeinalipour-Yazti, and D. Gunopulos, "SmartTrace: Finding similar trajectories in smartphone networks without disclosing the traces," in *Proceedings of the 2011 IEEE 27th International Conference on Data Engineering, ICDE 2011*, pp. 1288–1291, April 2011.
- [13] S. Matyas, C. Matyas, C. Schlieder, P. Kiefer, H. Mitarai, and M. Kamata, "Designing location-based mobile games with a purpose - Collecting geospatial data with cityexplorer," in *Proceedings of the 2008 International Conference on Advances in Computer Entertainment Technology, ACE 2008*, pp. 244–247, December 2008.
- [14] Sensorly. <http://www.sensorly.com>.
- [15] S. B. Eisenman, E. Miluzzo, N. D. Lane, R. A. Peterson, G.-S. Ahn, and A. T. Campbell, "The BikeNet mobile sensing system for cyclist experience mapping," in *Proceedings of the 5th International Conference on Embedded Networked Sensor Systems (SenSys '07)*, pp. 87–101, Sydney, Australia, November 2007.
- [16] Y. Liu, Y. Zhao, L. Chen, J. Pei, and J. Han, "Mining frequent trajectory patterns for activity monitoring using radio frequency tag arrays," *IEEE Transactions on Parallel and Distributed Systems*, vol. 23, no. 11, pp. 2138–2149, 2012.
- [17] P. Zhou, Y. Zheng, and M. Li, "How long to wait?: predicting bus arrival time with mobile phone based participatory sensing," in *Proceedings of the 10th International Conference on Mobile Systems, Applications, and Services (MobiSys '12)*, pp. 379–392, ACM, June 2012.

- [18] L. Barkhuus, M. Chalmers, P. Tennent et al., "Picking Pockets on the Lawn: The Development of Tactics and Strategies in a Mobile Game [C]," in *Proceedings of UBIComp*, pp. 358–374, 2005.
- [19] C. Schlieder, "Representing the meaning of spatial behavior by spatially grounded intentional systems," *Lecture Notes in Computer Science*, vol. 3799, pp. 30–44, 2005.
- [20] M. Bell, M. Chalmers, L. Barkhuus et al., "Interweaving mobile games with everyday life," in *Proceedings of the CHI 2006: Conference on Human Factors in Computing Systems*, pp. 417–426, April 2006.
- [21] P. Kiefer, S. Matyas, and C. Schlieder, "Playing on a line: Location-based games for linear trips," in *Proceedings of the 4th International Conference on Advances in Computer Entertainment Technology, ACE 2007*, pp. 250–251, June 2007.
- [22] N. Bulusu, C. Chou T, S. Kanhere et al., "Participatory Sensing in Commerce: Using Mobile Phones to Track Market Price Dispersion," *Proc. Urbansense*, pp. 6–10, 2008.
- [23] L. Deng and L. P. Cox, "Live compare: grocery bargain hunting through participatory sensing," in *Proceedings of the 10th Workshop on Mobile Computing Systems and Applications (HotMobile '09)*, pp. 1–6, ACM, New York, NY, USA, February 2009.
- [24] B. L. Sullivan, C. L. Wood, M. J. Iliff, R. E. Bonney, D. Fink, and S. Kelling, "eBird: a citizen-based bird observation network in the biological sciences," *Biological Conservation*, vol. 142, no. 10, pp. 2282–2292, 2009.
- [25] M. Bell, S. Reeves, B. Brown et al., "EyeSpy," in *Proceedings of the SIGCHI Conference*, p. 123, Boston, MA, USA, April 2009.
- [26] E. Kanjo, "NoiseSPY: a real-time mobile phone platform for urban noise monitoring and mapping," *Mobile Networks and Applications*, vol. 15, no. 4, pp. 562–574, 2010.
- [27] K. Han, E. A. Graham, D. Vassallo, and D. Estrin, "Enhancing motivation in a mobile participatory sensing project through gaming," in *Proceedings of the 2011 IEEE International Conference on Privacy, Security, Risk and Trust, PASSAT 2011 and 2011 IEEE International Conference on Social Computing, SocialCom 2011*, pp. 1443–1448, October 2011.
- [28] B. Hoh, T. Yan, D. Ganesan, K. Tracton, T. Iwuchukwu, and J.-S. Lee, "TruCentive: a game-theoretic incentive platform for trustworthy mobile crowdsourcing parking services," in *Proceedings of the 15th International IEEE Conference on Intelligent Transportation Systems (ITSC '12)*, pp. 160–166, IEEE, Anchorage, Alaska, USA, September 2012.
- [29] K. O. Jordan, I. Sheptykin, B. Grüter, and H.-R. Vatterrott, "Identification of structural landmarks in a park using movement data collected in a location-based game," in *Proceedings of the 1st ACM SIGSPATIAL International Workshop on Computational Models of Place, COMP 2013*, pp. 1–8, November 2013.
- [30] L. Duan, T. Kubo, K. Sugiyama, J. Huang, T. Hasegawa, and J. Walrand, "Incentive mechanisms for smartphone collaboration in data acquisition and distributed computing," in *Proceedings of the IEEE Conference on Computer Communications (INFOCOM '12)*, pp. 1701–1709, Orlando, Fla, USA, March 2012.
- [31] D. Yang, G. Xue, X. Fang et al., "Crowdsourcing to smartphones: incentive mechanism design for mobile phone sensing," in *Proceedings of the 18th Annual International Conference on Mobile Computing and Networking (MobiCom '12)*, pp. 173–184, ACM, August 2012.
- [32] J.-S. Lee and B. Hoh, "Sell your experiences: A market mechanism based incentive for participatory sensing," in *Proceedings of the 8th IEEE International Conference on Pervasive Computing and Communications, PerCom 2010*, pp. 60–68, April 2010.
- [33] Z. Feng, Y. Zhu, Q. Zhang, L. M. Ni, and A. V. Vasilakos, "TRAC: Truthful auction for location-aware collaborative sensing in mobile crowdsourcing," in *Proceedings of the 33rd IEEE Conference on Computer Communications, IEEE INFOCOM 2014*, pp. 1231–1239, May 2014.
- [34] X. Zhang, G. Xue, R. Yu, D. Yang, and J. Tang, "Truthful incentive mechanisms for crowdsourcing," in *Proceedings of the 34th IEEE Annual Conference on Computer Communications and Networks, IEEE INFOCOM 2015*, pp. 2830–2838, May 2015.
- [35] J. Xu, J. Xiang, and D. Yang, "Incentive Mechanisms for Time Window Dependent Tasks in Mobile Crowdsensing," *IEEE Transactions on Wireless Communications*, vol. 14, no. 11, pp. 6353–6364, 2015.
- [36] J. Xu, J. Xiang, and Y. Li, "Incentivize maximum continuous time interval coverage under budget constraint in mobile crowd sensing," *Wireless Networks*, vol. 23, no. 5, pp. 1–14, 2017.
- [37] A. Subramanian, G. Kanth S, and R. Vaze, "Offline and Online Incentive Mechanism Design for Smart-phone Crowdsourcing," *Computer Science*, pp. 1–12, 2013.
- [38] D. Zhao, X.-Y. Li, and H. Ma, "How to crowdsource tasks truthfully without sacrificing utility: Online incentive mechanisms with budget constraint," in *Proceedings of the 33rd IEEE Conference on Computer Communications, IEEE INFOCOM 2014*, pp. 1213–1221, May 2014.
- [39] L. Jaimes G, I. Vergara-Laurens, and M. Labrador, "A Location-Based Incentive Mechanism for Participatory Sensing Systems with Budget Constraints," *Dissertations Theses-Gradworks*, vol. 25, no. 3, pp. 103–108, 2012.
- [40] H. Jin, L. Su, D. Chen, K. Nahrstedt, and J. Xu, "Quality of information aware incentive mechanisms for mobile crowd sensing systems," in *Proceedings of the 16th ACM International Symposium on Mobile Ad Hoc Networking and Computing (MobiHoc '15)*, pp. 167–176, ACM, Hangzhou, China, June 2015.
- [41] X. Zhang, Z. Yang, Y. Gong, Y. Liu, and S. Tang, "Spatial Recruiter: Maximizing sensing coverage in selecting workers for spatial crowdsourcing," *IEEE Transactions on Vehicular Technology*, vol. 66, no. 6, 2017.
- [42] J. Xu, H. Li, Y. Li, D. Yang, and T. Li, "Incentivizing the Biased Requesters: Truthful Task Assignment Mechanisms in Crowdsourcing," in *Proceedings of the 2017 14th Annual IEEE International Conference on Sensing, Communication, and Networking (SECON)*, pp. 1–9, San Diego, Calif, USA, June 2017.
- [43] H. Xiong, D. Zhang, G. Chen, L. Wang, V. Gauthier, and L. E. Barnes, "ICrowd: Near-Optimal Task Allocation for Piggyback Crowdsensing," *IEEE Transactions on Mobile Computing*, vol. 15, no. 8, pp. 2010–2022, 2016.
- [44] Y. Wang, X. Jia, Q. Jin, and J. Ma, "QuaCentive: a quality-aware incentive mechanism in mobile crowdsourced sensing (MCS)," *Journal of Supercomputing*, vol. 72, no. 8, pp. 2924–2941, 2016.
- [45] Z. He, J. Cao, and X. Liu, "High quality participant recruitment in vehicle-based crowdsourcing using predictable mobility," in *Proceedings of the 34th IEEE Annual Conference on Computer Communications and Networks, IEEE INFOCOM 2015*, pp. 2542–2550, May 2015.
- [46] D. Fudenberg and J. Tirole, *Game Theory*, MIT Press, 1991.
- [47] V. Krishna, *Auction Theory*, Academic Press, 2009.
- [48] C. Tanas and J. Herrera-Joancomarti, "When users become sensors: Can we trust their readings?" *International Journal of Communication Systems*, vol. 28, no. 4, pp. 601–614, 2015.
- [49] L. Kazemi, C. Shahabi, and L. Chen, "GeoTruCrowd: Trustworthy query answering with spatial crowdsourcing," in *Proceedings*

of the 21st ACM SIGSPATIAL International Conference on Advances in Geographic Information Systems, ACM SIGSPATIAL GIS 2013, pp. 304–313, ACM, November 2013.

- [50] James., *The Wisdom of Crowds: Why The Many Are Smarter than The Few and How Collective Wisdom Shapes Business, Economies, Societies and Nations*, Doubleday, 2004.
- [51] R. B. Myerson, “Optimal auction design,” *Mathematics of Operations Research*, vol. 6, no. 1, pp. 58–73, 1981.
- [52] Gowalla [EB/OL]. <http://snap.stanford.edu/data/loc-gowalla.html>
- [53] Brightkite [EB/OL]. <http://snap.stanford.edu/data/loc-brightkite.html>.

