

# Adaptive GP-based Algorithm for Hardware/Software Co-design of Distributed Embedded Systems

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**Keywords:** Embedded Systems, Genetic Programming, Genetic Algorithm, Architecture, Hardware/Software Co-design, Adaptive Systems.

**Abstract:** In this work, a novel adaptive approach to co-design of embedded systems is presented. The approach is based on developmental genetic programming. Unlike most of existing algorithms, presented methodology involves evolving co-synthesis process, not the system architecture directly. Genotype is a tree which nodes include system construction options. The system can adapt to the environment by increasing chromosomes which give better results in each situations. Half of the next populations is created using genetic operators (crossover, mutation, reproduction). Second half is obtained by generating additional solutions but with different probability of the options.

## 1 INTRODUCTION

Nowadays we are surrounded by many embedded systems: SoC systems, modern cars, mobile phones, digital cameras, etc. Thus it is necessary to find effective design methodologies. Co-design (De Micheli and Gupta, 1997) is a process which automatically gives an architecture of embedded system. The goal of the process is to optimize parameters such time, cost or power consumption. Most of existing solutions (eg. Jiang, Eles and Peng, 2012) assume distributed target architecture consisting of many processing elements (PE), which can be divided into two groups: programmable processors (PP) and hardware cores (HC). Co-design process consists of: 1. allocation – choice of number and types of resources and communication channels; 2. assignment – choice of PE for each task and transmission between resources; 3. task scheduling – determining when each task should begin its execution.

Most of existing methods are iterative improvement algorithms (Yen and Wolf 1995; Deniziak, 2004) which start from sub-optimal solution and, by local changes, try to improve the system quality. Usually, as the initial solution, the fastest architecture (where each task is executed on different PE) is selected, but the results are still sub-optimal. Constructive algorithms (Bharat,

Lakshminarayana and Jha, 1997) build system step by step by choosing PE for each task separately. Those methods tend to stop in local minima of optimizing parameters.

Probabilistic algorithms, especially genetic algorithms (Chehida and Auguin, 2002; Purnaprajna, Reformat and Pedrycz, 2007), can escape from local minima. This group of algorithms is represented for example by simulated annealing (Eles, Peng, Kuchciński and Doboli, 1997). Good results were obtained using developmental genetic programming (Deniziak and Górski, 2008). This algorithm builds initial population and generates next populations using genetic operators.

The most important weakness of this methodology is that probability of choosing each option is constant. In some cases obtaining better solutions is possible only after changing the probabilities. Therefore in computer system design adaptive algorithms are more and more popular (Shankaran, Roy, Schmidt, Koutsoukos, Chen and Lu, 2008).

Genetic programming (Koza, Bennett III, Lohn, Dunlap, Keane and Andre, 1997) is an extension of genetic algorithms (Holland, 1992). The main idea of genetic programming is the evolution of computer programs. The most important difference between genetic algorithm and genetic programming is the difference between genotype (the tree) and phenotype (the final solution). Each node in

genotype represents parts of computer programs.

In this article a new self-adaptive approach based on developmental genetic programming (Koza, 2010) is presented. The main advantage of proposed solution is the possibility of making changes of probabilities when the algorithm is running. Thus the algorithm can adjust to the behaviour without manual modification of initial conditions. Probability of stopping in local minimum is decreasing. Algorithm is described in section 3. Sections 4 and 5 present experimental results and conclusions.

## 2 PRELIMINARIES

Embedded system is specified by an acyclic directed graph called the task graph. Each node  $v_i \in V$  represents task, and edge  $e_i \in E$  presents dependence between tasks. Every edge has a label  $d_{ij}$  which describes the amount of data that has to be sent between two connected tasks. Example of a task graph is presented on fig. 1. The graph includes 7 tasks.

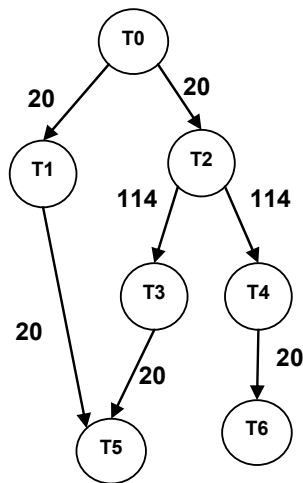


Figure 1: Example of task graph.

Table 1 presents an example of a resource database for the graph on figure 1. Here we proposed to use two programmable processors (PP1 and PP2), two Hardware cores (HC1 and HC2) and two communication links (CL1 and CL2). Every task is defined by time of execution (t) and an area occupied by this task. Areas occupied by the tasks mean the size of memory needed to execute these task. Each communication link is defined by a bandwidth (b) and an area (s) occupied by the link connected to PE. HC can only execute one task.

Table 1 also includes the area (S) occupied by each PE. The area of the tasks implemented in HC includes the area occupied by the core. Task T2 is not compatible with PP1, and task T5 can't be implemented in HC2. Communication link CL2 is not compatible with PP1.

Table 1: Resource database.

Task	PP1 S=200		PP2 S=300		HC1		HC2	
	t	s	t	s	t	s	t	s
T0	150	4	120	6	50	180	30	250
T1	40	3	35	2	14	100	10	140
T2	-	-	320	17	250	200	150	650
T3	235	10	220	15	140	160	90	200
T4	165	8	150	10	65	100	40	140
T5	70	4	40	5	25	100	-	-
T6	23	2	20	1	5	40	2	80
CL1, b=6	s=2		s=2		s=10			
CL2, b=15	-		s=2		s=15			

Target architecture of the system described by the above graph consists of n processes, m programmable processors and p communication links (CLs) selected from available resources as specified in table 1. Overall area ( $S_o$ ) of the constructed system is described by the following formula:

$$S_o = \sum_{i=1}^m S_{PE_i} + \sum_{j=1}^n S_j + \sum_{k=1}^p \sum_{l=1}^{P_k} S_{CL_k, PC_l} \quad (1)$$

T is the time when execution of the last task is finished. Parameters u and q are set manually. The fitness function (F) is described below:

$$F = u * S + q * T \quad (2)$$

The goal of co-design is to find an architecture with the lowest F value.

## 3 THE ALGORITHM

In accordance with genetic programming rules the genotype is evolving. It is based on task graph, each node in the tree corresponds to equal system constructing function. The embryo is an implementation of the first task on randomly chosen PE. At the beginning initial population is created containing randomly generated genotypes.  $\Pi$  is the size of initial population:

$$\Pi = \alpha * n * p \quad (3)$$

where:  $n$  – number of tasks in task graph,  
 $p$  – number of possible PEs,  $\alpha$  – parameter which controls the number of individuals in populations; it is set manually.

Table 2: Options for constructing system.

Step	Option
PE	a. min ( $s*t$ ) between used PEs
	b. PE with the lowest time of execution of all allocated tasks
	c. the fastest
	d. min ( $s*t$ )
	e. the lowest cost
	f. not used from kind of the rarest used
CL	a. the lowest cost
	b. the highest b
	c. last used
Task scheduling	list scheduling

The system is constructed by executing functions in order corresponding to the level of the node in the genotype tree. Then solutions are sorted by the lowest fitness function. Algorithm counts how many times each function appears in first rank list, the percentage result is a new value of the probability of a chosen option. New populations are obtained using genetic operators: crossover, mutation and selection (half of the population) and by generating new individuals using options in table 2 but with modified probability. The number of individuals obtained by using genetic operators is given:

- $\Phi = \beta * \Pi / 2$  – individuals obtained by selection;
- $\Psi = \gamma * \Pi / 2$  – individuals obtained by crossover;
- $\Omega = \delta * \Pi / 2$  – individuals obtained by mutation;
- $\beta + \gamma + \delta = 1$  – this condition should be satisfied to have the same number of individuals in each population.

The values of parameters  $\beta$ ,  $\gamma$ ,  $\delta$  are set manually. They control the evolution process.

Selection copies the  $\Phi$  solution from the current population. Individuals are chosen randomly but with different probability dependent on the position in rank list:

$$P = \frac{\Pi - r}{\Pi} \quad (4)$$

Crossover chooses randomly the  $\Psi$  solutions. To prevent the algorithm from stopping in local minima, the best of chosen individuals are crossed over with the worst. The crossing point is selected randomly - the same for both genotypes and then substitutes the sub-trees.

Mutation randomly selects one individual and one node, afterwards changes option in this node to a different one from the option list, but with probability currently selected in the population.

The process is stopped when solution with lower function  $F$  wasn't found in next  $\epsilon$  steps (last  $\epsilon$  generations). Parameter  $\epsilon$  is set manually.

Figure 2 shows an example of genotype for the task graph of figure 1.

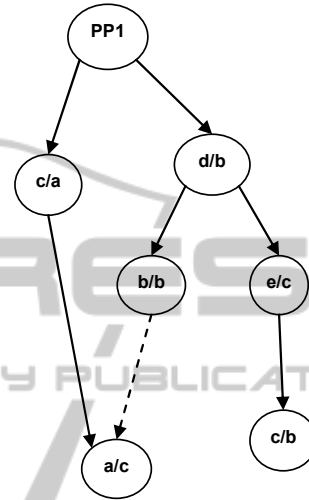


Figure 2: Example of genotype.

Implementation of the first task (the embryo) is chosen randomly on PP1. Second task is executed on HC2 as the fastest. For the transmission between  $T0$  and  $T1$  CL1 is chosen. Third task can be implemented on PP2 choosing option min ( $s*t$ ) and CL1 is used for the transmission. Fourth task can be assigned to HC2 (PE with the lowest time of execution of all allocated tasks), CL2 is chosen for the transmission (the highest b). Next task can be executed on PP1 using option the lowest cost. Sixth task can be assigned on PP2 (min ( $s*t$ ) between used PEs). For the last task the fastest implementation (HC2) was chosen, and CL2 was used for the transmission (the highest b).

## 4 EXPERIMENTAL RESULTS

Because of very large computational complexity of the co-design problem, the only way to check effectiveness of the proposed methodology is to compare the performance with other existing methods. All experiments were carried out on randomly generated graphs with 10 and 30 nodes.

In table 3 the results are compared with DGP

algorithm (Deniziak and Górski, 2008) and Yen-Wolf (Yen and Wolf, 1995) for co-design. Algorithm DGP was compared with algorithm Ewa (Deniziak, 2004). Part of the results were also obtained using the task graphs presented in the present work. Algorithm Ewa was proved to be more effective than MOGAC (Dick and Jha, 1998). In every experiment the parameters were set to:  $u=8$ ,  $q=1$ ,  $\epsilon=5$ ,  $\beta = 0,1$ ,  $\gamma = 0,3$ ,  $\delta = 0,6$ .

Table 3: Experimental results.

graph	Yen Wolf	DGP		ADGP	
		min F	Average F	min F	Average F
10	12899	9017	9247	<b>8179</b>	<b>8538</b>
30	28301	18835	19067	<b>16439</b>	<b>21402</b>

For the graph with 10 nodes, the min. function F value obtained by ADGP was 8179, while for DGP it was 9017, and for Yen-Wolf it was 12899. The average value of function F, for probabilistic algorithms, was also obtained by ADGP – 8538 while for DGP it was 9247. For bigger graph (with 30 nodes) the best average function (18835) was for the DGP algorithm (21402 for ADGP). However comparing the best results the ADGP gives better results for both presented graphs (8179 for graph with 10 nodes, and 16439 for graph with 30 nodes) when compared with DGP (9017 for graph with 10 nodes, and 18835 graph with 30 nodes) and Yen-Wolf (12899 for graph with 10 nodes, and 28301 for graph with 30 nodes).

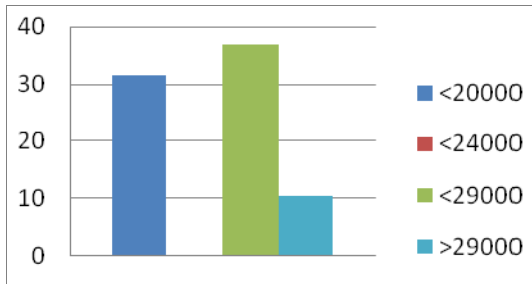


Figure 3: Percentage range of results for  $\alpha=10$ .

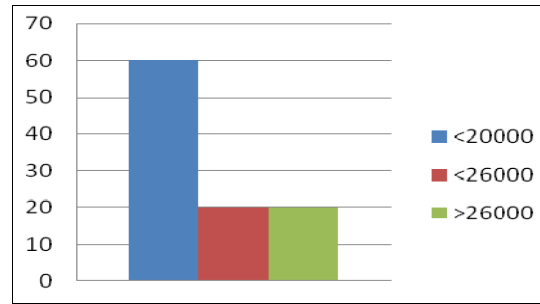


Figure 4: Percentage range of results for  $\alpha=20$ .

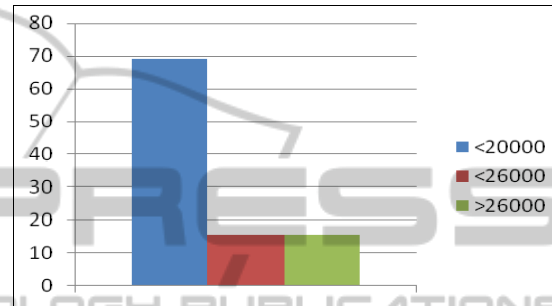


Figure 5: Percentage range of results for  $\alpha=30$ .

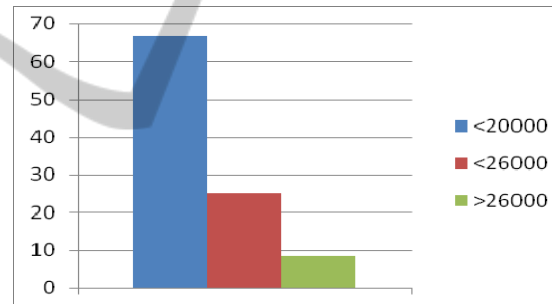


Figure 6: Percentage range of results for  $\alpha=50$ .

Comparison of obtained results for a graph with 30 nodes with different value of parameter  $\alpha$  is presented in table 4. The last column presents percentage difference between average values of DGP and ADGP.

The average results, as presented in table 4, indicate that the algorithm DGP gives solutions with lower F function value but the best individuals are obtained by the methodology presented in this work.

Table 4: Comparison of the results for different size of population.

$\alpha$	DGP		ADGP			$\Delta$ [%]
	min F	average F	min F	average F	max F	
10	19131	19249	<b>16884</b>	<b>23549</b>	<b>30030</b>	22
20	18835	19105	<b>17278</b>	<b>24101</b>	<b>40514</b>	26
30	18835	19008	<b>16673</b>	<b>19953</b>	<b>28046</b>	5
50	18835	18915	<b>16439</b>	<b>19977</b>	<b>28857</b>	6

Figures 3, 4, 5 and 6 indicate that the algorithm is not random. When parameter  $\alpha$  was 10 most of the best results in each trial had the F value between 24000 and 29000 but a large group of best individuals had the value of function F lower than 20000. So it was not accidental that best system was found by using our presented algorithm. Analysis of other figures with bigger value of parameter  $\alpha$  allows to notice more dependencies. In almost every situation most of the best results (60-70% of obtained individuals) are in first (the lowest) area and number of best results in last area (the highest value of F function) is decreasing. When parameter  $\alpha$  was 10 the average value of function F was 23549 for ADGP, while the function value for DGP was 19249. Similar results were obtained for  $\alpha=20$  (24101 for ADGP and 19105 for DGP). For  $\alpha=30$  the average function F was 19953 for ADGP and 19008 for DGP. The bigger parameter  $\alpha$  the smaller the difference between average values of DGP and ADGP (parameter  $\Delta$ ). When value of  $\alpha$  was at least 30 that difference was only about a 5%. However the best solutions (with the smallest function F value), in every cases, were obtained using ADGP (16884, 17278, 16673 and 16439 for adequate values of  $\alpha$ ). What is more the percentage difference of the best solutions obtained with presented methodology and DGP is much bigger than average values of function F. This indicates that ADGP can be more effective than DGP. With increasing  $\alpha$  the maximum value of function F is also reduced.

## 5 CONCLUSIONS

In this work a new approach based on developmental genetic programming for co-synthesis of distributed embedded systems specified by task graphs has been presented. The main innovation of the approach is that the algorithm is based on statistics adaptive to the environment. This is achieved by changing the probability of selection of options constructing the system. First experimental results show that results obtained by the presented methodology are better than those obtained using other known approaches. It should be noted however that in some relatively rare cases results can be worse because of the probabilistic nature of the algorithm.

To compare DGP and ADGP some test like t-test, Mann-Whitney test or Wilcoxon test (Ruxton, 2006) can be made, but we were afraid that they may underestimate the true significance of results.

The future work will concentrate on examining

another chromosomes, genetic operators. We will also test different representations of genotype tree.

## ACKNOWLEDGEMENTS

This work is supported by the Foundation for Polish Science, under grant "Mistrz 2012" No. 9/2012: "New methodologies for designing next-generation micro-electronic circuits".

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