

Parallel Markov-based Clustering Strategy for Large-scale Ontology Partitioning

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Abstract: Actually, huge amounts of data are generated at distributed heterogeneous sources, to create and to share information on several domains. Thus, data scientists need to develop appropriate and efficient management strategies to cope with the heterogeneity and the interoperability issues of data sources. In fact, ontology as schema-less graph model and ontology matching as dynamic real-time large-scale data integration enabler are addressed to design and develop advanced management mechanisms. However, given the large-scale context, we adopt ontology partitioning strategies, which split ontologies into a set of disjoint partitions, as a crucial part to reduce the computational complexity and to improve the performance of the ontology matching process. To this end, this paper proposes a novel approach for large-scale ontology partitioning through parallel Markov-based clustering strategy using Spark framework. This latter offers the ability to run in-memory computations to provide faster and expressive partitioning and to increase the speed of the matching system. The results drawn by our strategy over real-world ontologies demonstrate significant performance which makes it suitable to be incorporated in our large-scale ontology matching system.

1 INTRODUCTION

Nowadays, the proliferation and the adoption of emerging technologies have spawned new research disciplines. Every day, enormous amounts of data are generated in several sectors (Manufacturing, health, social life etc.) resulting in what-is now called Big Data (Bello-orgaz et al., 2016; Jin, 2015). Therefore, appropriate processing and harnessing of this data could reveal sound knowledge and valuable insights and could herald new impetus potentials to sustain productivity growth.

Given the fact that Big Data reside at distributed, heterogeneous sources, we argue that the design and development of advanced Big Data management techniques and technologies requires effective integration mechanisms (cleaning, matching and transforming) and effective analytical exploitations. However, there are many challenges that encumber managing Big Data ranging from those caused by the features of Big Data, as well as, those related to the current data processing strategies (Chen et al., 2013; Chen et al., 2014).

Hence, to build efficient Knowledge-based systems, we address Big Data aspects from data management perspectives by proposing a Big Data management system based on semantic data models as a data integration enabler to cope with Big Data challenges (Mountasser et al., 2015). The integration strategy aims to aggregate various heterogeneous data sources to discover valuable insights in a wide array of domains. As a schema-less graph model, ontologies can describe the knowledge aspects of any domain and can be suitable to resolve data heterogeneity and interoperability issues of overlapped domains.

From this regard, we have already proposed a dynamic large-scale ontology matching approach in conjunction with Big Data features that discover correspondences among resultant ontologies from each data sources (Mountasser et al., 2016). Moreover, we focus on decomposing large and complex ontologies into simpler subsets with performance and scalability-friendly data structures that contribute on the reduction of computational complexity and improve the performance of our system. However, in large scale context, massive

amount of ontologies entities can cause performance impediments during the ontology matching process which negatively impacts the system scalability. Therefore, to proceed matching of large-scale ontologies, ontology partitioning strategies must be adopted to split ontologies into a set of disjoint partitions to increase matching accuracy and to improve memory consumption.

The objective of ontology partitioning approaches is to partition the entities of ontology into several disjoint clusters, so that, the cohesiveness among the entities in a cluster is high while the coupling crossing different clusters is low. For that, this paper presents a novel approach for large-scale ontology partitioning through parallel Markov-based clustering strategy over distributed architecture using Spark framework.

The rest of the paper is structured as follows. In section 2, we describe the related work in the field of graph-based ontology partitioning in the large-scale context. Section 3 describes our proposed methodology and the implementation details. Section 4 provides a comprehensive evaluation of our system on real-world ontologies of various domains and sizes over distributed platform.

2 RELATED WORK

Hu et al., (2008) develop a structure-based partitioning algorithm that firstly, partitions the entities of each ontology into a set of clusters based on their structural proximities, then, they construct blocks using RDF sentences assignment to those clusters.

Similarly to the latter, Albergawy et al., (2011) propose a hierarchical clustering-based approach that represents ontologies as direct acyclic graph. The approach represents each node its own single element cluster, then, the algorithm iteratively merges clusters in descending order of structural similarity. Albergawy et al., (2015) introduce a seeding-based clustering technique that identifies the seeds of clusters using a distribution condition, then; the remaining entities are placed into clusters based on a membership function.

Unfortunately, these works perform ontology partitioning, far afield from the available opportunities of parallel platforms. In other words, using better computational resources can improve memory consumption and achieve faster results. For this reason, using the Hadoop distributed platform, Mountasser et al., (2016) propose parallel entity-assignment clustering system that aims to partition

large-scale ontologies by parallelizing and distributing clustering tasks over available computational resources. First, the algorithm parses and splits ontologies into smaller and simpler resource-based subsets. Using these latter, the system create clusters centroid through the combination of several metrics based on the node importance philosophy. Then, it assigns remaining nodes to their proper clusters based on several similarity metrics.

3 IMPROVED MARKOV CLUSTERING

Let us assume that all the ontologies used by this approach are in the OWL form. Ontologies in this form can be organized as a Directed Acyclic Graph with its nodes describing entities of ontology and the edges between nodes describing the relations (taxonomic and non-taxonomic) between entities.

Our goal of ontology clustering is dividing ontology into a set of clusters with related entities based on a graph structure. To the best of our knowledge, there is no study relating the large scale ontology partitioning using Markov clustering models. Consequently, this paper introduced a novel approach for parallel large-scale ontology partitioning using Markov clustering strategy.

3.1 Preliminaries

In this section, we highlight some pertinent definitions and concepts concerning graph description and Markov clustering strategies, used throughout this approach.

3.1.1 Ontology Parsing

Our approach builds a finite ergodic Markov chain model of ontology by mapping ontology classes to states in the Markov chain and by mapping all relations between classes to state transitions. Hence, ontology is modelled as a directed acyclic graph by considering concepts as a finite set of nodes and including taxonomic and non-taxonomic relationships between classes as a finite set of directed edges.

3.1.2 Notations

Throughout this paper, we assume that $G = (V, E)$ is a directed acyclic graph with V and E represent the node set and edge set respectively. Let A be the

adjacency matrix corresponding to the graph G , with $A(i, j)$ denoting the weight of the edge between the vertex v_i and the vertex v_j . If the graph is non-weighted, which is the case of ontologies, then, the weight on each edge is fixed to 1.

A column stochastic matrix M associated to a graph G can be interpreted as the matrix of the transition probabilities of a random walk defined on the graph, e.g. the i^{th} column of M represents the transition probabilities out of the vertex v_i . The most appropriate way of deriving a column stochastic transition matrix M for a graph G is to simply normalize the columns of the adjacency matrix to sum to 1. Moreover, we define the canonical transition matrix by $M_G = AD^{-1}$, where D is the diagonal degree matrix of the graph G .

3.2 Markov Clustering Approaches

The Markov clustering algorithm is a commonly used graph-based clustering strategy that incorporated the structure of the graphs to reveal the clusters structure.

Markov clustering algorithm (MCL) has been adopted in a wide range of applications (Enright et al., 2002; Wong et al., 2008). The algorithm allows the search for structurally homogeneous subsets by considering a random walk on the graph based on the paradigm that a “random walk that visits a dense cluster will likely not leave the cluster until many of

its vertices have been visited.”. Rather than simulating random walks, MCL iteratively transforms the stochastic flow matrix associated with the graph. It offers various advantages. It is significantly tolerant to noise and behaves robustly (Chen and Ji, 2010).

3.2.1 Markov Clustering

MCL algorithm is an iterative process that applies three operators- expansion, inflation and pruning- to the stochastic matrix until convergence. The stochastic matrix M associated with a graph G is defined by normalizing all columns of the adjacency matrix of G . These operators are mapping the space of the stochastic matrix to itself (Satuluri and Parthasarathy, 2009).

Expand operation: simulates a random walk on the graph (i.e. normal matrix squaring). Thus, it increases the flow between existing nodes.

$$\text{Expand } (M) = M * M \quad (1)$$

Inflate operation: regulates the flow in the graph, strengthens the strong flows and weakens the weak ones. Each element of the matrix is raised to the power of inflation parameter r , then, matrix normalization is performed so that columns sum to 1.

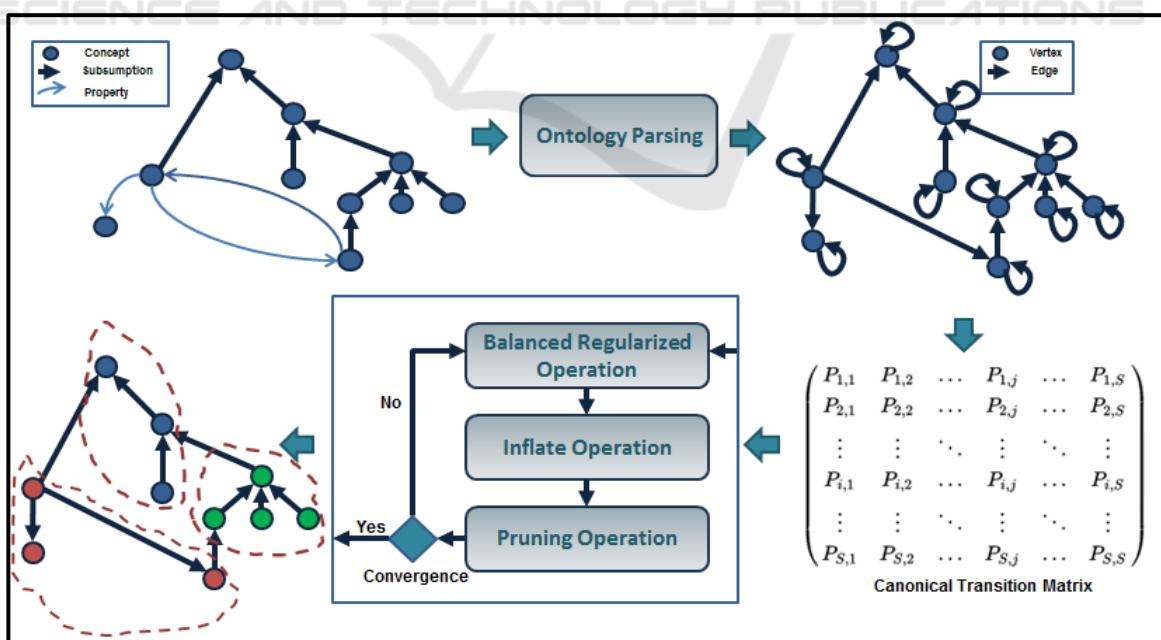


Figure 1: The improved parallel balanced regularized Markov clustering process.

The parameter r can control the outcome of the algorithm by determining the granularity of the obtained clusters, in such a way that, larger parameter (r) can produce finer granularity, and more clusters.

$$Inflate(M) = \frac{M(i,j)^r}{\sum_{k=1}^n M(k,j)^r} \quad (2)$$

Pruning operation: In each column, entries' having values less than some threshold (heuristically computed) is removed, and the remaining entries are normalized to make the column sum to 1. This step aims to reduce the non-zero value in the matrix and hence reduces memory consumption, which helps to accelerate the convergence of the process. Finally, the iteration is interrupted upon reaching a matrix that is invariant under k expansions and inflations.

However, in spite of its advantages, MCL has drawn several limitations; MCL lacks scalability and suffers from fragmentation issue (large clusters and singleton cluster) which is not ideal in large-scale cases.

3.2.2 Regularized Markov Clustering

To retain the strengths of MCL and reduce its limitations Satuluri and Parthasarathy, (2010) proposed a regularized variant of MCL that improves the accuracy and the scalability of the clustering process. Regularized MCL was proposed as a variant of MCL to produce more accurate results and typically more compact clusters than MCL. The RMCL algorithm resolves the output fragmentation issues through regularizing the distribution flow out of the node on conjunction to its neighbours (Satuluri, 2012). Therefore, the Expand operator in MCL algorithm is replaced by the regularize operator which updates the flow distribution of each node.

$$\text{Regularize}(M) = M * M_G \quad (3)$$

where M_G is the canonical flow matrix of the graph G .

Essentially, the impact of the regularize operator consists on setting the out-flow distribution of a node to be the weighted average of the out-flow distributions of its neighbours (Ginanjar et al., 2016). This operator ensures the permanent influence of the original topology of the graph on clustering process beyond the first iteration.

3.2.3 Balanced Regularized Markov Clustering

The BRMCL is a balanced variant that preserves the native features of R-MCL. Instead of using M_G as the weight matrix, we construct a new regularization M_R using both the current flow matrix M and the canonical flow matrix M_G . For that, given a flow matrix M associated with the graph, the following concepts must be defined:

- **Node mass:** Defined as the sum total of the flows into the node, in such a way that, nodes with higher mass attract more nodes in the graph towards them.

$$mass(i) = \sum_j M(j,i) \quad (4)$$

- **Node propensity:** Defined as the weighted average of the masses of the nodes that flows into this node.

$$propensity(i) = \sum_j M(j,i) * mass(j) \quad (5)$$

The distribution of masses of the “Attractor” nodes is a proto-indicator of the distribution of final cluster sizes (i.e. nodes imbalanced clusters reflects imbalanced masses distribution). The aim is to push more nodes towards attractors having lower mass, thus requires that weight of each neighbour of a given node in the regularization matrix M_G must be in inverse proportion to the propensity of the neighbour. This means that at each iteration step, we need to construct a new regularization matrix M_R while maintaining the rest of R-MCL unchanged. The new regularization matrix M_R is given by:

$$M_R = \text{normalize}(M_G * P^b) \quad (6)$$

where P is the diagonal matrix with the propensity vector p along the diagonal.

The normalize operation rescales each column so that each column sums to 1. We notice that, the balance parameter b specifies the extent to which higher-propensity neighbours are to be penalized, in such a way that higher the value of b is the greater the penalty on high-propensity neighbours.

3.3 Improved Parallel Markov Clustering

Given the introduced approaches, there are still some critical limiting factors in working with Markov clustering especially for large scale graphs, since the performance of the ontology clustering

(partitioning) process can be a critical part of the upcoming ontology matching process performance.

Regularized Markov Clustering still suffers from the scalability and storage issues, resulting from high time and space complexity of the clustering process (Bustamam et al., 2012). At the core of the Regularized variants of Markov clustering, we can notice that its complexity is dominated by the iteratively sparse matrix-matrix multiplication and normalization steps, which is an intensive and time-consuming component. Thus, for scalability and performance-gain reasons, we need to develop computationally efficient algorithm that performs parallel sparse matrix-matrix computations and parallel sparse Markov matrix normalizations in order to improve the MCL performance.

To overcome the above MCL's issues, we propose a parallel Markov clustering approach that tries to improve the performance of the Markov Clustering by implementing parallel tasks for expansion, inflation and pruning operators using Spark framework (See Figure 1), which is a fast and general-purpose cluster computing system.

3.3.1 Apache Spark Framework

Apache Spark is a unified programming environment that provides computing framework designed for scheduling, distributing, and monitoring applications that consist of many computational tasks across many commodity worker machines (computing cluster) (Shanahan and Dai, 2015).

The computational engine Spark Core provides the basic functionality of Spark, including components for memory management, task scheduling and fault recovery mechanisms, interacting with storage systems. Furthermore, it offers the ability to run in-memory computations to provide faster and expressive processing and increase the speed of system. In-memory processing is faster since no time is spent in moving the data and processes, in and out of the hard disk. Accordingly, Spark caches much of the input data on memory for further explorations leading to more performance iterative algorithms that access the same data repeatedly.

3.3.2 Our Implementation

In order to improve the MCL performance, the parallel implementation of the Regularized Markov Clustering algorithm constitutes an important challenge. Thereby, we introduce a very fast Markov clustering algorithm using Spark framework to

perform parallel sparse matrix-matrix computations operations, which are at the heart of Markov clustering.

First of all, the resulting graphs from large scale ontology are generally sparse; thus, Markov clustering storage issues can be resolved using distributed sparse matrix data structures offered by the resilient distributed datasets (RDD) (Bosagh et al., 2016), which are partitioned collections of objects spread across many compute nodes that can be manipulated in parallel. These matrices are distributed across computational nodes by entries using *CoordinateMatrix* implementation, by rows via *RowMatrix* or via blocks by implementing *BlockMatrix*.

Moreover, the distributed sparse matrices offered by Spark ignore the large amount of zero entries, found in the initial stochastic matrices of Markov clustering algorithms. Hence, the distributed matrices can reduce the computational load by avoiding the additions and multiplications with null entries, since the zero values do not influence any of the Markov clustering operations. Furthermore, Spark comes with a library containing common computational functionality (Spark MLlib) (Meng et al., 2016), especially for matrix-matrix computations. These properties are the primary source of acceleration of our system.

Besides, Spark provides a way to parallelize our Markov clustering strategy across clusters, while hiding the complexity of distributed clustering programming, network communication, and fault tolerance in order to ensure the effective and reliable use of cache memory and the process balanced load. These latter is enhanced by dividing data according to performance and scalability-friendly data structures, aiming to dynamically adapt the system to fine-grained allocation of both resources and computations based on the workload. The pseudo-code for our parallel Markov Clustering implementation is given in the following:

```

Input: An ontology O, Balance parameter b, Inflation rate r
Output: Clusters Set C={C1, C2, ..., Cn}

{ //Phase 1: Ontology Parsing}
//get ontology concepts
Nodes:= Concepts(O)
//taxonomic and non-taxonomix
Edges:= Relations(O)
//create associated graph
G := CreateGraph(Nodes,Edges);
//Graph adjacency matrix
A := Adjacency(G)
{ //Phase 2: Markov Clustering}

```

```

A := A + I // Add self-loops
//Initialize M as the canonical
flow matrix
M := MG := A*D-1
repeat
    // Compute mass vector
    mass(i) = ΣjM(j,i)
    // Compute propensity vector
    p(i) = ΣjM(j,i)*mass(j)
    P := diag(p)
    // Compute regularized matrix
    //Normalize MR so that each column
    sums to 1.
    MR := MG*P-1
    M := Mreg := M*MR
    M := Minf := Inflate(M, r)
    M := Prune(M)
until M converges
Interpret M as clustering Sets

```

4 EXPERIMENTAL EVALUATION

In order to evaluate the performance of our approach and the execution time, we conducted a set of experiments using a distributed architecture. We implemented our system in Java; ontologies were parsed using Jena Apache. All processes are elaborated within Apache Spark Framework as programming environment that provides computing framework designed for scheduling distributing computational tasks across many computing nodes.

4.1 Data Sets

The Performance of our approach is evaluated over the anatomy data set that contains two large ontologies of human and mouse anatomy which contains 3306 and 2746 concepts respectively, and the DBpedia ontology release DBpedia_2015_10.

4.2 Experimental Architecture

All the experiments were carried out using the Apache Spark which is an open source, in-memory analytics computing framework. For this experimentation, we use a cluster of 10 slave machines and one master machine. Each node is equipped with 3.4 GHz Intel(R) Core i3(R) with 4 GB memory, Java 1.8 and Ubuntu 14.04 LTS.

4.3 Experimental Results

In order to incorporate the Markov clustering approach in our large-scale ontology matching

system, we must evaluate the scalability of the clustering approach. In our implementation, we attempt to validate the performance and the effectiveness of the proposed approach via a set of experiments on real world ontologies.

The simulation ran by using default expansion parameter (square), parameters of inflation $r=1.5; 2$ and 2.5 , balanced parameter $b=0, 1.5,$ and 2 and pruning threshold $\epsilon=0.000001$. The simulation is performed several times with different parameters of inflation to look at the speed and the number of formed clusters.

The number of resulting clusters from the improved BRMCL simulation using the inflation rates $1.5, 2$ and 2.5 vary from 1523 to 2136 clusters for Human ontology, from 1622 to 1968 clusters for Mouse ontology and from 519 to 533 clusters for DBpedia ontology. We can notice that varying the inflation parameter can result in clustering of different granularities, in such a way that, if the inflation parameter gets higher, the clustering algorithm predicts more clusters with smaller size.

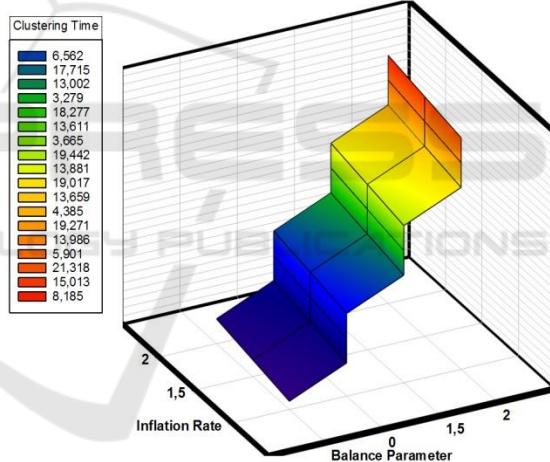


Figure 2: Clustering Time related to the inflation rate and the balance parameter.

As shown in Figure 2, we clearly notice that the runtime of our clustering implementation is related to the inflation rate and the balance parameter. Thus, having more balanced clusters can be achieved by increasing the balance parameter, for the reason that higher values of this latter lead to more severe down weighting of nodes with high propensity values, which consequently, provoke more iteration operations and lead to a slower convergence for the clustering process. By contrast, the incorporation of the balanced strategy improves the clustering quality by allowing the discovery of balanced clusters (See Table 1, Table 2 and Table 3).

Despite these impediments, our parallel Markov-based clustering implementation demonstrates significant performance and provides faster and expressive partitioning of the large-scale ontologies.

Table 1: Clustering results for the Human ontology.

		Clusters Number	Clustering Time	% of Balanced Clusters
b = 0	r = 1.5	1523	16,492 s	11%
	r = 2	1785	17,032 s	27%
	r= 2.5	2136	17,336 s	33%
b = 1.5	r = 1.5	1523	17,715 s	21%
	r = 2	1785	18,277 s	28%
	r= 2.5	2136	19,442 s	33%
b = 2	r = 1.5	1523	19,017 s	28%
	r = 2	1785	19,271 s	35%
	r= 2.5	2136	21,318 s	46%

Table 2: Clustering results for the Mouse ontology.

		Clusters Number	Clustering Time	% of Balanced Clusters
b = 0	r = 1.5	1622	12,853 s	15%
	r = 2	1787	13,071 s	17%
	r= 2.5	1968	13,473 s	22%
b = 1.5	r = 1.5	1622	13,002 s	35%
	r = 2	1787	13,611 s	46%
	r= 2.5	1968	13,881 s	51%
b = 2	r = 1.5	1622	13,659 s	41%
	r = 2	1787	13,986 s	58%
	r= 2.5	1968	15,013 s	63%

Table 3: Clustering results for the DBpedia ontology.

		Clusters Number	Clustering Time	% of Balanced Clusters
b = 0	r = 1.5	519	3,112 s	44%
	r = 2	527	4,016 s	51%
	r= 2.5	533	6,562 s	53%
b = 1.5	r = 1.5	519	3,279 s	47%
	r = 2	527	3,665 s	59%
	r= 2.5	533	4,279 s	68%
b = 2	r = 1.5	519	4,385 s	47%
	r = 2	527	5,901 s	61%
	r= 2.5	533	8,185 s	70%

5 CONCLUSIONS

In this paper, we presented our parallel Markov-based partitioning strategy considered as a crucial part of the large-scale ontology matching process, which aims to cope with the velocity issues and to increase the performance of the matching system. Our strategy provides faster and expressive

partitioning through dynamic, real-time in-memory computations based on the Spark distributed programming environment.

From the results drawn by our strategy over real-world ontologies, it is apparent that our parallel Markov-based partitioning approach presents significant performance results for partitioning large ontologies, which consequently make the approach suitable to be incorporated in our large-scale ontology matching system.

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